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Some Theoretical Problems suggested by THE MOVEMENTS OF INTEREST RATES, BOND YIELDS AND STOCK PRICES
IN THE UNITED STATES SINCE 1856



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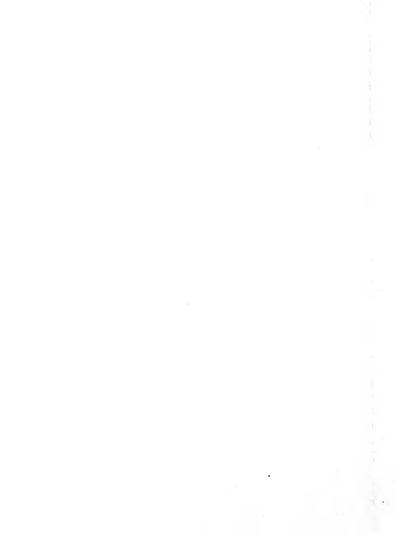
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(Resolution of October 25, 1926, revised February 6, 1933)



Some Theoretical Problems suggested by

THE MOVEMENTS OF INTEREST RATES, BOND YIELDS AND STOCK PRICES IN THE UNITED STATES SINCE 1856

FREDERICK R. MACAULAY



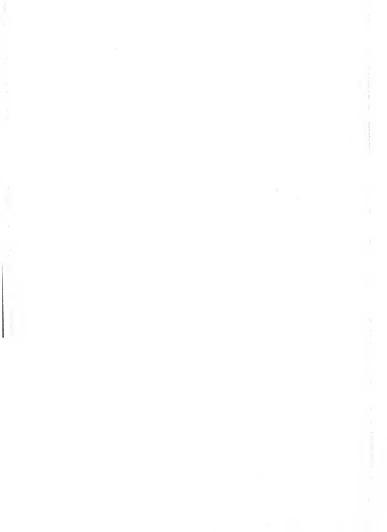


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To My Friend WESLEY CLAIR MITCHELL



ACKNOWLEDGMENTS

I wish to thank sincerely Miss E. Gail Benjamin, who aided me in the earlier stages of the statistical work of this book, Miss Celeste Nason, who assisted me later, and Miss Dorothy Achilles, who was in charge of that work as the book went to press. Miss Achilles made most of the calculations and drew all the charts.

To Miss Martha Anderson goes deep appreciation of her careful editorial scrutiny and of the laborious work of seeing the book through the press.

I am grateful to the Metropolitan Life Insurance Company for clerical aid in the collection of bond prices and the calculation of yields. My friend, the late Walter Case, defrayed the expenses of collecting stock prices and constructing the stock price index numbers.

To Dr. Wesley C. Mitchell I am indebted not merely for scientific and scholarly criticism throughout the course of the study, but also for a friendship without which it is literally and exactly true that this book would never have been written.

F. R. M.



PREFACE

This book is a striking example of the way in which scientific problems evolve when they are attacked by a thoughtful and thorough investigator.

As Dr. Macaulay explains, he planned at the outset to study the course of interest rates and bond yields in the United States over a long period with a view to ascertaining what statistical relations these rates and yields bear to one another, to the prices of stocks and commodities, to the physical and monetary volume of trade, and to credit and banking activities. One outcome of this plan is the collection of index numbers and time series presented in the Appendix. Men of affairs and students will find in these tables a skillfully and carefully compiled record of past experience that can be put to many practical and scientific uses. No other investigator of interest rates, bond yields and security prices has made so thorough an examination of the surviving data about past transactions in American financial markets, or prepared such trustworthy measures of the various types of fluctuation that these rates, yields and prices have undergone.

This part of Dr. Macaulay's work goes far beyond the task of making a faithful compilation of scattered data. Not only did he make critical use of his sources, such as we expect of a classical scholar who is trying to establish a sound text, but he also observed characteristics of his materials that had received little or no attention. The effort to see clearly what was dimly visible in the original data led him both to extend his collections and to invent ingenious methods of measuring the characteristics that he had found.

While he was studying the behavior of his series relating to bond yields, interest rates, stock prices, commodity prices, bank clearings, and pig iron production, Dr. Macaulay tested numerous hypotheses concerning the interrelations among their movements. Though he found that most of the relations that have been announced by others failed conspicuously over the long periods covered by his data, he also found that

xi

some rules of thumb hold good most of the time. But the more he wrestled with these problems, the more critical he became of purely empirical relations, and the more desirous of finding out why his different series behave as they do.

This striving for rational understanding of his statistical results carried Dr. Macaulay back to antecedent questions concerning the basic characteristics of the several classes of objects he was observing. He had to ask himself a series of fundamental questions about things that we usually take for granted. What are bond 'yields', interest rates, shares in corporations? For what purposes do men want bonds, loans, shares, commodities, gold, money? Why do they make investments for different terms at different rates? What is the 'duration' of a loan?

These questions and their congeners involved a consideration of the economic planning in which men are more or less consciously engaged. One factor appeared to be involved in all plans. Virtually every present transaction into which men enter involves the future—a future that may belong to the 'specious present' or that may be far removed. In few transactions is this element more prominent than in buying bonds or lending money. To understand the behavior of bond yields and interest rates it is necessary to take account of futurity—a factor that constitutes one of the leading differences between the natural and the social sciences. because it does not complicate the explanation of physico-chemical phenomena but does dominate the planning of men and so must be considered in explaining human behavior. In his Institutional Economics Professor John R. Commons has recently directed the attention of economists to the role played by the future in men's transactions with one another; but Dr. Macaulay brings more definite data to the treatment of the theme and carries the analysis further.

Of course the future is always uncertain. Men try to foresec, sometimes spending much systematic effort, often contenting themselves with vague anticipations, accepting what has been as an adumbration of what will be. There has been not a little speculation among economists about such matters as the extent to which forecasts of future price fluctuations influence the present demand for loans. Out of such speculations have been spun theories concerning the relations among the movements of prices, interest rates, investments, volume of credit, and production. By taking the clear test case of bond yields and short term interest rates, both considered with reference to the same period, Dr. Macaulay is able first

PREFACE xiii

to demonstrate what the mathematical relationship between the two sets of movements would be if men forecast the future correctly, and second to demonstrate that the actual relationships are commonly of an opposite sort. Though the theoretical relations that would exist between other paired series if the future were accurately known are less simple in their logic, he is able to show how dubious are numerous explanations of the actual relations that credit men with greater ability to foresee the future than they possess.

This discussion of the role played by the future in economic behavior grows out of Dr. Macaulay's efforts to solve the problems attacked in the latter part of his book. Coming later in time so far as the progress of his thinking is concerned, it comes earlier in logical order and is properly placed in Chapter I. Readers interested only in the historical facts concerning interest rates or security prices may not at first grasp the relevance of this philosophical analysis, penetrating as they may admit it to be. But if they follow the argument as it unfolds, their thinking will evolve as Dr. Macaulay's did, and they will see that the book is 'all of one piece'. The beginning really prepares for and illuminates the end.

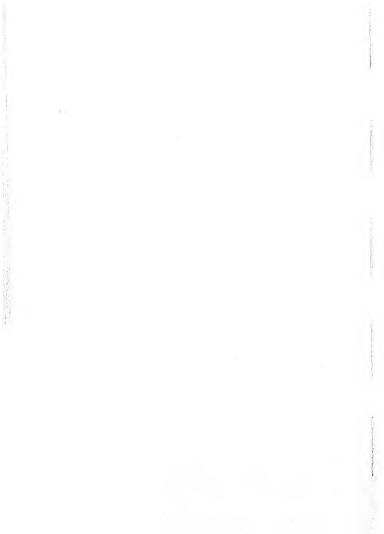
But the end of the book is not the end of the investigation. For, much as Dr. Macaulay has contributed to our understanding of the behavior of bond yields, interest rates, stock prices, commodity prices, clearings and production, and of the interrelations among these variables, his largest service lies in formulating fundamental problems of economics in a way that opens them to attack, in providing better and more abundant data concerning them, in forging tools for analytic use, and showing how to carry the work further. Many a reader will lay down this book longing to enter himself on the enticing tasks that Dr. Macaulay suggests.

WESLEY C. MITCHELL DIRECTOR OF RESEARCH



CONTENTS

Pref	ace by Wesley C. Mitchell	xi	
Ι	Introduction	3	
II	The Concept of Long Term Interest Rates	24	
III	Some Theoretical and Practical Difficulties of Comparing		
	Long Term Interest Rates at Different and Especially at		
	Widely Separated Dates	54	
IV	The Relation of the Movements of Bond Yields to the Grades		
	of the Bonds-Economic 'Drift'	85	
V	Bond Yields, Economic 'Drift', and the Prices of Common		
	Stocks	128	
VI	Interest Rates and Commodity Prices	163	
VII	Factual Leads and Lags and Empirical Forecasting	209	
List	of Tables	237	
List	of Charts	239	
Арр	endix		
Α	Tables (see separate list)	A3	
В	Professor Irving Fisher's Statistical Measures of 'Price		
	Change'	A311	
С	The Meaning of Gold Yields of Bonds Payable Principal and		
	Interest in Currency	A327	
D	Methods for Computing Cyclical and Trend Graduations and		
	Moving Seasonals	A331	
E	Short Term Interest Rates	A335	



Some Theoretical Problems suggested by the movements of interest rates, bond yields and stock prices in the united states since 1856 $\,$

"The real trouble with this world of ours is not that it is an unreasonable world, nor even that it is a reasonable one. The commonest kind of trouble is that it is nearly reasonable, but not quite. Life is not an illogicality; yet it is a trap for logicians. It looks just a little more mathematical and regular than it is; its exactitude is obvious, but its inexactitude is hidden; its wildness lies in wait."

-G. K. Chesterton

CHAPTER I

INTRODUCTION

The theoretical and statistical studies contained in this book are an outgrowth of an investigation of the course of interest rates and bond yields in the United States since 1856 and of the statistical relations of those rates and yields to one another, to stock and commodity prices, to the physical and monetary volume of trade, and to credit and banking conditions. Directly or indirectly, the questions discussed are nearly all concerned with the relations of interest rates and security prices to the problem of explaining why we have those recurring periods of prosperity and depression which are commonly termed 'business cycles'.

Throughout the studies, we have emphasized the essentially numerical nature of the interest concept. Instead of stopping with the statement that a rate of interest is a measure of an exchange relation between present money and promised future money payments, we have devoted considerable space to the elucidation of some of the mathematical implications inherent in this particular 'measure'. The usefulness of this procedure is strikingly apparent in the discussion of the relations between long and short term interest rates. The conclusions arrived at with respect to what those relations would be, if men's actions could be and were based on complete knowledge of the pertinent facts and logical use of such knowledge, follow simply and directly from the mere mathematical nature of long and short term rates. Statistical examination reyeals that the relations as they actually occur show a definite tendency to run counter to these theoretical rationalistic expectations. Now the suggestiveness of such an opposition can hardly be overemphasized. The reflections to which it gives rise inevitably lead to the realization that The tables and charts concerned with the relations of the rates and yields to credit and banking conditions, with the theoretical and statistical discussion of those aspects of the subject, are to appear in another volume.

the type of economic relationship which it so clearly illustrates must necessarily be extremely common. A recognition of this fact is, as we shall see later, of fundamental importance not only to the student of interest rates and the business cycle but also to all who are concerned with the more general subject of the nature and significance of the springs and origins of economic conduct.

Persistent emphasis on the distinction between what actually does occur and what would occur if men knew all that was relevant and acted logically has tended to make many of the answers suggested in this book primarily answers to new questions rather than new answers to old questions. No attempt has been made to solve formally any of the age-old philosophic puzzles which, in economic theory, have been grouped under the general title of 'the interest problem'.

Historically, discussions concerning interest began with queries as to its justification. Was it equitable or was it merely legalized robbery? Whether it should be permitted at all was long one of the most debated subjects in the entire field of economic thought. The question was considered by Aristotle. It engaged the Schoolmen of the Middle Ages in endless wordy argument. With the emergence and development of economics as a separate discipline in the 18th and 19th centuries, the controversy was taken over by the economists. Their treatment of the subject early showed a distinct advance over that of the Schoolmen. They soon sidetracked the ethical question of whether interest should be received and given for the more purely economic questions of why it is demanded and how it can be paid. The answers to these two related problems, as given by the earlier economists, carried with them an atmosphere of reality which had been totally lacking in the dialectics of the Schoolmen. However, the solutions were in general extremely naive. Indeed, it is impossible to deny that some of the air of reality they possessed was the air of reality that so often resides in that brand of 'common sense' which is eventually discredited by careful scientific analysis. With the gradual development of economic theory the solutions proposed tended to become less and less naive, but not to a corresponding extent more and more scientific. The metaphysical poison of the Middle Ages continued to work in the system of economic thought. Once again, as in the days of the Schoolmen, there arose a tendency to treat the problem as one of logically explaining a set of recognized and simple facts. Seldom was any effort made to enlarge

the horizon of facts to be explained. Usually the struggle was for a neat and internally consistent explanation of the few facts (or assumed facts) that were accepted by all as the counters in the game. Under such circumstances, it is hardly surprising that, even as late as the closing years of the nineteenth century, occasional pauses in the heated discussions between economists, not only as to why interest is and can be paid but even as to how it should be defined, were usually traceable to exhaustion or death rather than to any progress towards agreement.

Within recent years fewer books and articles of a primarily controversial nature have been written on the general problem of why interest exists. No longer is each full-fledged economist supposed to have his own individual and unique 'theory of interest'. Eclectic theories have become popular. It is being stressed that there is truth in most of the theories. Their differences are being explained as the result of concentrating attention too exclusively on particular aspects of the problem. The seeming tendency towards agreement which is thus arising carries with it, however, a strong suggestion of that toleration which commonly appears in the discussion of a problem when either its importance or the possibility of any ultimate solution is no longer considered great. Underlying the collection and attempted welding together of various elements from different interest theories lies the suggestion that immediate further progress is believed improbable if not impossible. The incentive to thresh the old straw over again is wanning.

When grappling with the question why interest is paid at all, economists have too generally neglected to ask themselves what use they expected to make of the answer. Like the man who has light-heartedly tackled a picture puzzle, they have too often been primarily interested in solving the problem rather than in using the solution. He looks forward to the moment of triumph when the picture will be completed and he can throw the pieces back into the box. When the economist applies his solution to the actual facts of the market place, he generally does so, not to explain those facts but to prove that they can be explained, not to throw light on them but to show that, when 'properly considered', they do not conflict with his solution. The solution becomes a hobby. When facts clash with it, the facts inevitably give way. A bludgeon that is continually used to overcome any difficulties encountered in applying the theory to specific cases is to deny

that the specific cases are interest rates at all or to 'explain them away' by stating that they involve an interest element and elements of essentially different nature.

Most interest theories attempt to explain 'pure' interest only. However, the nature of 'pure' interest is invariably left quite obscure. It is, of course, almost always that interest for which the theory proposes an explanation, but never do the attempts to define it as 'riskless' interest or in any other direct manner bear up well under critical scrutiny. It is of little use to have an answer to the question 'why interest is paid at all' if the answer does not help us to solve or at least understand those less ultimate but more immediate and direct problems that are concerned with the levels and movements of actual rates.

Economists have gradually come to recognize that the interest problem is essentially a numerical problem and should be approached as such. It is fundamentally a problem of interest rates. Any discussion that neglects or under-emphasizes this consideration can hardly be expected to be very fruitful. At best, answers to the question 'why interest is paid at all' tend to be inadequate and incomplete because the question is inadequate and incomplete. It is a non-quantitative, nonnumerical question and it consequently leads to non-quantitative, nonnumerical answers. Such statements as that interest exists because men naturally value present purchasing power more highly than future purchasing power or that it can be paid because money capital can be used productively by entrepreneurs may or may not be open to the criticism that they beg the question. They certainly require mathematical development before they can be used to handle the quantitative, numerical puzzles that the actual data present. Without such development, they are mere truncated explanations which, even if true, are hardly more than unattached items in the system of economic thought. Of course, one must not expect the rigid exactness of a physical law in a mere economic generalization, but to stop with any such non-numerical explanations as the preceding is almost as if the Newtonian formulation of the theory of gravitation-bodies attract one another with a force that is directly proportional to the product of their masses and inversely proportional to the squares of their distances-were to stop with the words 'bodies attract one another.' Even if perfectly true-which modern astronomers would deny-the 'law', in such an incomplete form and without further development, would be less useful as a key

to the movements of the solar system than the earlier but numerical generalizations of Kepler.

However, any mathematical development of an hypothesis that has inherent weaknesses inevitably brings them to the surface and makes them more apparent. Most theories of why interest is paid at all fail to explain the facts of the actual market not primarily because the theories are non-quantitative but for a more fundamental reason. They commonly assume a degree of rationality and capacity in the conduct of human affairs that does not and cannot exist. Ieremy Bentham's 'pleasure calculus' gave a false picture of the activities of men not merely because their lives are not controlled by the search for happiness but also because they are unable to solve the problems of the pleasure calculus. Too much effort has been expended on trying to 'adjust' the actual phenomena of interest rates to some theory that involves assumptions that are not applicable to the actions of human beings in a real economic environment. Too little effort has been made to discover all relevant facts about actual rates and their behavior, and from those facts to find out. among other things, how human beings really do function.

The interest problem has been prematurely attacked. Too much attention has been paid to solving it, too little attention to formulating it. What do we mean by a rate of interest? What are the essential mathematical characteristics involved in the very concept? What are the quantitative facts about actual rates and why are the facts as they are? How and why do rates vary among themselves at the same time, and how and why do they vary from time to time? How, and with what regularity, are interest rates statistically related to other economic phenomena? What are the most important factors that logically should influence rates? And what are the factors that do influence them? To what extent and under what circumstances do the movements of rates seem consistent with rational human conduct, and to what extent and under what circumstances is explanation hindered rather than helped by assumptions of rigid rationality?

It is a hopeful sign that studies of rates have, for some time, been appropriating much of the attention that formerly was given to discussions concerned with the nature of interest as such. Measurement, and reasoning that does not attempt immediately to reach back into ultimates, normally precedes consideration of the nature of the thing itself. It is an old saying that the last thing to be discovered in a

science is what it is all about. However, in the welter of historical records and 'statistical studies', the student of interest rates must not forget that truth does not grow like Topsy. While attempting to avoid the Scylla of fruitless dialectics, he must beware that he is not drawn into the Charybdis of meaningless empiricism. A statistical study that presents nothing but raw facts may sometimes be extremely valuable while one that presents 'correlations', or other evidences of empirical relationships, as though they were explanations, may easily become a delusion and a snare. Something more than the mere presentation of an index number of bond yields, an index number of commodity prices, and a correlation diagram such as that seen in Chart 17 is necessary to disclose the character of the causal relations (if any) that exist between the two series. Such charts and diagrams are, of course, suggestive and important. But, if much progress is to be made, examination of facts must be followed by a serious attempt to understand them, to think the matter through. Mere empiricism will not do. Real explanations come by way of shrewd conjecture followed by adequate testing—the oldfashion road of intelligent hypothesis and rigid verification. However, the road of hypothesis and verification is, in economics, almost necessarily a different and more difficult road to travel than it is in such sciences as astronomy, physics or even biology.

The generalizations of the physical sciences are concerned with the world outside man. The sequence of the seasons, the alternation of day and night, the speed of light, and the relations of oxygen, hydrogen, nitrogen and carbon to animal and vegetable life were as they are before man appeared on the earth. On the other hand, the very essence of economics is that it is a study of human behavior, of the life of man and basically of the mental life of man. It takes cognizance of facts in the external world, not for their own sake, but only because of their relations to the mind of man. It is a study of some of the causes and effects of those conscious or unconscious decisions that men inevitably make in their rational or instinctive struggle to 'earn a living' and to satisfy at least some of their desires by adjusting the external world to themselves and-perhaps-thereby securing happiness and well-being. Conditions in the external world of course influence such decisions and are influenced by them but, fundamentally, economics is concerned with mental rather than with physical phenomena, with 'desires' and 'decisions', 'happiness' and 'well-being', rather than with bread and butter

or bricks and mortar. Physical facts or generalizations, even though they be of the greatest economic importance, cannot by themselves constitute economic facts or laws.² Only indirectly is economics interested in the facts of agricultural chemistry or the laws of mechanical engineering, the constitution of bread and butter or the strength of bricks and mortar. It is primarily a study of decisions and not of actions, of how men mentally compare and measure the significance for themselves of various actual and possible conditions in the external world and not of how they physically obtain or alter those conditions. It is primarily concerned with the rationale of how men value things and not with the technique of how they produce them.

Because economics is a study of the behavior of men, economists will probably never be able to make much use of the concept of necessity (or invariable sequence) which permeates the physical sciences. Economic 'laws' in the strict sense of the word will probably always be merely statements of more or less pronounced 'tendencies'. Economics is one of the social sciences, and the chain of causation in all the social sciences is necessarily indirect rather than direct, mediate rather than immediate. The mind of man is always the connecting link-and the disturbing element. Large crops do not lead to low prices in the same direct manner in which great distance from the sun is associated with low orbital velocity. Even if it were true that high interest rates were inevitably associated with rising commodity prices, the high rates could hardly be considered a result of the rising prices in the same direct manner that the movements of a dynamo result in an electric current. The manner in which overexpansion of credit may lead to economic convulsions in a community is fundamentally different from the manner in which a large dose of strychnine leads to physical convulsions in an individual.

Furthermore, the peculiar characteristics of the indirect causation ² Though the expression of physical generalizations in economic rather than physical terms may sometimes be highly desirable in order to make their economic importance obvious, it does not alter their essential nature. Economics as such is concerned with how men tend to react to certain physical facts (when known) and not with what those physical facts are. The 'law of diminishing returns in agriculture' may be used as an illustration. That, after a certain stage is reached, successive applications of 'labor and capital' (cultivating and fertilizing, for example) give rise to successively declining increments of agricultural produce is primarily a biological and not an economic fact; though, of course, an extremely important biological fact to consider when attempting to understand why men carry on agriculture as they do.

that is seen in economic phenomena do not result from the mere fact that life with its struggle is an essential part of the picture. It is true that life always introduces the element of struggle, the struggle to exist, to 'make a living'. But the struggle with which economics is concerned is always man's struggle. It is imaginable that one might work out a system of economics for the beavers or the bees but it would not be the economics we are discussing. It is almost impossible to imagine a system of economics for the oysters or the trees and the flowers. Yet they are all just as much engaged in 'making a living' as is man. It would not be helpful to attempt to define economics in such a manner that the reaching down after water by the roots of a tree could be considered an economic phenomenon. Strictly speaking there is no economic life without man. Man, with the particular type of brain and nervous system that he possesses, is always the essential element in the problem.

And right here we encounter the obstacle that will always block the attainment of any such exactitude in economics as is possible in the physical sciences. The minds of men do not admit of the same definite analysis as do the events of the external world. Paradoxical as it may sound, one of the chief differences between the world of matter and the world of mind is that the world of matter is essentially reasonable and the world of mind is not. Reason arose because of its relation to the world of matter. It helps man to conquer his environment. The possibilities of understanding and coping with the external world that the use of reason offers man are almost boundless; its possibilities in the way of understanding and forecasting his own activities are strictly limited. Those activities are partially, though only partially, rational. The presence of a modicum of reason is the disturbing element in the problem which stands in the way of any complete solution by reason.

If men's activities were purely instinctive—a mere matter of tropisms—they could be handled (though of course not by man!) in the way that such facts are handled by the biologist. On the other hand, the implications of the opposite assumption of <code>complete</code> knowledge and <code>absolute</code> rationality are much more difficult to discuss. Such an assumption must, from its very nature, be so far removed from reality as to make convincing analysis almost impossible. It amounts to assigning to man metaphysical attributes of the same incomprehensible nature as

those that the more philosophic religions commonly assign to deity. On the other hand, one might wonder whether the difficulties involved in analyzing the implications of any such assumption were not primarily the result of its absoluteness rather than of its nature. It might well seem reasonable to think that, in so far as men's activities approached a condition of complete rationality, in so far as they were based on complete knowledge of all that was relevant and rigidly logical use of such knowledge, they might be studied and their significance brought to light and understood by using the methods of the purely dialectic sciences of logic and mathematics-even if the limiting case, in which absolute rationality is assumed, presented insuperable philosophic difficulties. It might be thought that, to the extent that all men had knowledge of all facts and conditions that had any appreciable bearing on the solution of their economic problems, and to the extent that their reactions to those facts were logical rather than emotional, reasoned rather than erratic, economic adjustments by individuals to their environment would occur in the same methodical and mathematically predictable manner as do physical adjustments in the external world.

However, as things are, even those individual adjustments that are deliberately and consciously made show little tendency to be well adapted to the ends in view unless the facts on which action should be based are relatively easily obtainable and the required logical processes fairly simple. Even in the absence of emotion, serious individual maladjustments tend to occur whenever the relevant facts are difficult or impossible to discover or the necessary logical processes are complicated and involved. And only if the factual and logical bases for the individual's economic activities were almost unimaginably perfect, could even social economic forecasts be made with anything like the warranted assurance with which astronomical forecasts are now made.

Of course, the disturbing effects that such factors as presence of emotion, lack of logic and insufficiency of knowledge have on the economic behavior of *individuals* would not merit the attention we are giving them if *socially* they always 'canceled out'. If the vagaries of individual conduct were always 'normally' distributed round a strictly rational 'mode', in other words, if the 'deviations' were of the nature of 'accidental' rather than, for example, 'systematic' or 'constant' *errors*, their curbing effects on the development of economics as a strictly logical social science might be small or negligible—unless the 'scatter'

were excessively great. The strictly rational 'mode' could always be discovered by taking a large number of individual observations, and the importance of the 'deviations' of these observations could be expressed in terms of 'probable errors' or other measures of variability. Not merely the 'law', but also the degree of assurance with which the science could be extended by unveiling the logical and mathematical implications of the 'law', could be definitely formulated. The science of statistics has been designed to handle problems of precisely this kind.

It is, however, not worth while attempting to develop in detail the possibilities of such a purely hypothetical condition. It is and always will be thoroughly unreal. The disturbing social effects of the inadequate solutions that individuals obtain of their particular economic problems result from the fact that many of the inadequate individual solutions do not and never will 'cancel out'. The reason for this condition lies in a fundamental characteristic of almost all those adjustments that constitute economic behavior. Normally they are adjustments of the present to the future. 'Planning' is the essence of rational economic life and planning looks to the future and not to the past or present. Knowledge of the past or present is normally useful to the 'entrepreneur' or typical 'planner' only in so far as it helps him to forecast and handle the problems of the future. Adequacy of economic adjustments to present conditions is almost always essentially dependent on how adequate is the adjustment to the future. And the existence of such violent social disturbances as are commonly discussed under the general title of 'business cycles' strongly suggests that society at large may well be little, if any, more capable of foreseeing and adjusting to the future than are the individuals of which it is composed. If the existence of business cycles demonstrates anything, it demonstrates that the economic maladjustments of individuals do not always 'cancel out' socially.

Social, as well as purely individual, economic maladjustments tend to increase in severity with an increase in the complexity of an economic system. With the development of large-scale production for the market, the importance of 'planning' becomes increasingly great. With an increasing use of credit, the punishments meted out for inadequate planning (resulting from incorrect forecasting) become increasingly severe. The most elementary form of production is consumer-production—production for one's own consumption. The most important distinction between consumer-production and production for

the market is that, while the consumer-producer needs to forecast only his own desires (and such physical factors as weather) the producer for the market must forecast not merely the desires of other persons but also their (future) ability and willingness to pay a price sufficiently high to give him a satisfactory surplus over his cost of production. He must forecast demand and not merely desire.

Furthermore, if the consumer-producer, when he comes to the stage of consumption, has changed his mind and wishes that he had applied his work to other ends, there is unlikely to be any serious maladjustment for him or any maladiustment whatever for the community at large. The economic disturbances in a frontier agricultural society in which each farmer is practically self-sustaining are primarily traceable to physical rather than strictly economic origins, to plant or cattle pests or to drought, rather than to price fluctuations. When economic distress occurs in such a community it results from deficient and never from excessive crops. When Robinson Crusoe planted his corn, the only forecasts he had to make were physical forecasts—that the seeds would germinate and the plants mature. He did not need to consider whether the price per bushel of the resulting corn would be high enough to pay his total costs and still leave him a living surplus. He was free from the dangers of strictly economic disturbances. He did not need to fear that, if the dollars received for the total crop were insufficient to pay the interest on the mortgage on the island, the cannibals would come and throw him into the sea.

Social maladjustments would not tend to increase in severity if the possibilities of adequate forecasting increased rapidly enough to offset the effects of the increasing complexity and intricacy of economic life.³ Such a condition is, however, extremely unlikely to occur sponta-

a Though the complexity is essentially an economic complexity, its origins are technological as well as purely economic. The fact that in a rural community the construction by the farmers themselves of a system of roads to be communally owned contains no such potentialities of economic disturbance as result from the building of a railroad is explainable by economic and not by technical differences between the system of roads and the railroad. The railroad is producing 'for the market'; the roads are not. The railroad has been financed by means of stocks and bonds whose owners, unless their affairs are to be to a greater or less extent disorganized, must receive their return in cash and not 'in kind'. But it was the technical magnitude and complexity of the railroad that led to its being financed so differently from the roads and producing 'for the market' rather than for its stock and bond holders. In one European country after another, economic crises began to appear sporadically

neously under any economic system containing as large an element of 'laissez-faire' as still exists in the economic systems of such countries as England and the United States.* It is easier to ask questions than to answer them. Under a regime of relatively uncontrolled freedom for individual economic initiative, it is easier to build up a system in which knowledge of the future is of paramount importance than it is to foreast that future. The fundamental problem is one of social control. It should not be allowed to remain one of mere individual forecasting. However, diagnosis comes before treatment. Before we consider what might be done to reduce the social ill effects of errors in individual forecasting, it is highly desirable that we understand something about the sources of those individual errors that have the most serious social effects—in other words, those errors that socially neither 'cancel out' nor have any other constant relation to a rational norm.

Individual errors in economic forecasting do not usually cause economic disturbances if socially they 'cancel out' or even if the deviation of their social average from the rational norm tends to be always of approximately the same algebraic magnitude. It is violent fluctuations of the average—especially when such fluctuations involve a change of sign—that are usually the essentially disturbing elements. So long as men continue to place an extremely high value on diamonds that absurdity introduces no appreciable economic strain. But, if they suddenly came to their senses, the diamond market would collapse. The effects of mass enthusiasm or mass depression are usually of importance to the student of economic fluctuations only because the community is at one time abnormally enthusiastic and at another time abnormally depressed. Even panic is economically destructive primarily because of its unusual and erratic occurrence. If the community at large had, year in and year out, a rather critical and even somewhat (Footnote 8 concluded)

soon after the introduction of banking, but they did not begin to take on their

modern characteristics until the advent of the industrial revolution.

⁴ Director's Note: "This, while true, does not imply the contrary contention that economic stability would be more certain under rigid forms of social regimentation. The recurring unbalances under complete 'faissez faire' may be less serious than the economic unwisdom of a dictatorship. The path to stability should lie between the two extremes." M. C. Rorty.

⁶ Of course, the control must be both intelligent and stable. The possibilities of accurate long term forecasting are decreased rather than increased by a steady stream of unsound economic legislation, enacted on the theory that the best way to find out whether the effects of passing a bill will be good or bad is to pass it and see.

sceptical attitude towards banks, we should almost certainly have a much better banking system than we have. We must remember that, at the time it occurs, panic may be more logical than not. A general run on the banks may be the result of a belated public realization of the prevalence of grossly incorrect economic forecasting by the bankers, horrowers, depositors, and the community at large. Its explosive and destructive character may be traceable largely to the fact that it did not come sooner.

But erratic emotion is a less fundamentally disturbing influence than either insufficient knowledge or the inability to draw warranted and useful conclusions from what is known. Ignorance is the mother of panic. And, because the most necessary knowledge is knowledge of the future, we must remain largely ignorant. Even such a product of man's own thought as an invention of radical economic importance may burst on an industry like a bombshell.

The future is never certain. But, in all too many instances, thoroughly warranted conclusions as to future probabilities are not drawn. The possession of the necessary knowledge of the present, even when such knowledge is easily obtainable, is rare; and the ability to predict, with any great degree of assurance, even the probable future from that knowledge is still rarer. The logic we lack, and the logic necessary to handle adequately the more difficult problems of economic life, is more than a mere ability to distinguish the valid from the invalid moods of the syllogism. It is the ability to distinguish the relevant from the irrelevant facts around us and to reason assuredly from such data. However, such reasoning, like the reasoning in all scientific prediction, must obtain its major premises from the particular science involved. But economics, in its present stage of development, may not be prepared to supply the necessary premises. And how few of us have any profound and penetrating understanding of the theoretical and empirical conclusions it is prepared to supply. Lack of knowledge of the future is a fundamentally disturbing factor but the effects of inability to handle logically the facts of the present must not be underestimated. Indeed, if that inability were less, our knowledge of the future would be greater.

The unwise economic conduct of individuals that shows itself in poor forecasting is the major source of social economic disturbances. But it is not the only source. Paradoxically, there is another source in

individually wise economic conduct. There is a type of shrewd individual conduct that takes no cognizance of the social repercussions of its actions and that may be almost as socially disturbing in its own field as illogical conduct or conduct based on inadequate knowledge. And we here exclude 'criminal' conduct. When bankers lend increasingly huge sums on stock and bond collateral because, as in 1928 and 1929, rates are high and they feel that such loans are extremely safe, they may be acting, even if unconsciously, not merely in a fundamentally anti-social manner but also in a fundamentally unintelligent manner—in spite of the fact that, from a narrowly individualistic standpoint, any single bank may be economically justified in so increasing its collateral loans. This is an excellent illustration of the specious nature of the doctrine of 'the invisible hand'.

But the difficulties of foresight as compared with 'hindsight' become apparent when we notice the present differences of opinion, among even professional economists of the highest standing, as to the ultimate effects of the purchases of huge amounts of long term Federal bonds by the banks of the country during the past few years.

The effects of the social maladjustments that result from inaccurate forecasting or anti-social behavior on the part of individuals are commonly cumulative. A pressure-momentum develops on the downside just as an opportunity-momentum had developed on the up-side. Not merely those individuals and institutions that have been guilty of the grossest and most inexcusable miscalculations but also multitudes whose economic activities have been relatively sane and rational are overwhelmed when the unprepared-for future becomes the inescapable present. While the up-momentum has its origin in increased purchasing power, the down-momentum has its origin in decreased purchasing power. The one necessarily involves an element of decision; the other does not. While the up-momentum attains its volume through its hypnotic effects on social behavior, the down-momentum introduces the element of necessity. Few are forced to buy during an upward movement of security prices, many are compelled to sell during a pronounced downward movement. Aesop's fable of the contention between the sun and the wind as to which was the more powerful is not especially enlightening as to what happens when the wind is of tornado force.

What light does this long discussion of some of the essential characteristics of economic life throw on the problems of economic 'hy-

pothesis and verification'? Let us review some of our conclusions. We have seen that economic activities are activities of men in their struggle with their environment. We have seen that the mental characteristics of men are quite as important as the physical characteristics of their environment. We have seen indeed that the physical environment is only one aspect of the total economic environment; that men build up through law and custom an extraphysical environment that, in many ways, affects their economic activities as directly and powerfully as does the purely physical environment. We have seen that most economic activities are peculiarly concerned with the future; that forecasting is of the essence of such activities. But we have seen that the economic future cannot be accurately known and that, though it is conceivable that it could be forecast with a fairly high degree of probability, successful forecasting is now rare. Few men have either the necessary knowledge of the present or the technical equipment and ability to deduce the future from such knowledge.

Because of these facts, we hinted at the possibility of two almost independent systems of economics. The one system would be philosophic, logical, mathematical, and hypothetical; the other system would be empirical, statistical, and actual. In their most extreme forms, the hypothetical system would be concerned with what would occur if economic activities were logically adjusted to one another and to a real though unknown future, while the empirical system would degenerate into a compilation of unexplained historical and statistical 'precedents'.

There are in existence virtually no illustrations of the extreme form of the first system. But the reason is not that the mathematical economists have felt this presentation of the problem to be too unreal, but that they have not sufficiently appreciated the importance of the fact that economic adjustments to be satisfactory must be adjustments to the future. Illustrations of the second system in its most extreme and absurd form are very common. The 'forecasting' woods are full of them.

In slightly less extreme forms, examples of these two systems have existed side by side since the beginnings of economic thought. But there has been no clear recognition of the extent to which their differences are traceable to the fact that so often they are investigating different things. It has almost always been tacitly assumed that they were investigating the same thing, though in different ways. Strange

consequences have inevitably followed. When methods of investigation that are peculiarly applicable to one of the systems have been applied to the other, more or less uninterpretable results or even complete failures have sometimes appeared; the extent of the failure depending, of course, on the degree to which, in the particular economic phenomena under discussion, what men actually do differs from what they would do if their knowledge were adequate and their actions were rational. The mathematical economist, when he really has been investigating the actions of a non-existent 'economic man', has defended a failure to reproduce the facts of the market place by suggesting that his solution was that to which conditions tended and that deviations were merely the result of 'disturbing factors'. The statistician has struggled to formulate a rigidly logical foundation for the 'behavior pattern' that his correlations seemed to suggest. Each has always assumed that there is only one possible economics.

In virtually all discussions of 'method' in economics it has been tacitly assumed that the value of studying what would occur if men acted rationally depends on how closely an analysis of hypothetical rational behavior explains how, in fact, they do act. No one has seriously suggested that one of the chief reasons for studying the economics of a 'rational' society might be because it would, in some respects, be so unlike the economics of real life. Yet we have in this chapter come to the conclusion that erratic social irrationality constitutes one of the chief reasons for the major economic disturbances of society.

The commendation attached to economic analyses that are primarily based on how men would act if their knowledge were adequate and their reasoning good has been declining for decades. On the other hand, the commendation attached to any study of how men actually do function in economic life has been steadily increasing until a stage has now been reached at which the discovery of statistical 'relations' is almost assumed to be of the greatest possible value whether or not they seem to admit of any significant explanation. One of the chief uses of such studies is naturally in the field of empirical forecasting; if the crop be so large, the most probable price per bushel will be such and such; if a country enters a period of monetary inflation the effects will probably be similar to what they were in such and such a similar instance (if a really similar instance can be found); if such and such an economic series has 'turned up' such and such another series will prob-

ably promptly follow, etc., etc. However, we must remember that purely empirical study of how men seem to have acted in the past will not necessarily solve the problem of how they will act in the future. Though it present empirical relationships that may seem as worthy of confidence as did 'Bode's Law' to the astronomers of one hundred years ago, in actual application such relationships and generalizations may, at any time, fail as signally as did that 'law' with the discovery of the planet Neptune. If the variables are related in a clearly causal manner, as for example size of crop and price per bushel, the statistical study of the relationship may be useful not only to the business man and the speculator but also to the economist. It may advance his understanding of both how and why things occur as they do. But if no explanation of why a functional relationship should exist can be supplied by other than a grossly ad hoc hypothesis, the 'generalization' may 'work' for years and then fail forever. And, of course, be theoretically quite unfruitful.

While, as we have noted, the 'laws' of a completely 'rational' economy cannot be formulated, the relations that would exist under specific instances of accurate forecasting of particular aspects of the future are, as illustrated in Chapter II, often easily uncovered. The natural line of approach to such problems is the logical and mathematical. If writers on 'deductive' economics-whether 'mathematical' or nonmathematical-formulated more definitely their underlying assumptions and pointed out more carefully how closely or distantly those assumptions corresponded to conditions as they actually exist, we should almost immediately see a distinct cleavage between studies that are primarily concerned with what would occur under specific hypothetical conditions and those that are primarily concerned with what usually does occur. In many problems two distinct 'solutions' would be substituted for an ambiguous single solution. For example, it is inevitable that any reasoning based on the assumption that present conduct tends to be accurately adjusted even to merely particular aspects of the future would often lead to results and solutions far from 'fact'. However, though such results would be recognized as solutions of different problems from those which economists have, in the past, believed they were setting themselves, they would hold their own important position in the scheme of economic thought.

Both types of investigation are desirable. They attack two distinct

aspects of the economic problem. In the effort to reach a complete understanding of the economic activities of mankind, they support each other; but not always in the manner in which they are usually supposed to do. In attacking a particular problem the usefulness of neither is dependent on both giving the same solution. The dual approach to a problem in which the two solutions are different may be as enlightening as in the case of a problem in which the two solutions are approximately the same.

The study of what would occur in a 'rational' economy has, of course, relatively more importance for him who would understand in order that he might change and improve 'the rules of the game' than for him who merely desires to win under the existing rules. Its importance is primarily theoretical and social rather than practical and individualistic. Its appeal is to the legislator and reformer rather than to the entrepreneur and speculator. In those fields in which forecasting of socially erratic data is attempted, even understandable generalizations will derive their social value not merely from the degree of regularity with which they have 'worked' in the past but also from the opportunity which they present to study the effects of the deviations of the actual from the strictly rational and to consider the theoretical and actual extent of the economic disturbances to which such deviations may lead.

Though it may well be that, for many problems concerned with economic reform, it is not necessary to know exactly what would occur under specified conditions of 'rationality', it will always be extremely helpful to keep clearly in mind the possible import of that hypothetical question. That the actual is only by accident ever the strictly 'rational' should never be forgotten. That the chief reason for the deviations of the actual from the 'rational' is the inability of human beings to foresee the future, let alone adjust the present to it, immediately suggests a whole group of possible economic reforms. The first has long been recognized. It involves a study of the problem of how to forecast ⁶ However, even the entrepreneur or speculator, if he be well advised, is careful not to stake too much on a generalization whose rationale neither he nor professional economists understands, unless it so regularly and obstinately gives an adequate description of the facts as to compel belief that it must be more than a mere empirical curiosity. Though he may not be interested in how men would act if their knowledge were superhuman and their logic absolute, he may well be somewhat chary of basing actual operations upon an inductio per enumerationem simplicem that is anything but free from exceptions.

the future. To the extent that the future can be foreseen it can be prepared for.

It is, of course, highly desirable to learn how things actually have occurred—and particularly how closely or distantly they have followed a 'rational' pattern; to study the problems of economic prediction even into the fields of 'irrational' sequences; to investigate not only the empirical relations between crop sizes and crop prices but also the empirical relations between long and short term interest rates. However, the mere fact that so much effort has already been expended on attempts to improve the quality of empirical forecasting strongly suggests the possibility that no such forecasting will ever be adequate to prevent even such gigantic world-wide economic disturbances as that from which we have but recently emerged.

A more hopeful approach is that of control. Instead of attempting to improve the quality of forecasting, we might attempt to make forecasting less necessary. Any economic system functions within a legal pale. Much can be done by mere legal elimination of conditions that make forecasting peculiarly important. However, mere legal restrictions will probably never usher in an economic millennium. If an economic society is to be a highly successful society it should function as a society. We must break away from the mysticism of 'laissez-faire'. Times without number 'the invisible hand' has led mankind into the economic ditch. Positive social action is absolutely necessary. In spite of the inevitable difficulties, the hope of the world lies in truly social, as opposed to merely individualistic, economic planning. To the extent that the future can be made, instead of awaited, the disturbing social effects of erroneous and inadequate individual forecasting may become a thing of the past. Of course, adequate public planning is extremely difficult. No system of 'trial and error' will take the place of brains. Without brains, public planning may be extremely dangerous. We must always remember that the essential objective of public planning should be to make legitimate and desirable private planning easier and not more difficult—unless we are willing to 'go the whole hog' and lapse into a communist state.

The succeeding chapters of this book suggest a number of ways in which the necessity and importance of particular types of individual forecasting could be reduced by mere prohibitory edict.

Perhaps the most conspicuous is suggested by the light that the irra-

tional relations found to exist between present long and future short term interest rates throws on the indefensible business custom of deliberately using long term bonds as short term investments. It is surely 'looking for trouble' to allow commercial banks to invest any large percentage of their deposits in long term bonds.

Probably the most important element of social economic control that the topics discussed in this book will inevitably bring into the reader's mind is the control of the general level of commodity prices. Though it be foreign to our present purposes to delve deeply into the various proposals that have been presented as solutions of that controversial problem, it is certainly not foreign to our purposes to emphasize the social benefits that would accrue from any reduction in the violence of price fluctuations.7

One of the most lamentable results of human inability to foresee the economic future is the 'anti-social' forecasting to which it gives rise. In his efforts to foresee what will occur, the individual tends to lose sight of what logically would occur. If he is to be personally successful in the speculative aspects of his business life, he must strive to forecast not only those occurrences of the external world that will influence his competitors but also how those competitors will react to such influences-and to their forecasts of how he and others will act. Inevitably he tends to forecast their future actions by means of their immediately preceding actions. In all his speculations he tends to 'follow the trend'. He hesitates to buy on a falling market or sell on a rising one. There is little more limit to his optimism than to his pessimism. When sugar, some years ago, went to twenty-five cents a pound

⁷ Director's Note: "It may be in order to suggest that the only 'control' of commodity prices which is economically sound is indirect control through elimination of the causes of violent price fluctuations. Such causes are, in the main, non-monetary in character-in spite of current beliefs to the contrary. Furthermore, even from the standpoint of the believer in monetary control of price levels, it is possible to demonstrate that such control is impracticable and wholly dangerous, if not absolutely impossible, with respect to the wholesale prices of basic commodities. Such prices must fluctuate individually and in a group, as part of the mechanism of economic balance and adjustment, even though 'costs of living' or other more general price indices are stabilized. The problem of avoiding long term secular changes in price levels must be clearly separated from that of control of short term fluctuations. It is desirable that the latter variations should not be accentuated (as by a vicious circle of credit contraction), but, within the limits required for ordinary economic adjustments, they are desirable rather than undesirable." M. C. Rorty.

at retail, housewives who had never speculated and never owned more than ten or twenty pounds of sugar began to buy it by the barrel.

But let us not end this introductory chapter on such a pessimistic note. Social consciousness and social conscience are growing. It is primarily the intellectual difficulties of the problem that keep us out of the promised land. And with the slowly spreading recognition of this fact a will to conquer these difficulties is arising. Can we not believe, with H. G. Wells, that "a time will come when men will sit with a volume of history or some old newspaper before them, and ask incredulously, 'was there ever such a world?'"

CHAPTER II

THE CONCEPT OF LONG TERM INTEREST RATES

Theoretically, a rate of interest is a measure of an exchange relation between present economic goods and future economic goods of so nearly the same kind as to be, for the purposes of the exchange relation, considered identical. In actual practice, the concept is almost invariably purely monetary. Though interest rates the world over are continually being expressed in terms of the convertible or inconvertible currencies of various countries and in terms of metallic monetary standards such as gold or silver, they are seldom expressed in terms of any such non-monetary commodities as wheat or cotton or even in terms of any 'composite' commodity whose price might be assumed to fluctuate with 'the general level of commodity prices'.

There are two essential elements in the interest concept. To derive any rate of interest from a stated set of facts, we must know (1) what is the ratio of the future quantity of money or other good, in which the rate is to be expressed, to the present quantity for which it is being exchanged, and (2) what is the length of time elapsing between the 'present' and 'future' of the particular problem. For example, if a lender gives up a present \$10,000 in exchange for a promised payment of \$11,025 two years from now and if he actually receives the \$11,025 at the expiration of the two years, the rate of interest which he will have received during the two-year period will be $10\frac{1}{4}$ per cent biennially, or $10\frac{1}{4}$ per cent per two-year period.

If the lender had obtained the \$11,025 at the end of the two-year period by lending \$10,000 for a payment of \$10,500 at the end of the first year, and then lending this \$10,500 for a payment of \$11,025 at the end of the second year, he would be able to say not only that he had realized 10½ per cent biennially during the two-year period but also that he had realized 5 per cent annually during each of the one-year periods. However, only by assuming that he had obtained the same

24

rate in each of the two years could he accurately describe the rate during the two-year period of the first case as 5 per cent per annum. Unless such an assumption be made, the 5 per cent figure is a mere 'average'. It tells us nothing about the rates which either the lender or the borrower should consider that he had actually realized in the separate years. For example, if the lender could have obtained only 4 per cent per annum for a one-year loan, he must logically consider that he is obtaining more than 5 per cent per annum for the second year. Moreover, this same reasoning applies in its fullness to even such an apparently clear-cut case as that in which a present \$10,000 is exchanged for \$500 payable one year hence and \$10,500 payable at the end of two years. If the lender could have obtained only 4 per cent per annum for a one-year loan, he must think of the \$500 payment as made up of \$400 interest and \$100 payment on the principal sum, and of the \$600 difference between \$10,500 and \$9,900 as one year's interest on a loan of \$9,900, 'Long time interest rates' are always mere 'averages' of short time rates.

At 5 per cent per annum, compounded annually, \$10,000 would, in two years, grow into \$11,025. The \$10,000 is the 'present value' of \$11,025 due two years hence with interest at 5 per cent per annum, compounded annually. The 'present value' of a specified sum of future money, due in a specified time, and upon the assumption of a particular uniform rate of interest until the payment of the future sum and a particular 'compounding period', is such a sum of present money as would grow into the specified future sum, in the specified time, at the specified rate of interest and with the specified 'compounding period'. The concept is purely mathematical. The question whether the assumptions are, in fact, legitimate or absurd has nothing to do with the problem of calculating the 'present value'. If 6 per cent per annum had been assumed as the rate of interest, instead of 5 per cent, the 'present value' of the \$11,025 due two years hence would have been \$9,812.22+ instead of \$10,000. If 100 per cent per annum had been the assumed rate, the 'present value' would have been \$2,756.25 instead of either \$9,812.22+ or \$10,000. Having made these preliminary observations, we are in position to discuss the meaning that must be attached to the 'vield' of a 'bond'.

In the modern economic world the commonest examples of 'long time interest rates' are furnished by the 'yields' of long term 'bonds'.

The typical bond is a promise to make a series of periodic 'interest' payments (usually one every six months) and a payment of a 'principal' sum at 'maturity'.\text{\text{'}} The 'yield' of a bond selling at a specified price is that rate of interest which, if it be assumed in order to obtain the 'present values' of the various future payments, will make the sum of such 'present values' equal the specified price of the bond.

If the reader will examine a 'bond table', he will find that if a 4 per cent \$100 bond, interest payable semi-annually, maturing in 2½ years, sells for \$97.68, it 'yield 5 per cent per annum'. However, since ordinary bond tables give, as the annual yield, twice the semi-annual yield, this '5 per cent per annum' means that the yield is 2½ per cent per six months' period, compounded semi-annually. But exactly what does this semi-annual yield of 2½ per cent mean? Like most mathematical questions, this may be correctly answered in many ways, but two seem peculiarly enlightening.

The price paid for the bond (\$97.68) equals the sum of the 'present values' of the five \$2 'interest' payments and the \$100 'principal' payment. The 'present value' of the \$2 interest payment due six months hence is $\frac{$2.00}{1.025}$ or, to the nearest cent, \$1.95. Similarly the present value of the \$2 interest payment due one year hence is $\frac{$2.00}{(1.025)^2}$, or \$1.90, and the present value of the interest payment due eighteen months hence is $\frac{$2.00}{(1.025)^3}$, or \$1.86. The present values, to the nearest cent, of the five \$2.00 interest payments are: \$1.95, \$1.90, \$1.86, \$1.81,

¹ The semi-annual payments made to the investor are semi-annual payments and nothing more. To term them 'interest payments' is somewhat misleading, but the terminology is so thoroughly established, and in general so well understood, that to speak of 'dividend payments' or to introduce some other term would probably be more disturbing than to keep to the established usage. Similarly the 'principal' of a bond is universally understood to mean the 'face' of the bond or the amount payable at maturity (excluding the last coupon) and not the amount originally lent or the amount later invested in the bond by any subsequent purchaser.

¹⁸ The usual practice of the makers of bond books is to calculate the yields in terms of the 'compounding period' and to assume that the compounding period equals the time between interest payments. This yield is then multiplied by the number of compounding periods in a year and presented as a yield per annum. This is a harmless convention—if understood. Of course 2½ per cent compounded semi-annually amounts to 100(1.0252-1) or 5.0625 per cent, and not 5 per cent, compounded annually.

\$1.77. Similarly, the present value of the principal payment of \$100, due in $2\frac{1}{2}$ years, is \$88.39. The total of these six present values is \$97.68, and this is therefore the price paid for the bond.

Another way of looking at the problem, which some persons find even more enlightening, is the following: the buyer pays \$97.68 for the bond. If he is to receive $2\frac{1}{2}$ per cent semi-annually on his investment, there will be owing to him, at the end of six months, $2\frac{1}{2}$ per cent of \$97.68, or \$2.44. However, he accepts \$2 (the 'interest' payment called for by the first 'coupon') and leaves the extra 44 cents with the borrower to draw $2\frac{1}{2}$ per cent semi-annually. The borrower then owes him \$97.68 + \$0.44, or \$98.12. This now bears interest at $2\frac{1}{2}$ per cent semi-annually. And so forth. The procedure can be clearly shown in a table

Value of bond at time of purchase (price paid) Accrued interest (2½ per cent of 97.68)	\$97.68 + 2 .44
Value of bond just before payment of first coupon	100.12
Payment of second coupon	2.00
Value of bond immediately after payment of first coupon	98.12
Accrued interest (2½ per cent of \$98.12)	+ 2.45
Value of bond just before payment of second coupon	100.57
Payment of second coupon	— 2.00
Value of bond immediately after payment of second coupon	98.57
Accrued interest (2½ per cent of \$98.57)	+ 2.46
Value of bond just before payment of third coupon	101.03
Payment of third coupon	— 2.00
Value of bond immediately after payment of third coupon Accrued interest (2½ per cent of \$99.03)	99.03 - - 2.48
Value of bond just before payment of fourth coupon	101.51
Payment of fourth coupon	— 2.00
Value of bond immediately after payment of fourth coupon	99.51
Accrued interest (2½ per cent of \$99.51)	+ 2.49

The amount the holder of the bond receives at maturity—\$100.00 principal plus \$2 interest (called for by the fifth coupon)

102.00

From the above illustrations the reader will notice that, though the present value of a distant future payment is of course less than the present value of a near payment, there is, in terms of dollars, only one 'yield' for the bond.² The 'yield' is a *single rate of interest* such that the present value of all the future payments, if they were calculated by assuming this rate (with the *semi-annual* compounding convention), would equal the price paid for the bond. It is a technical mathematical concept.⁴

In the illustration of the bond maturing in 2½ years, bought at \$97.68 and paying \$2 semi-annually, which we have been using, a naive and simple way of looking at the rate of interest would be to state that for two years the buyer receives 2.047 per cent semi-annually on his investment of \$97.68, * and then for six months receives 4.422 per cent semi-annually on his investment (still \$97.68). * Finally, at the expiration of the last six months, he also receives the return of his loan, namely \$97.68. Or, using the semi-annual compounding convention of the bond tables, the bond would be thought of as paying 4.094 per cent per annum for two years and then 8.844 per cent per annum for six months. However, neither of these figures is the 'yield' of the bond. The bond has only one yield, namely, 5 per cent per annum. The 'yield' is a species of 'average'.

² Assuming, of course, that the compounding period is stated—as, for example, quarterly, semi-annually, or annually. In our discussion we are assuming semi-annual compounding. See note Ia.

⁸ⁿ \$2 is 2.047+ per cent of \$97.68.

^{4 \$102 - \$97.68 = \$4.32,} which is 4.422 per cent of \$97.68.

⁵ The 'yield' per annum of a single payment loan (no 'interest' payments) is a simple function of the geometric averages of the various 'accumulation factors' for the separate compounding periods, whatever those factors or the rates of which they are functions may be assumed to be. For example, if the compounding period be a year, the 'yield' per annum of a single payment loan due in three years and carrying 4 per cent interest the first year, 5 the second, and 6 the third year is 100 ($\sqrt[8]{1.04 \times 1.05 \times 1.06}$ —1) or a shade less than 5 per cent.

On the other hand, the buyer, in making up his own mind as to what he would be willing to pay for the bond, might use, as his *personal* rates of interest, 4 per cent per annum for the first six months, $4\frac{1}{2}$ per cent for the next six months, then 5 per cent, $5\frac{1}{2}$ per cent, and 6 1/10 per cent. Using these particular rates he would find that he could afford to pay just \$97.68 for the bond. Four per cent, $4\frac{1}{2}$ per cent, 5 per cent, and 6 1/10 per cent would be the rates of interest that he considered appropriate and that he was using for the successive half-yearly periods, but they would not be the 'yield' of the bond. There would be only one 'yield' to the bond, namely, 5 per cent per annum ($2\frac{1}{2}$ per cent per half-year).

Though we have been emphasizing that there is only one 'yield' to a bond, it does not follow, as we have also suggested above, that because there is only one 'yield' there is only one rate of interest. Indeed, there is clear-cut evidence that this is not true. For many economic purposes the 'yield' of a bond must be considered as an average of various rates of interest used during successive future periods.

Variations in the 'yield' of loans of the same grade but of different maturities would seem not only to offer conclusive evidence that 'yield' should be thought of as an average, but also to throw some light on the *implicit* interest rates for the successive years. Both municipalities and corporations often offer 'serial' bonds with a large choice of maturity, the various maturities having different 'yields'. For example, on May 15, 1930, the City of Detroit, Michigan, offered to the public \$9,350,000 of 4½ per cent bonds of which not less than \$227,000 matured each May 15 from May 15, 1931 to May 15, 1960. The 'yields' at which the various maturities were offered were: 1931, 3.50 per cent; 1932, 4.00 per cent; 1933, 4.10 per cent; 1934, 4.20 per cent; 1935 to 1960 inclusive, 4.25 per cent.

If the above 'yields' were properly adjusted to the market, and if costs of underwriting are excluded, the City of Detroit could, on May 15, 1930, borrow for one year at 3.50 per cent. Unless the city would have had to pay, on May 15, 1931, more than 4 per cent to borrow (Footnote® concluded)

When there are 'interest payments' the 'average' is of a less simple and unweighted kind than in the case of a single-payment loan. But it is essentially an average,

⁶The different rates of interest for the successive periods covered by the bond must, of course, be such that they give the same total present value as would be obtained by assuming the uniform rate of interest called the 'yield'.

for another year, it would have been cheaper to make two separate successive loans, each running one year, than to borrow for two years at 4 per cent, as the second maturity proposes. Indeed, a little computation will prove that unless the city would have had to pay on May 15, 1931 as high a rate as 4.524 per cent, it would have been as cheap to borrow twice, each time for one year (once on May 15, 1930 at 3.50 per cent, and again on May 15, 1931 at 4.524 per cent). as it was to borrow once for two years at 4 per cent.7

If the schedule of 'yields' has any logical foundation it must mean that the Detroit municipal authorities or their banking advisers considered (whether quite consciously or not) 3.50 per cent a 'proper' rate of interest to use during the first year and 4.524 per cent a 'proper' rate to use during the second year. Assuming then these two rates of interest, we may from the 'yield' (4.10 per cent) of the bond maturing in three years (May 15, 1933) discover the implicit rate of interest assumed to be proper the third year. Proceeding in this manner we find that the 'yields' for the successive maturities of these Detroit bonds implicitly involve a set of interest rates for the successive years. These implicit interest rates are 3.500 per cent, 4.524 per cent, 4.311 per cent, 4.529 per cent, 4.475 per cent, 4.247 per cent, 4.250 per cent

7 If a 41/4 per cent bond having two years to run 'yields' 4 per cent, it sells for \$100.476. How such a bond may just as well be considered as giving a return of 3.50 per cent per annum during the first year and 4.524 per cent per annum during the second year, as 4 per cent per annum during both years, is shown in the following table (the error of one cent on a thousand dollar bond results from dropping decimals): Daine anid for the board

Price paid for the bond	\$100,476
Accrued interest (1.75 per cent of \$100.476)	1.758
Value of bond just before payment of 1st coupon	102.234
Payment of 1st coupon	2.125
Value of bond immediately after payment of 1st coupon	100.109
Accrued interest (1.75 per cent of \$100.109)	1.752
Value of bond just before payment of 2nd coupon	101.861
Payment of 2nd coupon,	2.125
Value of bond immediately after payment of 2nd coupon	99.736
Accrued interest (2.262 per cent of \$99.736)	2.256
Value of bond just before payment of 3d coupon	101.992
Payment of 3d coupon	2.125
Value of bond immediately after payment of 3d coupon	99.867
Accrued interest (2.262 per cent of \$99.867)	2.259
The amount the holder of the bond receives at maturity-\$100.00 principal	
plus \$2.125 interest called for by the 4th coupon	\$102,126

(for the seventh year and for each succeeding year up to May 15, 1960).

On the same date (May 15, 1930) that the City of Detroit offered to the public the bonds just discussed, the New York Central Railroad Company offered a series of 41/2 per cent Equipment Trust Certificates with the same maturities as the Detroit bonds.8 The 'vields' at which the various maturities were offered were: 1931, 4.00 per cent; 1932, 4.20 per cent; 1933, 4.35 per cent; 1934, 4.40 per cent; 1935-45 inclusive, 4.50 per cent. The interest rates for the successive years implicit in these 'yields' are: 4.000 per cent, 4.412 per cent, 4.668 per cent, 4.564 per cent, 4.949 per cent, 4.500 per cent (for the sixth year and for each succeeding year up to May 15, 1945). A comparison of these figures with the corresponding figures for the Detroit city bonds shows that the two series are not very similar. While the railroad offers a full one-half per cent per annum more on the one-year notes. its two-year notes yield only one-fifth per cent per annum more than the city's two-year notes. As a result of these facts the implicit rate of discount for the second year is actually less for the railroad than for the city. Both the railroad and the city implicit interest series are quite irregular. For example, the city series shows a sharp peak in the second year and the railroad series a sharp peak in the fifth year. For the third year the city series is lower than in either the second or fourth year while the railroad series is higher than in either the second or fourth year. Similarly, the fourth year shows a maximum for the city series and a minimum for the railroad series.

By June 1931 the New York Central Railroad was offering more of this same series of 4½ per cent Equipment Trust Certificates (dated May 15, 1930 and maturing serially May 15, 1932 to May 15, 1945). The 'yields' at which the various maturities were offered, however, were startlingly different from what they had been in May 1930. For the successive maturities the 'yields' were:

YEAR	PER CENT	YEAR	PER CENT	YEAR	PER CENT
1932	2.00	1937	3.625	1942	3.85
1933	3.00	1938	3.70	1943	3.90
1934	3.50	1939	3.70	1944	3.90
1935	3.50	1940	3.70	1945	3.95
1026	3 625	1041	3.80		

⁸ Except that May 15, 1945 is the last maturity of the New York Central bonds, and May 15, 1960 the last maturity of the Detroit bonds.

This series shows irregularities in the implicit interest rates quite similar to those inherent in the two preceding illustrations. For example, the implicit interest rate for the fourth year is much lower than that

for either the third or fifth year.

The successive short term interest rates that are implicit in the 'yields' of serial bonds at the issue prices seem only by accident ever to be other than quite erratic. For example, while the mere fact that the future was unknown might explain why the Detroit authorities were willing to pay higher rates than 3.50 per cent on the longer term bonds, if the payment of such higher rates were necessary to complete their financing with the maturities they desired, it can hardly explain the curious ups and downs shown by the sequence of the various implicit short term (annual) rates. Any rational decision as to what should be the 'vields' assigned to the successive maturities in a group of serial bonds logically involves a conscious forecast of successive short term interest rates. It does not seem possible that the erratic short term rates implicit in the Detroit serial bonds (or in either of the two New York Central emissions) were the result of a detailed and definite set of forecasts of future short term rates or even that they were the result of the superimposing of a forecast of the future financial condition of the city (or the railroad) on any reasonable forecast of general market short term rates. In practice, the city authorities probably decided first upon the maturities and the amount to come due on each maturity and then made a rough-and-ready guess of the various 'vields' that would suffice to sell the bonds. We cannot even say that the 'yields' are estimates by the issuing group of the current appraisal of future short term rates by the bond-buying public. The rates themselves offer almost conclusive evidence that no such appraisal is made by either the issuing group or the bond-buying public. The primary reason that implicit short term rates are nearly always erratic would seem to be that they are almost never the result of conscious forecasting. Though they are mathematically implicit in the various 'vields' no recognition is given to that fact.9

The reader must not, from the above discussion, assume that we consider 'yield' to be a useless concept. Though it must be thought of as an average, it is an average of which we cannot discover the individual items. The fact that a train makes a 100 mile run at an 'average' speed of 40 miles an hour is a piece of real information even if we know nothing about its speed at various times and places. We have seen that even the 'implicit' rates which may be obtained from the 'yields' of serial

If future rates for the highest grade of six-month obligations were being accurately forecast, a bond of the highest grade would, theoretically, realize in each future half-yearly period between coupons the same return as that carried by six-month obligations at the beginning of the period. The price of the bond must fluctuate in such a manner as to attain this objective. If in a tight short term money market in which six-month obligations of the highest grade are selling on a 7 per cent per annum basis, a 4 per cent bond be selling at par, its price at the end of the six-month period must have risen to \$101.50, if it is to show a return of 7 per cent per annum for the six-month period. This, of course, means a fall in the 'yield' during the six months. To preserve the theoretical relationship between present long term and future short term interest rates, the 'yields' of bonds of the highest grade should fall during a period in which short term rates are higher than the yields of the bonds and rise during a period in which short term rates are lower.10 Now experience is more nearly the opposite. The forecasting of short term interest rates by long term interest rates is, in general, so bad that the student may well begin to wonder whether, in fact, there really is any attempt to forecast.

However, an examination of the courses of 'time' and 'call' money rates offers almost conclusive evidence that forecasting is really attempted and that at least one reason it is so badly done is that it is so difficult. Both 'time loans' and 'call loans' are loans made to stock brokers with stocks and/or bonds as collateral. The only outstanding (Footnote® concluded)

bonds are largely mathematical deductions from economic material which cannot bear the strain of such analysis. Furthermore, even if we knew the forecasts of tuture short term rates implicit in the 'yield' of a bond, we would, for many purposes, prefer the average. Not only has it the advantage of brevity that is possessed by all averages, but it also has a lack of ambiguity that the individual items could not possess. We must remember that, while the 'yield' is the same for the buyer as for the seller of the bond, the individual estimates of future short term rates may be different for each buyer and seller in the market. Even the implicit rate deprivation of some form serial bonds are, at best, only short term rates in the minds of the corporatived from serial bonds are, at best, only short term rates in the minds of the corporation's officials. We must not forget that any particular maturity may fail to sell, or, if the series is sold as a unit, the prices that later emerge in the open market may be quite different from those of the original issue.

¹⁰ In general, though less accurately, the *prices* should *rise* in periods of high short time interest rates and *fall* in periods of low short time rates. Fall or rise in 'yield' is, of course, not necessarily associated with rise or fall in price. If a bond selling above par is to retain a constant 'yield' it must fall in price continually. In a similar manner a bond selling below par must rise in price.

difference between the two types of loan is the length of time they run. 'Call loans' run 24 hours; 'time loans' run from one to six months. Now, if it were actually known that money placed on 'call' for the next ninety days would yield exactly 6 per cent per annum, no bank or other lender would place money on 'time' for that period at a lower rate than 6 per cent per annum. Generally the lenders would insist upon a little more than 6 per cent to recompense them for having their funds in a less liquid condition. As periods of high call rates are periods of disturbed mionetary conditions, this differential would be greater when the next ninety days are to show high call rates than when they are to show low call rates.

In line with these facts, 90-day time loan rates would, theoretically, always be as high as or higher than an average (of the type described in note 5) of call rates for the succeeding ninety days. In periods preceding low call rates, 90-day time rates would range only a little higher than the average call rate for the next ninety days but, in periods preceding high call rates, time rates would range appreciably higher than the average call rate for the next ninety days. Moreover, unless the movements of the differential were very erratic, 90-day time rates would, week by week and month by month, show the same ups and downs as the average of call loan rates for the next ninety days. Furthermore, as they would move with an average of future call loan rates, they would reach maxima and minima distinctly earlier than call loan rates. In general, we would expect 90-day time loan rates to reach maxima and minima about 45 days (or 1½ months) before call loan rates. What are the facts?

In the first place, a comparison of 90-day time loan rates with averages of call loan rates for the next ninety days shows that the time rates usually range higher than the call averages, as theory would lead us to expect. However, the relation of the magnitudes of the differentials to the levels of the call rates is not what we might anticipate under good forecasting. When the future call averages are low, the time rates almost always range much higher than those averages; when the future call averages are high, the time rates range little if any higher than the averages. When the future call averages are extraordinarily high the time rates are commonly lower than the averages. Seldom do the time rates correctly forecast a period of extraordinarily high call rates. Even when they reach as high a maximum as

the call averages, the maximum usually occurs too late to constitute any forecast. Over and over again, in a period immediately preceding high call rates, it was possible to borrow on time and relend on call (during the 'time' period) at a large profit.

An examination of a chart on which are plotted 90-day time money rates and the averages of call money rates for each succeeding ninety days reveals little evidence of good forecasting. When 4- or 6-month time money rates are similarly compared with the proper averages of future call money rates, even less evidence of good forecasting is forth-coming. This applies not only to time money *levels* but also to the timing of movements and the positions of maxima and minima. Time loan rates fail to forecast call loan rates because neither borrowers nor lenders of money on 'time' know much more than nothing at all about the future course of call loan rates.

But this is not the whole story. Before the Federal Reserve system went into operation both call and time loan rates showed pronounced seasonal fluctuations. The existence of these seasonal fluctuations was almost universally recognized and their chief characteristics were fairly well known. It was admitted that both call money rates and time money rates contained two elements—a seasonal and a non-seasonal. Under such circumstances, would it not be natural to believe that the poor forecasting of call money rates by time money rates was the result of poor forecasting of the non-seasonal element in the call money rates and to expect that the time money seasonal would, upon examination, be found actually to forecast the call money seasonal?

At last we have arrived at something that was really known about future short time interest rates, and we find the theory that forecasting is necessarily attempted is at last upheld by the data. The time money seasonal shows unmistakable evidences of attempted forecasting of the call money seasonal, as may be seen by comparing the monthly seasonal for time money rates (Chart 20 11) with a three-month moving average of the monthly seasonal for call money rates. It is true that the lag of the three-month average call money seasonal is usually closer to one month than it is to the one month and a half which the theory would in general demand. However, the essential thing is that there is a distinct lag; the time money seasonal moves before the call money seasonal. 13

¹¹ For the figures see Appendix A, Table 22.

¹² For the figures see Appendix A, Table 21.

¹³ This may be clearly seen from Chart 20 where the two seasonals are presented.

Here we have evidence of definite and relatively successful fore-casting. The chief trouble seems to be, not that the time money seasonal does not move early enough, but that it does not move far enough. Its fluctuations are too small. Year after year the fluctuations of the three-month moving average of the call money monthly seasonal are greater than the fluctuations of the time money monthly seasonal. The borrowers and lenders of time money seemed loath to adjust their rates completely to what they knew of the call money seasonal. This is somewhat strange because profits could have been made by those who noticed the discrepancy. Before the Federal Reserve system went into effect stock brokers should have borrowed more heavily on call for the first eight months of the year and more heavily on time for the last four months of the year.

If, from call and time loan rates we eliminate the seasonal fluctuations, and then compare the two resulting series, we find the forecasting even worse than for the two original, unadjusted series. Bankers and brokers acted as if they knew virtually nothing about future cyclical or other non-seasonal movements of call money rates. They did know something about the seasonal fluctuations. What they knew about they were able to forecast, at least approximately; what they did not know about they were unable to forecast at all—except by accident.

In much of the preceding discussion of the relations that, theoretically, would exist between long and short term interest rates we have implicitly made one fundamental assumption which in actual practice may or may not be warranted: the assumption of payment. In connection with any loan there are always two rates of interest which may or may not be the same: first, there is the promised or hypothetical vield, which can be calculated at the time the loan is made or the bond is purchased, but which may never materialize; second, there is the realized or actual yield which cannot be known until the last payment has been made. If a 4 per cent bond, maturing in 30 years, be purchased at 90 and held for 221/2 years, and if, during that time, forty-five \$2.00 payments be made but no payments of any kind thereafter, the promised yield is 4.62 per cent but the realised yield is zero per cent. Only on the assumption of absolute certainty of payment is it legitimate to say that the promised yield of a bond should logically be an accurate forecast of (completely determined by) the course of

future short term interest rates. In actual practice, a forecast that is quite distinct from any forecast of short term interest rates is introduced into the determination of the *promised* yield—the forecast of the degree of certainty of the future payments. The *realized* yield is not, of course, a forecast at all, as it does not come into existence until after the event.¹⁴

Realized yield concerns the real though unknown future; promised yield concerns a hypothetical future which may or may not materialize. It is a mere forecast. However, though the realized yield has, in this sense, a reality that the promised yield does not possess, it is the promised yield that is almost invariably referred to when the word 'yield' is used without designating its meaning. The 'yield' of a bond is the promised yield. This fact must never be forgotten. Its recognition clears up many theoretical difficulties.

In calculating the 'vield' of a bond the assumption is made that all future interest payments and the principal payment will be made on the dates specified in the bond. Of course, such an assumption is necessarily absurd in the case of a perpetuity—such as Canadian Pacific debenture 4's or any 'preferred' stock. The chance that all future payments will be made is negligibly small for any extremely long term bond, such as West Shore 4's of 2361. The importance of this condition from a practical standpoint may, of course, easily be overemphasized. If West Shore 4's of 2361 are bought to yield 5 per cent per annum to maturity, the price paid will be \$80.00 for each \$100 face value of the bond. This \$80.00 present payment may be distributed as follows: \$73.23 is paid for the interest payments of the first fifty years, \$6.20 for the interest payments of the next fifty years, and only 57 cents for all succeeding interest payments and the payment of the principal sum —on the assumption of a uniform interest rate of 5 per cent per annum for all future inter-coupon periods.

'Certainty of payment' is for most purposes a purely psychological concept. Only to the extent that it is an opinion in the minds of buyers and sellers can it affect the price of bonds. Security in the opinion of buyers and sellers is commonly spoken of as though it were security in fact. Security in fact can be known only when the future has be-

¹⁴ In the light of promised and realized rates of interest, the concept of 'pure interest' (as a promised rate) is seen to be a merely psychological concept. The 'pureness' is necessarily a forecast rather than a fact.

come the past. As the future cannot be known security is always relative; absolute security is a pseudo idea. An actual bond (before maturity) can never be absolutely secure in fact. So many buyers and sellers of bonds may think of it as absolutely secure that its market price may act as though it were extremely (though not necessarily 'absolutely') secure. In general, the more buyers and sellers who consider a bond to be absolutely secure or nearly so, the lower will be its 'yield'. There is, however, no point at which one can stop and say 'this is absolute security'.

How arbitrary and unreal, from an economic standpoint, may be the mathematically necessary assumption of payment is illustrated by the variation in the 'yields' of bonds containing identical promises as to future payments—that is, bonds carrying the same 'coupon rate' and having the same maturity. We immediately realize that, for bonds having the highest 'yields', such 'yields' are merely 'promised' and will probably never be 'realized'. From an economic standpoint they are primarily indexes of lack of confidence in the certainty of the future payments rather than indexes of how those payments would at present be valued—if there were perfect assurance that they would be paid on the promised dates.

The assumption of payment (which must be made before the 'yield' can be calculated) is seen to be, in such cases, if not an assumption demonstrably contrary to fact, at least of very dubious validity. 'Promised' yield is not necessarily 'realized' yield.

The concept of 'pure' or 'riskless' interest is metaphysical. The practical contrast is not between 'pure' and 'impure' but between 'promised' or 'expected' and 'actual' or 'realized'. It is quite quixotic to attempt to divide the 'promised' (or even 'realized') return from a bond into 'interest' and 'profits' or something else. Moreover, such a division is unnecessary for either theoretical or historical treatment. Bonds and other interest-bearing obligations may be classified according to their ('promised') yields without introducing the concept of 'pure interest', and the economic significance of such yields may be studied without deciding what the rate of 'riskless' yield would be. All rates of interest are of economic importance. The movements of the yields of second grade bonds sometimes have a much more direct bearing on changes in economic conditions than the movements of the yields of first grade bonds. For example, the yields of bonds of superlative

quality may actually *fall* during a period of great business disturbance and distrust—while the yields of second grade bonds are *rising*. The existence at any time of an abnormally large volume of bonds selling at prices that show extremely high 'yields' is almost certain to be of great economic significance, even though it is not necessarily any evidence that 'long term interest rates as such' are extremely high.

Sometimes distrust of all securities becomes so great that 'investment' deteriorates into 'hoarding'. Many erstwhile investors now demand actual cash, in extreme cases actual specie. Even the highest grade bonds are no longer acceptable. The hoarder demands what he believes to be 'absolute security'. He will accept zero or even negative interest (rent of a safe deposit box). However, such a condition differs only in degree and not in kind from the more commonly occurring flight from the lower grade long term securities into the highest grade short term obligations.

Generally speaking, the relative economic importance of securities of various grades varies with their total market values. If any large proportion of the total market value of securities outstanding in a community is by most persons considered almost absolutely safe, fluctuations in the yield of those securities are, of course, of great economic importance. On the other hand, in a community where there are almost no investments that are generally considered superlatively safe, fluctuations in the yield of such investments are of only academic interest. While movements of the yield of securities considered superlatively safe might be of great importance in a community such as England in the last years of the nineteenth century, it would have little significance in a community such as California in the 1850's. When money in California was commonly lending at 18 to 24 per cent per annum, some few individuals were undoubtedly satisfied to invest in securities yielding them less than 6 per cent per annum. Fluctuations in the yield of such securities were of little economic significance in that community at that time.

The destructive effects of a fall in the prices of bonds are not necessarily dependent on whether the bonds were originally (before the fall) considered high or low grade. The chief reasons that usually make a fall in the prices of high grade bonds more serious than a fall in the prices of low grade bonds are two. In the first place, the total market value of such bonds outstanding (before the fall) is usually

much greater than the total value of the low grade bonds. In the second place, banks usually invest more heavily in high grade bonds than in low grade bonds, and anything that affects the solvency or even liquidity of the banks is always peculiarly serious. In periods when banks are carrying a large volume of low grade bonds, a fall in the prices of those bonds may be almost as serious as a fall in the prices of high grade bonds.

Not only the economic importance of the yield of investments that are considered superlatively safe but also the yield itself is affected by changes in the volume of such securities available. The yields of securities of even as high a grade as United States Liberty Bonds and Treasury Certificates have in the past often been unmistakably responsive to the larger fluctuations in the amount outstanding. This is not, to any appreciable extent, the result of a general belief that certainty of payment is affected more than negligibly by such fluctuations. It merely illustrates the fact that an increase in the volume of even such securities does not automatically create new purchasers—except at lower prices—any more than an increase in the supply of a commodity creates new purchasers—except at lower prices.¹⁶

Furthermore, the volume of investment funds demanding the highest degree of safety is affected by changing opportunities for earnings in less secure investments. The relation of the yield of the highest grade investments to the yield of other investments is always important. Seldom do many persons demand security at any price. Usually, many are willing to take risks with the hope of larger returns than they could obtain from investments that they consider 'absolutely secure'. If the speculative opportunities connected with investments that are believed to have some element of risk seem to increase, the proportion of the investment funds of the country that will demand 'absolute security' will probably decline. The yield of 'absolutely secure' investments will advance. If the opportunities connected with investments recognized as having some element of risk seem to decline or if the risks seem to have increased, the proportion of the investment funds of the country demanding great or 'absolute' security will probably increase.

The evil effects of a pronounced *rise* in the yield of any class of ¹⁵ In spite of partial offsetting by the possibility of 'discounting' at the Federal Reserve banks.

bond are, for some purposes,¹⁶ more easily understood if we speak, as we did a few paragraphs back, in terms of a *fall in price*. For example, the great damage is done by the fall in the *prices of bonds already on the market*, not by the rise in the rates of interest that corporations that wish to engage in new borrowing will have to pay. The effect of the fall in the prices of outstanding obligations is in the present. The effect of the higher yields of the new bonds is in the future. A fall in the prices of bonds actually outstanding immediately affects the financial position of all their holders, while the drain on the resources of a borrowing company, that results from a rise in the rate it must pay on a new issue, will extend over the life of the bond. The first has a concentrated and immediate effect; the effect of the second is spread out thinly over many future years.

A pronounced fall in the price of bonds actually outstanding is serious not only because it destroys present purchasing power, but also because it leads to one of the vicious circles of the business cycle. If the bonds have been used as collateral for loans, that collateral must be increased or a part of the loan must be repaid. If it be repaid by selling some of the bonds, such 'distress selling' tends to lower the price of the bonds just as directly as does the forced selling of any commodity. Contrary to ordinary economic assumptions, things are being sold, not because they are dear, but because they are cheap.'

From a theoretical standpoint it would seem that major fluctuations in the yields (or prices) of bonds of the highest grade should be relatively more important in periods of prosperity than in periods of de
10 In discussing the action of bonds in the business cycle it sometimes seems easier to think in terms of price than in terms of yield. Why should we not substitute price for yield in all our discussions? Probably the simplest way to answer this question is to point out that 'yield' may often be a better way to measure price than prices themselves. It measures a corrected rather than a raw price. It may be considered as the reciprocal of an adjusted price—a price that has been corrected for varying coupon rates and maturities. Though it is highly desirable to remember the implications involved in 'yield', those implications do not need to frighten us from using the concept. It is not only extremely useful but almost necessary.

¹⁷ This vicious circle is, of course, made still more vicious by those who sell, because they become afraid that prices may go so low that they would eventually be forced to sell—or merely because they believe prices are going lower.

Economists have usually underemphasized the importance of price movements as compared with price levels in inducing purchases or sales. In the speculative markets, commodities and securities are as often bought because their prices have been going up, or sold because their prices have been going down, as because their prices are low or high.

pression. As bonds of the highest grade are those bonds which are generally so considered, there are naturally more of them in periods of prosperity than in periods of depression. A rise in the yield of bonds of the highest grade occurring in the midst of a period of prosperity should be of greater significance than a fall in their yield in a period of depression. Of course this reasoning is somewhat complicated by the fact that a rise in yield (or fall in price) always exerts positive pressure, while the effects of a fall in yield (or rise in price) are largely negative; it creates opportunities rather than necessities or compulsions. An examination of the historical facts strongly supports the thesis that a rise in the yield of interest-bearing obligations of the highest grade—whether they be of long or short maturity—has greater power to terminate a period of prosperity than has a fall in their yields to initiate such a period.

We have seen that, if 'promised' rates were 'realized' and if long term rates accurately forecast short term rates, it would be relatively unimportant to an investor whether he bought long or short term securities. If he bought short term when he really needed long, he would have to be continually reinvesting; and, if he bought long when he needed short, he would have to sell. But both the short and the long term returns 'realized' would be the same whether they were obtained from a succession of short term investments or from a long term investment with possibilities of sale. The price fluctuations of a long term bond would be exactly sufficient to adjust the successive implicit short term rates of the bond to the future rates for future short term loans—no more and no less. The price fluctuations of the bond would therefore be unaffected by the interval to maturity. A 4 per cent bond selling at \$90 must rise to \$91.15 in six months if the return is to be 7 per cent per annum for those six months-whether the bond matures in five years or a century.

Of course, bond *prices* do not move this way in the actual market. Not only do they tend to fall rather than rise in periods of short term stringency, but also the more distant their maturity the greater are their *price* fluctuations. The *price* fluctuations of the highest grade bonds maturing in ten years tend to be appreciably greater than the price fluctuations of those maturing in two or three years. But the increase in *price* fluctuation resulting from an increase in time to maturity is not as great as it would be with a constancy of *yield* fluctuation. The

longer the maturity the smaller the yield fluctuations—though, because the *price* fluctuations *increase* with an increase in time to maturity (rather than remain constant), the decrease in extent of fluctuation in yield with lengthening of time to maturity is not nearly so great as it would be if the long term rates accurately forecast the short term rates. ¹⁸ The longer the maturity of a bond the greater are the *price* fluctuations, and hence the greater are the fluctuations in the actual short time return realized by buying at the beginning and selling at the end of the short time period. If we define the 'ninety-day yield of a bond' on a particular date as the return that would have been realized if the bond had been bought on that date and sold (without commissions) ninety days later, we find that the 'ninety-day yields' of even the highest grade long term bonds have usually fluctuated much more violently than ninety-day time money rates—usually more violently than even ninety-day averages of call money rates.

An important reason why bond yields (and prices) fluctuate as much as they do is that few buyers of long term bonds buy them with the intention of holding them to maturity. They expect to sell them at some indefinite time in the future. Now to determine what the selling price will be at any particular future date requires something more than even absolute assurance that all interest payments and the principal payment will be met on the dates specified in the bond, and exact knowledge (if it were attainable) of future short time interest rates for the entire life of the bond. The buyer must know what will be the opinion of buyers and sellers concerning these matters on that future date—and whether the potential future buyers will also be not only willing but able to pay. They can not be forced to buy. Unlike short time loans, long time loans are not 'self liquidating'. Prior to its distant maturity, nobody has to buy or retire a particular long term bond at a particular time or go into bankruptcy. This is why it is so peculiarly inappropriate for banks to place any large percentage of their demand funds in long term bonds.

The fact that long term bonds are bought and sold and not necessarily or even usually held to maturity makes us realize again the artificiality of the concept of security in the case of 'promised' yield. Mere length of time introduces an element of real insecurity in all long ¹⁸ The movements of time and call money rates offer an exception to this generalization. Time money rates have fluctuated *less* than they would have if they had accurately forecast call money rates.

term loans. Only short term loans can be even imagined to be 'absolutely secure'. Who can make even a good guess as to what a particular long term bond will be selling for two years from now? Yet such a guess is an essential element of the 'security' of any short term loan that is to be made by buying the long term bond now and selling it two years hence.

We have, so far in this chapter, been discussing the subject of long time interest rates without asking the question: how much longer term is one loan than another? For a study of the relations between long and short time interest rates, it would seem highly desirable to have some adequate measure of 'longness'. Let us use the word 'duration' to signify the essence of the time element in a loan. If one loan is essentially a longer term loan than another we shall speak of it as having greater 'duration'.

Now the promise contained in a loan is either a promise to make one and only one future payment or a promise to make more than one future payment. If two loans are made at the same rate of interest, and if each loan involves a promise to make one future payment only, the loan whose future payment is to be made earlier is clearly a shorter term loan than the other. For example, if \$100 be lent for one year at 5 per cent per annum, the only payment to be \$105 at the end of the year, and if another \$100 be lent for two years at 5 per cent per annum, the only payment to be \$110.25 at the end of the two years, the first loan is clearly a shorter term loan than the second. If, on the other hand, either or both loans involve a promise to make more than one future payment, or if the rates of interest ascribed to the two loans are not the same, it may be extremely difficult to decide which is essentially the longer term loan.

It is clear that 'number of years to maturity' is a most inadequate measure of 'duration'. We must remember that the 'maturity' of a loan is the date of the last and final payment only. It tells us nothing about the sizes of any other payments or the dates on which they are to be made. It is clearly only one of the factors determining 'duration'. Sometimes, as in the case of a low coupon, short term bond, it may be overwhelmingly the most important factor. At other times, as in the case of a long term, diminishing annuity, its importance may be so small as to be almost negligible. Because of its nature, length of

time to maturity is not an accurate or even a good measure of 'duration'. 'Duration' is a reality of which 'maturity' is only one factor.

Whether one bond represents an essentially shorter or an essentially longer term loan than another bond depends not only upon the respective 'naturities' of the two bonds but also upon their respective 'coupon rates'—and, under certain circumstances, on their respective 'yields'. Only if maturities, coupon rates and yields are identical can we say, without calculation, that the 'durations' of two bonds are the same.

If two bonds have the same maturity and the same yield but one has a higher coupon rate than the other, the one having the higher coupon rate represents an essentially shorter term loan than the other. For example, if each bond is selling on a 5 per cent basis, a 6 per cent bond maturing in 25 years necessarily represents an essentially shorter term loan than a 4 per cent bond maturing in 25 years. This may easily be seen by comparing a \$400 face value 6 per cent bond maturing in 25 years with a \$500 face value 4 per cent bond maturing in 25 years. On both bonds the total of all future payments, both principal and interest, is \$1,000. But on the 6 per cent bond the payments are \$12 each six months for 241/2 years, and then a final payment of \$412, while on the 4 per cent bond the payments are \$10 each six months for 241/2 years, and then a final payment of \$510. It is plain that the \$1,000 is being paid earlier on the 6 than on the 4 per cent bond. Though both have the same 'maturity', the 6 per cent bond represents a loan of shorter 'duration' than the 4 per cent bond.

The difference in 'duration' of the two bonds is manifest in their prices. As the payments are made earlier on the 6 per cent bond, its price (if the 'yields' of the two bonds are the same) is necessarily higher. For example, as each bond 'yields' 5 per cent, the price of the \$400 face value 6 per cent bond will be \$456.72, while the price of the \$500 face value 4 per cent bond will be only \$429.10.

We see, then, that if two bonds have the same yield and the same maturity but different coupon rates, the bond having the higher coupon rate represents the loan of shorter 'duration'. Instead of examining in a similar manner the case in which the two bonds have the same coupon rate and the same maturity but different yields, and the case in which they have the same coupon rate and the same yield but different maturities, we shall now consider directly the general problem of how to measure 'duration'. Let us approach this problem by considering

the maturity of a bond as a function of the maturities of the separate loans of which it may be said to consist.

It would seem almost natural to assume that the 'duration' of any loan involving more than one future payment should be some sort of a weighted average of the maturities of the individual loans that correspond to each future payment. Two sets of weights immediately present themselves—the *present* and the *future* values of the various individual loans.

Future value weighting seems clearly inadmissible. It gives absurdly long 'durations'. If \$2,000 be lent at 5 per cent per annum in the form of two loans, one of \$1,000 at 5 per cent per annum ¹⁰ payable in one lump sum of \$1,050 at the end of one year, and one of \$1,000 at 5 per cent per annum payable in one lump sum of \$131,501.26 at the end of 100 years, the 'average maturity' or 'duration' of the two loans, if calculated by taking an arithmetic average of the two maturities, using the present values as weights, is 50½ years. If the future values (\$1,050 and \$131,501.26) be used as weights, the 'average maturity' is found to be more than 99 years.

In this illustration, the present values (or amounts lent) were equal. Let us examine a case in which the future values are equal. If \$959.98 be lent at 5 per cent per annum in the form of two loans, one of \$952.38 at 5 per cent per annum payable in one lump sum of \$1,000 at the end of one year, and one of \$7.60 at 5 per cent per annum payable in one lump sum of \$1,000 at the end of 100 years, the 'average maturity' or 'duration' of the two loans, if calculated by taking an arithmetic average of the two maturities, using the present values (\$952.38 and \$7.60) as weights, is about 21½ months. If the future values be used as weights, the average maturity is 50½ years.

How absurd it seems to think of a loan of \$2,000 made up of two loans each of \$1,000, one maturing in one year and one in 100 years, as having a 'duration' of over 99 years. And how absurd to think of a loan of \$1,000 made up of two loans, one of \$952.38 maturing in one year and the other of \$7.60—less than 1 per cent of the larger loan—maturing in 100 years, as having a 'duration' of 50½ years.²⁰ ¹⁹ In the present discussions, we have not followed the 'semi-annual compounding' convention. For simplicity of treatment, we have assumed throughout that payments are made annually and compounding is done annually.

20 If one billion dollars were to be lent as a single payment loan at 5 per cent per annum for one year, and one cent as a single payment loan at 5 per cent per annum But are not the results obtained by using *present* values as weights also open to criticism? If the 'durations' obtained by using *future* value weighting seem unmistakably too long, does not at least one of the 'durations' obtained from *present* value weighting seem very short?

Moreover, if the average maturity of two equal future payments be assumed to be the arithmetic average of the two maturities with the present values of the future payments as weights, some seemingly paradoxical results may appear. For example, if the yield be 5 per cent and if the two future payments be \$1 at the end of one year and \$1 at the end of 10 years, the average maturity will be about 41/2 years. If the dates of payment be one year and 27 years, the average maturity will be about 6.7 years. But if they be one year and 50 years the average maturity will be only 5.1 years, and if the dates of pavment be one year and 100 years the average maturity will be appreciably less than 2 years! In this particular illustration, the average maturity has a maximum when the second payment is made in about 27 years! However, these results do not seem so ridiculous if we remember that, as the date of payment of the second \$1 becomes arithmetically more and more distant, its present value, or the amount actually lent, becomes geometrically smaller and smaller. In the limiting case, in which the second \$1 is paid at infinity, the 'average maturity' is one year, but the amount of the loan for which the second dollar is to be paid is zero. The argument for present value weighting seems strong.21

(Footnote 20 concluded)

for 520 years, future value weighting would give the composite loan a duration of about 260 years.

21 The actuaries have proposed and solved a problem that must not be confounded with ours. It is termed the problem "of finding the equated time for a number of sums due at different times, or, in other words, the average date at which, on the basis of an agreed rate of interest, all the sums might be paid without theoretical advantage or disadvantage to either party" (British) Institute of Actuaries Text-Book, Part I, pp. 24 and 25.

The answer is a date such that, if the *sum* of all the *present* values of the different future payments was compounded to that date at the rate of interest used to obtain those individual present values, it would amount to the sum of all the future payments. This is a neat and symmetrical answer to the problem proposed, and it gives better results in practice than the common method of 'equating time', which is based on *future* weighting, but it seems an unreal answer to an unreal question. It is quite logical in assuming that the present value of the single future payment must equal the present value of the sum of the individual future payments, but it seems to beg the question when it also assumes that the *future* value of the single payment at the date of its payment must equal the sum of the individual

Now, if present value weighting be used, the 'duration' of a bond is an average of the durations of the separate single payment loans into which the bond may be broken up. To calculate this average the duration of each individual single payment loan must be weighted in proportion to the size of the individual loan; in other words, by the ratio of the present value of the individual future payment to the sum of all the present values, which is, of course, the price paid for the bond.²²

Let F = the 'face' value of the bond in dollars, i.e. the 'principal' sum in dollars;

I = the number of dollars paid semi-annually, i.e. the number of dollars called for by one 'coupon';

P = the number of dollars paid for the bond, i.e. the 'price' in dollars;

n = the number of half years the bond has to run, i.e. the number of half years to 'maturity';

R = the semi-annual *rate* of the 'yield', e.g. if the bond is selling to yield 4 per cent per annum, R = 1.02 (under the semi-annual convention of the bond tables);

Q = the ratio of the face value of the bond to a coupon payment, i.e., $Q = \frac{F}{I}$;

D = the 'duration' of the bond—in half years;

Then

$$D = \frac{\frac{I}{R} + \frac{2I}{R^2} + \frac{3I}{R^3} + \ldots + \frac{nI}{R^n} + \frac{nF}{R^n}}{\frac{I}{R} + \frac{I}{R^2} + \frac{I}{R^3} + \ldots + \frac{I}{R^n} + \frac{F}{R^n}}$$

(Footnote 21 concluded)

future payments each taken at its particular date of payment. This assumption overweights the time importance of distant payments.

28 In terms of the symbols of the next paragraph.

$$P = \frac{I}{R} + \frac{I}{R^2} + \frac{I}{R^3} + \dots + \frac{I}{R^n} + \frac{F}{R^n} = \frac{I}{R-1} - \frac{\frac{I}{R-1} - F}{R^n}$$

Summing the terms in the numerator, and in the denominator, of this fraction and substituting QI for F, we find that

$$D = \frac{R}{R-1} - \frac{QR + n(1+Q-QR)}{R^{n} - 1 - Q + QR}.$$

An examination of this expression for the value of D shows that the larger the value of Q the greater the duration; in other words, the smaller the 'coupon' payments are relatively to the face value of the bond the greater is the duration of the bond. Furthermore, the larger the value of R the smaller the duration. D increases with n, though, if R be greater than $1+\frac{1}{Q}$, in other words if the bond be selling below par, D reaches a maximum before n reaches infinity, declining gradually thereafter to $\frac{R}{R-1}$, the value reached when n equals infinity.

When Q = 0, in other words, when the series of future payments constitutes a mere annuity without any 'principal' payment whatever,

 $D = \frac{R}{R-1} - \frac{n}{R^n - 1}.$ When Q equals infinity, in other words, if the loan is single payment, D = n.

If R = 1, in other words if the 'yield' of the bond be zero,

$$D = \frac{\frac{n^2 + n}{2} + nQ}{\frac{n + Q}{n + Q}}.$$
 Unity is the limiting value of D as R approaches infinity.

$$=\frac{R}{R-1} - \frac{QR + n(1+Q-QR)}{R^n-1-Q+QR}$$

$$=\frac{R(R^n-1-Q+QR) - (R-1)[QR + n(1+Q-QR)]}{(R-1)(R^n-1-Q+QR)}$$

which, when 1 is substituted for R, takes the indeterminate form of $\frac{0}{0}$. However, the fraction may easily be evaluated by the ordinary methods of the calculus. The first derivative of the numerator divided by the first derivative of the denominator is, if R = 1, still indeterminate. However, taking second derivatives, we get $n (n+1) R^{n-1} + 2nQ$

 $n (n+1) R^{n-1} + 2Q - n (n-1) R^{n-2}$

Letting R = 1 in this expression we obtain the value for D given in the text,

When $n=1,\,D=1.$ When n equals infinity, as when a bond (such as Canadian Pacific debenture 4's) has no maturity date, $D=\frac{R}{R-1}$.

But, if R be greater than $1+\frac{1}{Q}$, in other words if the bond be selling below par, D will attain a maximum value before n reaches infinity. ²⁴ However, unless R be very large, the value of n making D a maximum will be large and the maximum value of D will be very little greater than the value associated with an infinite value for n. ²⁶

A short table presenting the relations between time to maturity and duration, for a 4, a 5, and a 6 per cent bond each selling at par, will illustrate the ordinary characteristics of the duration concept (p. 51).

The concept of 'duration' throws a flood of light on the fluctuations of bond yields in the actual market. Not merely do the yields of long term bonds tend to fluctuate much less violently than the yields of short term bonds or the rates on short term loans, such as are represented by commercial paper, but the relation between maturity and violence of fluctuation in yield is much as we would expect to find it from our analysis of the nature of 'duration'. While there is a great difference between the amplitude of the fluctuations in yield of bonds of "4 The explanation of seeming paradoxes of this type has already been discussed.

²⁶ Equating to zero the derivative of D with respect to n leads to an insoluble equation; but an approximate solution is that, for other than extremely large values of R,

D will reach a maximum when n is a shade greater than $\frac{R}{R-1} + \frac{QR}{QR-Q-1}$. For example, if a 4 per cent bond be selling on a 6 per cent basis (3 per cent per half year on the semi-annual compounding convention), $\frac{R}{R-1} + \frac{QR}{QR-Q-1}$ equal 134½, and this is approximately the value of n (in half years) that will, in

equal 134½, and this is approximately the value of n (in half years) that will, in fact, make D a maximum. But this maximum value of D, when n equals 134½, is less than 34½ half years and when n equals infinity D equals 34½ half years, a decline of less than two months in its value.

A higher yield will, of course, give a maximum value for D with a smaller value for n and the difference between the maximum value of D and its value when n equals infinity will be increased. For example, if the 4 per cent bond be selling on an R $\overline{\text{OR}}$

8 per cent basis, — + — will equal 78. When D is actually a maximum, n lies between 78 and 79 half years. The maximum value of D is then slightly less than 27½ half years but the value of D when n equals infinity is only 26 half years, a difference of a little more than half a year,

DURATION IN YEARS 26

YEARS	4 PER CENT	5 per cent	6 PER CENT	
TO MATURITY	BOND	BOND	BOND	
1	.990	.987	.985	
3	2.857	2.823	2.790	
6	5.393	5.257	5.126	
10	8.339	7.989	7.662	
15	11.422	10.727	10.094	
25	16.026	14.536	13.254	
50	21.970	18.765	16.273	
100	25.014	20.353	17.120	
Infinity	25.5	20.5	17.167	

extremely short maturity and of those having ten years or so to run, and an appreciable difference between the fluctuations in yield of the latter and of bonds having forty-five or fifty years to run, there is virtually no discernible difference between the action of these last bonds and the action of those having a hundred years or more to run.

The concept is, of course, full of theoretical difficulties. It is easy to think of the 'duration' of a bond as increasing while the time to maturity is decreasing, if 'long term interest rates' are declining during the period. It would seem only logical, for the purposes of our problem, to think of time not in terms of years or months but in terms of its relation to the growth of capital. But in all our illustrations we have, for purposes of computation, used as 'yield' the yield of the individual bond whose 'duration' we were discussing. This amounts to assuming that 'duration' is lengthened by mere increase of security as well as by a true decrease in the 'preference for present over (assured) future money'.

But this assumption leads us into one of the quagmires of 'pure' interest. Are the promised future payments of a low grade bond really

²⁶ If the interest were payable and compounded annually, instead of semi-annually, the durations would be slightly greater than those given above, the difference increasing with increases in the time to maturity. For infinite maturities they would be one-half year greater, that is 26, 21 and 173/6 years instead of 251/4, 201/2 and 17 1/6 years.

If the ordinary concept of 'equated time' (see note 21) were used to calculate duration, no maximum values would appear. A bond with an infinite maturity like British Consols or Canadian Pacific debenture 4's would have an infinite duration. A 6 per cent bond selling at par and maturing in 10 years would have a duration of 7.95 years (instead of 7.66 as in the text table), if it matured in 25 years its duration would be 15.50 years (instead of 13.25), for 50 years its duration would be 23.45 (instead of 16.27), for 100 years 32.92 (instead of 17.12), and if it matured in 200 years its duration would be 43.39 years instead of less than 17 1/6 years as in the text table.

discounted at higher rates than the promised future payments of a high grade bond, or is the difference in 'yield' traceable not to any difference in rates of discount but to a difference in what is discounted, this being, in the case of an ultra high grade bond, the actually promised payments, but, in the case of a low grade bond, the mathematical 'expectations' that result from multiplying each promised payment by the assumed probability that it will be met? ²⁷

Another difficulty connected with the problem will be merely mentioned. We have made the assumption that the rate of interest for each future six month period is the rate corresponding to the 'yield' of the bond. Now the reader realizes that this assumption may easily be contrary to fact. However, we drew attention, earlier in this chapter, to the insuperable difficulties connected with any attempt to discover the real rates of discount for each half-yearly period in the future. If we knew these future discount rates we might then be able to state that two bonds which, at different dates, each had the same number of years to run, the same coupon rate and the same 'yield' had quite different durations

If, for example, the 'yield' of the earlier bond involved a set of relatively high discount rates for the years of the immediate future and low discount rates for the succeeding years to maturity, while this condition was reversed for the later bond, the earlier bond would have a longer duration than the later bond. Because the coupon rates, yields and maturities are identical, the prices of the two bonds will be the same. In other words, the sum of the present values of the future payments will be the same. Hence that bond in which the earlier payments are relatively heavily discounted, and therefore the 'weights' applicable to the shorter constituent maturities are relatively light, will have a longer duration.

The difficulties connected with the problem of arriving at a completely satisfactory concept of 'duration' are, indeed, extremely great. Any proposed solution almost necessarily involves some paradoxes. We have tried to open the reader's eyes to the existence of the problem. The logical atmosphere in which the analysis has had to be carried on may seem to have been somewhat rarefied at times; but we believe that, if the reader has followed the arguments carefully, he will at least not

²⁷ But see Ch. III, note 8,

accuse the writer of being like the good Puritan knight who, in religious controversy,

". . . could raise scruples dark and nice, And after solve 'em in a trice As if Divinity had catch'd The itch, on purpose to be scratch'd."

CHAPTER III

SOME THEORETICAL AND PRACTICAL DIFFICULTIES OF COMPARING LONG TERM INTEREST RATES AT DIFFERENT AND ESPECIALLY AT

WIDELY SEPARATED DATES

A RATE of interest arises out of an exchange of present money for a promise to make one or more future money payments. It is a peculiar inverse function of the price paid for the promise. The promise is personal property—a chose in action. It may be bought and sold like any commodity. The problem of comparing the prices—or yields—of such promises at different dates is naturally very similar, in some respects, to the problem of comparing the prices of commodities at different dates. However, because the promise, if it be considered a commodity, is undoubtedly a commodity sui generis, the two problems are in some significant ways decidedly different.

Let us first notice an important similarity. Just as there are different commodities, so are there different promises. To talk of the price of bonds—or, inversely, of the rate of interest—is like talking of the commodity price. In any important market at any particular time there are many commodities and many commodity prices, many promises and many rates of interest. And the promises, like the commodities, differ not only as to their nature but also as to their quality. To compare call money rates on the New York Stock Exchange in 1890 with the yield of West Shore 4's in 1936 would be almost as absurd as to compare the price of potatoes in London in the year 1800 with the price of pig tin in the same city in the year 1900. And to compare the yield of a low grade bond at one date with the yield of a high grade bond at another date would be nearly as meaningless. For commodity prices or interest rates at different dates to be significantly

comparable, the prices must be the prices of identical or approximately identical commodities and the rates the returns from identical or approximately identical loans.

But here we strike an important difference between the two problems. It is much easier to decide whether two commodities at different dates are approximately identical than it is to decide whether two loans at different dates are approximately identical, though, even in the commodity price problem, this difficulty is much greater than it at first sight seems to be.

The brute materiality of physical objects tends to obscure the fact that, as economists, we are interested in only certain of their psychic implications. While the feeblest intelligence may grasp that the economic significance of a bond lies in the promise it represents and not in the mere piece of paper, it is not so easy to see that the economic importance of each and every economic good lies in its possibility of satisfying human desires and not in its mere physical presence, and that consequently a particular physical object may have great economic significance at a particular date even though its importance was negligible at an earlier date or will be so at a later date. Even if they were not subject to physical deterioration or change, innumerable manufactured objects would have an economic history more or less like that of a moustache cup, a hoop skirt, a spinning wheel, an hour glass or a prairie schooner. Though the particular physical object be unused and therefore remain physically unchanged, its economic significance (for all other purposes than those of the antiquarian) dribbles away like water out of a leaky pot. Even if a Model T Ford of the vintage of 1916 had been preserved in a vacuum, what would it sell for now? The value attached to particular economic goods changes with the introduction of new means of satisfying desires.

The change with time in the economic significance of physical objects is one of the chief obstacles encountered in the problem of attempting to compare the 'general level' of commodity prices at widely different dates. During the last twenty years there has been a great increase in the comfort and mechanical efficiency of the transportation that the automobile purchaser gets for his dollar. 'Automobile prices' are much lower than they were twenty years ago. But exactly how much lower? What can one mean by 'automobile prices'? What commodity can we use in 1936 to compare with a Model T Ford in 1916,

and what can we use in 1916 to compare with any of the standard models of 1936?

An automobile may present a rather extreme illustration of obsolescence, but a similar process goes on with respect to most commodities, and the longer the time elapsed the greater become the difficulties of adequate comparison. To compare the cost of living in Boston in 1938 with its cost in 1838 may not be quite so difficult as to compare the cost of living in a small village in the far north of Canada with the cost of living in a small village in the interior of Brazil, but the sources of at least one of the difficulties are the same. Many of the commodities that are used in the one time or place are quite different from those used in the other time or place. While buggies, candles, spinning wheels and clipper ships may have been important in the economic life of Boston one hundred years ago their present importance in the same city is virtually nil.

In Chapter II we drew attention to the fact that the relative economic importance of a particular type of loan may be much greater in one place than it is in another place at the same time, or at one time than it was at another time in the same place. In this respect the difficulties of comparing interest rates at different dates are somewhat similar to those to which we have just been referring in connection with commodity prices. However, we must now draw the reader's attention to some peculiarities of promises to pay that make interest rate comparisons even more difficult than commodity price comparisons.

Though their relative *economic* importance may change, there are many commodities whose *physical* characteristics are practically the same yesterday, today and forever. A ton of pig iron in 1938 may be physically the same as was a ton of pig iron in 1838. Systems of grading such commodities as wheat, corn or cotton make it possible to quote the prices of virtually the same physical things over long periods. But the problem of grading loans is quite another story.

A loan is not a physical thing. The buyer of a bond does not buy even future money, he buys only a *promise* to make future payments. And that promise may become as unsubstantial as was the grin of the Cheshire cat after the cat itself had vanished. Earnings may disappear and even apparently sound collateral become valueless. The price of a bushel of wheat or a ton of pig iron can be determined in the open market without knowledge of who grew the one or mined the other,

but the value of a bond cannot be even estimated from an analysis of its terms without considering the degree of confidence that should be placed in the promises it contains. The question, what should middling upland spot cotton sell for at the present moment on the New York Cotton Exchange has at least some meaning; but the question, what is a fair price at the present time on the New York Stock Exchange for a 4 per cent bond maturing in twenty years has none. To mean anything the latter question would have to tell us something about the 'grade' of the 4 per cent bond.

But the 'grade' of a bond is the grade of the promise it represents. For the yield of a bond at one date to be as legitimately comparable with the yield of another bond at another date as is the price of a pound of middling upland spot cotton at one date with the price of another pound of middling upland spot cotton at another date, the promise represented by the one bond at the one date should be the same or virtually the same as the promise represented by the other bond at the other date not merely with respect to terms ' but also with respect to goodness.

But with respect to what kind of 'goodness' should the promises be equivalent? In the first place, it clearly cannot be that essential and intrinsic goodness-or lack of goodness-that a determinist philosopher might say the bond possessed on the date in question but which would not be made apparent until the date of maturity.2 For, if we interpret 'goodness' in this manner, we must grade the promises of all bonds that, in fact, made all 'interest' payments and the 'principal' payment on the dates called for in the bonds as perfect-exactly one hundred per cent 'good'-during all the time the loans were outstanding. But the possession of this unforeknown and unforeknowable 'perfection' would be a quite fantastic reason for believing in the legitimacy and usefulness of comparing the yield of one such 'perfect' bond at one date with the yield of another such bond at another date. We must remember that the yields of such 'perfect' bonds differ tremendously on the same dates. Though two 4 per cent bonds maturing in twenty years may each meet all future obligations on time, the one bond may be selling at the present moment on a 31/2 per cent basis and the other on a 6 per cent basis.

¹ For the usual bond, maturity and coupon rate.

² In case of default, perhaps not even then. Cf. Aristotle, De Interpretatione, Ch. 9.

In grading bonds at any particular date, we are concerned with how good the bonds were, not with how good they turned out to be. It is, of course, true that, in a metaphysical sense, how good they turned out to be was how good they really were. But prices and yields can be directly affected only by forecasts of the future, never by the facts of the future. It is, therefore, to forecasts that we must restrict our concept of goodness. It is true that to grade bonds on any basis of how good they seemed to be, or even should have seemed to be, is to lean upon a flimsy reed. But there clearly is nothing else to do.

Having come to this conclusion, we are faced with the question, should the grading be based on actual or on ideal forecasting, on how good the bonds seemed to be or on how good they should have seemed to be. At once we notice that any 'should have seemed' grading is tarred with the same stick as grading based on what the future eventually revealed. It is almost always clear, after the event, that, though the future was essentially unknowable, a more shrewd and intelligent analysis of the facts that were available should have prevented much of the bad forecasting that actually occurred.

And this difficulty cannot be overcome by arbitrarily limiting the range of facts upon which forecasts 'should have' been based. The essential element in any 'should have' system of grading must clearly be that no pertinent and important consideration shall be neglected. To assume, for example, that, for purposes of yield comparisons, bonds can be more correctly graded by some simple mathematical formula whose variables are all derivable from either present or past financial reports of the debtor corporation than they are in fact graded in the open market is to exhibit an optimism that is difficult if not impossible to defend.

The most intelligent bond buyers are of course interested in how their bonds are 'rated' by the better statistical services, but they desire and obtain more information than is yielded by the symbols AA or B1+. Some years ago the executives of a large statistical organization, which had for years been publishing bond 'ratings', finally came to believe so strongly in the reliability of their own ratings that they initiated a 'switching' service for bond owners. The theory upon which the service was based was that, if a client owned bonds that were selling on a definitely lower yield basis than the average yield of bonds of the same 'rating', he should sell them and 'switch' into bonds of the

same rating but selling on a higher yield basis. The 'service' was soon abandoned.

But, even if the difficulty of deciding how the bonds *should* have been graded were much less than it is, the question would still have to be answered, is this the kind of grading demanded by the problem? When comparisons of even commodity prices at different dates are being made, is not the relevancy of the prices dependent on what the buyers and sellers *thought* they were exchanging rather than on what they actually were buying and selling? Has not the comparative ease of discovering, for so many important commodities, what actually is being bought and sold obscured the fact that this consideration is, after all and paradoxical as it may sound, in some respects of only secondary significance?

Because a seemingly normal and healthy dairy cow that had been sold 'as is' by one farmer to another for one hundred dollars died the following day, the price paid is not described as a price for moribund cattle; though, if the condition of the cow had been apparent at the time of sale, she should have been priced on the basis of 'hide and tallow'." If, before the Cripple Creek strike in Colorado, the land on which the mines were later located had been bought and sold as grazing land, no student of prices would now think of describing the early prices per acre as prices per acre of an extremely rich gold field. If a consignment of eggs were sold at a sheriff's sale, without recourse, and if the buyers had understood and believed that the eggs were at least relatively innocuous, the price would not be describable as a price of 'spots and rots'—even though that was the real status of the consignment.

Bonds vary in quality as much as do eggs; and the history of bond a It is, of course, true that unless the farmer wanted the cow in order to supply his own family with milk, he was buying not merely a promise to provide that future commodity but more fundamentally a promise to provide future money income. The purchase of a cow could have turned out to be a poor investment not because the cow died but because of a fall in the price of milk. This is, however, completely outside the realm of ordinary commodity price history. The student of the history of commodity prices can and does brush such considerations aside. He presents a table showing dairy cattle prices at different dates without discussing whether the purchasers did or did not act wisely. He is recounting the prices of an economic good that is also a physical object and his definition is in terms of physical characteristics. His is a history of the prices of physical objects as those prices were made by people who believed they were buying things having such and such physical characteristics.

prices demonstrates conclusively that, unlike eggs, bonds are usually graded very incorrectly by the market-and the statisticians. Collapse of the credit of a corporation is seldom seen far in advance; on the other hand, innumerable bonds that pay on time all coupons and the face of the bond are graded low throughout their existence. This is, of course, exactly what might be expected. As the future cannot be known, bonds must be graded on a probability basis and, unless they are of an ultra-superior quality, the information available for grading them on such a basis is almost always quite inadequate.

And, though the market's rating must be considered as of a probability type, it undoubtedly is not arrived at by conscious mathematical calculations. Indeed, the attempt to make any definite and simple mathematical assumptions as to the elements of the probabilities involved easily leads to conclusions that run counter to what is commonly assumed to be fact—such conclusions, for example, as that the yields of low grade, high yield bonds should be expected to fluctuate less than the yields of high grade, low yield bonds. And the attempt to formulate mathematical assumptions whose development will not lead to results that conflict with facts or apparent facts all too easily leads to obviously ad hoc hypotheses.

The simplest of all probability hypotheses is that the probability of payment of each and every promised future payment is always the same, $\frac{9}{10}$, for example. With this assumption, the price of the bond would, on any specified date, be 90 per cent * of the price on the same date of a bond containing an identical set of promises but rated by the market as 'absolutely secure'. However, unless the bonds were perpetuities, the yield of the lower grade bond would fluctuate less than the yield of the 'absolutely secure' bond.5

Such an assumption as that the probabilities of payment are all equal is, of course, quite fanciful. It assumes that the successive probabilities

Less in a community that did not care for gambling and possibly more in one that did.

⁵ The lower the yield of a particular bond the greater percentage effect on its yield has a specified percentage change in its price. For example, if a 4 per cent bond maturing in eighteen years falls five per cent in price, from 100 to 95, its yield will increase ten and one quarter per cent (from 4.00 per cent to 4.41 per cent); but if it falls five per cent in price, from 120 to 114, its yield will increase fifteen per cent (from 2.60 per cent to 2.99 per cent).

are completely independent of one another and that the question whether a particular payment will or will not be met is unrelated to whether the preceding payments have been met.6 But similar strange conclusions result from developing much more appealing hypotheses.

The simplest assumption having any appreciable air of reality is that no payment will be met unless all preceding payments have first been met, but that, as soon as one payment has been met, the probability that the next payment will be met is the same as previously had been the probability that the preceding payment would be met. Under this compound assumption, if the probability that the first payment will be met be designated p, the probability (as of the same date) that the second payment will be met will be p2, and the probability that the nth payment will be met will be p". In these circumstances the functional relationship between the lower grade bond and the 'absolutely secure' bond is not (unless the bonds be perpetuities) simply expressible in terms of prices, though it is so expressible in terms of yields. On any specified date the R more 7 of the lower grade bond will equal $\frac{1}{R}$ times the R of the

'absolutely secure' bond.8

"Even 'income' bonds are not exceptions. The payment or non-payment of preceding coupons is at least evidence of ability or lack of ability to pay the next coupon. R = the multiplier corresponding to the yield, e.g., if the bond is on a 4 per cent per annum basis, R = 1.04 (per annum). Under the semi-annual convention of the bond tables R would, of course, equal 1.02 (per half-year) (see Ch. II).

8 The price of the lower grade bond is obtained by discounting, not its actually promised interest and principal payments, but their mathematical 'expectations' at the yield of the 'absolutely secure' bond. The price of the 'absolutely secure' bond conals.

and the price of the lower grade bond equals

for the price of the lower grade bond is the same as would be obtained by substituting R for R in the expression for the price of the 'absolutely secure' bond. I and n are, by the hypothesis of identical promises, the same in both bonds.

For definitions of I, n, and R see Ch. II.

The reader should note here, in passing, that, if the lower grade bond be assumed to differ from the higher grade bond not in the rates at which the future promises are discounted but in the valuations placed on those promises (the 'expectations'), it For example if $p=\frac{99}{100}$ and if, on a particular date, the yield of the 'absolutely secure' bond were 2 per cent per half year, the yield of the lower grade bond would be 3-1/33 per cent per half year. If the yield of the 'secure' bond advanced to 4 per cent per half year, the yield of the lower grade bond would become 5-5/99 per cent per half year—one and two-thirds times instead of double its former rate of 3-1/33 per cent. The yield of the lower grade bond equals a constant term plus a constant multiple of the yield of the 'secure' bond (see note 9). Its percentage fluctuations are therefore *smaller and not larger* than those of the yield of the secure bond.¹⁰

It would, of course, be possible to construct hypotheses with respect to the market's estimates of the probabilities of the various payments being met that would not be inconsistent with the requirement that low grade, high yield bonds should fluctuate in yield much *more* than high grade, low yield bonds. But any such hypothesis would necessarily be a mere mathematical curiosity.

(Footnote 8 concluded)

will have an essentially shorter 'duration', because the size of the 'expectations' would decrease as their distance in the future increased. Now we know that extent of fluctuation in yield with the passage of time is an inverse function of duration. But it is hard to say whether or not we have here any significant clue as to why low grade bonds might tend to fluctuate in yield more than high grade bonds.

The R of the secure bond equals 1.02 and hence the R of the lower grade bond equals 1.02 $\times \frac{100}{00}$ (see note 7). From this result we get 3-1/33 per cent per half

year as the yield of the lower grade bond.

In general, if \mathbf{r}_1 represent the yield of the 'absolutely secure' bond and \mathbf{r}_2 the yield of the lower grade bond, \mathbf{r}_2 will equal 100 $\frac{(1-\mathbf{p})}{(\mathbf{p})} + \frac{\mathbf{r}_1}{\mathbf{p}}$ or a constant term

plus a constant multiple of the yield of the secure bond.

in If the yield of the lower grade (higher yield) bond is to fluctuate exactly as the yield of the 'absolutely secure' bond, in other words if $R_2-1=k$ (R_1-1), where k is greater than unity, then p, or the probability that each payment will be made if the preceding payment has been made, is such a function of the yields of the two bonds that the larger their yields the smaller is this probability of payment of the lower grade bond. This, of course, amounts to a fluctuation in grade.

As we have seen,
$$p = \frac{R_1}{R_2}$$
, but, because $R_2 - 1 = k (R_1 - 1)$,
$$\frac{R_1}{R_2} = \frac{1}{k} + \left(\frac{k-1}{k}\right) \frac{1}{R_2}$$
 which increases and decreases as R_2 (or R_1 , as $R_2 = 1 - k + kR_1$) does the contrary.

We saw in the preceding chapter that the yield of a bond was demonstrably an average, a complicated type of average it is true, but essentially an average. The assumption that the rates of discount used during successive future periods are identical was there proven quite unwarranted. Though it is for many purposes a convenient and useful fiction, it is always a fiction. We illustrated this fact by bringing to the surface the different rates for different future periods *implicit* but hidden in the yields of serial bonds, and we described and explained how the 'average' that we term the 'yield' of a bond tells us nothing about the rates of interest of which it is an average. We furthermore showed that there is no such custom of conscious and deliberate calculation as would lead to any significant market pronouncement concerning the various rates assigned to the different future periods. Indeed, to assume the existence of any such pronouncement would be almost as unscientific and indefensible as to indulge in a 'pathetic fallacy'.

We find ourselves, therefore, faced with a dilemma. We can be virtually certain that any mathematical hypothesis based on the assumption that the constituents of the yields are consciously considered would not give even an approximately true picture of how the grading is actually done and the yields actually arrived at. But to shut our eyes to the

composite nature of the yields would be quite as disastrous.

And to top all, our hypothesis would be designed to fit not known facts but preconceived fancies. For, startling as it may sound, we do not know that lower grade bonds actually do fluctuate in yield appreciably more than do higher grade bonds. Indeed, there are strong reasons for suspecting that the excessive fluctuation in the yields of socalled lower grade bonds is primarily an indication of fluctuation in the grades assigned by the market to such bonds rather than an indication that violent fluctuations in yield normally accompany low, but unchanging, market grading.¹¹

²¹ Sometimes, though rarely, the long term movements of the yield of a particular bond of not quite the highest grade are, for many years, so nearly the same as the long term movements of the yields of bonds of the very highest grade as to suggest strongly that the grade of the slightly poorer bond has been relatively stable throughout the period. West Shore 4's of 2361 (Bond No. 70) is such a bond. As may be seen from Chart 2, the long term trends of the yields of that bond (see Line C of chart) from 1885 to 1930 showed no permanent drift away from the index of the yields of bonds of the very highest grade (Line B and Line D—which has the same trend as Line B). However, as may be seen from the chart, the intermediate

And averaging the yields presents no logical solution of the problem of comparing the yields of second grade bonds at widely separated dates. One who had not examined the data carefully and considered the problem critically might easily think that bond yields should, not merely practically but also theoretically, be much better adapted to the making of index numbers than are commodity prices. Surely, such an one might reason, bonds have a homogeneity that commodities do not possess. They are concerned with the satisfaction of one great and undifferentiated desire—the desire for money in the future, while the different desires that can be satisfied by different commodities are almost as varied and multiform as are human wants.

Is not the difference between a high grade bond and a low grade bond (of approximately the same duration) like the difference between a high grade and a low grade sample of the same commodity rather than like the difference between two disparate commodities? Is it not the difference between high grade raw cotton and low grade raw cotton or between good potatoes and poor potatoes rather than the difference between cotton and potatoes?

And is even a difference between two bonds that results from a great difference in their durations so fundamental as is the difference between the two commodities? Cannot the one bond be substituted for the other in a way that is quite impossible with the commodities? The proceeds received when a short term bond matures may be reinvested; and both short and long term bonds can always be sold. While an investor is holding a bond, is not the type of good he is receiving from it unaffected by the length of time that the loan has still to run?

And surely, if we were to restrict our choice of bonds to those whose durations were long and not too violently different, we could virtually eliminate the effects upon their yields of fluctuations in their grades by averaging the yields. Why not take a hint from students of changes in the general level of commodity prices? Simply select a representative group of bonds and follow them through from month to month and year to year by means of some kind of averaging.

The complete answer to this engaging but artless suggestion is that all the evidence indicates that the variations in the market's grading of individual bonds with the passage of time are of such a nature that (Footnote 11 concluded)

and cyclical movements of the yields of West Shore 4's were, during all this long period of forty-five years, usually less than those of bonds of the very highest grade, their effects could *not* be eliminated by any ordinary averaging of the yields of the bonds. The variations in grade, at different times, of individual bonds in a group are not of a chance or accidental type, fluttering back and forth about some constant norm but always showing the same relation to and distribution about that norm. Even in the form of averages, there is no stability to the grades. *There is no 'constant norm'*. The average and the whole distribution of grades undoubtedly drift in great secular swings, immense waves, and even up and down with the movements of the business cycle.

Though fluctuations in the yields of bonds that are not of ultrasuperior quality, relatively to the yields of bonds of such quality, are not closely enough related to fluctuations in the earnings of the debtor corporations to make grading upon this basis feasible, they are definitely and unmistakably correlated with such fluctuations. And, because the earnings of nearly all corporations tend to rise and fall with the business cycle and, in any particular industry, to move together over long periods of time, the grades that the market assigns to the bonds inevitably tend to drift as a group and to move up and down together. Over nearly all the period covered by the statistics of this study the steady secular decrease in the 'spreads' of the yields demonstrates unmistakably that the lower grade railroad bonds were improving in grade as a class. When they were not doing so, they were declining in grade as a class.

It is, of course, true that the lack of confidence engendered by a business depression tends to increase the relative demand for bonds of the highest grade and to decrease the relative demand for bonds of lower grades, and it is also true that the absolute volume of bonds of the highest grade declines and the absolute volume of bonds of lower grades increases (as those that were formerly of the highest grade move into lower classes). And it is further true that the distribution of bonds by grades could be of such a type that the pressure of bonds new to the grade would be an inverse function of the grade. And it is hard to say how much of the increase in the 'spread' of the yields of a group of bonds of different grades during a pronounced decline in general business may be the result of any such vicious combination of depressing factors. But we must remember that such factors cannot materialize and become operative unless there first occurs a change in grading, and that, therefore, they cannot be held accountable for more

than a part of the increase in 'spread'. Chart 15 suggests strongly that at least their ultra long term effects are quite negligible.

And, finally, it is perhaps worth noting that the makers of even commodity price index numbers do not attempt to eliminate the effects of variations in *grade* by averaging. As far as possible they quote the prices of identical grades from year to year, and when changes in

grade become necessary they adjust for them.

Ordinary index numbers of the yields of second grade bonds are to a greater or less extent like index numbers of stock prices, and such index numbers are, in one respect, almost sui generis. At least over long periods of time their chief interest lies in the picture they give of changes in the nature of the things whose prices are quoted. When the price of aluminum falls from a large number of dollars per pound to a small number of cents no one suggests that the figures indicate that aluminum was in the early days a distinctly different metal from what it was later. But a long-continued and pronounced rise in the price of the common stock of an aluminum producing corporation would usually 12 be accepted as proof that the market believed that the earning power of the corporation had increased—in other words, that there had been a change in the nature of the thing that was being bought and sold.18

This consideration does not, of course, even suggest that the economist should be uninterested in the movements of the prices and yields of second grade bonds—any more than that he should be uninterested in the movements of stock prices. But it does suggest in the strongest possible manner that he should consider carefully the meaning of such movements and realize the inherent difficulties of deducing conclusions concerning the movements of 'interest rates' from such material. The economic consequences of a collapse in the second grade bond market may be just as serious if it is primarily caused by fears of declining earnings as it would be if it were primarily caused by a rise in the 'preference for present over future goods'. And long term trends in the quality of second grade bonds may be quite as interesting as long

¹² In the absence of some important technical factor such as a radical change in the capitalization of the corporation.

¹⁸ Of course some of the rise of a stock or second grade bond may result from a decline in the rate at which expected future dividends or interest payments are discounted. The presence of such an influence would usually be shown by a fall in the yields of long term bonds of the very highest grade.

term trends in interest rates as exemplified in the yields of bonds of the highest grade, but it is highly desirable not to confuse the two.

However, if for no other reason than that the problem is presented in a simpler form, the student of interest rates will tend to be primarily concerned with the yields of the very highest grade bonds rather than with the yields of those of lower grade. The difficulty of measuring the market's estimate of the former is distinctly less than of the latter. Though their yields may not properly be described as 'pure interest'whatever that may be-there are strong reasons for believing that the estimates of their 'probability of payment' undergo no such radical changes as occur with bonds of lower grade. Though individual bonds that have been given the highest possible rating by both the market and the financial statisticians may within a few years fail to pay interest, no such serious variation in grade is found in the market's rating of AAA or A1+ bonds as such. Though it may not be the same nominal bond, there is always the possibility of using at the later date some bond that the market will apparently be rating the same or nearly the same as it rated the earlier bond. This, as we have already seen, is not true of lower grade bonds.

Bonds of the highest grade are bonds than which there are none better. To a very large extent, the market itself tells us which they are. They are, in general, those bonds that have the lowest yields. Yet an index number using each month the yield of the particular bond showing the lowest average yield during that month is not satisfactory, for the movements of the prices and yields of individual bonds of even the highest grade are often influenced by other factors than those affecting such bonds in general. For example, if the market for a particular bond is 'thin', relatively small purchases by a trustee or other insistent purchaser may run the price up beyond what it normally would be. Or again, rumors that the holders of a small 3 per cent issue selling for 85 may be offered par to clear the decks for a reorganization could easily raise the price to a point at which the yield of the bond would have no general economic significance. In Chapter IV we discuss at some length the problem of deciding what is the most representative yield for the very highest grade of bonds in view of the fact that it is inadvisable to trust entirely to the yield of the individual bond having the lowest vield.

Although confining one's consideration to bonds of the highest grade



may eliminate most of the difficulties encountered when the attempt is made to use lower grades, it does not remove them all. Rates depend not only on the security or reliability of the promise but also on what is promised. Time is of the essence of the interest problem and we saw in Chapter II that the rates imputable to different intervals of future time are almost never the same. Because of this fact the yields of long and short term bonds of even the highest grade would seldom even theoretically be the same.

And, because all bonds except perpetuities change their 'durations' with the passage of time, mere averaging of the yields of the same nominal bonds is open to the same criticism that could be levelled against comparing cattle prices on appreciably different dates by comparing the prices of identical cattle on the appreciably different dates. The age distribution of the cattle should be the same on the two dates but, as they are the same cattle, this cannot be true. If they are now each four and a half years old, a comparison with four years previous would give a result entirely different from what it would if they were now all ten or twelve years old. When we compare the prices of cattle at two different dates we do not take the prices of the same cattle. We take the prices of cattle that are not merely approximately the same grade but also of comparable ages. Even bonds of the highest grade are not exempt from this influence. If their maturities be at all close, they change appreciably in 'duration' with the passage of even a short period of time and this change affects definitely the essential nature of the loan.

From a strictly theoretical standpoint, it would seem necessary to find, for each date, bonds of the same coupon rate and maturity. However, the practical investigator will remember that rates depend on duration', rather than on 'years to maturity', and that, if the 'duration' of a bond is not too short, increases or decreases of a few years in the 'time to maturity' affect the yield only negligibly. And, of course, yields could (at least theoretically) be corrected by a statistically-derived equation relating yield to duration.¹⁴

¹⁴ Practically, any such correction is dangerous. Because bonds whose quotations are usable for any particular dates are relatively few, and the scatter of their yields and durations is very considerable, it is difficult to discover whether the empirical (as opposed to logical) relationship between yields and durations is even of the same kind at different dates. Moreover, even if it were always the same and even if we knew exactly what it was, the wideness of the scatter of the data from which it was derived would introduce a high degree of probable error into

After security and duration, the theoretically next most interesting factor influencing the yield of bonds is taxation. A strong case can, of course, be made for considering the return from tax-free investments as theoretically a purer index of the 'preference for present over future goods' than is the return from taxed investments. Both types merit study. But they must not be confused or mixed. Under a graduated income tax law, it is impossible to express one as a function of the other without introducing a third variable. And, if the tax-exemption is only partial, as is usual, the complications of use and comparison are still further increased. With the introduction of the income tax into American finance, the whole status of such bonds of course completely changed.

A minor practical difficulty encountered by the economic historian who attempts to use the yields of tax-exempt or partly tax-exempt bonds is that, aside from Federal bonds and a very few municipal and state bonds, the markets have usually been relatively poor, and quotations (because sales were largely 'over the counter') less easy to obtain and less reliable than quotations for bonds of the larger corporations. In the earlier period covered by this study it was often impossible to identify state or municipal bonds from the printed titles in the price sheets. For example, for a number of years there were quotations on the Philadelphia Stock Exchange for 'Penna. 6's', but for most of the period we were unable to discover what particular bonds were being quoted, there being at all times different 6's of various maturities outstanding. Finally, the reader must remember that a tax-exempt municipal bond is not necessarily of higher grade than a corporation bond because it sells on a lower yield basis. Its 'probability of payment' may be very definitely less.

Other factors affecting the yields of bonds are theoretically less intriguing though many are of great practical importance. But their nature is such that their influence can seldom be allowed for.

Changes in yield resulting from changes in the relative importance of a particular bond in the general economy because of changes in its markets or marketability are practically impossible to measure or over-

⁽Footnote 14 concluded)

the statistically-determined constants. The artificiality of the resulting theoretical

yields would offset any possible increase in their homogeneity.

However, the statistical questions involve interesting problems in multiple cor-

However, the statistical questions involve interesting problems in multiple correlation and someone may at some time care to follow them further than we have attempted to do.

come. Indefiniteness in the promise itself, such as exists in callable bonds and in bonds payable in two or more currencies at the option of the holder, may under some circumstances not be important; but when it is, it is extremely difficult to correct for, and attempts to do so seem undesirable if bonds with less ambiguous promises are readily available. Convertible bonds and bonds carrying special privileges of any kind, such as 'circulation' privileges, present similar difficulties. The promise to make future money payments is only one of the elements determining their prices and yields. They are mongrels and it is next to impossible to measure the degree of their contamination.

Changes in markets and marketability may have appreciable effects on the yield of a bond. Paradoxical as it may sound, a case may be made for the contention that, if the yield of a bond is to represent a simon-pure long-term interest rate, the bond must have no market whatsoever. The purchaser must buy it because he is willing to exchange present money for certain specified future money payments. If the yield is to be an index of his preference for present over future money he must buy the bond because it promises to pay him certain sums of future money on the dates specified in the bond. If he buys \$100,000 worth of United States Treasury 3's of 1951 with the intention of selling them in five or six months, because he wishes to make a short term investment and calculates that he can obtain a satisfactory return by the transaction, his personal valuation of the promises contained in those bonds probably affects little if at all the price he is willing to pay for them. He may own a profitable business and feel certain that, if he is to continue in business, he will, in a few months. need the \$100,000-or whatever he may sell the bonds for. Under such circumstances, he might be unwilling to pay more than thirty or forty thousand dollars for the bonds, if he knew that he could not hypothecate or sell them. The fact that he actually pays par or more has little or no relation to any personal valuation of the promises contained in the bonds. The bonds do not mature for 15 years and the only personal comparison that he makes between present and future money is a six-month comparison—nothing more.

Though a corporation may sell a long term bond under conditions that make it illegal for the corporation to retire the issue before maturity, or even to buy individual bonds in the open market, few purchasers—especially if they are individuals or 'natural persons' and not

corporations—would be likely to advance present money if the only good they could obtain in return was the privilege of receiving the interest payments and the principal payment when it became due. Natural persons seldom give to the buying of a bond the same kind of consideration that they give to the purchase of an annuity. The price they pay for the annuity is a real measure of the personal importance that they attach to the promised future payments. They seldom buy long term bonds in any such frame of mind. The marketability of a bond is one of the essential factors that determine its price and yield.

Legal restrictions and even mere custom powerfully affect the markets. As soon as a bond gains entrance to the 'legal' group in which trustees may invest, its price rises. And customs change. Forty years ago the prejudice against 'industrial' bonds was wide spread. The recent collapse of both 'guaranteed' and other real estate mortgages may affect all real estate loans, good, bad and indifferent, for some years to come.

Indefiniteness in the promise itself is sometimes so disturbing as to preclude all possibilities of using yield comparisons as indications of interest rate movements. Though callable bonds may, when selling much below their call price, be apparently unaffected by this element of uncertainty, as they approach that price their yields often begin to lose all significance. If there is any strong feeling in the market that they may actually be called, the yield becomes more or less that of a short term loan whose maturity is the callable date. In any case the yield is affected by a factor that can be neither measured nor corrected for except by comparison with another bond that seems strictly the same in all respects save the callable feature. But why, under such circumstances, use the callable bond at all?

Another illustration of indefiniteness in the promise is seen in bonds that are payable in whichever of several currencies the holder may choose to demand. Though such a clause may have little or no effect on the yields in times when all the currencies referred to in the indenture are rigidly bound together by some such tie as gold convertibility, in times of disturbance and chaos in the foreign exchanges its effect on the prices of the bonds may be so pronounced as to make the yield in any particular currency quite misleading if considered as an interest rate

As we have already said, bonds granting valuable rights and privi-

leges unrelated to the promise to make future money payments are, for the student of interest rates, mere mongrels. The yields of United States 'circulation' bonds were not, in the years before the Federal Reserve system, interest rates in any simple and direct sense of the term. Convertible bonds selling anywhere near their conversion price act as stocks and not as bonds.

Most of these difficulties are, of course, of greater theoretical than practical importance. When attempting to make really significant comparisons of bond yields at different dates, we can easily refuse to consider mongrel bonds whose prices are affected by other factors than their promises to pay money. We do not need to use convertible bonds. Bonds containing indefinite or uncertain promises can likewise be eliminated. We do not need to use callable bonds—certainly not when their price is anywhere near the call price. The problem of taxable or non-taxable bonds can be solved by deciding how we wish to define yield. When the decision is made, we do not need to mix the two types. Much can be done to obtain bonds whose marketability does not undergo any violent change during the period in which the bonds are used.

Of course, the accuracy of interest rate or bond yield comparisons becomes more and more open to question as the difference in time increases. This is true, even if all possible adjustments are made for changing grade, etc. The yield statistics presented in this volume cover seventy-nine years, and it cannot be denied that it would be extremely difficult to describe the characteristics of a bond of the year 1890, let alone 1857, that would be strictly comparable with any particular bond at the present time. If the credit of the borrowing corporation or municipality is such that its bonds are today generally considered 'absolutely' safe in any but a metaphysical sense, the problem would seem easier. But we must remember that, in 1890 or 1857, bonds of this class may have been relatively more or less scarce, in view of the demand for them, than they are now. The yields of even United States government bonds have, at various times, been unmistakably affected by changes in the volume outstanding. This can only very partially be accounted for by any change in the degree of 'security'. An increase or decrease in the relative volume of even the highest grade bonds outstanding will, in the absence of artificial influences, inevitably affect their yield. Though a technically correct comparison might be made.

the significance of their yields would be different at different dates.15

Over both short and long periods it is easier to obtain an accurate measure of changes in the average yield of the highest grade bonds than it is to obtain an accurate measure of changes in the yield of bonds of any lower grade. The primary reason for this is that we can give at least a rough and ready answer to what we mean by the best bonds. As soon as we leave the relatively secure ground that they are bonds than which there are none better, and that, in general, they are the bonds that have the lowest yields, and discuss bonds of any lower grade we are faced with the problem of defining their grade. The second reason is that the best bonds do not change grade in any such free and easy manner as do other bonds. Their yields are but little affected by the changing fortunes of individual corporations or even by the changing fortunes of an industry as a whole.

If the earnings of a corporation cover the interest charges on a bond thirty times, the market takes little or no notice of a change in conditions such that the charges are covered only twenty times. On the other hand, a change from one and a half times to once only will probably be considered extremely serious. The yield may rise violently. The lower the grade of a bond the more it tends to act like a common stock. It comes to be significantly affected not only by interest rate factors but also by potential earnings. Whether the yields of the highest grade bonds are, at any particular time, of more or less economic importance than the yields of bonds of some specific lower grade, their meaning is simpler and their values are easier to obtain.

Until the World War there was a rather pronounced tendency for the movements of the yields of the highest grade bonds in the different financial centers of the world to become more and more alike. However, this similarity was almost non-existent in the earliest period covered by our statistical studies and was only irregularly noticeable after the disturbances to the various monetary bases that came during the War. The interest rates and bond yields presented in this volume are all from the eastern financial centers of the United States, indeed chiefly from New York City.

For the study of long term as opposed to short term rates, primary

¹⁵ Comparisons of recent and early figures for even call money rates or commercial paper rates are properly subject to considerable questioning. There seems little doubt that the security of each of these classes of loans was much less in the earlier period.

reliance has been, aside from the last few years, placed on the yields of American railroad bonds. Index numbers based on the yields of municipal bonds or bonds of corporations other than railroads have been introduced only for the sake of checks and comparisons. Such a procedure may seem to need some defense. The reader, especially if he is not an American, may wonder why, if we were primarily interested in the highest grade bonds, we did not use United States government bonds. The sufficient reason is that, during most of the period covered by this study, their yields were seriously affected by their circulation privileges. The bonds were intimately tied up with the whole structure of the national banking system. American 'National Banks' were allowed to issue 'National Bank Notes' based on United States government bonds that they had deposited with the Comptroller of the Currency, Consequently the bonds were bought for two reasons: first, because of the interest they paid; second because they could be used as collateral for the issuance of currency. The yields were naturally much lower than if the bonds had been valued for their interest payments alone

It might be thought that, since the formation of the Federal Reserve system, the yields of Liberty and Treasury Bonds could be considered an adequate index of long time interest rates in the United States. However, it must not be forgotten that they also carry special banking privileges, such as eligibility for use as collateral with the Federal Reserve banks at par. Finally, the investigator who might consider using them is faced with the practical difficulty that the yields of most of them are ambiguous. The maturity dates are not fixed. They are callable bonds.

We have used index numbers based on the yield of New England municipal bonds as a check on the results obtained from the railroad bonds. We did not consider using such indexes as a substitute for the railroad indexes. The market for municipal bonds has never been such a highly developed market as that for railroad bonds. The accuracy and adequacy of the quotations on which our index of the yields of New England municipals is based are not to be compared with the accuracy and adequacy of the railroad quotations. Available quotations were neither very good nor very numerous. Moreover, the fact that the holder of municipal bonds has always had certain tax exemptions, which were sometimes more and sometimes less valuable, made such

bonds poor material for our purposes. We dropped them entirely as soon as the Federal Income Tax Law began to function.

We were faced with the necessity of using bonds from one or more industries. We discovered that if bonds are to be used from more than one industry, each industry should be used by itself for a reasonably long period. Switching back and forth or using even the best bonds of two or more industries at the same time may easily lead to undesirable statistical results. Rather than to switch from one to another, it would seem better to use bonds from different industries independently, construct an index from each industry and attempt to arrive at conclusions by comparing the indexes.

When the decision to use only one industry had finally been made, the railroad industry was the inevitable choice. There was no other industry whose securities were of comparable importance in January 1857, the date we knew we could reach by using railroad bonds. Until many years after 1857 good public utility bonds were scarce. Until very recently, the bonds of no other industry have had the high credit rating of railroad bonds. Even in the recent collapse of railroad credit, railroad bonds of the very highest grade sold on a lower yield basis than any other corporation bonds. We constructed some very helpful index numbers based on the yields of public utility bonds in recent years. But, during most of the period studied, not only were such bonds few in number and mostly of rather low grade but also they were seriously affected by ambiguity of yield. Most of them had callable or convertible features, or both.

Accurate daily quotations for the prices of railroad bonds on the New York Stock Exchange are available back to January 1, 1857. We were unable to find any official sheets before that date. We did not attempt to carry the study further back by using quotations from newspapers. Entirely aside from the fact that newspaper quotations were, in the early days, not nearly so accurate as those contained in the official sheets, it did not seem worth while to attempt to go further back than 1857. January 1857 carries the series into the period that preceded the panic of 1857. Only a few years earlier the railroads were in their mere infancy and price quotations were very scarce and the yields unmistakably but irregular representatives of interest rates. Even for the year 1857 we found only thirteen bonds that could be used. Moreover, the scatter of the yields was very great. The best bond we used in January

1857 had a yield of 6.27 per cent while the worst bond we used had a yield of 9.84 per cent. It is apparent that, in order to get even thirteen bonds in 1857, we had to include some decidedly questionable ones.¹⁶

The original sources from which we calculated the yields for the individual bonds were in all instances price quotations, never yield quotations. Almost all the bonds were listed on the New York Stock Exchange, a very few being obtained from the Philadelphia, Boston or Baltimore Exchanges. No 'over the counter' quotations were used.17 For those bonds that were listed on the New York Stock Exchange we obtained quotations for the period January 1857 to December 1877 from the New York Stock Exchange official sheets referred to above. From January 1878 to the present time our primary source for quotation for bonds listed on the New York Stock Exchange was the files of the Commercial and Financial Chronicle, and the Financial Review 18 published by the same journal. In many instances, mathematical calculations that were made on the yields suggested that certain price quotations were wrong. Wherever such a suggestion occurred other sources than the Commercial and Financial Chronicle were used as checks.

In the very earliest period we felt compelled to use almost every rail-road bond for which we could obtain continuous or nearly continuous quotations (unless the movements of its yield were unmistakably erratic and violently different from the movements of the average of the group), but in the period after the first few years, we chose the bonds with considerable care. In the first place, we discarded all bonds whose yields were so high as to indicate that their credit was decidedly poor. We knew that their prices would move more like stock prices than we desired. We were studying interest rates. When the movements of the yield of a bond showed any great irregularity, we investigated what was happening to the road and in the market at that time. Usually we 19 But the reader must not assume that we present an average of the yields of these bonds as picturing anything more than the condition of the industry. How these yields were used to obtain the yields of hypothetical bonds of superlative grade is discussed in the next chapter.

17 Only in constructing the indexes of the yields of New England municipal bonds

did we use 'over the counter' quotations.

¹⁸ The Financial Review was not used before 1878, because the prices that it quoted were 'bid' prices on Friday of each week. All the prices for railroad bonds used in this book are actual sale prices. Bonds listed on the Philadelphia, Baltimore and Boston Exchanges were obtained from various sources, official sheets, magazines, etc.

found some outside influence that made the bond undesirable. After a large number of such investigations, we discarded bonds without investigation, when the movement of their yields was so violently erratic as to warrant the assumption that an investigation if made would disclose some good reason for elimination.¹⁰

Few bonds with callable or convertible features were used. The decision whether such a bond could be used was based on two considerations. First, we checked its action with the action of a tentative general index to see whether the callable or convertible features seemed to have any discoverable effect on its yield. Second, we attempted to decide logically whether the bond would or would not, in the near future, be influenced by either the callable or convertible feature. In case of doubt the bond was not used.²⁰

As far as possible we used only bonds having fairly continuous price quotations. We considered the absence of quotations for two or more months in succession much more serious than their non-availability for the same number of months not in succession. Interpolations were made on the assumption that the movements of the logarithms of the yields of the particular bond in the interpolation period were the same

¹⁰ Had the technique described in Chapter IV been developed before we began our study, instead of as we progressed, we undoubtedly would have been much less particular about what bonds we included.

20 Whether a bond will or will not be called depends upon its yield to maturity at the call price on the call date. If the particular corporation or government can borrow at the call date (and pay expenses of floating the issue) at a lower rate than the yield of the bond to maturity at the call price and on the call date, the bond will be called, otherwise it will not.

For example, if a 6 per cent railroad bond, having forty years to run, is selling for \$114 (to yield 5.17 per cent to maturity), but is callable thirty years from now at \$112, there might be no good reason for assuming that it would be called—in spite of the fact that it is not only selling above par but also above the call price. On the call date at a price of \$112, with ten years to run, the yield would be 4.50 per cent. It might easily happen that this particular railroad would not call the bond because it could not save money by so doing.

There is one serious exception to the above statements. Sometimes the yield to maturity on the call date and at the call price is a relatively unimportant element in deciding whether the bond will or will not be called. Suppose a bond maturing twenty years from now were callable in ten years at a price that would give a yield of only 2 per cent from the call date to maturity. Such a bond might be called if it were necessary to get that particular bond out of the way to clear the decks for some consolidation or reorganization. Even rumors of such consolidations or reorganizations will powerfully affect the price (and hence the yield) of a bond. However, such cases are rare. We discarded only two bonds on this account.

as the movements of the logarithms of the general index, plus or minus a straight-line trend.²¹ An examination of Appendix A, Table 3 will show that interpolations are not numerous. Only in seven years were they in excess of ten per cent of the total number of individual yields. The largest percentage of interpolations (13.63) occurs in the thirteenmonth period January 1898 to January 1899. After 1919 almost no interpolations were necessary.

With very few exceptions, no bond was selected unless it could be used in the index numbers for at least six years without coming closer than ten years to maturity. Since 1909 no bond was kept in the indexes after it had less than fourteen years to maturity. The inclusion of relatively short term bonds in the earlier period was unavoidable. There were not enough longer term bonds available at that time.

No attempt was made to attain a geographical distribution of the rail-roads whose bonds were used. We are concerned with interest rates, not with changing economic conditions in various parts of the United States. It was considered more important to know that the bonds were being bought and sold in the same market than to know the geographical location of the property. Even Canadian railroad bonds were used if they were actively traded in on the New York Stock Exchange.

Because we were primarily concerned with interest rates rather than $^{\rm 21}$ The actual arithmetic of the procedure was as follows: suppose the yield of a bond was lacking for June and that in the particular 13 months under discussion 27 bonds were used. Now suppose that we had the yields of 25 bonds for May, June and July. From these 25 bonds index numbers of yields for the three months would be constructed. The difference between the logarithm of the yield of the particular bond in May and the logarithm of the yield of the index in May would then be found. Similarly the difference between the logarithm of the yield of the particular bond in July and the logarithm of the yield of the index in July would be found. If the logarithm of the yield of the particular bond in July, minus the logarithm of the yield of the particular bond in July, minus the logarithm of the index number in May be represented by x, and the logarithm of the yield of the particular bond in July, minus the logarithm of the index in July be represented by y, then to the logarithm of the index number in June is added $\frac{x+y}{2}$. The anti-logarithm of the result is then taken as the yield of the particular

After the first index had been constructed some new bonds were introduced. However, the existing interpolations were not then recalculated, since it was apparent that so little difference would be made that recalculation would not be worth while. The interpolated yields are therefore not always exactly what they would have been had they been based on the final index number. The effects of this technical inconsistency are, of course, neglicible.

with mere security prices, we did not hesitate to use two or more bonds of the same road. Indeed, we sometimes used two bonds of the same road and secured by the same mortgage, but of different issues, where the only difference was in the coupon rates. The reader must remember that even if two bonds are of the same road, have identical maturity, security, etc., if they are not identically the same bonds, they commonly show a considerable degree of variation in their minor erratic fluctuations. Arbitrage in bonds does not entirely eliminate such differences. If an individual has a block of bonds which he desires to sell and places them on the market in rather rapid succession, his selling will depress the price of that particular bond without necessarily affecting to a corresponding degree the price of another bond, though it be of the same road and have the same maturity and an almost identical position in the capital structure.

The prices from which yields were calculated were arithmetic averages of the high and low prices for each bond for each month. It would have been impossible within the time at our disposal to have calculated monthly averages from daily quotations-and few of the bonds were sold every day in the month. The average monthly price obtained from a high and a low was assumed to be the price of the bond at the middle of the month. The yields were first calculated from ordinary bond tables and then checked with a Johnson and Darville bond yield chart.22 In Appendix A, Table 1 is given a description of each bond used; in Appendix A, Table 2 are given the monthly high and low prices of each bond used from January 1857 to January 1879 inclusive. The latter table was introduced for this particular period to facilitate the work of future students of the subject. We felt that some investigators might be interested in checking up the relations of the price of greenbacks in gold to the movements of these bonds during this period and for that purpose might be interested not only in yields but also in prices. The table is not continued beyond January 1879. In the succeeding gold period the reader is likely to be satisfied with 'yields'. Moreover, while it is difficult to obtain some of these prices of the earlier period, it is relatively easy to obtain the prices of the later period. 22 The use of this nomograph makes arithmetic interpolation between yields and between dates unnecessary. The possible error in reading is seldom more than one one-hundredth of one per cent. The chart was patented in 1922 by its inventors and is sold by Prentice-Hall Inc., New York City. It is described, with illustrations, in Justin H. Moore's Handbook of Financial Mathematics, pp. 501-5.

They are nearly all contained in the files of the Commercial and Financial Chronicle. In Appendix A, Table 3 is presented the yield of each individual bond monthly from January 1857 to January 1936, inclusive. Appendix A, Chart 29 shows the period during which each individual bond was used in the construction of index numbers.

Having selected the bonds and calculated their yields we proceeded to consider the construction of index numbers.²³ The first problem that now presented itself was that of adjusting the yields in order to equalize the maturities—or better perhaps say to equalize the 'durations'. As our problem was the measurement of long time interest rates, it seemed desirable to define the term 'long'. If we defined 'long' as 15 or any other specific number of years' 'duration', we were immediately faced with the fact that, in any particular year, perhaps none of our bonds had a duration of exactly 15 years. Moreover, even if each of their durations were exactly 15 years, with each succeeding year those durations would decrease.

We asked ourselves, would it not be possible from the actual yields of bonds with various durations to calculate what the probable yield would have been if each bond had had at all times the same duration say 15 years. We puzzled over this problem for some time. In some periods we found a quite perceptible degree of correlation between yield and duration. In general when short term rates such as those for call money, time money and commercial paper were high, the bonds with shorter durations tended to show the higher yields, and vice versa, when short term rates were low, the bonds with shorter durations tended to show the lower yields-though in almost all cases there were some evidences of 'lag'. However, the scatter was always extremely great and the correlation always small. The bonds differed not only in duration but also in grade. The regression was unmistakably nonlinear though the curvature was, of course, distinctly less than if maturity had been used instead of 'duration'. We experimented with various functions of the yields; and with partial regression, attempting to introduce the element of security into the problem by assuming it to be measurable in terms of the yields themselves. But the scatter invariably 23 Index numbers intended to show the course of long term interest rates must be based on vields and not on prices. A 4 per cent bond selling on a 5 per cent basis will increase in price from year to year if it remains on a 5 per cent basis. Similarly a 6 per cent bond selling on a 5 per cent basis will decrease in price from year to year. Neither price movement would have any simple relation to the interest rate problem.

remained so large as to make any equation derived from the data unmistakably worthless. We finally gave up all attempts to correct for 'duration'. The adjusted yields always seemed to smack too strongly of unreality.

We must admit that consequently a disturbing element, for which we have not corrected, remains in all our results. Moreover, as both the average maturity and the average duration of the bonds we used were shorter in the earlier than in the later period, the index numbers naturally refer in the earlier period to shorter term interest rates than they do in the later period.

In constructing any index number of railroad bond yields for such a long period as from 1857 to 1936 it naturally is impossible to carry the same bonds through the index. The bonds mature and disappear and, if they are being used to measure long term interest rates, they must be discarded years before they mature. This condition naturally necessitated many substitutions in the index. Such substitutions were always made in a January. The resulting index number is therefore a 'chain' index number, made up of 79 separate pieces, each extending over 13 months. The direct comparisons are always from one January to the second January, from the second January to the third, and so on, the intervening months falling into their respective places. In other words, there is always a group of bonds that is unchanged from one January to the next, making possible a comparison from that January to the next with an identical group of bonds. The 79 separate index numbers, each covering 13 months, were chained together in the following manner: If the January 1924 average obtained from the yields of the group of bonds used in the 13 months, January 1924 to January 1925, was eleven-tenths of the January 1924 average obtained from the yields of the group of bonds used in the 13 months, January 1923 to January 1924, it would be multiplied by ten-elevenths. If the adjustment were being made backwards the second January average would be multiplied by eleven-tenths.

As the bonds used in the index number are changed, comparisons of distant dates might be thought to become more and more dangerous. On the other hand, we must remember that railroad bonds constitute a relatively homogeneous group. The introduction of even an entirely new group of bonds each January would not necessarily lead to bad results. We seldom changed any large percentage of the bonds in any

one January. Both the number dropped and the number introduced were usually small, but this is probably not very important. Perhaps as many dangers are connected with keeping the same bonds throughout as arise from changing them. We must remember that there is no particular magic in continuing to quote the price of 'the cow with the crumpled horn' until she becomes a museum piece.

No 'weighting' was used in the construction of any of the various index numbers.24 Each yield has a weight of one. It did not seem advisable to attempt to assign other than equal weights to the individual yields. While it would be possible to construct a set of arbitrary weights based on the number of bonds outstanding, the number traded in, or other similar criteria, it is questionable whether there would be much value in any such procedure. Weighting by number of shares outstanding would seem highly reasonable if we were constructing an index number of stock prices. And weighting by number of bonds outstanding might be defended in the construction of an index of bond yields that was designed not to exhibit the course of interest rates but rather the fortunes of the borrowing corporations and of the investing public. It would seem a distinctly arbitrary and erratic system of weighting were we concerned primarily with interest rates. On the other hand, if we use number of bonds traded in as a basis for a set of weights, we shall find ourselves weighting an issue less and less heavily as it becomes seasoned. The heaviest trading occurs immediately after a bond is issued. Some of the best bonds become more and more inactive, until finally they cannot be used at all because months elapse without a single sale. If, however, anything happens to shake the confidence of the investing public in an issuing corporation, its bonds come out of safe deposit boxes and the volume of trading immediately increases.

As our index numbers are—from the nature of the data—necessarily 'chain' numbers, it is extremely important that no type of averaging used shall involve any mathematical 'drift'. We present index numbers based on geometric and arithmetic averaging, but the averages are averages of the yields themselves. They are not averages of 'relatives'. Not merely the geometric but also the arithmetic averages are therefore free from mathematical drift.

²⁴ Except the implicit weighting in the illustrations of the results of constructing chain index numbers from January to January from averages of relative prices with either the earlier or the later January as 'base'.

There are drifts in the averages, to be sure, but they are not mathematical drifts. They are economic drifts. They are caused by secular and cyclical changes in the grades of the bonds. Because their outlook is more seriously affected by fluctuations in earnings, lower grade bonds of course change in grade more violently than do bonds of better grade. This explains why the geometric and arithmetic averages show long time tendencies to drift together or drift apart. From 1857 to 1872 and from 1920 to 1930, and indeed in general from 1857 to 1930, indexes based on arithmetic averaging and indexes based on geometric averaging drift together as we move forward in time. During other periods, such as 1911 to 1920 and 1930 to 1932, they move more or less sharply apart.

But the drift is an economic drift. So long as an industry as a whole is, either because of general business conditions or because of conditions peculiar to the industry, in a period of health and growth, the spread between the yields of any two bonds, one low grade and one high grade, will tend to decrease. Similarly, the 'scatter' of the yields of a group of bonds of various grades will tend to decrease and hence the arithmetic and geometric averages of the yields will tend to approach each other. If the industry enters upon a period of declining business and profits, the scatter of the yields and hence the spread between the arithmetic and geometric averages will tend to increase.

But this drifting together and apart of the arithmetic and geometric index numbers is of greater theoretical than practical importance. For all practical purposes (as may be seen from Appendix A, Table 4) the two index numbers move together. But there is a drift in *both* which is of great importance. In January 1925 the figure for the geometric index (4.774 per cent) and the figure for the arithmetic index (4.776 per cent) are respectively the actual geometric average and the actual arithmetic average of all the bonds used in that month. However, the chain index constructed from geometric averages shows a yield of 9.517 per cent in January 1857 although the actual geometric average of all the bonds used in January 1857 was only 7.994 per cent.

Moreover, the above comparison does not present the picture in as strong colors as it should be presented. There is every reason for believing that the bonds which each month throughout the period showed the very lowest individual yields were much more nearly of the same grade throughout the period than was the average of all the bonds. Now the geometric average index number for January 1857 (9.517, per cent) is

152 per cent of the yield of the 'best bond' in the same month (6.27 per cent) though in January 1925 the index (4.774 per cent) is only 106 per cent of the yield of the best bond used in that month (4.50 per cent). The arithmetic differences are even more startling than the ratios. In January 1857 the difference between the geometric index and the yield of the best bond was 3.25 per cent while in January 1925 it was only 0.27 per cent. The relations of the geometric index to the yields of the best bonds and to the actual geometric averages of the bonds used each year may be seen in Chart 1. The evidences of a pronounced downward drift are unmistakable.

The arithmetic average index numbers show a slightly greater downward drift. We have used the geometric average index numbers to illustrate drift because the reader is less likely to wonder whether he is not faced with a problem of *mathematical* drift or, as Professor Fisher terms it, 'bias'.

In the next two chapters we discuss further the nature of this economic drift. We describe not only how it can be eliminated to obtain index numbers of the yields of hypothetical bonds of superlative grade but also how it can be separated out, measured, and used by itself as an index of the degree of difference at any particular time between the movements of the yields of high and low grade bonds. Finally, we describe its relation to the movements of the prices of common stocks and show how, when properly interpreted, it brings together all securities into one great family.

CHAPTER IV

THE RELATION OF THE MOVEMENTS OF BOND YIELDS TO THE GRADES OF THE BONDS— ECONOMIC 'DRIFT'

 $T_{
m HE}$ drift of the arithmetic and geometric index numbers of railroad bond yields referred to at the close of the preceding chapter is, as we there stated, not a mathematical drift. It is an economic drift. It is not like the upward drift of chained arithmetic averages of relative prices or the downward drift of chained harmonic averages of relatives. During most of the period covered by this study (January 1857 to January 1936) the drift has been downward but that direction was not mathematically necessary. Indeed, the drift was sometimes upward. For example, while the geometric index figure (see Appendix A, Table 4-1) for January 1857 (9.52) was more than 151 per cent of the yield of the lowest yield bond used in that month (6.27) and the index figure for January 1929 (4.50) was only 104 per cent of the yield of the lowest bond for that month (4.33), the index figure for January 1933 (5.22) was 128 per cent of the lowest yield for the month (4.06), or *larger* than the percentage (127) that the index figure for January 1865 (6.87) was of the lowest yield for that month (5.43). In other words, using such a criterion of drift, we find a pronounced downward drift from January 1857 to January 1929, a period of seventy-two years; but, on the other hand, when we compare January 1865 with January 1933, sixty-eight years from the one date to the other, we find for the period as a whole, a slight upward drift.

An examination of Chart 15, on which a cumulation (inverted) of the drift ' is presented, shows that the *upward* drift of the yields of the lower grade bouds was so great in the recent economic collapse that, from November 1928 to June 1932, the cumulated drift recovered all 'The method used to measure drift is explained later in this chapter.

the ground it had lost from 1865 to 1929. The picture presented by Chart 15 is one of rapid drift downward from 1857 to 1872, an irregular but roughly horizontal movement from 1872 to about 1900, a renewal of the rapid drift downward from 1900 to 1912, an upward drift from 1912 to 1920, a pronounced down drift from 1920 to 1929 followed by an up movement, so violent that it can hardly be described as a 'drift' at all, that lasted until the middle of 1932.

In 1913 Professor Wesley C. Mitchell published an index number of the yields of ten American railroad bonds, monthly, from January 1890 to December 1911 inclusive. Now, though there seems to have been little or no 'drift' in railroad bond yields from 1890 to 1900, there was a pronounced down drift from 1900 to 1912 and hence the total drift from January 1890 to December 1911 was strongly downward. This downward drift showed itself, as was to be expected, in Professor Mitchell's group of bonds. He noticed and explained it. His discussion and comment runs, in part, as follows: 6

"The differences shown by Table 19 among the net yields of the ten bonds may readily be accounted for by differences in the proportionate value of the underlying properties, by the existence or non-existence of prior liens, by the relative financial strength of the issuing or guaranteeing corporations, etc. Similarly, the frequent changes in rank among the bonds may be ascribed to alterations in these particular conditions, which a well-advised investor considers in estimating the risks he runs in buying securities.

"But there is one fact of more general interest about these differences in yield. The margins between the higher and lower yields have grown narrower in the course of twenty years. In 1890 the maximum difference was 5.24–3.88 per cent=1.36; in 1900 it was 4.40–3.42 per cent=0.98; in 1909, 4.24–3.87 per cent=0.37. The chief cause of this narrowing of the margins has been an improvement since the middle nineties in the credit of the lower grade issues among investors. The risks imputed to the holding of bonds of such railways as, for example, the Chicago and Eastern Illinois have diminished. With one exception—the bonds of the West Shore Railroad—all the bonds gave lower yields in 1911 than in 1890. The West

² For the figures, see Table 6, Appendix A.

⁸ Note again that in Chart 15 the cumulated drift is inverted.

⁴ There were no substitutions; the same ten bonds were used throughout the period. ⁵ The violent up-drift during 1907 was immediately offset on the cumulated drift by the violent down-drift of 1908 and the first half of 1909 (see Chart 15).

⁶ Business Cycles (University of California Press, Berkeley, 1913), pp. 156 and 157.

Shore bonds, guaranteed principal and interest by the New York Central and having over 400 years to run, were rated decidedly higher by investors in 1890 than any other security in the present list. But, since then, the improvement in the financial condition and prospects of other railways has gradually brought their obligations closer to the high standard of securities guaranteed by the New York Central. Indeed, in recent years the bonds of the Burlington, the Milwaukee, and the Central of New Jersey have frequently outranked the bonds of the West Shore."

This is all quite as one might expect. Movements of the yields of bonds of the highest grade reflect primarily changes in 'long term interest rates'. On the other hand, movements of common stock prices reflect also the market's estimate of future earnings and dividends. Bonds other than those of the highest grade naturally partake of the nature of both the highest grade bonds and common stocks. The movements of their yields are affected not only by long term interest rate considerations but also by forecasts of earnings. In Chapter V it is shown that there has been a noticeable similarity between the major movements of the cumulated railroad bond yield 'drifts' and the major movements of prices of railroad common stocks. And the secular trend of railroad stock prices was upward from January 1890 to December 1911 while the secular trend of the cumulative bond yield drift was downward.

But, though the drift in the index numbers based on arithmetic and geometric averages of the yields themselves is not a 'mathematical' drift, the reader may possibly wonder to what extent it is a merely technical drift. In the selection of the bonds, those that improved in quality year after year were not discarded because of that fact but those that deteriorated very rapidly (as the roads became bankrupt or ran into great financial difficulties) were eliminated. And, as the reader will realize later in this chapter, the retention of such bonds throughout their periods of deterioration and collapse might easily have affected to a greater or less extent the movements of the cumulated 'drift'—by reducing its downward movements and increasing its upward movements.

Indeed, if such deteriorating bonds had been retained, the cumulated drift line of Chart 15 might possibly have been more a shadow of the

⁷ In connection with this inverse relation, the reader must note that the comparison is not between stock prices and bond prices but between stock prices and bond yields (see Chart 15).

stock price line than it is. It is intriguing to think so. When an economist presents an interesting statistical relation to his readers' attention, it is pleasant to imagine and he may easily be tempted insidiously to suggest that, if the data were more adequate or more skillfully handled, the relation would stand out even more strikingly than it does. And, in at least one minor movement (from January 1903 to January 1904, during which time stock prices declined violently while the cumulated 'drift' of the bond yields also declined, instead of advancing as it would have been expected to do), the non-conformity is clearly traceable to the difference in the action of medium grade and definitely low grade bonds, as seen in the non-linearity of the scatter.

But, unfortunately, tests with unchanging groups containing bonds of grades ranging all the way from the highest to really low grade suggest strongly that the elimination of bonds when they begin to deteriorate rapidly, as evidenced by the rise in their yields, has usually only a very minor effect on the *long term* movements of the cumulated linear drift. Convexity of the scatter ¹⁰ over a short period of falling stock prices tends to be followed by concavity while stock prices are recovering and the *long term* effects on cumulated linear slopes to be thus offset.

That mere changes in the list do not necessarily increase the downward drift is well illustrated (though not proved) by comparing the cumulated drift of our changing list of bonds from January 1890 to December 1911 with the cumulated drift of Dr. Mitchell's unchanging list of ten bonds. The ratio of Dr. Mitchell's index number to our unadjusted geometric index was, in January 1890, 1.04. In January 1900 it was 1.03, and in January 1911, 0.99. The ratio of his index number to our unadjusted arithmetic index was in January 1890, 1.03, in January 1900, 1.02, and in January 1911, 0.99. The downward drift of his index number was therefore slightly greater than that of our unadjusted numbers.

Indexes from which drift has not been eliminated are not indexes of the yields of a uniform grade of bonds. They have, moreover, no essential relation to the average yield of all bonds outstanding

⁸ The reader must be reminded again that the cumulated drift line of Chart 15 is, on that chart, *inverted*.

⁹ See Chart 8 and discussion in the last section of this chapter, ¹⁰ With respect to the x axis,

or to the average rates at which new issues are coming out. They are indexes 'of the net returns which permanent investors have received upon current purchases of bonds' only if the assumption be made that the investors bought only these particular bonds. To have included a few bonds of a lower grade than those used would probably have altered not merely the level of the index numbers, but also their movements. In a period of downward drift, it would increase the downward (or decrease the upward) movement of the index numbers. Though it is true, as Dr. Mitchell has suggested, that index numbers from which drift has not been eliminated tell a different story from those without drift, that story, as we shall see, is more difficult to interpret than he indicated:

"The average yield of all ten bonds is the best available gauge of the changes in the rates which large American corporations have paid for new loans on long time since 1890, and also the best gauge of the net returns which permanent investors have received upon current purchases of bonds. But it is distinctly not the best gauge of changing rates upon long loans of substantially uniform security. For the latter purpose the yield of the West Shore bonds is preferable, since the financial credit of the guarantor was so firmly established in 1890 as to be little shaken by the years of depression and little strengthened by the years of prosperity. In other words, the yields of this issue reflect the changes in the supply of, and the demand for, loan capital for fixed investment with less distortion by the factor of risk than do the yields of the nine other bonds. But, since the yields of the other bonds are more typical of American experience since 1890, the detailed tables have been arranged to show both the net yields of the West Shore bonds, and the average net yields of all ten" (Business Cycles, p. 157).

Though Dr. Mitchell was correct when he stated that the yields of West Shore 4's give, during the period he was covering, a better picture of 'changing rates upon loans of substantially uniform security' than does his index based on the arithmetic average of the yields of ten bonds, the fact is that the yields of no single bond are completely adequate for this purpose. There are erratic movements in the yields of any individual bond, even West Shore 4's. Though West Shore bonds acted for long periods remarkably well, there is strong evidence that their grade varied appreciably at times. For example, a comparison of their yields with the yields of the very highest grade railroad bonds,

or better, with the '4.50 sigma' index, which we present and explain later, shows that the West Shore bonds were declining in grade from 1890 to 1900 and improving from 1900 to 1911. Since 1930 the bond has been definitely out of the class of bonds of the highest grade.

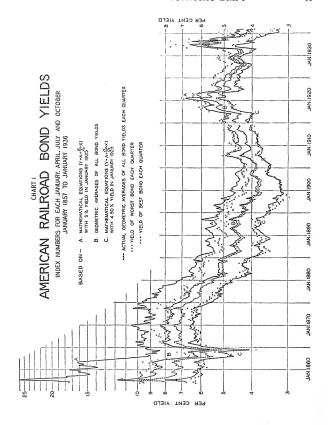
How well 'changing rates upon loans of substantially uniform security' may be measured by the yields of individual bonds may be seen by examining Chart 2. One of the indexes (line C) of that chart was constructed by chaining together the yields of three extremely high grade bonds: "1 bond no. 10 (Pennsylvania 6's, due December 31, 1880) is used from January 1857 to January 1870; bond no. 33 (Lehigh Valley 6's, due June 1, 1898), from January 1870 to January 1886; and bond no. 70 (West Shore 4's, due January 1, 2361), from

January 1886 to January 1936.

If, instead of constructing an index number by chaining together the yields of a few high grade bonds (as is done in Chart 2), we use as the index for each month the yield of the bond showing the lowest yield in that month, we should, theoretically, obtain an even closer approximation to a measure of the yield of long term loans of an extremely high and nearly unchanging degree of security. The difficulties of this procedure are practical rather than theoretical. Because any especially good bond may shoot forward into first place in any particular month, such an index tends to be distinctly more erratic in its minor movements than one constructed by chaining together a few superlative bonds. Furthermore, the necessity of removing entirely from the field of choice a specific high grade bond because it has approached too close to maturity may cause sudden erratic movements in the level of the entire index number. The next best bond available may be selling on an appreciably higher yield. Of the bonds we used in this study, the yields of those having the lowest yield each January, April, July and October, together with various index numbers, are presented on Chart 1.

It might be thought that an improvement on both procedures outlined above could be made by constructing a chain index number, using each month the yield of the bond having the lowest yield in that month and carrying the same bond through to the next month. Each of the individual index numbers that would be chained together would be

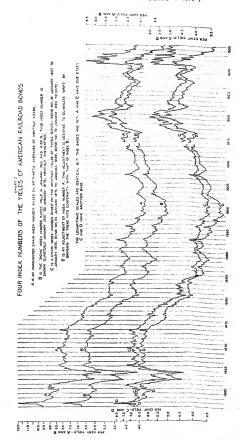
¹¹ The West Shore bonds were allowed to remain in the chart after 1930 to illustrate how a bond may suddenly deteriorate even though it has been high grade for years.



only one month long. The first piece would consist of the yield of the bond having the lowest yield in the first month and the yield of the same bond in the second month. The second piece would consist of the yield of the bond having the lowest yield in the second month and the yield of this same bond in the third month, etc. Such an index number would be free from the sudden changes in level that result from using each month the unadjusted yield of the bond having the lowest yield in that month. Moreover, during periods when the chaining procedure happened to use the yields of only one specific bond, the results would, of course, be similar to those shown by line C of Chart 2.

However, when the bonds used are not the same bond, a clear-cut upward mathematical drift would be introduced. In any particular month the bond selected is the bond having the lowest yield in that month. If the same bond has the lowest yield in the next month, the movement of the index will be the same as the movement of an index that used each month the unadjusted lowest yield. If the bond used in the first month is not the bond having the lowest yield in the second month, it must have a higher yield. One step in an upward drift has been made. That step can never be retraced. We begin all over with the bond having the lowest yield in the second month. In general, the shorter the periods used for the individual index numbers, the greater will be the upward drift. It was clearly not worth while to calculate such an index number on a monthly basis merely for the purpose of showing that it had an upward drift such as to make it totally unusable.

But we did calculate one such index on an annual basis—January to January each year. Beginning in January 1857 with the yield of the bond having the lowest yield in that month (6.27 per cent) and working forward, the index gives a value of 5.63 per cent for January 1879. In that month the yield of the 'best bond' was 4.86 per cent, and even the geometric average of all the bonds used was only 5.71 per cent. By January 1900 the index is 3.83 per cent. This is greater than the geometric average of all the bonds used in that month (3.73 per cent). The yield of the best bond was only 3.18 per cent. In January 1932 the index stood at 7.73 per cent. This is not only much greater than the yield of the best bond in that month (4.57 per cent) and greater than the geometric average (5.68 per cent) but also actually a shade greater than the yield of the bond showing the highest yield of any bond used in that month (7.72 per cent). The results



would have been still more startling if we had constructed the index on a monthly instead of a yearly basis.

An index number constructed by chaining together individual pieces each of which consisted of the yield of the lowest yield bond at a particular date and the yield of the same bond in the preceding year or month would show a contrary mathematical drift, downward instead of upward.

More interesting results may be obtained if we do not restrict ourselves to one bond. Index numbers constructed from the best five bonds in each yearly period naturally show much less erratic and individualistic movements than index numbers constructed from the yields of single bonds.

Our bonds are in annual groups. Each group contains quotations for the yields of certain bonds from January to January inclusive. If out of such a group we select the five bonds having the lowest yields in the first January and the five bonds having the lowest yields in the second January-whether or not they be the same-and compare the geometric average of the yields of the five bonds chosen in the first January with the geometric average of the yields of the five bonds chosen in the second January, we obtain a set of 79 index numbers each extending from one January to the next.12 The result of chaining together these 79 index numbers is presented in Chart 3 (line B). Line D is the '4.50 sigma' index, which we later present as a tentative solution of the problem of drift. It will be seen that the index constructed from the best five bonds, in the manner we have just described, is very similar to the '4.50 sigma' index. The downward drift is slightly greater but the year-to-year movements are almost identical. This particular five-bond index has, of course, no mathematical drift. For example, the same results would be obtained if the index were cal-

¹² Though the 'best' five (or lowest yield) bonds chosen in a particular January in order to construct the index number from the preceding January to that January are usually the same as the best five bonds chosen in that January to construct the index number from that January to the succeeding January, they are not always so. The dropping of old bonds and the introduction of new bonds sometimes prevents such a condition. For example the 'best' five bonds chosen for January 1925 to construct the index number from January 1924 to January 1925 are not the same bonds as those chosen to construct the index number from January 1925 to January 1926.

culated from month to month as if it were calculated from year to year.

Chart 3 shows two other indexes based on the best five bonds each January. One of these (line C) is constructed by chaining together yearly indexes in each of which the geometric average of the yields of the best five bonds in the earlier January is compared with the geometric

CHART 3
FOUR INDEX NUMBERS OF JANUARY YIELDS OF AMERICAN RAILROAD BONDS

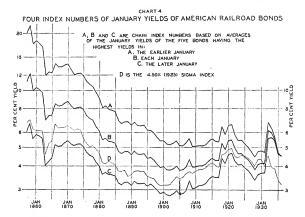


ric average of the yields of the same five bonds in the later January. In the other index (line A) the five bonds are the best five in the later January and the comparison is made with the yields of the same five bonds in the earlier January. Both the upward drift of the index of yields based on choosing the bonds in the earlier January. 18 and the downward drift of the index based on choosing the bonds in the later January are, of course, mathematical and not economic drifts. The drift would in each case have been greater if the indexes had been constructed from month to month instead of from year to year. The three

¹³ As a digression, it may be interesting to note that the index based on choosing the best five bonds at the beginning of the year gives a rather sad picture of the fate of the investor who would buy nothing but bonds with the very lowest possible yields, on the assumption that such low yields proved the bonds to be of the most desirable type, and insisted upon selling them, whenever their yield rose, and reinvesting in other 'superlative' bonds.

index numbers based on the 5 bonds having the lowest yields each year are presented in Appendix A, Table 5.

Chart 4 is introduced as a further illustration of mathematical rather than economic drift and to show the dangers of attempting to correct for economic drift by means of introducing a mathematical drift that is in the opposite direction. The bonds chosen each January are



the *worst* five bonds instead of the best five bonds, that is, the five bonds having the highest yields instead of the five bonds having the lowest yields. Throughout most of the period 1857–1936 there has been a pronounced downward economic drift in the yields of these 'worst' bonds. However, the mathematical upward drift introduced by picking them in the later January and comparing the geometric average of their yields in that January with the geometric average of the yields of the *same bonds* in the earlier January (see line C) is more than sufficient to overcome the downward economic drift.¹⁴

On the other hand, the intermediate movements show driftings apart and driftings together. After remaining below D until January 1931, ¹⁴ Indeed, if the chaining had been from month to month instead of from year to year, line C would have shown an almost continuous uprand drift when compared with the 4.50 sigma line.

the line C suddenly shoots up and remains thereafter much above D. The minor movements of the two lines often have little or no relation to each other. While the adjustment for drift obtained by using the best five bonds, regardless of whether they were or were not the same bonds in both Januaries, is an economic adjustment and led to relatively good results throughout, the adjustment based on choosing the worst five bonds in the later January is purely mathematical. The goodness of the results in any period is quite accidental.

It is quite illegitimate to attempt to eliminate economic drift by means of a formula giving a mathematical drift in the opposite direction. In the first place, the economic drift is not necessarily in the same direction in one period as it was in the preceding period, whereas the mathematical drift tends to be always in the same direction. In the second place, any mathematical drift that results from 'chaining' varies in degree with the duration between the items chained. Monthly chaining gives a more pronounced drift than yearly chaining.

The disturbing effects of economic 'drift', of course, usually increase with the length of time covered. Over short and comparatively undisturbed periods index numbers from which drift has not been eliminated often have a relatively definite and simple significance. Without any great error, they may be interpreted as picturing the movements of the yields of bonds of the same grade. Over long periods they may, however, have little essential relation to the yields of bonds of any specified grade. Even if the same bonds are used throughout, their grade at the end of the period, as seen from the relation of the average of their yields to the yields of the best bonds, may be entirely different from what it was at the beginning of the period.

Of course, if we had been interested only in eliminating drift, we might, as has already been suggested, have done so pretty well by some such procedure as the chaining together of indexes made up from the yields of the five lowest yield bonds whether they were the same bonds at both dates or not. But we were fully as much interested in discovering the characteristics of drift and how it can be measured as we were in eliminating it. We wished not merely to present a picture of the movements of the yields of railroad bonds of the highest grade but also to show how bonds of lower grade acted and to present in as simple a mathematical form as possible the statistical relations between the movements of the yields of bonds of different grades.

And, finally, we hoped to be able to bring the movements of stock

prices into the bond yield picture.

We soon came to the conclusion, already presented in the preceding chapter, that no definite solution could be obtained by studying the financial statements of the railroads. 'Margins of safety', etc., are illusory and misleading. The real 'margin of safety' that counts is in the future, not the past. It is better to trust to the opinion of the market. The simple and direct way to decide whether, at a particular time, one bond should be considered as of a higher or lower grade than another bond of the same coupon rate, maturity, marketability, etc., is to compare their yields. The problem is therefore to discover the relation between the movements of the yields and the yields themselves. When this problem is solved it becomes possible to construct, as a by-product, an index number of the yields of the highest grade bonds—even if the grade desired be somewhat higher than the grade of any of the bonds used in discovering the relation.

The railroad bonds we used had as long maturities as were available. Since, as already mentioned, we did not adjust for differences of duration, we formulated our problem as that of discovering, with the data available, what were the relations between the yields of identical bonds at different dates. We began our experiments by considering the matter graphically. We made scatter diagrams in which the yields at a particular date of the various bonds in a group were plotted along the x axis and the yields at a later date along the v axis. We plotted the logarithms of the yields rather than the yields themselves, because a linear relationship seemed more logical on a logarithmic scale than on a natural scale. For many reasons, we desired a linear relationship and the use of a linear relation with a natural scale would tend to lead to absurdities in just the region where we did not wish absurdities-the region of the lower yields. For example, if a straight line were fitted to the yields as such, it might cut the axes and so suggest that a positive yield in one period should be considered as normally associated with a negative yield in another period.

After constructing and examining a number of scatter diagrams, we next considered how we ought to fit straight lines to the logarithms of the data. What should be the criterion of fit? We of course realized that the yields in neither the earlier nor the later period—say the earlier or the later January—could logically be considered as independent vari-

ables. Both the yields in the earlier and the yields in the later January had to be considered as dependent variables. We did not wish to know what would be the probable yield in the later January of a particular bond having a specified yield in the earlier January any more than we wished to know the probable yield in the earlier January of a particular bond having a specified yield in the later January. For the same sort of reasons that we did not find it desirable to pick the best five bonds in either the earlier or the later January but in both Januaries, we desired a backwards and forwards relation between the yields in the two Januaries. To borrow an expression from the theory of least squares, our problem must be considered one in which both variables are assumed to be 'tinged with error'. 15 The straight line must not be fitted in such a manner that the sum of the squares of either the vertical or the horizontal deviations of the data points from the fitted line be made a minimum but in such a manner that the sum (or, academically, onequarter of the sum) of the squares of the vertical and horizontal deviations be made a minimum, 16 if the size of the errors to which the two variables are subject is the same.

Both variables should be, for the purposes of our problem, considered as 'subject to error'. But we cannot assume that the size of the 'errors' to which each variable is subject is the same. In other words, we cannot assume that the 'errors' of the two variables should have equal weights. Using 'error' in the statistical sense of deviation, we know that the two variables are not subject to the same degree of 'error'. Their liability to error is clearly in proportion to their standard deviations. Before fitting the straight line we must therefore weight the variables in inverse proportion to the squares of their standard deviations. Such weighting will exactly correct for the fact that their liability to 'error' is in proportion to their standard deviations.

This may all sound rather high-handed. At first glance it might seem simple and proper to give the logarithms of the yields in each January equal weights. However, in a statistical problem in which both variables are considered as subject to 'error', the assumption of equal ¹⁵ Of course the statistician uses the word 'error' in a Pickwickian sense. When he measures the average height of a class of school children and finds that it is so many feet and so many inches, he does not consider the fact that all the children are not of that height as really an 'error' of either God or man.

16 Cf. Merriman's The Determination by the Method of Least Squares of the Relation between Two Variables... both Variables being Liable to Errors of Observation (U. S. Coast and Geodetic Survey, 1890), p. 687.

weights may be very misleading. It tends to prevent any real consideration of the problem of weighting. Only if the variables are measured in absolutely unlike units, such as length and weight or pressure and temperature, will the existence of the problem be even noticed. When, however, as in our problem, both variables are expressed in percentages—or logarithms of percentages—there is a strong tendency to let mere words lull us into the assumption that we have a problem requiring equal weights. However, in our particular problem, a procedure based on such an assumption would have led us to treat a one per cent deviation of observation from theory in one January as of the same importance as a one per cent deviation in the succeeding January, although the scatter of the yields in the later January might be so much greater than the scatter of the yields in the earlier January that their standard deviation was double that of the yields in the earlier January.

The slope of the straight line, fitted in such a manner that the sum of the squares of the vertical and horizontal deviations of the observed from the theoretical values (when weighted in inverse proportions to the squares of the standard deviations of the two variables), will be a minimum, is $\frac{\sigma_y}{\sigma_x}$, where σ_x = the standard deviation of the logarithms of the yields at one date and σ_y = the standard deviation of the logarithms of the yields at the other date. From the mean of the system,

the equation of the line is $y = \frac{\sigma_y}{\sigma_x} \ x^{\text{note 17}}$

17 The weighting is in inverse proportion to the squares of the standard deviations, rather than in inverse proportion to the standard deviations unsquared, because the criterion of fit is that the squares of the 'deviations' shall be a minimum.

The 'deviations' are not, of course, equal to the perpendicular and horizontal distances of the observational points from the fitted line. For example, a y 'deviation' is not equal to the perpendicular dropped from the observational point to the fitted line, as it would be if the x variable were being considered independent. A y 'deviation' is the difference between the y of an observational point and the y of the corresponding theoretical point on the straight line. And that theoretical point is not perpendicularly above or below the observational point. The slope of the line joining an observational point to its corresponding theoretical point on the straight line is

 $^{-\}frac{\sigma_y}{\sigma_x}$, that is, the slope of the fitted line with a negative sign. Now the sum of the squares on the two sides of a right angled triangle adjacent to the right angle is equal to the square on the hypotenuse. It is, therefore, the sum of the squares of the oblique distances of the observational points from the corresponding theoretical points on the fitted straight line that is made a minimum.

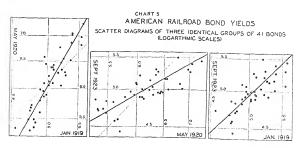
If the straight lines be fitted in this manner, all index numbers based on readings from the fitted lines will fulfill the 'circular test'. If, on the other hand, the observations at the two dates be weighted 'equally', or indeed in any other ratio than in inverse proportion to the squares of their standard deviations, the index numbers obtained from readings on the fitted lines will not fulfill the 'circular test'. Some form or other of purely mathematical drift will be introduced. The results obtained by moving along from one month to the next in constructing the index numbers will not be the same as if we move from one January to the next January.

If ordinary 'regression' lines, in which only one variable is considered dependent, were fitted, the resulting index numbers (of lower than mean yields) would drift violently upward if the earlier dates were taken as the independent variables and violently downwards if the later dates were taken as independent. An index number constructed from our January-to-January scatters by taking the earlier Januaries as the independent variables and showing a yield of four and one-half per cent in January 1927 shows a yield of less than one-billionth of one per cent for January 1857. If the later Januaries be considered independent, a seven per cent yield in January 1857 is associated with less than one-billionth of one per cent in January 1927. The results would be even more extreme if the chaining were from one month to the next instead of from January to January. 18

The fulfillment of the circular test may be illustrated by Chart 5. That chart contains three scatter diagrams. The same 41 bonds appear in each diagram. The heavy fitted line in each diagram represents the theoretical relation (weights of the variables in inverse proportion to the squares of their standard deviations) between the yields at an earlier date and those at a later date of bonds of different grades. The 18 In computing the scatter from one January to the next, the coefficient of correlation (r) might possibly equal +1. If r equaled +1, the fitted lines obtained from assuming one or other of the variables independent or from assuming them both dependent would, of course, be identical. The observations would all lie in the line.

If r is not equal to +1, both the equal weights line and the sigma line will be steeper than the x-as-independent-variable line, and less steep than the y-as-independent-variable line. When $\sigma_y = \sigma_x$, the equal weights line and the sigma line will be identical. Each will be inclined 45°, that is, have a slope of +1. When σ_y is not equal to σ_x , the sigma line will fall between the equal weights line and the 45° line. It will, therefore, be steeper than the equal weights line when σ_y is greater than σ_x and less steep when σ_y is less than σ_x .

light line inclined at an angle of 45 degrees is the line on which all points would fall if the ratio of the yield of each bond at the later date to the yield of the same bond at the earlier date had been, for all bonds regardless of grade, the same as the ratio of the geometric mean of the yields of all the bonds at the later date to the geometric mean of the



yields at the earlier date. The first diagram compares the yields in January 1919 and the yields in May 1920, a period during which high grade bonds acted better than lower grades. The second diagram compares the yields in May 1920 and September 1923, a period during which high grade bonds acted worse than low grade bonds. The third diagram covers both periods. It compares the yields in January 1919 and September 1923, a period during which there is no correlation between the grades of the bonds (as evidenced by their yields) and how they acted. The heavy fitted line in this diagram therefore coincides with the light 45 degree line.

Now, if we find, from an examination of the first diagram, that a yield of x in January 1919 should theoretically, as determined by a point on the heavy fitted line, be associated with a yield of y in May 1920 and, from an examination of the second diagram, that a yield of y in May 1920 should theoretically be associated with a yield of z in September 1923, we may know that, if from the third diagram we ask what yield in September 1923 should theoretically be associated with a yield of x in January 1919, the answer will be z. Index numbers constructed from readings of straight lines fitted by the method of least squares in such a manner that the sum of the squares of the vertical

and horizontal deviations, weighted in inverse proportion to the squares of their respective standard deviations, is a minimum, fulfill the 'circular' test. To avoid the continual use of lengthy phrases we shall from now on call a straight line fitted in such a manner a sigma line. We coined this term because the slope of such a line is $\frac{\sigma_y}{\sigma}$.

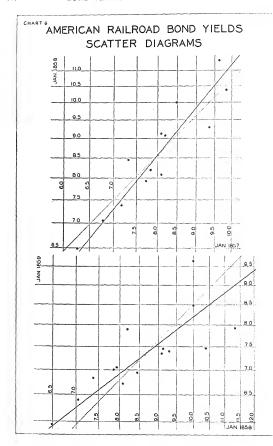
Chart 6 contains 79 scatter diagrams, one for each pair of Januaries from January 1857 and January 1858 to January 1935 and January 1936. Sigma lines are fitted to each scatter. From the nature of the slopes $\frac{\sigma_y}{\sigma_x}$ of a sigma line, the slope of a line fitted for two widely separated dates can easily be computed from the slopes of the lines for the intervening sections. Thus, if the standard deviation of the yields of a group of bonds be σ_x , in January 1920, σ_y in January 1921 and σ_z in January 1922, the slope of the sigma line for January 1920 and January 1921 will be $\frac{\sigma_y}{\sigma_x}$, for January 1921 and January 1922 $\frac{\sigma_z}{\sigma_y}$, and

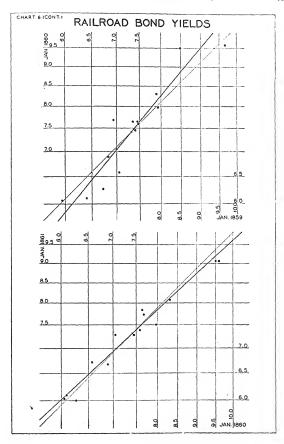
for January 1920 and January 1922 $\frac{\sigma_z}{\sigma_x}$. From the upper line of Chart 15 the reader can estimate the slope of the sigma line for any two dates. This upper line of Chart 15 represents the cumulated product of the slopes of the successive sigma lines fitted to the scatters of the yields in successive adjacent pairs of months. As the chart is drawn on a logarithmic scale, a difference in height of the line for any two different dates represents the logarithm of the slope of the sigma line applicable to those two dates. The annual and quarterly equations of the sigma lines are presented in Appendix A, Tables 7 and 8. The slopes

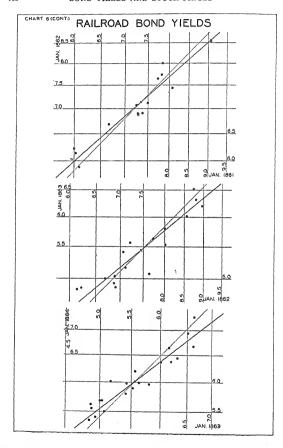
The sigma lines may be used for two purposes and are so used in this study: (1) to construct index numbers, (2) to illustrate, measure and study the differences in the movements of the yields of bonds of different grades in different periods.

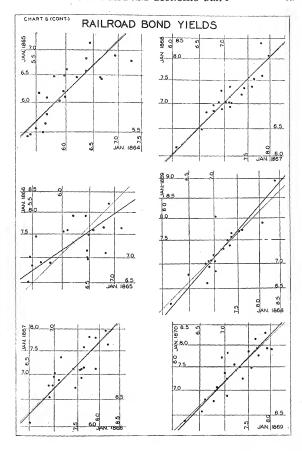
of the monthly equations are given in Table 9.

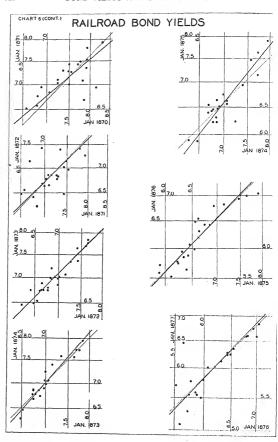
Beginning with any given yield at any particular date, we may construct a complete index number from January 1857 to January 1936. But the reader must not assume that such an index number would necessarily give a picture of the action of bonds of the same grade throughout the period. If the original yield with which the computative The 'difference in height' on the chart may be exactly determined from column 2 of Table 6 in Appendix A.

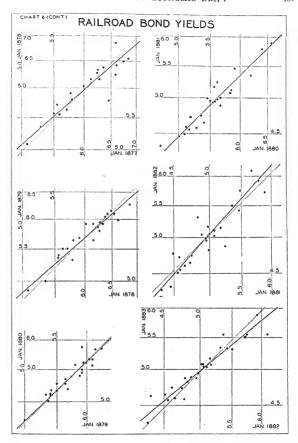


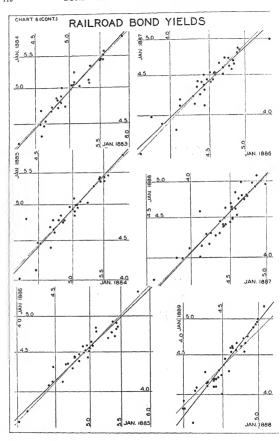


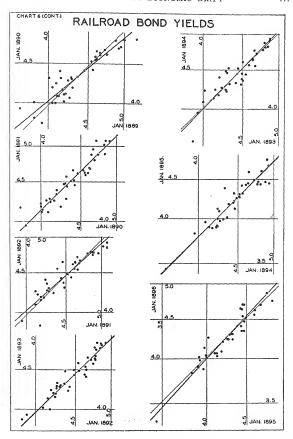


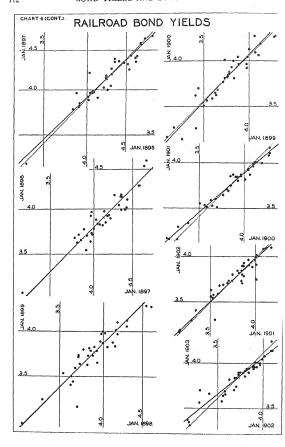


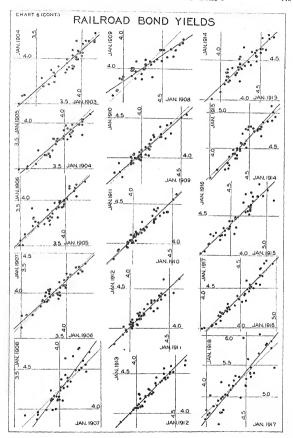


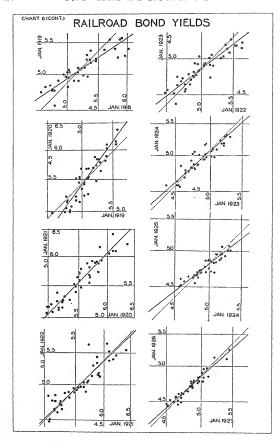


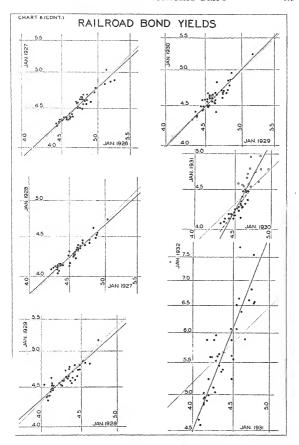


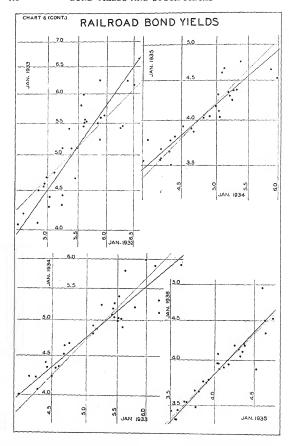












tions begin is a relatively high yield for the date to which it is attached, the index number will be affected by *drift*; and the essence of drift is that it is not a characteristic of the yield of bonds of low but unchanging grade but a movement *that results from change of grade*. The next step in the calculation is, therefore, from a new base, a new grade.

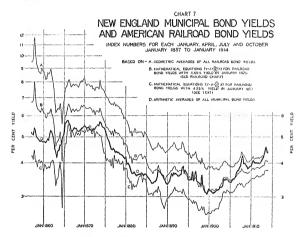
Drift, therefore, remains a disturbing factor unless the original yield from which computations begin is as low as the yields of bonds that at the time are so adequately 'covered' that none but really profound changes in the financial status of the debtor corporations could appreciably lessen the complete confidence of the market that all future payments would be met.

But the original basing point yield cannot safely be chosen appreciably lower than this, in other words appreciably lower than the yields of the best bonds, without introducing an element of unreality which results in an unmeaning pseudo drift in the direction opposite to that to which inferior bonds are subject. Of course, this simply means that extrapolation cannot, without sooner or later introducing palpable absurdities, be carried far into the unreal region of yields so low that no actual bonds can be found having such yields.

The index number that we calculated from the sigma equations to present a picture of the course of the yields of railroad bonds of the highest possible grade, a grade often slightly higher than that of any actual bond, was constructed by assuming a yield of 4.50 per cent in January 1925 and working backward to January 1857 and forward to January 1936. The lowest yield of any bond we used in January 1925 was 4.50 per cent. However, this is quite accidental. Throughout the entire period from January 1857 to January 1936, the sigma index, though it is more often lower than it is higher, tends to run fairly close to the yields of the lowest yield bonds. But it has no rigid relation to any individual yield. It weaves in and out among the lowest yields only because, in its character as an index from which 'drift' was presumed to be eliminated, it was designed to do so.

However, there is a possibility that some 'drift' remains in even this 4.50 sigma index. The 'best bonds' considered were after all only the best *railroad* bonds. Now an examination of the levels and movements of the highest grade New England municipal bonds in the period before 1914 can hardly fail to suggest that the best railroad bonds of the earlier years were not relatively so high in grade as were those of the

later years.²⁰ In Chart 7 there is presented not only the 4.50 sigma index, which shows a yield of 4.50 per cent in January 1925 and a yield of 6.75 per cent in January 1857, but also a sigma index that shows a yield of only 4.23 per cent in January 1857. A comparison of these two railroad sigma indexes with the index of the yields of New England municipal bonds presented on the same chart suggests that



either the yields of the New England municipal bonds had an upward drift during the period covered by the chart (January 1857 to January 1914) or the 4.50 sigma index had a downward drift. Since about 1875 the long term trend of the New England municipal bond index resembles the trend of the sigma index giving 4.23 per cent in Januare 1 the top prices of 1857 the long term 5 per cent (gold) bonds of Boston and Massachusetts both sold at 99, to yield only a small fraction more than 5 per cent; during 1880 Boston 4's of 1899 sold as high as 105; at the top prices of 1897 both Massachusetts 3's of 1923 and Maine 3's of 1921 sold at par. Now the lowest monthly yield of any railroad bond in our 1857 list was 6.17 per cent; in 1880 the lowest monthly yield was 4.31; in 1897 the lowest yield was 3.08. The differences between these railroad yields and the Boston, Massachusetts and Maine yields are 1.1 per cent, 0.7 per cent and 0.1 per cent.

ary 1857 more than it does the trend of the sigma index giving 6.75 per cent in 1857.

The great differences in the movements of the New England municipal bond index and the railroad sigma indexes during the Civil War period are peculiarly difficult to explain. And possibly no great effort to do so is warranted. An examination of Chart 6 will immediately show how very appreciable the probable errors of the slopes of the sigma lines in parts of this period must necessarily be. And the assumption of linearity seems sometimes very difficult to defend. ²¹ Chart 15 would suggest that, if the relation depicted by that chart is real, the measurement of drift from the wide and possibly non-linear scatters of the Civil War period may be very unreliable. For example, the downward drift must surely be underestimated from January 1862 to the middle of 1864 and overestimated from the middle of 1864 to the end of 1865.

But one of the difficulties of this argument is that great irregularities in the relationship pictured in Chart 15 occur in periods, such as that from the middle of 1877 to the end of 1880, in which the scatters are closely packed around the fitted straight lines and during which there is no great difference in trend between the New England bond index and the railroad sigma indexes. An adequate explanation of the difference in the movements of the municipal and railroad indexes during the Civil War may possibly lie in the different effects of the paper money inflation of the period on the prices and yields of the two types of bonds. However, we failed to develop any very appealing hypothesis offering an explanation on this basis.²²

²¹ Compare the January 1864 and January 1865 scatter in Chart 6.

²² The index of the yields of New England municipal bonds is a quarterly index.

Monthly quotations are not regularly available,

The sources of the original quotations are materials gathered by Joseph G. Martin, a Boston stock broker, and his successors in his firm. For the period from January 1857 to January 1862, Mr. Martin's early book entitled "Twenty-one Years in the Boston Stock Market" was employed. The quotations is this book for 1857, 1858 and 1859 are monthly for the first day of the month. However, in 1860 and 1861 only quarterly quotations appear, namely, for January 2, April 2, July 2 and October 2 of 1860, and for January 1 (sic), April 1, July 1 and October 1 of 1861. The quotations used from January 1862 to January 1914 are from annual pamphlets issued by Mr. Martin at the end of each year. These pamphlets were entitled "Stock Market Fluctuations" or "Stock Quotations from January — to January —" or other closely similar titles that varied somewhat from year to year. Copies of these pamphlets are to be found in the Boston Public Library.

The credit standing of the leading New England municipalities underwent, during the period 1857-1914, no such radical changes as did the credit standing of many American railroads. Indeed, the best of the New England municipal bonds seem to have deserved about the same rating in 1857 as they did in 1914. That, throughout this entire period-aside from the erratic Civil War interruption-the railroad 4.50 sigma index drifts irregularly but continually downward relatively to the New England municipal index would seem therefore to present evidence of some significance. Our holding to the 4.50 index, in spite of this evidence, requires some explanation if not defense. Such an explanation or defense hangs naturally on two considerations: first, the difficulty of deciding how much drift, if any, remains in the 4.50 sigma index and, second, the virtual certainty that any attempt to obtain, from operations restricted to the railroad bond data, an index containing much less drift than the 4.50 sigma index would lead to highly questionable results.

When attempting to decide how much drift, if any, remains in the 4.50 index, we must remember that a difference in the yield of two bonds may result from a difference in the markets for the bonds as well as from a difference in the degrees of public assurance that the promised future payments will be met. The placing of a bond on a list of investments legal for trust funds and savings banks inevitably affects its yield. And mere custom has often almost the force of law. Only gradually did railroad bonds attain the legal status and the popularity with the most conservative investors that they possessed by the early (Footnote 22 concluded)

The quotations appear to have been at times estimated from the author's knowledge of the municipal bond market. There are occasionally bankers' huying rates when no transactions were actually recorded. The quotations are 'over the counter' rather than open public market quotations such as we used for railroad bonds. There are strong reasons for believing, however, that Martin's quotations, though they were not recorded with the same official exactness as were those of the railroad honds, and though their accuracy proved, on experiment, to be insufficient to stand the strain of the signar procedure, reflect with substantial correctness the movements of New England municipal bond prices and yields in the Boston market.

We made no attempt to extend the New England bond index forward beyond January 1914. In so far as we have made comparisons of railroad bond yields and municipal bond yields after January 1914, we have contented ourselves with the Standard Statistics monthly index of the yields of 15 municipal bonds. This index goes back to January 1900 (see Chart 10). Shortly after January 1914 the Federal income tax with its municipal bond exemptions began to introduce into the picture an extraneous element whose effects are difficult to measure.

years of this century. But, from 1857 to 1930, municipal bonds of the highest grade were 'prime' investments for the ultra conservative. As high grade railroad bonds came to be more and more introduced into the portfolios of such investors, they steadily weakened the monopoly enjoyed by the municipal bonds. With the increase in the composite supply, the yields of the municipal bonds inevitably tended to be greater than they otherwise would have been. The effect was the same as though the volume of the municipal bonds had itself been increased in the same proportion as the total.

Shall we then say that the yield of the railroad bonds was drifting down toward that of the municipal bonds or that the yield of the municipal bonds was drifting up toward that of the railroad bonds, or shall we say that both these things were happening, that the yields were drifting together? From January 1921 to the end of 1929 the interest bearing debt of the United States government declined steadily month after month and year after year. Throughout this period the yields of Federal bonds showed a pronounced long term downward trend relatively to the 4.50 sigma index. Shall we, therefore, say that, as these government bonds were throughout the period acknowledged to be of the very highest grade, the 4.50 sigma index had, during this period, an upward drift? And that, during the year 1931 for example, in which the interest bearing debt increased by leaps and bounds and in which the yields of Treasury bonds advanced much more rapidly than did the 4.50 sigma index, that index had a downward drift?

The 4.50 sigma index gives a picture of the course of the yields of railroad bonds of an ultra-superlative grade. It is hard to say just what meaning would have to be given to it if it were adjusted to the movements of high grade bonds in one or more other markets. It certainly would not give us a picture of that economic noumenon 'pure interest'.

A study of the corporations themselves gives us considerable reason to believe that the very best railroad bonds in the early period were inferior to the best bonds in the later period. But, from the yields of the best bonds in the early period or even from the yields of all the bonds in all the periods, it is difficult if not impossible to calculate plausibly what would have been, in the early period, the yield of a railroad bond of apparently as high grade as the very best railroad bonds in the later period. We have already referred to the danger involved in extrapolating the sigma lines far into the region of hypo-

thetical bonds of a higher grade than any actually existing bonds. This danger exists not merely because of the high probable error of the slopes of a few of the sigma lines for some of the January to January scatters and the high probable error which always appears as the slopes are cumulated, but also because of the evidences that the scatters are sometimes and perhaps always non-linear even on the log scale we have used.²³

The non-linearity of the relation between the yields at two dates, that sometimes appears when extremely high-yield securities are included in the scatter diagram, is illustrated by Chart 8. On that chart are plotted the yields of all bonds and dividend-paying preferred stocks listed on the New York Stock Exchange for which quotations could be obtained for both January 1903 and January 1904. An examination of the chart will show that, though a straight line gives a fairly plausible fit to the yields of the railroad bonds we actually used, it gives an extremely poor fit to the total scatter.24 An hyperbola is suggested as an empirical curve that might describe more or less adequately the complete scatter. The railroad sigma line lies close to the lower arm of the hyperbola. The non-linearity of this scatter explains the lack of similarity between the cumulated-product-of the-slopes-of-the-sigmalines and the course of railroad stock prices in this period (see Chart 15). It is, of course, difficult to say to what extent the rather radical short term differences between the (1925) 4.50 sigma line and the (1857) 4.23 sigma line, such as the complete elimination by the 4.23 line of the 1873 peak (see Chart 7), are rational, are the result of high probable errors in the cumulated linear slopes, or are the result of nonlinearity of the scatters.25

²⁸ Chart 15 gives some support to the idea that the non-linearity is not of a constant type and that, over long periods, its disturbing effects tend to cancel out every now and then leaving approximately the same result as that obtained from the linear hypothesis. Whether this be true or not, non-linearity has certainly been very disturbing during some short periods, such as January 1903 to January 1905, a period about to be discussed in the text.

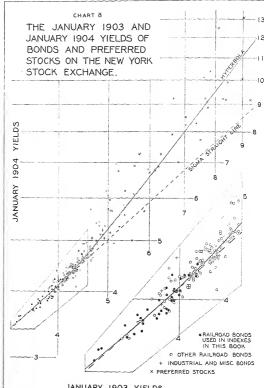
24 In only one year out of the seventy-nine, 1857-1936, did this non-linearity affect the particular group of bonds we used in our index. In 1929-30 only twenty-eight bonds were used to calculate the sigma line. These are the bonds that appear as black dots on Chart 6. The white dots on this chart are the bonds that were omitted in that one year because they affected the linearity of the scatter. Two sigma lines appear on the chart. The solid line is fitted to the entire scatter. The broken line is fitted to the twenty-eight bonds and is the one we actually used in our calculations.
25 Even the 4.50 sigma index sometimes shows a small amount of erratic irregularity

Chart 9 shows the yields of nearly all the railroad and public utility bonds listed on the New York Stock Exchange or the New York Curb Exchange for which quotations were available for the weeks ending January 7, 1930 and January 6, 1931. The interesting feature of this chart is that, though the railroad scatter appears to be distinctly nonlinear, the public utility scatter appears to be comparatively linear, at least outside the range of almost absurdly high yields. There was, in this period, no such collapse of public utility credit as there was of railroad credit.

Because scatter diagrams are so enlightening we have presented a large number-84 in all. The primary reason for having each of the 79 diagrams of Chart 6 cover a period from one January to the next was that we substituted bonds only in January. Each diagram contains all the bonds used in a thirteen-month period. If we had used more critical dates, we would have had to use fewer bonds. Monthly scatter diagrams are seldom very impressive. The drift in a single month is usually so small as hardly to be manifest on a chart. The slopes of the sigma lines are nearly always close to 45°. Of course in a disturbed market even monthly charts are very instructive. Changes in grades are so violent that some of the monthly charts may look like yearly charts of a more normal period. Drift is unmistakable. Interesting as it would be to cover the recent past in much greater detail than the rest of the period, it was decided not to do so in this study. To have presented monthly scatter diagrams for even the last few years would have necessitated the publication of too many charts.

(Footnote 25 concluded)

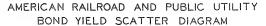
in its minor month-to-month movements. Line D of Chart 2 presents an index constructed by using a mathematical graduation that follows extremely closely all but the most minor movements of the 4.50 index (see Chart 14 to realize how closely) and on this graduation superimposing, as a substitute for the 'deviations of the 4.50 index, the deviations of the chain index number constructed from the arithmetic averages of the actual yields from a similar 'graduation of that index. The resulting composite index follows the 4.50 index in all respects except that it tends to eliminate the irregularities that sometimes appear in the most minor fluctuations of the 4.50 index. The composite index runs from January 1837 to January 1936 monthly. For the period from January 1857 to January 1879 the 4.50 sigma index was calculated only quarterly. Both the extreme similarity of the two indexes and their minor differences may be seen by comparing lines B and D of Chart 2.



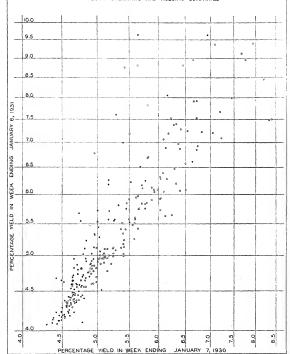
JANUARY 1903 YIELDS

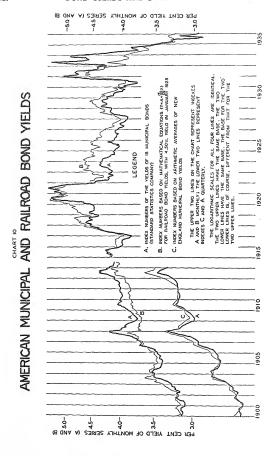
NOTE: CHART IN LOWER RIGHT HAND CORNER IS AN ENLARGEMENT OF SIMILAR SECTION OF GENERAL CHART

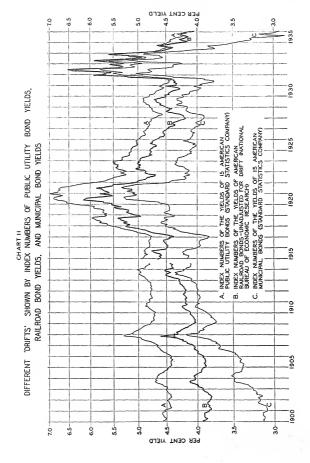
CHART 9



- . . YIELDS OF INDIVIDUAL RAILROAD BONDS
- YIELDS OF INDIVIDUAL PUBLIC UTILITY BONDS
 BOTH OPERATING AND HOLDING COMPANIES







CHAPTER V

BOND YIELDS, ECONOMIC 'DRIFT', AND THE PRICES OF COMMON STOCKS

In the preceding chapter we discussed the relation of the movements of bond yields to the grade of the bonds. At one stage of that discussion we introduced a scatter diagram containing not only bond yields but also the yields of preferred stocks. To go one step further and bring into the picture common stocks, the most junior securities of all, leads to some interesting results. But, before presenting those results, it is desirable to refresh the reader's memory of the nature of a corporation and the relation of bondholders and stockholders to the corporation and to each other.

A corporation is a juristic person; in the words of the Dartmouth College Case it is "an artificial being, invisible, intangible and existing only in contemplation of law". It is capable of acting in many but not in all respects as though it were a natural person. As a legal entity, it takes and holds property, and conveys the same; it contracts obligations, and it sues and is sued, in its corporate name, in the same manuer as a natural person. For such purposes, the stockholders or 'members' of the corporation are disregarded. They compose the corporation, but they are not the corporation.\(^1\)

Though the stockholders may be thought of as owning the corporation, they do not own and cannot convey the corporate property.² But

² This is technically true even when all the stock is owned by one person. While the

¹ We must not obscure our present discussion by overloading it with exceptions and qualifications. For example, it is, of course, true that the concept of the corporation as a legal entity, separate and distinct from the members who compose it, is a mere legal fiction, introduced for the convenience of the corporation and of those who do business with it; and that, under certain circumstances, the fiction will be disregarded, and the fact that the corporation is really a collection of individuals be recognized in equity and even at law.

they have a definite beneficial interest in the corporate property, as may be seen from the fact that the courts have held that interest insurable. It is true that, upon dissolution, the legal title to the corporate property does not vest in the stockholders, but they still retain the beneficial interest therein, and, if the legislature has made no provision by which they can reach the property, and enforce their rights, they may come into a court of equity, and obtain relief. Such a court has jurisdiction, unless it has been taken away by statute, to reach the property of the defunct corporation, to cause the debts due it to be collected, and to distribute the assets, after payment of the creditors, to the beneficial owners, that is, to the members or stockholders.

The stockholders' beneficial interest in the corporate property extends to the profits of the corporation. A stockholder has the right not only to participate in dividends when they are declared but also to maintain a suit in equity to compel the directors to declare and pay a dividend if it is wrongfully withheld.

The bondholder is a creditor of the corporation. His claims are prior to those of the stockholder but they are limited and he has no vote nor, so long as the corporation is living up to its promises, has he any means of controlling the management. But, aside from the voting privilege, the interests of the bondholder and the stockholder in the corporation differ fundamentally only with respect to priority and limitation. The corporation is a cow from which each hopes to obtain milk.

And priority and limitation are not confined to bonds. Though the preferred stockholder may be classed by the law with the common stockholder he will tend to be classed by the economist with the holder of an income bond. And even the law has been known to waver in its discussion of preferred stocks and preferred stockholders. For example, some courts have held that a corporation has the power to create and issue preferred stock on the ground that such a transaction is virtually a borrowing of money, and that corporations have the power to borrow money, and may do it in this way.

The common stock is a blood brother of the preferred stock and the bond. Investments as a class constitute one family. They each originate in an exchange of present money for an expectation of future

⁽Footnote 2 concluded)

corporation exists, he is a mere stockholder of it, and nothing else. Cf. Button v. Hoffman, 61 Wisconsin.

money. If it were not for such an expectation they would have no exchange value. And they lose that value as the expectation dies out. The demand that comes from the possibility of buying them and later selling at a profit may exist for a time in a sort of economic vacuum, but it is essentially a derived demand and, in the absence of any (warranted or unwarranted) expectation of future returns, it sooner or later disappears.

Because the good that the common stock offers to its purchaser is an expectation of future money payments, the relation of its presentmoney price to its future-money payments is as unmistakably an interest phenomenon as is the relation of the present-money price of a bond to its future-money payments. In the fullness of time the stock will have a 'realized' or 'actual' yield just as will the bond. And, though the stock makes no 'promise', as does the bond, and therefore has no 'promised' or 'hypothetical' yield, its price discounts estimated future payments as truly as does the price of the bond.8 It is the absence of promises and the high degree of uncertainty as to what the stock will pay, with the resulting inadequate forecasting, that obscures the interest relation. The fundamental difference between an ultra high grade extremely long term bond and a low grade common stock is that the future-money returns of the bond can be forecast with more assurance than can those of the stock. That an individual investor may prefer the one type of security to the other, because he believes that their market prices do not correctly measure the differences in their respective future probabilities, is a matter that concerns individual forecasting of future payments but neither individual nor market discounting of those payments.4

The promises contained in the bond are not merely assurances that, if possible, certain sums will be paid. They are also maximum values a For discussion of the terms assumption of payment, promised or hypothetical yield, and realized or actual yield, see Chapter II. In this book the term yield, unless the context makes it apparent that realized or actual yield is referred to, means promised or hypothetical yield.

⁴ For example, that bonds are almost inevitably a poorer investment than common stocks on the eve of a great currency inflation is evidence merely of had market forecasting of how the inflation will affect the future money payments of the stocks. The rates at which future money is, at such a time, being discounted may be high or low, but, because they apply to the anticipated money payments of both the stocks and the bonds, they cannot explain why one is a better investment than the other. It is the error in the anticipation which explains that,

that cannot be exceeded. This is, of course, true of preferred stocks also. If the corporation is earning enough, the maximum values will year after year be the realized values. And this limitation leads to stability—the stability of a toy balloon pressing against the ceiling of a room. If the gas begins to escape, the balloon may drift down to the floor. But, only if it were outdoors could it ever soar to the clouds. There are upper and lower limits to the return from a bond. The return from a common stock has no necessary upper limit. Dividends may soar to the sky, but their only permanent level of stability is on the ground—with the corporation bankrupt.

The 'assumption of payment', which must be made before the promised or 'hypothetical' yield of a bond can be calculated (or obtained from a bond table), may, as we have seen, be a mere mathematical fiction for all except the highest grade of bonds. But, for common stocks it is not only a mathematical fiction but also an economic absurdity. Even if the chance that the promises contained in a bond will be kept is so negligibly small that the promises are little more than mere words, they are at least definite words and, as such, can stand the strain of mathematical manipulation.

But the common stock contains no promises. It is, of course, true that after sale, in other words after the event, the realized or 'actual' yield may be calculated for the period that the stock was held and for the ex-holder with the same assurance that it could have been calculated the stock been a bond, but the promised or 'hypothetical' yield completely eludes definite determination unless assumptions are introduced that are so grossly conjectural as to be virtually supposititious.

And even small variations in the assumptions affect greatly the hypothetical yields. The assumptions must extend far into the future. Theoretically, they must specify exactly the amounts and dates of all future payments. Of course, practically it is not necessary to take into account those payments that are to occur in the far distant future. But the future period that may be neglected is much more distant than the reader might imagine had he not carefully considered the matter. If it be assumed that a share of common stock selling for \$100 is to return \$4 per annum forever, it may be thought of as having a promised or 'hypothetical' yield of 4 per cent per annum. But, if the pay
This realized yield is, of course, not to be confused with the realized yield on a bond that has been held to maturity—or permanent default.

ments are to cease at the end of sixty years, the hypothetical yield must be less than 3½ per cent per annum. If they are to cease at the end of 46 years, the yield must be less than 3 per cent per annum. If at the end of 35 years, the yield must be less than 2 per cent per annum. If they continue just 25 years, the yield will be exactly zero per cent per annum. With still shorter periods, the yields are negative.

If such an assumption were made as that the dividend payments were to increase in geometric progression, the future that could be neglected would be still more distant. One of the strangest rationalizations of unending price rise that appeared in the months immediately preceding the stock market culmination of 1929 was evolved by a Wall Street economist. He presented to the directors of the investment trust with which he was associated statistical evidence that the wealth of the country increased in the long run about 3 per cent per annum. He then argued that corporations as a class should be expected to share in this growth at this rate and hence that their dividends should be expected. over the long run, to increase at least 3 per cent per annum; that is to say in such a series as \$4.12, \$4.24, \$4.37, etc., or \$4(1.03), \$4(1.03)2, \$4(1.03)8, etc. He then suggested that, with increasing financial stabilization of the country, these future dividends would eventually be discounted at a rate that would not exceed 3 per cent per annum. But, he continued, if distant enough payments were assumed, discounting them at this rate would give very high prices for the stocks. The suggestion was even made that, as there seemed to be no necessary time limit to the 3 per cent rate of growth in wealth, there should logically be no 'ceiling' whatever for stock prices. The phantasy

⁶ The present values of the future payments, discounted at $3\frac{1}{2}$ per cent per annum, are \$\frac{4}{1.035}\,^{\\$}, \\$\frac{4}{(1.035)^2}\,^{\\$}, \\$ etc. Now, from any ordinary compound interest and annuity table we may find that the sum of 60 terms of this series equals \$4(24.9447) or about \$99.78\. Therefore, if the stock is selling at \$100\, the yield is a little less than $3\frac{1}{2}$ per cent per annum.

⁷ If the dividends were \$4(1.03), \$4(1.03)², \$4(1.03)², etc., as in the illustration of the text, and if these dividends were discounted at 3 per cent per annum, the price of a share of the stock that was to pay the dividends should be just four times the number of payments that were to be made; in other words, four times the number of years that the succession of dividends was to continue, even if nothing whatever was to be paid thereafter. The present value of each future dividend payment is \$4.

was strangely reminiscent of the Petersburg Paradox in the mathematical theory of probability.

On the other hand, it is of course true that, in pricing stocks, the market undoubtedly attempts to estimate their earnings and dividend probabilities for at least the near future. To the investor, past earnings and dividends, except in so far as they offer clues to the future, are mere 'water over the dam'. Dividing last year's dividends by the present selling price of a stock will produce a function that, for certain very restricted purposes, may be of some interest to the student of economic history and the business cycle; but it is highly undesirable to call the function a 'yield' and thus, by the use of terms, insidiously to suggest that it is of the same nature as the ('hypothetical') yield of a bond.

Though the terms of a bond's promise of future money payments change with the passage of time (as the maturity date approaches), they change in a slow and definite mathematical manner. Unless the time to maturity be very short, or the dates for which comparisons are made be very far apart, no great change in the yield of a bond can occur without a change in price. For short periods, the yield of a long term bond is virtually a function of one variable—the price of the bond. But the 'yield' of a stock is essentially a function of two variables. This difference is clearly apparent if we compare the 'yields' of stocks with the yields of perpetual bonds. The (hypothetical) yield per cent of Canadian Pacific debenture 4's (bonds that are perpetuities) will always necessarily be 400 divided by the price of a \$100 bond. But the 'vield' per cent of Canadian Pacific common stock, whether it be taken as (100 times) the preceding year's total dividends divided by the present price of the stock or as some more complicated expression, will always be essentially a function of two variables—a fluctuating price and a fluctuating dividend rate. Sudden and great changes in the calculated 'vields' of a stock occur not only because of changes in price but also because of changes in dividend rate.

To compute either bond yields or stock yields, assumptions must be made concerning future payments. The computer of stock yields usually assumes that payments in the future will be at the same annual rate as they were in the immediate past. Having made this totally unwarranted assumption, he plunges into refinements. If an 'extra' or unexpected dividend be paid, he labors like the mountain to decide whether it is truly an 'extra' or should be considered as normal and 'regular'. If his decision whether it will or will not be regularly repeated turns out to be wrong, he 'revises' his preceding year's index of yields. And if the yields, as he calculates them, seem abnormally high or abnormally low, he tacitly suggests that future 'revisions' will probably correct his figures. He speaks of 'real' yields, meaning by the term what his yields will be when the future is known and all his 'revisions' completed. And all most seriously.

The market's valuation of both second grade bonds and common stocks may, for the purpose of throwing light on our present problem, be thought of as though it were a process of consciously forecasting interest or dividend payments and then discounting them at some particular rate of interest. The (hypothetical) yield of a second grade bond is then high, not because the promised future interest payments are discounted at a high rate but because of the low degree of expectation that the payments that will actually be made will be as great as the promised payments. It is as though the expected future payments, which for a high grade bond are taken as identical or virtually identical with the promised payments, are for a second grade bond taken as only

8 One of the largest financial 'services' in the United States writes: "On occasional instances, a consistent handling of the situation is impractical and arbitrary decisions must be substituted. This may at times necessitate revising a part of the recent data." 9 Sometimes the 'yields' of stocks seem, to their computers, abnormally low or abnormally high on almost any of the various bases used for calculating them; for example, in September 1929. However, even at that time the fact that prices were unusually large multiples of immediately preceding dividends was accepted only as evidence and not as proof that 'real' yields were abnormally low. The mooted question was whether earnings could increase sufficiently in the future to carry such extremely high prices. If the immediate future of earnings had been known, it would undoubtedly have been generally realized that stock prices were relatively even higher than their 'yields' suggested. Dividends had been increasing, and the fall in 'yields' was therefore not as great as the rise in prices. If 'yields' could have been calculated on the basis of the dividends to be paid in the not too distant future instead of those paid in the immediate past, they would have fallen even more than prices rose.

10 What a business is earning is, of course, more fundamentally important than what it is currently paying. If a corporation be earning much more than it is paying out in dividends, the stock will tend to sell on a relatively low 'yield' basis. When conditions are reversed, the stock will tend to sell on a high 'yield' basis. The ratio of price per share to earnings per share is a function that has been calculated and presented in much the same manner as the stock 'yield' concept, It has almost all the technical drawbacks of the yields concept with the additional one that earnings are never as accurately known as dividends.

some proper fraction of what is promised. The yield of the second grade bond is high because of the difference between the expected and the promised payments. But in so far as the analogy can be carried through at all, the 'yield' of a common stock is high because of the difference between the expected payments and the rate at which payments have recently been made. But recent rates of payment, though they may in exceptional circumstances turn out to be the same as future rates, are not the same as and cannot be substituted for promises.

If such an illegitimate substitution be made, we are faced with the difficulty that, when the 'promises' are actually broken, the 'vield' will fall violently; and, even after adjustment to the new conditions, may be no higher than before the promises were broken. If, at the time that the dividend payments on a stock paying \$8 per annum are about to be cut to \$4 per annum, the stock be selling for \$100 a share, its yield will fall immediately after the cut—unless the price instantly declines to \$50 a share. And, unless the price falls below \$50 a share. the new 'vield' will be no higher than the 'vield' before the dividend cut. When dividends are completely eliminated, 'yields' immediately fall to zero. Though the 'yield' of a stock may have been, before the elimination of dividends, as high as the yields of very low grade bonds, after the elimination it becomes lower than the yields of bonds of even the very highest grade. It seems clear that, whatever else it may be, a (hypothetical) stock 'yield' is not an animal of the same species, or even genus, as a (hypothetical) bond yield.

Not only economists and statisticians but also investors and business men, when comparing the market's valuation of two bonds, tend to express that valuation in terms of the yields of the bonds rather than in terms of their conventional 'prices'. Though conventional 'price' is a price and the yield is only a function of a price, the price of which the yield is a function is, to the extent that there is warranty for 'the assumption of payment', a more expressive, enlightening, and pertinent price than the merely conventional price. Indeed, the conventional price of even a high grade bond is, singly and by itself, almost destitute of meaning. The quantity of the 'good' to which the dollars of the price are related is not adequately specified. The price is, by convention, the price per \$100 of 'face value'. But 'face value' tells us only the amount of the last payment. It says nothing about when that payment is to be made or about the amount and timing of other payments that are

to be made in the interim. And these facts are essential. As a unit of the good, \$100 of 'face value' not merely is inadequate but also may be completely meaningless. Its *reductio ad absurdum* occurs with perpetuities—in which 'face value' is not even promised.

It is true that the price of which the yield is most simply and directly expressible as a function is analogous to the price of money in terms of a commodity rather than the price of a commodity in terms of money. But this inverse relationship leads to no difficulties. To state that the yield of a bond is 5 per cent per annum is to state that the relation between the *conventional* price of the bond and the promised future payments is *as it would be if* a promised payment of \$105 due any time before maturity were worth \$100 payable one year earlier. As a corollary, we have the less general conclusion that the price which, minus unity, equals the yield of the bond is a price of a unit of *present* money in terms of promised money due one year hence.

For comparing the market's valuation of two bonds, conventional prices are, by themselves, quite useless. But they may give us some information if the comparison is between the market's valuation of a bond at one date and its valuation of the same bond at another date. No necessary conclusion can be drawn from the fact that, even on the same date, one bond sells for 90 and another bond for 110. But if, at one time, a bond sells for 90 and, at another time, for 110, we know at least that the yield was lower at the 110 price than it was at the 90 price. A change in yield must occur whenever a bond crosses par. Also, a change in yield must occur whenever, from an earlier to a later date, the plus or minus deviation of the price of a bond from par increases absolutely (not algebraically). And, if the bond be a perpetuity, we are not restricted to such vague and special non-quantitative conclusions.

Because the importance of the final or 'face value' payment decreases with an increase in time to maturity, comparison of the market's valuation of two bonds by means of their mere conventional prices (per \$100 of 'face value') reaches its reductio ad absurdum, as we have noticed, when there is to be no final payment, in other words when the bonds are perpetuities. However, if the comparison is of the market's valua-

¹¹ This is all, of course, 'as if'. Unless we make the arbitrary and unreal assumption of uniformity in the rates of discount used in each future compounding interval, yield must be considered a mere average (see Ch. II).

tion of a perpetuity at one date and its valuation of the same perpetuity at another date, conventional price tells exactly the same story as yield. If yield halves, price doubles, etc. The yield of a perpetuity is merely a constant multiple of the reciprocal of the conventional price of the perpetuity.

The advantage of knowing and using not only the conventional price but also this multiplier, in other words the advantage of using yield, when comparing the market's valuation of the same perpetuity at different times, is that the yield gives an indication of grade and the conventional price (by itself) gives none. Our discussion (Ch. IV) of the relation of movement of yield to yield itself (as an index of grade) would have been impossible in terms of mere conventional prices, even if all our bonds had been perpetuities. But conventional prices, though they would not have related movements to grades, would, if all the bonds had been perpetuities, have told us just as much about the movements themselves as did yields.

Strictly speaking, common stocks have no grade in the sense in which the term is used of bonds, the sense in which, other things being equal. highness of grade shows itself in lowness of yield. The 'grade' of a bond depends upon the capacity of the issuing corporation to fulfill the promises contained in the bond. Yield may be low and grade high because of the greatness of the corporation's capacity or because of the smallness of its promises. If the most senior issue of a corporation be small enough, the bonds may remain 'first grade' throughout a receivership. But common stocks are most commonly described as 'high grade' when their dividends have been large and regular or even increasing, and low grade when they have been nil, small and irregular or decreasing. The 'vield' of the stock has little or no relation to this concept of grade. Price is its real indicator. The poorest grade of common stocks will have the lowest 'yields'-namely zero; and the 'yields' of all common stocks will be related to the market's estimates of the rosiness of their dividend possibilities rather than to the degree of assurance with which those dividends can be forecast. A prospect of increasingly large dividends will lower the 'vield' of a common stock, but a bond whose coupons called not for uniform but for increasing payments would not, because of that fact, sell on a lower yield basis.

But, though common stocks cannot be classified as to grade in the same way that bonds can be, their place in the investment family, to

which bonds and preferred and common stocks all belong, may be described in terms of a concept that is at least related to the concept of bond grade. This concept is the concept of priority. If there be two bonds of the same corporation that differ only as to their seniority, the more senior bond will be of a higher 'grade' than the less senior, because its claim to payment will be prior to that of the less senior bond. And, if the corporation have preferred stock outstanding, that stock will (except in very unusual circumstances) be of a lower 'grade' than any of the corporation's bonds. In this sense, the common stock will be of a still lower grade. The claims of all the bonds will be prior to those of the preferred stock and the claims of the latter prior to the claims of the common stock.

Of course, such a classification by priority, embryonic as it is, is strictly possible only with the securities of a single corporation. But the fact that common stocks are junior to the other securities of their own corporations and hence, as a group, more uncertain as to their future payments than bonds suggests that the fluctuations in the valuations placed upon them by the market should be expected to be more like those of low grade than those of high grade bonds. And they are so. There are, of course, exceptions to this generalization. Some common stocks act more like high grade than really low grade bonds. But the generalization holds of common stocks as a group. Our future discussion therefore runs in terms of index members and not in terms of individual stocks. And the index numbers are, of course, index numbers of stock prices, and not index numbers of stock 'yields'. The concept of stock 'yield' is, as we have seen, quite useless for our purposes.

The stocks whose prices are used in this book are all American railroad stocks. Our decision to restrict ourselves to railroad stocks was not made merely because of the relationship between railroad stocks and railroad bonds. It is true that, in recent years industrial and public utility stocks have been relatively more important in the American speculative and investment markets than railroad stocks. But railroad stock prices present not merely a much more homogeneous but also a much longer series. ¹² Our railroad stock price indexes go back monthly

12 Cf. Wesley C. Mitchell, Business Cycles, pp. 170, 171:

"The number of industrial stocks regularly bought and sold on the market in every year since 1890 is too small to make significant averages."

While it would have been possible, from Boston quotations, to construct index

to January 1857—a period of seventy-nine years. Until about 1909 the railroad stock market was the American security market par excellence. Only in the last twenty years or so has its relative importance seriously declined.

We have not used the prices of preferred stocks. The number of railroad preferred stocks paying dividends regularly and having their prices quoted has always been so small as to prevent an index of their prices having any broad general significance. And, whether they paid dividends or not, it seemed undesirable to mix them with the common stocks.

The list of stocks used includes, at all times, virtually all the railroad common stocks whose prices were being regularly quoted on any of the great exchanges. The names of the railroads and the periods during which their stocks were used is graphically exhibited in Chart 32. Most of the changes in the list were made necessary or desirable by consolidations of one kind or another. For example, stocks No. 21 (New York Central) and No. 22 (Hudson River) were used from January 1857 to January 1870, and stock No. 23 (New York Central and Hudson River) from January 1870 to January 1936. However, if a stock became so inactive as to lack quotations for many months at a time, it was usually dropped from the list. In some instances stocks were not used while the railroad was in the hands of a receiver and undergoing reorganization. In a very few instances they were not used during a period in which exceptional circumstances only negligibly related to their investment values were violently disturbing their prices. Thus Northern Pacific was not used during the year of the corner (1901). Sometimes it was possible to bring a stock back into the list. For example, Northern Pacific was brought back in January 1906. (Footnote 12 concluded)

numbers of the prices of copper mining stocks or cotton mill stocks back as far as January 1857—the date we begin our railroad indexes—few persons would claim that such indexes would have anything approaching the general economic significance of an index of prices of the railroad stocks. And their relation to the yields of railroad bonds—which are the bonds we have used—would be difficult to interpret.

The monthly 'index of industrial stock prices' of the New York Federal Reserve Bank runs from January 1872 to date. But it is, in its early years, composed entirely of transportation, communication and mining stocks. The stocks used in 1872 were: Adams Express, American Express, Consolidated Coal, Delaware and Hudson Canal, Maryland Coal, Pacific Mail, Quicksilver Mining, Quicksilver Mining, ptd., United States Express, Wells Fargo Express, Western Union.

CHART 12

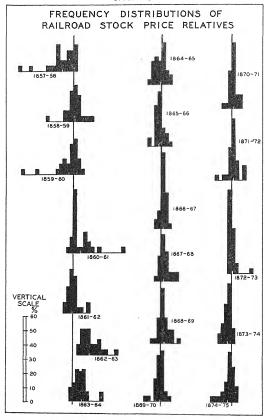


CHART 12-CONTINUED

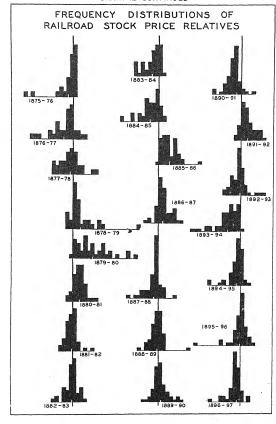


CHART 12-CONTINUED

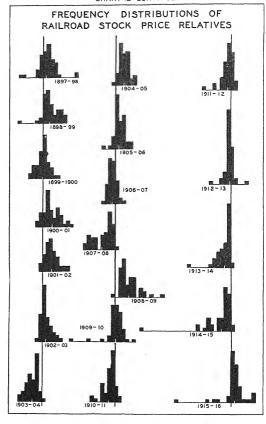
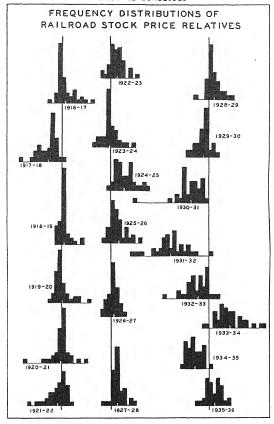


CHART 12-CONCLUDED



But, as may be seen from Chart 32, the instances in which a stock was

dropped and later reinstated are few indeed.

Before discussing methods of measuring changes in the general level of railroad common stock prices, it is desirable to point out some characteristics of the price movements of the individual stocks. We must remember that, though their 'grades' may not be definitely measurable, the stocks are of different grades. Some are more speculative—less like high grade bonds—than others. Though all are 'common' stocks, they vary in their degrees of 'commonness'.

Appendix A. Table 14 gives the percentage that the price of each stock, in any particular January, was of the price of the same stock in the preceding January. Chart 12 presents 79 frequency distribu-

tions based on this table—one for each year from January 1858 to January 1857 to

January 1935. This chart shows that most of these distributions are skewed in the direction of the general price change. In a year of rising prices they are skewed to the right; in a year of falling prices to the left.

The poorest stocks—those of the most overbonded roads—tend to show the greatest percentage price movements, both during periods of collapse and during periods of recovery. Now, though it is not logically necessary, the poorer stocks usually sell for fewer dollars per share than do the more conservative and less speculative stocks. The lower priced stocks, therefore, tend to show greater percentage fluctuations in price than do the higher priced stocks.13 But the relation does not exist merely because the lower priced stocks tend to be the lower grade stocks. It is partly psychological. Speculators seem to prefer to operate in relatively low priced stocks. If a sound and conservatively managed corporation, whose stock sells at a high price per share and shows only small per-18 But their dollar or 'point' movements are generally smaller than those of the higher priced stocks. During a bull market, a stock that begins by selling for \$100 a share will probably rise in price a smaller percentage but a larger number of dollars or 'points' than will a stock that begins by selling for \$16 a share.

A curious empirical formula that describes the apparent tendency of price movement fairly well is that stock prices move equal increments on their square roots. Thus, if in a bull market stocks that sold for \$100 per share rise in price to about \$144 a share, stocks that sold for \$16 a share will tend to rise to about \$36 a share. centage fluctuations, reduces greatly the market price of the stock per share by paying a large stock dividend, the new and lower priced stock will almost immediately begin to show larger percentage price fluctuations than did the old and higher priced stock.

From such strange material many types of index number could be constructed. The questions answered by some would be important, those answered by others would be trivial or even bizarre. Perhaps the first conclusion that one approaching the subject would come to would be that there was little if any importance attached to 'one share' as a unit of measurement. An index number based on totals of the prices of one share of each stock would be of the same type as an index number of commodity prices that was based on totals of the prices of one pound of each commodity. Any aggregate of actual prices calls for some weighting. The price movements of Pennsylvania stock are more important than the price movements of Western Maryland.

With almost no exceptions, the index numbers of stock prices that are currently published fall into one of three groups. All three are based upon arithmetic averages of actual prices. The first and largest group contains the 'unweighted' indexes. These are arithmetic averages of the prices of one share of each stock.\text{14} The second group contains index numbers in which each stock is weighted by the number of shares outstanding. The monthly index numbers (see Appendix A, Table 10, column 6 and Table 17) presented in this chapter fall in this group (for weights, see Appendix A, Table 15).\text{15} The third group contains index numbers in which the prices of the various stocks are weighted in proportion to their 'activity'—the number of shares that are bought and sold \text{16}

The purpose of weighting is to make movements of the prices of the more 'important' stocks influence movements of the index num-

¹⁴ Often a set of weights is gradually introduced because of stock dividends. For example, the New York Times index of the prices of 25 industrial stocks is constructed by multiplying the present price of each stock by the number of shares that now correspond to one share at the time that the stock was introduced into the index. Though the divisor is still 25, the total number of shares is now much greater than 25.

¹⁵ As do the various weekly and monthly index numbers of stock prices published by the Standard Statistics Company of New York. Its index numbers extend back to January 1918.

¹⁸ Professors Irving Fisher and W. I. Crum have each published index numbers of stock prices weighted by activity.

bers more than do movements of the prices of the less important stocks -if possible, in proportion to their importance. The question becomes one of deciding what shall be meant by 'importance'? Important for what? From the standpoint of an individual holder, the 'important' stocks are those that he owns, and the relative importance of their (arithmetic) price movement is in the absence of other factors in proportion to the number of shares that he owns of each. But all shares outstanding are owned by someone. May not the relative social importance of (arithmetic) fluctuations in the price per share of the stock of a particular corporation, therefore, well be thought of as a function of the number of shares that the corporation has outstanding; and, in the absence of the disturbing effects of other independent variables such as the extent to which the stock of the corporation is used as collateral for loans, etc., may not the relative social importance of (arithmetic) fluctuations in the price well be thought of as varying directly with the number of shares outstanding?

It is of course true that, if the price at which a share of stock is sold be multiplied by the total number of shares outstanding, the resulting figure may easily be quite unrepresentative of any intelligent valuation of the entire enterprise. Dr. Wesley C. Mitchell drew attention to this fact in his *Business Cycles* (p. 171):

"Whether the market prices of stocks in 100-share lots may be interpreted as showing accurately changes in the prices of the business enterprises concerned is highly questionable. If 1,000 shares in a railway which has 100,000 shares outstanding be sold at \$80 per share on a given day, it does not necessarily follow that the whole proprietary interest could be sold (or bought) for \$8,000,000. Indeed, it is seldom safe to infer the price for the total supply of any kind of goods from the current market price per unit that cannot be known except in the rare cases when such sales are actually made and the terms published. Hence we must content ourselves with taking the figures for what they are—prices of shares in business enterprises."

We must remember, however, when considering the above remarks of Dr. Mitchell, that, though a multiplication of price per share by total number of shares outstanding does not necessarily show what "the whole proprietary interest could be sold (or bought) for", it does determine the valuation that will be put on each and every one of the separate parts or 'shares' of the proprietary interest by the individual owners of those parts and by their creditors—such as banks. Loans are made and are called on the basis of the market prices per share of the collateral behind the loans.

For most economic purposes the 'importance' of the market price of a share of the stock of a corporation depends upon the number of shares outstanding. The economic importance of two shares of stock is not necessarily greater because they represent interests in two corporations than it would be if they represented an interest in only one corporation. To weight prices per share by the number of shares outstanding would seem a simple and logical way of allowing each separate individual share an importance not dependent upon the size of the corporation to which it belongs. If prices are not weighted by the number of shares outstanding, the prices of the shares of small corporations are given an importance they do not merit. If Corporation A has 1,000,000 shares outstanding and Corporation B only 100,000, a five dollar rise in the price per share of the stock of Corporation A tends to be ten times as important as a five dollar rise in the price per share of the stock of Corporation B. The price of each separate share in Corporation A is, we may assume, as important as the price of each separate share in Corporation B, and there are ten times as many of them.

The usefulness of index numbers of stock prices in which the prices of the various stocks are weighted in proportion to their market activity is very restricted. For some theoretical purposes connected with the 'equation of exchange' and for some practical purposes connected with the forecasting of stock prices by watching changes in the internal 'technical' condition of the market, the relative 'importance' of the prices of stocks may be thought of as varying directly with the number of shares sold. During a period in which a speculative football, such as Auburn Motors once was, is traded in much more actively than the stock of a much larger and economically more important company, such as General Motors, there is a sense in which fluctuations in the price of Auburn are more 'important' than fluctuations in the price of General Motors. But it is a narrow and technical sense.¹⁷

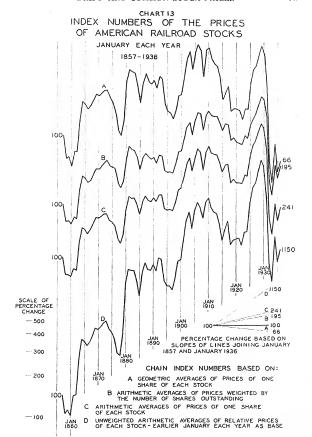
Index numbers of stock prices that are weighted by 'activity' are sub
17 Of course, when a stock becomes extremely inactive (or abnormally active), its
price may become a much less reliable measure of careful and significant valuation
by the market than it would be in more normal circumstances. But this is a matter
that concerns the adequacy of the pricing process and not the importance of the
commodity.

ject to a quasi mathematical drift. In periods of advancing prices there is a pronounced tendency for individual stocks to be abnormally active when they are advancing in price more rapidly than the general market. The opposite tendency-to be abnormally active when they are declining more rapidly than the general market during a period of general decline-is very much less pronounced. The reasons for these conditions are partly technical and partly economic; but, if individual prices are weighted in proportion to the changing turnover of the individual stocks, the net mathematical result is a pronounced upward drift in the index number during rising markets, accompanied by a much less pronounced downward drift during falling markets. If a stock moves from 100 to 120 during a short period of great activity (compared with the activity of other stocks) and falls back to 100 during a long period of relatively small activity, it affects the index number more while rising than it does while falling. It is theoretically possible for the price of each stock in the index number to be the same at the end of a period as it was at the beginning, and yet the index number show a pronounced movement.

All existing index numbers of the prices of common stocks contain 'economic drift'. This is not merely almost inevitable but also desirable and necessary if the indexes are to present faithful pictures of what actually occurs. Economic drift is the essential characteristic of the movements of common stock prices. Those prices are the prices of radically junior securities and economic drift is the very badge of their 'juniority'. To eliminate it from an index, if that were feasible, would be nothing short of emasculating the index.

But mathematical drift is a merely disturbing influence, whether it occurs in a pure or in a disguised and quasi form. Charts 3 and 4 were introduced to illustrate types of mathematical drift in index numbers of bond yields. Chart 13 performs a similar service for stock prices. Four index numbers of railroad stock prices are there shown. Each index is a 'chain' number, constructed by chaining together 79 separate index numbers, each extending from one January to the next. The indexes presented by the upper three lines on the chart (A, B and C) vary greatly in their movements, but are free from purely mathematical drift. The index represented by the lowest line on the chart (D) is subject to violent mathematical drift.

18 For the figures, see Table 16.



Indexes A, B and C are each based on averages of actual prices. The differences in their movements result from differences in the types of average used and from differences in weighting. The averages of index A are geometric, those of B and C arithmetic. The individual prices of A and C are unweighted, those of B are weighted each year by the number of shares outstanding.

From January 1857 to January 1936 index A shows a *fall* of 34 per cent, index C a *rise* of 141 per cent, but this drift apart is not a purely mathematical drift in the sense in which we have been using the term. It is not, for example, a drift whose direction could be predicted for unknown chance material. Neither the figures of index A nor the figures of index C would be changed if the time order of the data were reversed. If the 1936 prices of individual stocks had occurred in 1857, the 1857 prices in 1936, and the prices of the intervening years had been correspondingly reversed as to time order, index A would have advanced from 66 to 100 instead of declining from 100 to 66, and index C would have declined from 241 to 100 instead of advancing from 100 to 241.

In the absence of substitutions, any quasi mathematical drift found in the relation between geometric and arithmetic indexes occurs primarily because of differences in the economic drifts of the individual prices. It could not, of course, occur if it were not for a difference in the mathematical treatment of the data; but its direction and very existence depend, at all times, on differences in the individual drifts, and whenever these individual drifts are large and important, they are of economic rather than chance origin.

The ratio of the arithmetic average of n positive quantities to the geometric average of the same quantities equals $\frac{1}{n}$ th of the sum (i.e.,

the arithmetic average) of the ratios of the individual quantities to the geometric average.¹⁹ The product and hence the geometric average

. Hence the ratio of the arithmetic average to the

¹⁹ Let A represent the arithmetic average and G the geometric average. Then the n individual quantities may be represented by Gx_1 , Gx_2 , Gx_3 , ... Gx_n where each x represents the ratio of a particular individual quantity to the geometric average. Now A, the arithmetic average of the n quantities, of course equals $G(x_1 + x_2 + x_3 + \ldots + x_n)$

of these individual ratios necessarily equals unity, but their arithmetic average varies with and constitutes a species of measure of the 'scatter' of the original quantities. With both stock prices and bond prices (in the sense of the reciprocals of their yields), this scatter tends to decrease with the passage of time; though it sometimes increases for fairly long periods. But, whether it decreases or increases depends upon economic characteristics of the data rather than upon mathematical characteristics of the index numbers.

The economic characteristics of stock price data are such that changes and substitutions among the stocks tend to affect index A much more seriously than they do index C. Stocks may be removed from an index because the road has gone into bankruptcy; they are never removed (if sales continue to be regularly made) because of the excessive prosperity of the corporation. Now index A is much more affected by a specified percentage change in the price of a low priced stock than is index C. And the percentage changes of really low priced stocks are, or at least have been (on the way down), gigantic.

The effect on index A of carrying a stock into bankruptcy and then removing it from the index may be almost impossible ever to overcome, though the effect on index C be relatively small. If, in the final year that a stock was in the indexes, its price began the year at 4 and ended it at 1, the effect on index A would be no more than merely offset by a later rise in the price of another stock from 25 to 100. And, even if the low priced stock was not removed from the index but was carried through a reorganization of the road, the mere process of reorganization would render improbable a percentage recovery in the new stock sufficiently great to offset a previous decline of the old stock into the region of zero.

Stock prices are unlike commodity prices in that commodity prices, as handled by the maker of index numbers, are the prices of new and not of second-hand or worn-out commodities. Cost of production prevents the prices of new commodities dropping to zero, or even close to zero, and remaining there. Though an index based on unweighted geometric averages fulfills the 'circular test' and, in that sense, has no strictly mathematical drift, it develops a quasi mathematical drift when (Footnote ¹⁰ concluded)

geometric average, or
$$\cfrac{A}{G}$$
 equals $\cfrac{x_1+x_2+x_3+\ldots+x_n}{n}$.

it is constructed from data, such as stock prices, in which the size of the *ratio* fluctuations tends to increase as the price declines, approaching infinity as zero prices are approached, and in which there exists the very real possibility of permanently zero prices.

It is of general and fundamental importance to realize that the applicability, to any specific data, of no type of averaging or weighing can be determined a priori—by mere mathematical analysis—without considering the characteristics of the data and the purposes of the averaging. This view of the subject takes 'averaging' out of the vacuum in which it is so often discussed.

Even the index number represented by the lowest line (D) of Chart 13, subject as it is to the most violent mathematical drift, is perfectly adapted to answer certain practical questions. It is exactly the index number required to measure the changing fortune of an investor who began, in any January, by investing *cqual amounts of money* in each stock and, in each following January, rearranged his portfolio so that once again the market values of his individual holdings would be identical.

To the extent that index numbers based upon arithmetic averages of 'relatives' tend to show a definite upward drift even if constructed from mere chance data, their drift is purely mathematical. But the drift in index D is greater than would occur with chance data. This is largely the result of the fact that, during the four greatest upward surges of the railroad stock market, the lower priced and more speculative stocks enjoyed a much greater percentage advance than did the higher priced and more conservative stocks. And the lower the price of the stock the greater the number of shares used in index D. As the price advances the number of shares is reduced, new low priced stocks receiving the excessive weighting.

But, for the purpose of comparing the movements of stock prices with the movements of bond yields, this quasi mathematical element in the drift is as disturbing as is the purely mathematical element. It is as undesirable to overweight low priced stocks as it would be to overweight high priced stocks. We are even less interested in how an individual investor would have fared if he had always kept an equal amount of money invested in each security than how he would have fared had he always held the same number of shares of each security. Our problem is a social and not a merely individualistic one. We are concerned

with railroad common stocks as a type of security. We are therefore interested in what happened to railroad common stockholders as a class, but not in what would have happened to an individual if he had played the market in this way or that. We are interested in the changing value of the entire railroad system of the country—in so far as market prices can be used to measure changes in that value—rather than in changes in the price of arbitrary and insignificant or fluctuating and misleading units.

And, for such a purpose, there is only one index number. Indeed, were it not for changes in the number of shares outstanding and for the occurrence of amalgamations, consolidations and reorganizations with the attendant necessity of substitutions and changes in the list of stocks used, no question would ever arise. The price per share of each stock would, without discussion, be multiplied by the number of shares outstanding in order to obtain a figure for the total 'equity' value of each corporation—its worth to its stockholders. And these totals would then be added together. But, with not only changes in number of shares outstanding but also changes in capital structure that alter or even destroy the significance of the price of 'one share', 'chain' index numbers become absolutely necessary. Index B of Chart 13 is such a number.

The movements of index B are naturally more like those of index C than they are like those of index D. There is always some tendency for the stocks of the larger roads to be more conservative investments and therefore less violent in their price movements than the stocks of the smaller roads. Index B gives the greatest weight to the prices per share of the larger roads. It weights the various stocks in proportion to number of shares outstanding. Index C reduces this logical and desirable disparity of weighting by using only one share of each road. The larger roads receive no more weight than do the smaller. But index D goes so much further in this direction that it tends to introduce a system of *inverse* weighting. In so far as the stocks of the large roads are conservative and high priced and the stocks of the small roads speculative and low priced, the system of weighting is a complete reversal of common sense. The large companies are weighted the least heavily, the small companies the most heavily.

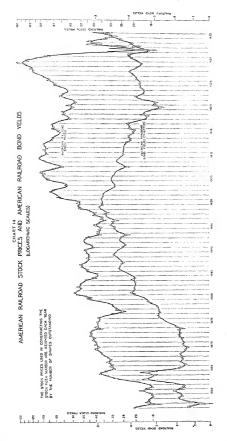
Index B is the only stock price index for which we present monthly figures. In the calculation of each link in the chain number (from one January to the next), prices were adjusted for all stock dividends,

rights, etc., that occurred during the thirteen months. After this had been done, the adjusted prices per share were multiplied by the number of shares outstanding in the earlier January. We used total number of shares outstanding rather than number of shares in the hands of investors other than railroads. The difference in the two types of index numbers would undoubtedly be microscopic, and the calculation of the weights, under the non-railroad investor assumption, would have been a piece of foolish labor.

Even if there were good reasons for eliminating all intercompany holdings when determining weights, it would mean only that our index tended to weight slightly more heavily than it should-but not in any such extreme manner as 'one share each' indexes—the stocks of the smaller roads. Little railroads do not hold the stocks of big ones to anything like the extent that big roads hold the stocks of little ones. Railroads much more usually buy stocks for control or for a voice in the management than they do for a mere share in the profits with other investors

Chart 14 presents the monthly movements of the railroad stock price index number, in which the prices of the individual stocks are weighted by the number of shares outstanding, and also the monthly movements of the 'adjusted' index number of the yields of high grade railroad bonds. The bond yield index is inverted and its scale is double that of the stock price index. As both scales are logarithmic, an upward movement of the bond yield index resulting from a halving of yields would, therefore, be of the same size as an upward movement of the stock index resulting from a quadrupling of prices.

It is at once apparent that the dissimilarities of the major movements of the two lines are much more striking than the similarities. The major long term movements of the bond yield line (inverted yields) are: (1) the irregular but violent up-swing from 1857 into 1864, followed by the short but violent down-swing into 1866; (2) the great upward swing from 1869 into 1899; (3) the great downward swing from 1899 to 1920; (4) the great, though extremely irregular, upward swing from 1920 to the date of writing. There was a fair degree of similarity between the trend movement of stock prices and the trend movement of the reciprocals of bond yields (as in the inverted line of Chart 14) from 1857 to 1864. There was, however, in railroad stock prices, no comparable movement to the violent down-swing of the bond yield recipro-



cals into 1866. During the great swing of the bond yield index from a high of 6.72 per cent in December 1869 to a low of 3.07 per cent in June 1899, stock prices were see-sawing up and down on a plateau. There was a drop definitely below the plateau into 1877 and a recovery definitely above the plateau into 1881, but in December 1869 the stock price index number stood at 37.52 and as late as June 1897 at no more than 36.45.20 During the first ten years of the great downward swing of the bond yield line from 1899 to 1920, stock prices doubled (from 51.14 in June 1899 to 105.83 in August 1909). It is true that the two lines move down together from 1909 to 1920 and up together from 1921 to 1927, and that, in the recovery after 1932, the major trends of both lines are upward. But the movements of the bond yield line, during the great 1929–32 collapse in stock prices, are little more than mere irregularities. There is no real similarity between the long term trends of the two series.

The 'cyclical' movements of the two series are much more closely related than are the long term trends. Lines D and E of Chart 21 represent the *deviations* of the bond yield and stock price mathematical graduations (presented, with the data, in Chart 14) from cycle-eliminating mathematical trends. Though there appear serious variations in the lags and even, at times, extra 'cycles' in one or other of these two deviations lines, there is, over the whole period, a real and rather striking similarity between them.

But the reader must remember that the disturbing effects of the dissimilarities of the long term trends do not exist in these deviations series. The short swings of the data, as they actually occur, show a much less uniform similarity between the two series than do the deviations. And even the similarity between the two series than do the deviations. And even the similarity between the two series than do folong term trend creates maxima and minima in the deviations series that do not exist in the original series. The deviations curve tends to pass through the zero line where mere points of inflection occur in the original series. For example, the stock price collapse that began in 1876 is accompanied by only a levelling off of the movement of the bond yield line of Chart 14. But in Chart 21 the deviations lines are strikingly similar in their movements through 1873, '74, '75, and '76. SimiTo For the figures from which Chart 14 was constructed see columns 5 and 6 of Table 10.

larly, the stock price rise into the sharp peak of 1902 is accompanied by a *fall* in the (inverted) bond yield line of Chart 14. The stock price collapse of the next year (1903) is accompanied, not by a reversal of direction after a rise, but only by an increased rate of decline of the (inverted) bond yield line of Chart 14. But, in Chart 21, the two series each show a definite minimum ²¹ in 1902.

In exceptional instances, the deviations curves of Chart 21 require very careful interpretation if they are not to be misleading. And, in at least one instance—when they suggest a stock price maximum (minimum on the inverted deviations line of Chart 21) at the end of 1930—one naturally feels that the mathematical rigidity of the 'cycle-eliminating' trend curve has introduced a palpable absurdity into the data. The collapse of (raw) stock prices that began in the autumn of 1929 was so sudden and the downward movement so precipitate and long-continued that the trend curve, in its efforts (if we may be permitted to use such an expression) to handle 1930, 1931 and 1932, turned down even more steeply than the seasonal-eliminating graduation of the data

That the short term or cyclical movements of stock prices and bond prices (as reciprocals of yields) should be more alike than the long term trends, if not as to the amplitude at least as to the timing of the movements, is as one would expect. The down swing of the economic cycle is a period in which the general demand is not primarily for more secure investments, but for more cash. It is a period of 'liquidation'—
a period in which an extraordinarily large percentage of debtors are being forced to pay off or reduce their debts, a period in which they are attempting to sell rather than merely to improve the grade of the securities in their portfolios. A reverse process goes on during recovery. As the community emerges from the vicious circle of compulsory debt payment or bankruptcy, with its inevitably depressing effects on potential investors who fear further declines, *all* types of security soon tend to advance.

The cyclical fluctuations of common stock prices are greater than the cyclical fluctuations of the prices of high grade bonds not merely because the expectation of future payment from the stocks fluctuates while that from the high grade bonds remains virtually constant but also because the stocks are, to a much greater extent than are bonds, ²¹ Stock Prices, but not bond yields, are inverted in Chart 21.

carried on loans. But the cyclical movements of the two types of security have essentially the same relation to the business cycle, the cycle of confidence, the cycle of debt contraction and debt expansion.²²

But there are no such simple reasons for expecting the *long term trends* of the two series to be similar. The compulsory liquidation on the cyclical decline and the plethora of funds for investment on the cyclical advance are each, in a sense, reactions from conditions that had become, both economically and psychologically, thoroughly extreme. A cyclical decline in stock prices is primarily a result of pressure rather than of a change in anticipated earnings—important as such a change may be. But this is not true of long continued movements of stock prices. Those movements are primarily the result of changes in anticipated earnings. But the prices of high grade bonds move with stock prices in business cycles, not because of the earnings factor but because of the pressure factor. For a changing list of bonds that are always of superlative grade, changes in the earnings factor may be assumed to be negligible.

And finally, the demonstration that the long term trends of the two series should not be expected to be necessarily the same may be put into the form of a reductio ad absurdum. If we assume that the long term movements of the prices (or yields) of bonds of superlative grade are much the same whether the bonds be railroad, industrial or public utility bonds, we realize that there is no inherent reason why the prices of superlative railroad bonds should not move up and down on their long time trends with the prices of industrial or public utility stocks as closely as with the prices of railroad stocks. But, while the cyclical movements of the three types of stock have usually been timed almost the same, their long term trends have often been quite different. For example, while railroad stock prices were declining from 1909 to 1920, the secular trend of industrial stock prices was definitely upward, from 1910 to 1919 strongly so.

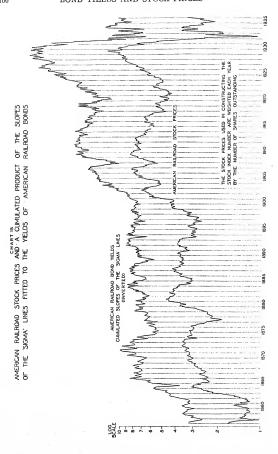
Of course, if we were to compare stock price movements with the movements of the prices of *low grade* long term bonds, we should expect to find a greater similarity than if the comparison were with bonds of superlative grade. But the increase in similarity, though definite, would not necessarily be great. We must remember that a bond, with ²² It is because it is a cycle of *confidence* that the movements of stock prices tend

22 It is because it is a cycle of confidence that the movements of stock prices tend to lag behind those of bonds. its maximum possible return, should be expected to act quite like a common stock only if that maximum return were so far above both the actual and the expected returns as to constitute no real 'damper' on upward movements. But the problems presented by bonds that are making no 'interest' payments or at best only reduced payments are, unless the bonds be income bonds, entirely different from those of common stocks. For example, the absence of dividend payments does not evoke the spectre of bankruptcy.

If, however, instead of collecting prices for a number of extremely low grade bonds—whose 'lowness' of grade would be undetermined—and comparing the movements of their prices (or yields?) with the movements of stock prices, we compare the movements of stock prices with a cumulation of the grade 'factor' given by the *slopes* of the 'sigma' lines, the results are rather interesting.

Chart 15 presents such a comparison. The reader will remember that, when the 'slope' of a sigma line is less than unity, the higher yield lower grade or in general more 'junior' bonds are acting better than the lower vield, higher grade bonds. They are either decreasing in yield more rapidly or increasing in yield less rapidly than the higher grade bonds or, in exceptional instances, decreasing in yield while the lower yield bonds are increasing. Also, the reader will remember that the mathematical equations represented by the sigma lines are of such a nature that, if the product of the slopes of consecutive sigma lines be cumulated, the result (in the absence of substitutions) will be the slope of the sigma line relating directly the yields of the bonds at the earliest and latest dates. Assuming the slopes of the sigma lines to be indexes of the degree of improvement or decline in railroad prosperity, or, more accurately, indexes of improvement or decline in the market's valuation of junior securities when compared with senior securities, we naturally feel that a comparison of stock prices with a cumulation of the sigma 'slopes' would surely be interesting.

The most cursory comparison of Charts 14 and 15 will convince anyone that, as we should expect, the *major* movements of stock prices follow much more closely and consistently the major movements of the cumulated sigma slopes (Chart 15) than they do the major movements of the yields of high grade bonds (Chart 14). But the short term movements of stock prices, whether separated from their long term trend as in Chart 21 or unseparated as in Chart 14, are more like the corre-



sponding short term movements of the (inverted) yields than they are like the short term movements of the cumulated sigma slopes (Chart 15).

Of course, this appearance of similarity in the major movements of railroad common stock prices and the cumulated sigma slopes of the bond yields and its frequent absence in the merely cyclical movements of the two series may both, to some extent, be statistical accidents. Though our index of railroad stock prices is an almost all inclusive index and is, for most purposes, logically weighted, it is theoretically perhaps, for the purposes of our present comparisons, too all inclusive and not quite logically weighted. Though the movements of the yields of railroad bonds of the highest grade should theoretically be virtually as closely correlated with the course of industrial stock prices as with the course of railroad stock prices-if either correlation were logically called for-the sigma lines derived from the movements of the yields of railroad bonds of various grades have no such necessary relation to the prices of industrial stocks as they have to the prices of railroad stocks. And, to carry the argument one step further, no such necessary relation to the prices of railroad stocks in general as they should be expected to have to the prices of the stocks of those particular railroads whose bonds were used in obtaining the sigma equations.

There are both practical and theoretical difficulties that make the construction of a stock price index number that would be more logically adapted to our immediate problem extremely difficult; and the general usefulness of such an index would be much less than that of the one we present. Whether it would increase or decrease the similarity of movement of the two lines presented in Chart 14 is hard to say.

For we must remember that the other function—the cumulated sigma slopes—is also anything but perfect from either a theoretical or a statistical standpoint. For example, the absence from the cumulated sigma slopes of a dip in 1903 and a recovery in 1904 is definitely explained by Chart 8 on which the non-linearity of the scatter outside the range of the bonds we used from January 1903 to January 1904 is clearly shown. The slope of the asymptote of the hyperbola that extends into the region of high yields is definitely greater than unity while the slope of the sigma line is less than unity.

And finally, though it would have been interesting and enlightening, if we had had the ability to do so, to have presented such functions of

stock prices and of bond yields and bond yield 'drift' as would have furnished an almost perfect correlation between the series, it would have been interesting as evidence only of the nature of the relationship, not of its existence. Chart 15 must be thought of as a test of how adequately the sigma system can represent a relationship that, from a priori considerations, may be assumed to exist, rather than as a demonstration of the existence of such a relationship.

CHAPTER VI

INTEREST RATES AND COMMODITY PRICES

The statistical study of time series has presented few more puzzling problems to the economist than those concerned with the relations between interest rates and commodity prices. The apparently high correlation between the movements of bond yields and the movements of commodity prices has been accepted, not merely by the man on the street but also by many professional economists, as virtually conclusive evidence that interest rates and commodity prices must be causally related in some extremely direct if not extremely simple manner. But the prevalence of this conclusion has resulted more from the aggressive assurance of a few hierophants than from a careful examination and consideration by their disciples of either the data themselves or the treatment of the problem by the masters.

The complete assurance that a persistent similarity between the movements of bond yields and the movements of commodity prices is so well established as to call loudly for explanation is typically expressed by John Maynard Keynes in his *Treatise on Money*. Mr. Keynes, after drawing attention to "the extraordinarily close correlation over a period of more than a hundred years between the rate of interest, as measured by the yield of Consols, and the level of prices, as measured by the Wholesale Index-Number", goes on to add that this correlation "is one of the most completely established empirical facts within the whole field of quantitative economics" and concludes that "it is very unlikely indeed that it can be fortuitous, and it ought, therefore, to be susceptible of some explanation of a general character".

¹ II, 198. The reader should be very careful that he does not give more weight than should be given to the expression "over a period of more than a hundred years" in the above quotation. A high correlation between two long extended series is an index of the closeness with which the two series can be expressed in terms of one another by a particular mathematical equation, usually a straight line with two defi-

As illustrations of how the relationship has been or can be demonstrated, Mr. Keynes presents first a table comparing 'adjusted' commodity prices with the yield of Consols by five-year periods from 1791 to 1919 and annually from 1920 to 1928. The 'adjustments' consist in increasing by 10 per cent the commodity-price figures for 1791–99, 1820–54, 1875–84 and 1926–28, by increasing by 20 per cent the figures for 1885–1914, and decreasing by 20 per cent the figures for 1891–20. Mr. Keynes describes these 'adjustments' as "dampening down the more violent movements" of the price series.²

Leaving the 'adjustments' with the statement that, "whilst making matters clearer to the eye", they are "not, however, at all necessary to establish the correlation", Mr. Keynes proceeds to introduce some of the statistical work of W. H. Coates and E. G. Peake. Mr. Coates, comparing annual figures for the yield of Consols with annual figures for the Statist index of British commodity prices, had found 4 that "the Pearsonian coefficient of correlation" between the raw annual figures for the two series was, for the period 1825-1924, $+.893 \pm .014$ and, if the yields of Consols were lagged one year, +.903 ±.012. Mr. Peake had found, for the years 1882-1913, high coefficients of correlation between the Statist price index number and the yields of London and Northwestern Railway Debenture Stock (r = +.880 without lagging and +.888 when the yield was lagged one year). He had also found lower but still relatively high coefficients between the commodity price series and short term money rates during the same period. Without lagging, the comparison with the average annual rate on 'floating money' gave r = +0.801 and the comparison with the discount rate on three months' bank bills gave r = +0.724. In each instance, lagging decreased the coefficients.5

In his popular summary of the movements of commodity prices and

(Footnote 1 concluded)

nite constants. Now such a high correlation gives no proof that the series can be as adequately expressed in terms of one another in their successive parts by the same equation—which the expression "over a period of more than a hundred years" might lead the careless reader unconsciously to assume.

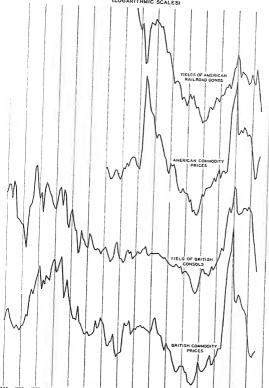
² Ibid., p. 199.

4 See Colwyn Report on National Debt and Taxation, Appendix XI, p. 101.

5 J. M. Keynes, Treatise on Money, II, 202.

³ Ibid., p. 200. Considerable insight into the nature of these 'adjustments' may be obtained by examining Chart 16 on which are presented annual data for (unadjusted) British commodity prices and the yields of Consols.

CHART 16-BOND YIELDS AND COMMODITY PRICES (LOGARITHMIC SCALES)



the yields of British Consols, Mr. Keynes writes: 6 "The broad character of the statistics since 1820 can be summarized as follows. Prices and Interest fell together from 1820 to 1850, rose together from 1851 to 1856, fell together in 1857–58, rose together from 1858 to 1864, fell together from 1866 to 1869, fell together from 1873 to 1896, rose together from 1896 to 1900, fell together from 1901 to 1903, rose together from 1905 to 1907, fell together in 1907–08, rose together from 1908 to 1914 and 1914 to 1920, and fell together from 1920 to 1923. And over and above these general trends, a number of the minor oscillations of the two are in the same direction." ⁷

⁶ Ibid., p. 201. ⁷ Ibid., p. 201.

The numbers of years in "these general trends" (in which the years 1865, 1870, 1871, 1872 and 1904 do not appear) are 31, 6, 2, 7, 4, 24, 5, 3, 3, 2, (7, 7), 4.

The 31-year period from 1820 to 1850 shows a very considerable dissimilarity in the 'minor oscillations' of the two series. But the trend of each series is undoubtedly downward throughout the period (see Chart 16). And the declines from the earliest to the latest year are almost identical. Prices (on the Sauerbeck-Statist index used by Mr. Keynes) were 31 per cent and the yield of Consols 30 per cent lower in 1850 than in 1820. The 31-year period is the period covered by the first of the

"general trends".

But, in the 25-year period from the price minimum year 1849 to the price maximum year 1873 the two series show no such similarity of long term trend. The Sauerbeck-Statist index for 1873 is 148 per cent of the 1849 figure, but the average yield of Consols was, in 1873, the same as in 1849. It is true that the yield of the high-yield year 1866 was 13 per cent higher than that of the low-yield year 1852; but 1852 is three years later than the price-minimum year 1849, and 1866 seven years earlier than the price-maximum year 1873. Mr. Keynes does not present the 25-year period 1849–73 as the period of one of the "general trends". He breaks it up into no less than four "general-trend" periods—1851–56, 1857–58, 1858–64, and 1866–69. The analysis stops with 1869. No reference is made to the period 1870–73, in which the commodity price index rose more than 15½ per cent while the yield of Consols hardly even fluttered—Sauerbeck's index for these four years being 96, 100, 109, 111; and the annual average prices of Consols 92.44, 92.71, 92.46 and

Mr. Keynes' action in not breaking up the 1873-96 period seems wise. There are no appreciable bond yield movements corresponding to the two minor upswings of annual commodity prices during the period. On the other hand, the trend of each series was undoubtedly downward throughout the period, though the commodity price decline was much more rapid in the earlier years than it was in the later and the bond yield decline much more rapid in the later years. The convex and concave appearance of the two trends may be seen in Chart 16.

Mr. Keynes next states that the two series "rose together from 1896 to 1900" and "fell together from 1901 to 1903". The first of these statements may be passed over without comment but the second calls for some hesitation. It is true that, from 1901 to 1903, with the data Mr. Keynes was using (Sauerbeck's index number of

Before coming to any decision as to the conclusiveness of Mr. Keynes' various arguments, the reader should, of course, examine the data. That's always a good thing to do! And it is especially desirable in the present instance. Many readers are inclined to investigate for themselves the statistical adequacy of a mere verbal summary. But few have the hardihood to face boldly that mystic clincher of argument, a high coefficient of correlation. And the advocates of the various theories concerning the relations between commodity prices and interest rates have no compunction about how they use that terrifying blunderbuss.

Professor Irving Fisher has for many years been intensely interested in demonstrating the existence and investigating the economic significance of a time relation between the movements of interest rates and the movements of commodity prices. He believes, as firmly as does Mr. Keynes, that the statistical history of the two series demonstrates an interrelation that "ought to be susceptible of some explanation of a general character". Over and over again he has marshaled the

(Footnote 7 concluded)

commodity prices and A. H. Gibson's figures for the yield of Consols), prices fell from 70 to 69 and yields from 2.917 per cent to 2.825 per cent. The yields for 1901 and 1903 are, of course, based on the prices of the new stock that the British Government had, in 1888, offered the holders of the old 3 per cent Consols. But the Government announced in 1888 that the new stock would carry 3 per cent interest until April 5, 1889; 23/4 per cent interest thereafter until April 5, 1903; and 23/2 per cent interest thereafter until April 5, 1923, after which date the Government could redcem it at par. Now the 'yields' that Mr. Gibson assigned to this stock are not calculated on the basis of these conditions. They are calculated on the assumption that the current rate would be paid in perpetuity. For example, the 1901 yield is obtained from the 1901 average price by assuming that 234 per cent of par would be paid in perpetuity (the terms of the bond to the contrary notwithstanding). The 1903 assumption seems to be that the total payment of that year (2 9/16 per cent of par, or one-quarter at 234 and three-quarters at 21/2) would be the amount paid per annum in perpetuity. The average price of the bond was 941/2 in 1901 and 903/4 in 1903. The correctly calculated yield was higher and not lower in 1903 than it was in 1901. We have, in Chart 16, presented the Gibson yields. They are the yields that are used by Keynes and Fisher. But they are not correct for the period 1888 to 1903 (compare Chart 16 with Chart 19 which shows prices of both series).

For the whole period 1896 to 1923 the reader may check up and weigh Mr. Keynes' analysis by consulting not only Chart 16 but also Chart 19 (price data for the two series).

Mr. Keynes does not present any "general trends" for the period after 1923 though his table (Treatise on Money, p. 199) gives prices and yields annually through 1928.

8 See Charts 16 and 19.

evidences that high and low interest rates tend to accompany high and low commodity prices. "These high correlations do not necessarily mean that the interest rate will always be high when prices are high and low when prices are low, but the tendency toward this is definitely established." And again, ". . . over long periods of time high or low interest rates follow high or low prices by about one year." 10

But Professor Fisher is not satisfied that the truly significant relation is between high and low prices and high and low rates. He finds a high correlation between levels difficult to explain. His theoretical analysis had suggested that interest rates (in terms of money) ought to be high while prices are rising and low while prices are falling. He therefore asked himself whether the interest rate figures, which seem directly dependent on price levels, cannot be presented at least as ade-

quately in terms of price changes.

In The Rate of Interest (1907) he had offered evidence that short term interest rates tend to be higher during periods of rising commodity prices than during periods of falling commodity prices, and to be functionally related to the rate of rise or fall. At the end of a rather long statistical section, he writes: "We therefore conclude with great confidence that, 'other things being equal', the rate of interest is relatively high when prices are rising and relatively low when prices are falling." ¹¹ The tables upon which this conclusion is based contain comparisons of 'bank' and 'market' short term interest rates in various financial centers with the annual percentage rise or fall of commodity prices during periods of rise and fall.

There is a statistical peculiarity of these early tables that does not appear in the revised form in which they are presented in Professor Fisher's later book, *The Theory of Interest* (1930). In the earlier book, periods described as periods of rising (or falling) prices include the final, but not the initial, years of rise (or fall).¹² But, even in the ⁹ Theory of Interest, p. 431.

10 Ibid., p. 430.

11 The Rate of Interest, p. 277.

¹² For example, if annual average prices ran 100, 104, 108, 104, 100, 104, 108, 104 ad infinitum, each period of 'rising' prices would be assumed to consist of two years with respective prices of 104 and 108; and each period of 'falling' prices would be assumed to consist of two years with prices of 104 and 100. The average price would, therefore, during years of 'rising' prices, be 106; and, during years of 'falling' prices, 102. Such treatment of the data is, of course, to be peculiarly deprecated

later book, we find evidences of the difficulty of deciding objectively how the 'periods' should be selected. For example, in the table 13 that compares London open market rates 14 with 'annual rates of change in the price level', the first four periods are given as 1825-34, 1834-39, 1839-52 and 1852-57. An examination of the lowest line of (our) Chart 16 would suggest not 1834 but 1832 as the bottom year of the decline in prices (the independent variable) from 1825; and 1849, rather than 1852, as the bottom year of the decline from 1839.15 But, if we make the seemingly unimportant substitutions of 1832 for 1834 and 1849 for 1852, we seriously affect the apparent significance of the entire table. The correlation between the interest rates (for each period) and the rates of change in the price level (for the corresponding periods) falls from the low figure +0.33 to the insignificant figure +0.23.16 And, if New York rates and American prices be used instead of London rates and English prices, the results are even more meaningless.17

By 1930, Professor Fisher himself was no longer enthusiastic about the tables comparing 'bank' and 'market' rates with average annual percentage movements of commodity prices. In the earlier book these (Footnote ¹² concluded)

when the objective is to demonstrate that high interest rates accompany not high but rising commodity prices. If rates were a constant multiple of prices, they would, with such treatment, appear to be higher during periods of rising prices than during periods of falling prices—as would the prices themselves.

18 Table VII, p. 527, The Theory of Interest.

14 The averages of the Bank of England rates of discount contained in this table need correction for the periods 1852-57 and 1858-64. They are averages of the annual rates given in the table on p. 520 of *The Theory of Interest*. The rates of that table reproduce, with a few corrections, a portion of the table that appeared on pp. 418-20 of *The Rate of Interest*. But some serious errors are uncorrected. The annual averages of the Bank rates for 1853, 1854, and 1855 remain 2.7, 2.1 and 2.9 instead of the correct figures, 3.7, 5.1 and 4.9. The corresponding figure for 1859 remains 3.7 instead of 2.7. A correction of these errors would somewhat improve Professor Fisher's ease. But the open market rates, which we discuss in the text, present his case more strongly than even the corrected Bank rates.

15 For the years 1831-35, the price index Professor Fisher prints and uses runs 92,

89, 91, 90, 92; for the years 1848-53, it runs 78, 74, 77, 75, 78, 95,

 16 The correlation for the period from 1858 to 1927 is only ± 0.19 .

¹⁷ Professor Fisher's table of New York rates and changes in American prices (Table VIII, p. 527, The Theory of Interest) must not be used. The calculations, and even the algebraic signs of that table, are inaccurate. For example, the period 1860-65, during which prices rose from 100 to 232 (on the price index used by Professor Fisher), or at the rate of 18.3 per cent per annum, is described as a period during which prices were fulling at the rate of 14.3 per cent per annum, etc.

tables constitute the backbone of a chapter. In the later book, they are tucked away among the appendices. Indeed, in the *text* of the later book, the theory that the *levels* of rates are simply and directly related to price *changes* is completely abandoned. On page 417 of *The Theory of Interest*, we read, "A very brief examination of the charts below indicates that there is little or no *apparent* relationship between *price changes* and interest rates in any of the periods studied in either country [Great Britain and the United States] except for 1898–1924 in Great Britain" (Professor Fisher's italics). On page 418, we read, "These results suggest that no direct and consistent connection of real significance exists between *P'* and *i*." ¹⁸ And, on page 427, "The studies of both the long term and short term movements of prices and interest rates give very similar results. In both studies the *r*'s are insignificant when *P'* and *i* are correlated directly, either with or without lagging. . . ." ¹⁹

But Professor Fisher is not disturbed by this fact now that he believes that he has discovered that rates are really related to price changes rather than to price levels—though not in any such simple manner as he once assumed and now rejects. That the coefficients of correlation between rates and price changes are small, he now feels is of no great consequence. "The small numerical value of r suggests that the relation can be revealed only faintly by P' and i directly. But a little consideration suggests that the influence of P' on i may be as-18 By P' Professor Fisher refers to rate of change in commodity price level and by i to interest rate (whether bond yield or short term rate). For a fuller discussion of the meaning of these terms see Appendix B.

¹⁰ The student of Professor Fisher's The Theory of Interest should consider very thoughtfully the significance of comparing P' with a lagged i. For example, if he wishes to understand just how, in a particular instance, varying the lag can affect the coefficient of correlation as it does, he will examine with great care the particular pair of series that are being correlated. He will study with great technical interest such data as those presented in the chart opposite p. 426 of The Theory of Interest, in order to discover how a coefficient of correlation between quarterly averages of short term interest rates and quarterly changes in commodity price levels can be —0.63 without lag, —0.16 when rates are lagged two years, +0.17 when rates are lagged four years, and reach a maximum (though it be no greater than +0.35) when the rates are lagged six years—in other words when the quarterly changes in commodity prices are correlated with quarterly short term interest rates six years ahead. (See chart number 50, p. 426, The Theory of Interest.)

And he might wonder how many more maximum and minimum values for r could be obtained if the lags were extended, a year at a time, until quarterly changes in commodity prices were being compared with quarterly short term interest rates a century later.

sumed to be distributed in time—as, in fact, must evidently be true of any influence. This hypothesis proved quite fruitful in my studies several years ago, in the course of which the theory of distributed influence or, if we wish to avoid the implication of cause and effect, of distributed lag was developed in considerable detail." ²⁰

The function that Professor Fisher uses to represent 'the aggregate influence' of past price changes on present interest rates, he terms $\overline{P'}$. "Arithmetically, $\overline{P'}$ is merely a certain weighted [arithmetic] average of sundry successive P''s." ²¹ The weights are the natural numbers beginning with unity. ²² The most recent P' has the heaviest weight. For example, if $\overline{P'}$ be a weighted arithmetic average of eight successive P''s, the weight assigned to the earliest P' will be unity, that assigned to the next P' will be two, and that of the most recent P' will be eight.

The coefficients that Professor Fisher obtained by correlating bond yields and short term interest rates with $\overline{P'}$, are, in almost every instance, higher than those he obtained by correlating them with P', but lower than those obtained by correlating them with P. In other words, rates and yields were usually more highly correlated with 'the weighted average of sundry successive' price changes than they were with the individual price changes; but not so highly correlated as they were with the raw prices. Before offering any suggestion as to the significance of this fact, it is desirable to present some of Professor Fisher's statistical results.

He applied the distributed lag $(\overline{P'})$ procedure to annual commodity price and bond yield figures for three periods 28 in Great Britain, (1820–64, 1865–97 and 1898–1924); and to one period in the United States, (1900–27). For the period 1820–64 in Great Britain, operations with the 'distributed lag' give a maximum coefficient of +0.46, $^{note\ 24}$ and direct correlation of the raw data a maximum coefficient of +0.57. $^{note\ 25}$ For the period 1865–97, the 'distributed lag' 29 The Theory of Interest, p. 419. Professor Fisher's italics.

²¹ Ibid., p. 419. See also note 18, this chapter.

²² Ibid., p. 421, lines 3-6 incl.

²³ Breaking the data up into 'periods' results, of course, in the mathematical equations or 'laws' relating the two variables to one another being (except by accident) different for each period.

²⁴ Read from Chart 46, p. 421, The Theory of Interest.

²⁵ Read from Chart 53, p. 430, ibid.

gives a maximum of +0.80, note 26 and the raw data +0.91. note 27 Only for the period 1898–1924, does the distributed lag procedure give a higher coefficient (+0.98 note 28) than the raw data (+0.93 note 29).

For the period 1900-27 in the United States, the distributed law gives a maximum coefficient of +0.857, note 30 while the corresponding

figure from the raw data is +0.92. note \$1

After discussing British and American correlations between $\overline{P'}$ and bond yields, Professor Fisher has a few words to say about the use of the \overline{P} procedure with American commodity prices and short term interest rates. He writes: "A study of short term commercial paper rates in relation to short term price movements corroborates the evidence obtained from correlating long term interest rates and price changes. The New York interest rates on short term commercial paper have been correlated with changes in the quarterly wholesale price indexes computed from monthly indexes of the United States Bureau of Labor Statistics for the periods 1890-1914 and 1915-1927." 32

For the period 1890-1914, he obtained from these quarterly data a maximum coefficient between P' and i of +0.37, note as by lagging ifour years. But, using $\overline{P'}$ in the form of an arithmetic average of thirty 'successive P' 's' (extending, therefore, over a period of seven and one-half years), he obtained a coefficient of +0.41. note 34 period 1915-27, he obtained a coefficient of +0.35, note 35 between P' and the quarterly short term rates of six years later. But, by using $\overline{P'}$ (Footnote 25 concluded)

Professor Fisher comments wistfully on the low figures for 1820-64. He writes: 'The British figures for 1820-64 give the lowest of any included in this study. These low figures are possibly due in part to the less accurate price indexes in those early years'. Ibid, p. 423.

26 Read from Chart 46, p. 421, ibid.

27 Read from Chart 53, p. 430, ibid.

28 Ibid., p. 423, line 23.

20 Read from Chart 53, p. 430, ibid. 80 Ibid., p. 423, line 26.

31 Read from Chart 53, p. 430, ibid.

32 Ibid., p. 425.

33 Read from Chart 50, p. 426, ibid. 84 Read from Chart 51, p. 427, ibid.

35 Read from Chart 50, p. 426, ibid.

36 The text does not state what years each series covers; whether thirteen years in each instance, that is, for example, 1909-21 for prices and 1915-27 for rates; or a mere seven years, that is 1915-21 for prices and 1921-27 for rates.

In the $\overline{P'}$ comparison of annual American prices with annual American bond yields

in the form of an arithmetic average of 120 'successive P''s' 37 (extending therefore over a period of thirty years) 38 , he obtained a coefficient of +0.738. 101 eas

This is an appreciable degree of correlation. But the correlation between the raw quarterly prices (P) and the raw quarterly rates for the same period $(1915-27)^{40}$ is, without lagging, +0.709. And, if the rates be lagged one quarter, +0.829. If the rates be lagged two quarters, r = +0.891. The rates be lagged two quarters, r = +0.891.

(Footnote 86 concluded)

for the period 1900-27, both types of comparison seem to have been made. See the notations in the body of Chart 47, p. 422, The Theory of Interest.

37 Compare first paragraph of note 36.

ns The coefficient of correlation is a measure of the degree of accuracy with which the relation between the two variables may be represented by a particular mathematical equation. There is always the chance that, when a period of time is broken up into pieces and correlation applied to the variables during each piece, the mathematical equations representing this relationship will differ greatly from piece to piece. The burden of proving that these differences are reasonable or at least not absurd is on the investigator who proposes the breaking up.

Now, if we interpret Professor Fisher's mathematical treatment of the problem described in the text as he asks us to interpret it, we find ourselves faced by an absurdity. The function $\overline{P'}$ is interpreted by Professor Fisher as 'a weighted average of sundry successive P' 's'. And, because the weights assigned to the successive P' 's run 1, 2, 3, n, the variations in the influence of any particular price change (i.e., a particular P') upon successive interest rates run n, 3, 2, 1. Or, in the words of Professor Fisher, ". . . . the form of variation of the weights is exactly-but in reverse order—the form in which the distributed influence of P' tapers off during successive periods of time" (The Theory of Interest, p. 420). But, while the correlation coefficient for the 1890-1914 period is obtained by assuming that the quarterly interest rates of that period are related in a linear manner to a \overline{P} that contains 30 successive P' 's, the coefficient for the 1915-27 period is based on the assumption that the rates are a linear function of a \overline{P} that contains 120 successive P' 's. This amounts to asking us to believe, for example, that the influence on interest rates of the change in price level that occurred during the last quarter of the year 1897 faded out completely by the second quarter of the year 1905 and remained zero until the first quarter of the year 1915 when it reappeared and did not disappear again until the year 1927.

If this absurdity be removed by using the same 'distributed lags' for both periods, the coefficients are greatly reduced. The numbers 30 and 120 (or at least some figure greater than 90) are an essential feature of Professor Fisher's argument. For example, if 30 be used for both periods, the 1915-27 coefficient is reduced from 0.738 to 0.52. If 40 be used, the coefficients are 0.60 and 0.34 instead of 0.738 and 0.41. If 50 be used, they are 0.63 and 0.11. (See *The Theory of Interest*, Chart on p. 427.)

39 Ibid., p. 427, lines 4-7 incl.

⁴⁰ For these data see *The Theory of Interest*, Appendix Tables XIV and XV, pp. 532 and 533.

⁴¹ The Theory of Interest, p. 431, lines 1-4.

As a statistical explanation of why the coefficients obtained by correlating the raw data ⁴² for selected periods sometimes run so high, the 'distributed-lag' theory seems very weak. In all but two of the comparisons made by Professor Fisher, the application of the theory lowers the coefficient. ⁴³

And, even if it usually raised the coefficient, that fact would not necessarily prove that rate levels were helpfully interpretable in terms of past price changes. For only technically is \overline{P}' a measure of price change. As the number of P' 's included in $\overline{P'}$ is increased, the configuration of \overline{P} (with such data as commodity price index numbers) usually approximates more and more closely the configuration of P, the original data.44 The reason for this condition is that, if the monthto-month (or year-to-year) fluctuations of the data are not too violent (and they seldom are with commodity price index numbers), $\overline{P'}$ tends to approximate a constant multiple of the deviation of the logarithm of the present price from an arithmetic average of the logarithms of a specified number of past prices. In other words, if for the original data we substitute their logarithms, $\overline{P'}$ (as calculated from the original data) tends to approximate a constant multiple of the deviations of these (logarithmic) data from an uncentered moving average. The levels of $\overline{P'}$ are, of course, affected by changes in this moving average. but, if the average covers a sufficiently long period of time, the configuration or 'shape' of the $\overline{P'}$ curve will tend to approximate that of the log P curve, and therefore, unless the fluctuations of P are very large, the configuration of the P curve also. It is questionable, therefore, whether, even if the use of $\overline{P'}$ raised the coefficients, we would be warranted in assuming that it did so because \overline{P} was a 'weighted average of sundry successive P''s' rather than because it was a deviation of $\log P$ from a moving base.

42 Prices and short term rates or prices and bond yields.

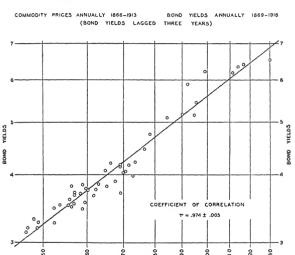
⁴⁸ One of these two comparisons supplies the only coefficient of correlation mentioned in the summary section 'Relations of Prices and Interest Interpreted' (*The Theory of Interest*, p. 438). Professor Fisher there writes: 'The rate of interest correlates very markedly with P, representing the distributed effect of lag. For recent years in Great Britain [1898–1924], the close relationship is indicated by r = +0.98 when i is lagged and the effects of P' are distributed over 28 years.'

⁴⁴ See Chart 48, p. 424, The Theory of Interest. Compare also the \overline{P}' and P lines of Chart 49, opposite p. 426, ibid.

However, as the use of $\overline{P'}$ instead of P does not tend to raise the coefficients, the suspicion naturally arises that the coefficients obtained from using $\overline{P'}$ are as high as they are because of the degree of similarity of configuration of $\overline{P'}$ and P; and not as high as when P is used

CHART 17

AMERICAN RAILROAD BOND YIELDS AND COMMODITY PRICES



because the base from which P (in the form of $\log P$) is measured (the uncentered moving average) is not as good a base (distorting to some extent the P configuration) as the simple horizontal straight line base that correlation itself introduces.⁴⁵

COMMODITY PRICES

But these criticisms must not blind us to the fact that casual inspection strongly suggests that there is a problem. Over long periods of ⁴⁵ See Appendix B.

time the two series seem to go up and down together. High correlations between them have been obtained and others are easy to obtain.40 But just what and how much do these correlations mean? We must not forget that a high coefficient of correlation between two time series should never be accepted as more than merely suggestive of even probable statistical functionality, let alone causal relationship, until the mathematical origins of the high correlation have been carefully investigated.

Does the high correlation exist with respect to both long and short term movements, to both trends and deviations from trends? If it exist for long term movements, are there many such movements or is the high correlation primarily a result of one or two great movements of the data? If it exist for short term movements, how consistent is the statistical relation? Does it hold only for 'hand-picked' periods or does it hold pronouncedly throughout the range of the data, as a whole and by pieces? If it holds by pieces, does it do so without necessitating radical changes in the mathematical equation or 'law' assumed to relate the one variable to the other? Does anything that is known about the series beyond the range of accurate numerical data make it extremely probable if not almost certain that the long term or even the short term movements are *not* highly correlated or are differently related to one another in such outside ranges?

It is apparent from Chart 16 that the long term movements of the data, for either England or the United States, are very few, and that, because of the relative insignificance of the minor movements, these long term movements control the coefficients of correlation. But, for England, it is a rough and violent control. Both series were very high in the early years of the nineteenth century, declined irregularly into the late nineties of that century, advanced to great heights in 1920 and declined irregularly thereafter. But the irregularities are so great as to require explanation. The 1798 peak in the yield of Consols occurred sixteen years before the 1814 peak in commodity prices. There is no movement of Consols that can be related to the almost

^{*6} For example, by using only a little statistical ingenuity in the choice of functions and lags (and chicane in the choice of period), we obtained for forty-eight years of American bond yields and American commodity prices a coefficient of +0.974 ± 0.005. The period covered is the whole period from the close of the American Civil War to the entry of the United States into the World War; 1866-1913 for the commodity prices and 1869-1916 for the bond yields (the bond yields are lagged three years). Both series are used in the form of logarithms. See Chart 17.

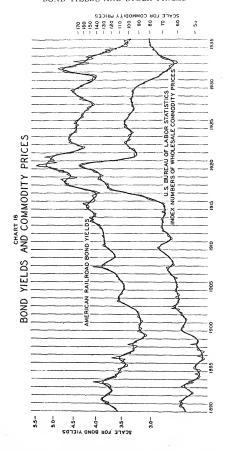
major reversal of trend in commodity prices from 1849 to 1873. And, though yields eventually completed their 1921 and 1922 fall in the thirties of the present century, they drifted slowly upward for ten years (1922-31) while commodity prices were declining; only renewing their collapse when commodity prices were ready to steady and begin a slow advance (see Chart 19). Ten years late on the decline instead of sixteen years early as in the early years of the preceding century.

Superficially considered, the American picture may seem less erratic than the British. Bond yields and commodity prices each show a huge trough beginning shortly after the close of the Civil War and ending in 1920. But, even in this period, the lags are very irregular. The early peak in bond yields came five years after the peak in commodity prices, and the beginning of the rapid decline was nine years later for yields than it was for prices. By the time the bottom of the trough was reached, in the nineties, the lag was less than three years; when the peak of 1920 was reached the lag had vanished.

Outside the range of the great trough, it is more difficult to show that American rates and prices were high and low or moved up and down together. Is the great fall in yields from 1857 to 1863 and 1864 to be tied up with the minor drop in commodity prices from 1857 to 1861? 47 Before coming to any such conclusion, it would be well to remember that bond yields began their Civil War collapse only after the gigantic rise of commodity prices had begun. There is every reason for believing that this great fall in yields can be more properly considered as economically associated with the tremendous synchronous rise in prices than with the negligible preceding decline. Similarly, the gigantic snapback of yields after 1864 can be more satisfactorily tied up with the synchronous collapse of prices than with the earlier rise.

Neither American series shows any appreciable trend from 1922 to 1929. But the violent rise in yields from the summer of 1931 to the summer of 1932 occurred in the midst of a continuous and rapid decline in commodity prices that lasted from the autumn of 1929 to the spring of 1933; and the great rise in commodity prices that began in the spring of 1933 was accompanied by a continuous and violent

⁴⁷ Though 1857 was a peak year for bond yields, the trend had been downward since the early forties. The increase in the 'spread' between prices and yields during the twenty years from 1840 to 1860 is therefore tremendous.



collapse of bond yields. These movements are well illustrated by Chart 18 on which monthly data are shown.

And even if the statistical relationship between the two series were much closer and more regular than it is, what then? Ten years before he wrote his *Treatise on Money*, Mr. Keynes, in his *Treatise on Probability*, sepalained and emphasized the importance of distinguishing between description and induction, correlation and causation. His remarks are so neatly worded that we cannot resist quoting from them.

"The Theory of Statistics, as it is now understood, can be divided into two parts which are for many purposes better kept distinct. The first function of the theory is purely descriptive. It devises numerical and diagrammatic methods by which certain salient characteristics of large groups of phenomena can be briefly described; and it provides formulae by the aid of which we can measure or summarise the variations in some particular character which we have observed over a long series of events or instances. The second function of the theory is inductive. It seeks to extend its description of certain characteristics of observed events to the corresponding characteristics of other events which have not been observed.

"The union of these two distinct theories in a single science is natural. . . . But this union is also the occasion of a great deal of confusion. The statistician, who is mainly interested in the technical methods of his science, is less concerned to discover the precise conditions in which a description can be legitimately extended by induction. He slips somewhat easily from one to the other, and having found a complete and satisfactory mode of description he may take less pains over the transitional argument, which is to permit him to use this description for the purposes of generalization. . . .

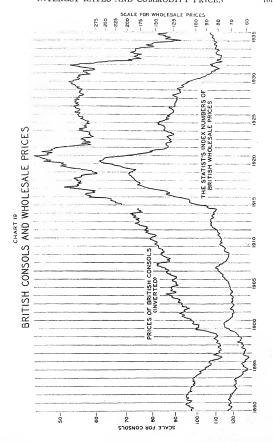
"... By the method of correlation tables and correlation coefficients the descriptive statistician is able to effect this object [the determination of the degree of correspondence between the two variables within the field of observation], and to present the inductive scientist with a highly significant part of his data in a compact and instructive form. But the statistician has not, in calculating these coefficients of observed correlation, covered the whole ground of which the inductive scientist must take cognizance. . . .

"The truth of this is obvious; yet, not unnaturally, the more com-

plicated and technical the preliminary statistical investigations become, the more prone inquirers are to mistake the statistical description for an inductive generalization. This tendency . . . has been further encouraged by the terminology in ordinary use. For several statistical coefficients are given the same name when they are used for purely descriptive purposes, as when corresponding coefficients are used to measure the force or the precision of an induction. The term 'probable error', for example, is used both for the purpose of supplementing and improving a statistical description, and for the purpose of indicating the precision of some generalization. The term 'correlation' itself is used both to describe an observed characteristic of particular phenomena and in the enunciation of an inductive law which relates to phenomena [of the same type] in general [both within and without the range of the observations]."

To treat a calculating machine as an instrument for the automatic attainment of theoretically useful economic generalizations is almost as unwarranted a procedure as was that of the Lagadan professor with his "project for improving speculative knowledge, by practical and mechanical operations," by which "the most ignorant person . . may write . . . philosophy, poetry, politics, laws, mathematics, and theology, without the least assistance from genius or study". To hold any naive faith in the ultimate efficacy of throwing numbers into a mathematical hopper may easily become as definite an obstacle in the path of inquiry as was the assumption by the mediaeval schoolmen that it was possible to obtain a comprehension of the world outside themselves by the critical study of words and their meaning completely divorced from the study of those things for which the words stood. And the dangers that inhere in any such naive faith are, as the quotation from Mr. Keynes has just suggested, extremely insidious dangers.

That no palpably absurd conclusion should ever be drawn from the occurrence of even the highest coefficients of correlation is so well recognized as to be assumed to merit no comment. No one suggests that, because the graduated seasonal curve of temperature in New York City shows (with a definite lag) a virtually perfect negative correlation with the varying seasonal distances of the earth from the sun, those variations in distance are the cause of summer and winter in this city—great distance causing the heat of summer and lesser of John Maynard Keynes, A Treatise on Probability, pp. 327-29.



distance the *cold* of winter. Indeed, no coefficient of correlation is ever thought of as offering even evidence, let alone proof, of causal relationship if its origin can easily be explained without any such assumption and if any causal conclusions would conflict radically with the facts as determined from evidence whose significance and interpretation is open to no such possibility of questioning.

But all too often when little or nothing is known concerning the possibility of causal relationship between the two variables, the absence of visible danger signals is unconsciously interpreted as proof of the absence of danger, and a high coefficient of correlation is seized upon with avidity as strong if not conclusive evidence of a direct and simple causal connection.

At best (when the correlation is virtually perfect) this type of reasoning is often almost indistinguishable from 'induction by simple enumeration', so contemptuously commented on by John Stuart Mill. "It consists in ascribing the character of general truths to all propositions which are true in every instance that we happen to know of. . . Whether the instances are few or many, conclusive or inconclusive, does not much affect the matter . . . provided no other experience of a conflicting character comes unsought." ⁵¹ "The name of Empirical Laws," writes Mill in a later chapter, ⁵² has been given "to those uniformities which observation or experiment has shown to exist but on which one hesitates to rely in cases varying much from those which have been actually observed, for want of seeing why such a law should exist. . . . If true at all, its truth is capable of being, and requires to be accounted for."

Of course any extremely great regularity of either coexistence or sequence, or statistically, any extremely high and persistent "correlation" between two or more variables (without radical changes in the functional relation) should suggest strongly that the nature of the relation and the possibility that it might be more than merely "empirical" should be carefully considered. Hypotheses to explain the regularity should be constructed and tested not merely for statistical adequacy but also for logical consistency and plausibility; and for the accordance or non-accordance with fact of the implications that they will necessarily involve. And, even if no hypothesis can be formulated that stands up

⁵¹ Logic, Book III, Ch. III.

⁵² Logic, Book III, Ch. XVI.

under investigation and analysis, the assumption should not too easily and cavalierly be made that the search for such an hypothesis should definitely be abandoned.

Writers on scientific method, and even scientific investigators, have sometimes too hurriedly assumed that unexplained apparent relationships were non-existent, accidental, or at best mere empirical curiosities. Bode's Law, according to which the relative distances of the various planets from the sun were expressed by an extremely simple formula, began as an arithmetic curiosity but became accepted as demanding explanation when, upon the discovery of Uranus, the distance of that planet from the sun was found to follow the 'law'. But, when Neptune was discovered and its distance from the sun was found to be quite different from that required by the formula, Bode's 'Law' became accepted, not as demanding explanation, but as the perfect example of accidental and unmeaning empiricism.

However, in recent years, astronomers have begun to suggest that Bode's Law fails to cover the cases of Neptune and Pluto, not because the relative distance of the planets from the sun should not be expected to follow any 'law' but because of the inadequacy of the particular 'law' Bode proposed. The suspicion is becoming general that Bode's Law is empirical primarily in the technical sense in which so many enginecring formulas are empirical rather than in the more fundamental sense in which any explanation of summer and winter in terms of the varying distance of the earth from the sun would be empirical: that it is empirical not because the relation it attempts to describe is non-existent, or scientifically irrelevant, accidental and without fundamental significance, but because the mathematical formulation of the law is of such a nature that, even if it covered all the facts with which it is directly concerned, it not only could not be used to unearth new facts and discover new relations by mere mathematical analysis, but its implications would conflict with the body of more rigidly established astronomical fact.

Merz could think of no more damning indictment of Mendeléef's periodic classification of the chemical elements than to suggest that it might be as purely empirical as "the once well-known but now [1896] forgotten law of Bode". ⁵³ But Mendeléef's classification is no longer a mere curiosity. The recognition of its fundamental signifi⁵³ History of European Thought in the Nineteenth Century, I, 422 and 423.

cance has grown steadily since Merz wrote. It is almost as easy to make the mistake of assuming that a rational law is merely empirical as it is to make the mistake of assuming that a mere empirical curiosity is rational.

An empirical law or unexplained generalization that presents, in a not palpably absurd form, an astonishingly adequate descriptive summary of observed facts usually merits careful consideration, but the consideration it merits varies with the adequacy of the descriptive summary. The summary is, at best, only an hypothesis. And, to the extent that it is full of holes and exceptions, it loses its right to demand consideration, let alone explanation. In this respect an empirical law differs from a well established and seemingly rational generalization that has been fitted into its proper place among allied scientific generalizations, that helps to explain them and that is explained by them. The unexplained perturbations in the orbit of the planet Uranus led Adams and Leverrier to suspect the existence of some other as yet undiscovered planet rather than to doubt the Newtonian formulation of the law of gravitation. The calculations of Leverrier concerning the size and position of the new planet were almost instantly verified by Dr. Galle's discovery of the planet Neptune.54

The 'explanation' that lifts a generalization out of the empirical and into the rational need not be of a directly causal type. Two variables, such as the diameter and circumference of a circle, may be functionally related without the suggestion of a causal nexus. A statistical 'law' relating the height and weight of men does not necessarily suggest that variations in either variable are caused by variations in the other. Similar illustrations may be taken from the field of economics. The high correlation between the prices of substitutes or partial substitutes, such as scrap and pig iron, is evidence of a functional but not of a one-way causal relation. Different effects of the same cause yield examples in which the variables themselves are not causally related to one another. For instance, the effects of year to year variations in rain-

⁵⁴ Of course, an exception that needs an ad hoc hypothesis to explain it always casts some degree of doubt on the original generalization until the ad hoc hypothesis is verified. We must not forget that Leverrier's later suggestion that the unexplained perturbations of the planet Mercury pointed to the existence of an undiscovered planet (Vulcan) between Mercury and the Sun was never verified, and that the perturbations of Mercury were explained only when Einstein's hypothesis had amended that of Newton.

fall on the year to year variations in the yield per acre of different crops in the same area. The seasons carry a succession of agricultural phenomena that may be described as functionally but not as causally related to one another. The peak in strawberry production precedes the peak in apple production, though the two production series are not causally related.

But the fact that the 'explanation' that lifts the empirical into the rational need not be of a directly causal type does not warrant throwing entirely aside the concept of causation. Though an almost impregnable metaphysical case can be made for the contention that the most desirable objective of science, and indeed the only one that it can possibly attain, is to describe phenomena completely and in the simplest possible manner, the unthinking acceptance of this doctrine may easily lead to meaningless and useless empiricism. It is all too easy to forget the tremendous significance that must be attached to the words 'completely and in the simplest possible manner'.

The casting out of the metaphysical devil of causation all too easily leads to his return with seven other devils. The economist must beware that the statistician, while seeming merely to describe mathematically certain characteristics of the data, does not insidiously suggest a causal relation, though the evidence be evidence only of the probability—or possibility—of a functional one. He must not allow himself to be befogged by professional patter about a 'multiplicity of causes' if there is a definite possibility that the variables that are being statistically compared are not themselves causally related. In such cases, he would usually be well advised to forget that science is merely description and to think in terms of a less refined but simpler metaphysics of verae course.

Now it is true that, in various countries and often for long periods of time, the movements of interest rates (or rather bond yields) and commodity prices have been such as to suggest that they might be rationally related to one another in some direct and simple manner. But, over the whole range of available data, the exceptions to this appearance of relationship are so numerous and so glaring that they cannot be overlooked. And the distribution of the exceptions is such as to awaken the liveliest suspicion that any theory which proposes an explanation of the apparent agreements should also explain the unmistakable exceptions. The exceptions are not scattered over the range

of the data in a haphazard manner; they occur in 'bunches'. And, the timing of these 'bunches' or *periods* of exception is such as not only to suggest why the exceptions occur but also to throw considerable light on the assumed functionality let alone causality of the periods of agreement.⁵⁵

Of course, if any formula that was not palpably artificial and ad hoc described at all adequately the entire range of the data, it could not reasonably be thrust aside without the most careful study of why it did so. But so far no one of the numerous attempts that have been made to develop even a good descriptive summary of the supposedly close relation has led to any such accurate and reliable account of all that has actually occurred as to call insistently for explanation. And, even if such a good descriptive summary existed, we should still be faced with the important question, what, if any, are the causal elements in the statistical relation.

The common assumption that, between the bond vield and commodity price series, such causal elements exist and are important has resulted not merely from the aggressiveness with which readers of economic literature have been assured that statistics support the contention that a functional relation exists; but also from the apparent simplicity of explaining why it should exist. But the 'explanations' are numerous and some of the more popular ones are mutually contradictory. Any explanation seems good enough, Indeed, all too often the elucidations sound suspiciously like what the Freudian psychologists term 'rationalizations'. And this is but what might be expected. If a formula be empirical in the fundamental sense that it is unrelated or only distantly related to the true causes of the phenomena it attempts to describe, it naturally tends to be difficult to explain. To ask why seasonal variations in the temperature of New York City are caused by variations in the distance of the earth from the sun or why the strawberry crop gives rise to an apple crop three months later is to

⁵⁶ In the statistical comparison of time series, mere absence of the highest degree of correlation, if the absence results from a moderate degree of irregularity in the relation over the whole period, may often reasonably be assumed to result from the disturbing effects of other causal factors. But, when the hypothetical relation sometimes disappears completely for years or even decades at a time, the investigator should seriously consider the possibility that causal relationship either does not exist or is of a more complicated and totally different kind from the simple and direct relation suggested by the correlation during the periods in which it is high.

propound questions worthy of a lawyer cross-examining an expert witness.

And, as we have already seen, of the mathematical relations that are presented by the various writers on interest rates and commodity prices, those giving the highest coefficients of correlation are often those that seem most suspiciously empirical and difficult to explain. For example, if the data be assumed to support the contention that the levels of interest rates or bond yields depend upon the levels of commodity prices, they indeed seem to prove too much. Professor Fisher has himself remarked that " . . . it seems impossible to interpret it [the association of high and low rates with high and low price levels] as representing an independent relationship with any rational theoretical basis. It certainly stands to reason that in the long run a high level of prices due to previous monetary and credit inflation ought not to be associated with any higher rate of interest than the low level before the inflation took place. It is inconceivable that, for instance, the rate of interest in France and Italy should tend to be permanently higher because of the depreciation of the franc and the lira, or that a billionfold inflation as in Germany or Russia would, after stabilization, permanently elevate interest accordingly. This would be as absurd as it would be to suppose that the rate of interest in the United States would be put on a higher level if we were to call a cent a dollar and thereby raise the price level a hundredfold. The price level as such can evidently have no permanent influence on the rate of interest except as a matter of transition from one level or plateau to another." 56

But the apparently high correlation between the levels of commodity prices and the levels of bond yields is explained with great confidence by the average businessman. It would seem permissible to lighten the present discussion by digressing for a moment to notice some of the explanations he offers. The commonest one is that interest rates and bond yields are naturally and logically higher in periods of high commodity prices than they are in periods of low commodity prices because in periods of high commodity prices "a dollar is worth less and hence lenders will insist on borrowers paying more dollars for a loan just as they pay more dollars per bushel for potatoes". The argument is that interest is a price—the price paid for a loan. For it to be high when prices in general are high is therefore quite as natural as for

the price of pig iron or the price of potatoes to be high when prices in general are high. Incomes must be adjusted to the level of commodity prices. Lenders, therefore, will naturally insist on higher in-

terest rates when prices are high than when they are low.

Persons who are satisfied with the above explanation never bother to ask themselves why borrowers, in a period of high commodity prices. should not insist that lenders, in return for the promise of a specified future money income, pay the borrowers more (present) dollars, because, in such a period, those dollars are worth less. But this idea has actually been used to develop the conclusion that high commodity prices, instead of being naturally accompanied by high interest rates, should naturally be accompanied by low rates. Of course, as interest rates and commodity prices show more of a tendency to be high and low together than vice versa, the theory, as an explanation of the actual facts, is worse than useless. But the reasoning, as such, is slightly more plausible than that presented in the preceding paragraph. As the Red Queen might have remarked, "I've heard nonsense, compared with which this would be as sensible as a dictionary." The argument has been definitely formulated as follows: "Money is valuable only as it commands commodities or services and therefore the price of money, which is interest, should vary inversely with the price of commodities." 57

The origin of the strange fallacies of confusion illustrated in the two preceding paragraphs is, of course, easily traceable to a muddle-headed use of the word *price*. The rate of interest may, for some purposes, be considered a *price*—but a different kind of price from the

⁵⁷ O. K. Burrell, The Behavior of Bond Prices in Major Business Cycles (Uni-

versity of Oregon Studies in Business No. 13), p. 62.

In this instance, the author's apparent assumption that the theory was useful to explain the facts as they are seems to have been made in a moment of inadvertence. Not only the statement on p. 6 where he writes, "Bond prices normally vary inversely with commodity prices . .", but also the context on p. 62 seems inconsistent with the idea that he really thought that the rate of interest even tended to "vary inversely with the price of commodities". The context on p. 62 runs as follows: "This long range rise in bonds and decline in commodities may be explained on two bases. In the first place, there is probably a causal relationship between the level of commodity prices and the level of bond prices. Money is valuable only as it commands commodities or services and therefore the price of money, which is interest, should vary inversely with the price of commodities. Probably a more fundamental explanation of the long term relationship between commodity prices and bond prices is that the same influences that operate to force commodity prices downward cause bond prices to move upward, and vice versa."

price of commodities. The *price* of a commodity at a specified date refers to an exchange relation between a specified quantity of money at the specified date and a specified quantity of the commodity at the same date. Potatoes are fifty cents a bushel when fifty cents of present money will exchange for one bushel of present potatoes. The relation is an exchange relation between different things at the same date. Now a rate of interest refers to a quite different kind of exchange relation. It is an exchange relation between the same thing at different dates instead of an exchange relation between different things at the same date. The relation is not between present money and present something else but between present money and future money. Money is on both sides of the equation.

And this brings up another phase of the absurdity inherent in the 'price' arguments—also unsuspected by their naive proponents. A price is a ratio. A rise in the potato price of cotton is a fall in the cotton price of potatoes. A high rate of interest indicates a high price for present money in terms of future money. But a high price for present money in terms of future money is a low price for future money in terms of present money. If either of these ratios is to be considered as the same kind of a price as the price of a commodity, it surely should be the price of future money in terms of present money and not vice versa. Present money can be used to buy future money or present commodities.⁵⁰

The recognition that the exchange relation to which a rate of interest attaches is an exchange relation between present money and future ⁵⁸ Even so-called 'future' contracts do not constitute real exceptions to this definition. Though a typical 'future' contract, such as a contract to buy and sell wheat or cotton on a specified future date or within specified future dates may be entered into at the present time and, though the exchange to which it refers may not actually occur until some time in the future, that exchange, when it does occur, will be of different things at the same date.

different things at the same date.

The case in which money is paid in the present in exchange for an agreement to deliver a commodity in the future is, of course, a hybrid. The price paid in the present is the price that, at present, seems a proper future price under a 'future' contract such as that just described, less a deduction determined by interest rate considerations. It contains two elements, a (future) price element and an interest rate element. Similarly with the purchase of a durable good such as a house. Whether the house is to be lived in by the owner or to be rented, the future returns are 'discounted'.

⁵⁹ It is this consideration that led us to suggest that the analogical reasoning back of the second of the two theories we have been examining is, in some respects, slightly more logical or at least more verbally plausible than that back of the first and commoner theory.

money, between the same thing at different dates, and not an exchange relation between different things at the same date has led to an extremely simple but also extremely naive explanation of why rates and prices have moved as they have. Because the explanation exhibits some real comprehension of the fundamental nature of interest rates, it offers, from a purely formal standpoint, a much more logical explanation than either of the two preceding ones. But it not only shows a deplorably inadequate acquaintance with the historical facts to be explained but also assumes on the part of borrowers and lenders a capacity to forecast the future that is positively fantastic. It explains why almost all men are either inordinately rich or excessively clever by drawing attention to the effectiveness of the almost universal desire to be one or the other—if not both.

When a lender gives up present money in exchange for a promise to pay future money, he relinquishes, so runs the theory, a possibility of present spending in return for a possibility of future spending. And, if the purchasing power or spending potentialities of a present dollar are greater than the spending potentialities of a future dollar, because commodity prices are at present lower than they will be when the future payments are to be made, the lender will insist upon and the borrower will acquiesce in a higher rate of interest than would be agreed upon by both if future commodity prices were to be lower than or even the same as present prices. The theory asserts that the buyer of a bond, for example, is not buying a series of future money payments but a series of future commodities and services (which the future money payments will be used to obtain). If the money prices of commodities and services are to be relatively high in the future, the future money income will necessarily buy but little. The present money price of the bond will therefore be relatively low, and the 'yield' or 'rate of interest' correspondingly high.

Of course, no one proposing this explanation of why rates and prices have moved as they have would think of even suggesting that borrowers and lenders, who are responsible for the movements of interest rates and bond yields, are capable of forecasting with complete and mathematical accuracy the future of commodity prices. They would no more think of making such a suggestion than they would think of suggesting that buyers and sellers of high-grade long-term bonds are capable of forecasting accurately the future of short-term interest

rates. However, an enlightening first approach to the problems presented by any theory that interest rates and bond yields are completely determined, or even usually greatly affected, by forecasts of future commodity prices may be made by beginning with just such absolute assumptions. What would be the movements of short and long term interest rates if borrowers and lenders, valuing future funds only because they could be used in the future to purchase commodities, were able accurately to forecast future commodity prices; and, because of their forecasts, so operated in the money and investment markets that both short and long term rates were always logically adjusted to the future movements of commodity prices—the short term directly, and the long term indirectly (in accordance with the principle of 'investment indifference'¹⁰⁰)?

Under these hypothetical conditions the *levels* of short-term interest rates would vary with the *rates of change* of commodity prices. If prices were *advancing* rapidly short-term rates would be *high* and, *vice versa*, if prices were *declining* rapidly short-term rates would be *low*. For example, if short-term rates could be assumed to remain constant at, say, four per cent per annum when the level of commodity prices was not changing; then, during a period in which prices were rising at the rate of 6 per cent per annum, rates would remain constant at a little less than ten and a quarter (10.24) per cent per annum.

If future commodity prices were to trace out a sine curve on a logarithmic scale, short-term interest rates (plus unity) would trace out a curve resembling the commodity price curve, but the maximum interest rates would occur when the slope of the logarithmic price curve was at a maximum, and the minimum rates when the slope of the price curve was at a minimum. The maxima and minima of the short-term interest rate curve would precede the maxima and minima of the commodity price curve by a quarter cycle.

⁶⁰ See Ch. II.

at In addition to the usual absurdities brought to light by a discussion of the implications of any such contrary-to-fact assumptions as those we are making, a peculiar and specific unreality is here suggested. If commodity prices were declining at the rate of six per cent per annum, short-term rates should stand at approximately minus two and a quarter (2.24) per cent per annum. But, as money is physically not a perishable commodity, bona fide negative rates, that is negative rates that are not measures of the value placed on some privilege or right unconnected with the receipt of interest, are even theoretically quite impossible beyond the extremely low percentage necessary to cover safe-deposit or other custodial charges.

Furthermore (under the doctrine of 'investment indifference'), during a period in which commodity prices were rising at a constant rate. and in which short-term interest rates therefore remained constant. the return that could be obtained by buying (without commission) a bond of hypothetically absolute security and later selling it (also without commission) would be a constant rate per annum—the same rate as the short-term rate. If the 'current' yield of the bond, as the brokers term it, in other words the yield on the arbitrary assumption that the bond is a perpetuity, were less than the constant short-term paper rate, the price of the bond would advance (and the 'current' yield decline) continually throughout the period; if the 'current' yield were greater than the constant short-term paper rate, the price of the bond would decline (and the 'current' yield advance) throughout the period. 62 Furthermore, if, at the beginning of any six months' period, the bond's vield to maturity were less than the short-term rate for the next six months, the yield to maturity would have to decline still further during that six months. But the bond would not necessarily advance in price. 63 And trice versa.

If the movement of interest rates were completely determined by a knowledge of the future movements of commodity prices and if it were known that commodity prices were, in the future, to move up and down in a sinusoidal manner, short term rates would, as we have seen, move in a similar manner but reach maxima and minima a quarter cycle early. However, as bond yields (to maturity) would be declining whenever short term interest rates were above the yield of the bonds and advancing whenever the short term rates were below the yield of the bonds, the bond yields would tend to reach maxima and minima ⁶² In each case, the assumption must be made that, because of complete knowledge of the future of commodity prices and short-term interest rates, the price of the bond at the time of purchase would be such as to permit these price movements to occur in such a manner as to end (at 'maturity') with the face of the bond plus the last coupon.

as If a 6 per cent bond having 2 years to run sells for 103.81, its yield to maturity is 4 per cent per annum. If at the end of six months (1½ years to run) it sells for \$\frac{1}{2}\$ (103.62, its yield is then 3½ per cent per annum. The realized return over the six months to a purchaser who bought at \$103.81 immediately after one coupon payment and sold at \$103.62 immediately after the next would be \$2.81 (\$3.00 coupon minus 19 cents depreciation in price) on an investment of \$103.81 or more than 2.7 per cent per half year. Assuming this to have been the semi-annual return on short-term money, we see the bond yielding at both dates less than the short-term rate and the yield falling between the dates but the price also falling. See Ch. II.

at approximately (very shortly after) the dates on which commodity prices reached minima and maxima. But the proponents of the theory do not offer it as an explanation of why bond yields should be low when commodity prices are high and high when commodity prices are love, but as an explanation of why yields and prices are so often high and low together.⁰⁴

Of course, if only the *near* future of commodity prices (and hence of short term interest rates) were foreseen, there would be no reason

64 Compare J. M. Keynes, A Treatise on Money, II, pp. 202 and 203.

"Nor can we regard the facts as an example of Professor Irving Fisher's wellknown theorem as to the relation between the rate of interest and the appreciation (or depreciation) in the value of money. Indeed quite the contrary, For the comnensatory movements which Professor Fisher postulates relate to the sum of money repayable a year hence against cash loaned today which will cover interest plus (or minus) an allowance for the change in the value of money during the year. Thus, if real interest is 5 per cent per annum and the value of money is falling 2 per cent per annum, the lender requires the repayment of 107 in terms of money a year hence in return for 100 loaned today. But the movements to which Mr. Gibson calls attention, so far from being compensatory, are aggravating in their effect on the relation between lender and borrower. For he shows us that, if prices are rising (e.a.) 2 per cent per annum, this will usually be associated with a tendency for the capital value of long-dated securities to be falling 2 per annum; so that the purchaser of long-dated securities will possess a year later a sum which is worth 2 per cent less in terms of money which is itself 2 per cent less valuable, so that he is 4 per cent worse off, the two factors of change not balancing, but aggravating, one another-whilst the variations in the rate of interest earned during the year in question are too small to make much difference."

The theory here attacked by Mr. Keynes is presented most openly in Professor Fisher's earlier book, The Rate of Interest. Mr. Keynes' criticism is useful because suggestive. But the reader should notice that he takes no cognizance of either the relation of 'investment indifference' which, theoretically, should exist between bond yields and (known) future short term interest rates or the distinction between 'promised' and 'realized' yields. Professor Fisher's contention was that, if 'real' (or 'commodity') interest for the next year was to be 5 per cent per annum and it was known that commodity prices were, during that time, to rise 2 per cent, a lender would insist that, if he were to lend his money for that year, 7+ per cent per annum must be 'promised' him. What effect his insistence should theoretically have on the yields of outstanding long term bonds Professor Fisher does not say. It is, however, at least imaginable that, if borrowers and lenders thought in terms of 'commodity' rather than 'money' rates and if they could see into the future of commodity prices for one year but not for more than one year, 'promised' yields on one-year loans could follow Professor Fisher's scheme; though, in the absence of knowledge of future short term rates beyond one year, bond prices and yields would not move in such a manner as to create a condition of 'investment indifference' and hence the return 'realized' by buying a bond and selling it one year later would not necessarily correspond to the 7+ per cent yield 'promised' in the one-year note.

for a relation of 'investment indifference' to arise between long term honds and short term notes. As a period of rising commodity prices approached and began to be foreseen, both short and long term rates would rise; the short term rates as soon as commodity prices actually began to rise and the long term rates almost immediately, because the foreseeing of the future high short term rates (which would come with the rising commodity prices) would produce an upward adjustment in the community's estimate of that peculiar 'average' of expected short term rates that would constitute a bond 'yield'. Such a condition could, of course, help to explain why 'investment indifference' is not a reality of the market place, why bond yields are always being 'adjusted' to short term interest rates but only to short term rates that are unmistakably imminent or have already materialized.⁶⁵

There is still another type of forecasting theory. It is that the movements of interest rates depend on forecasts of future commodity prices but that the forecasts are not necessarily good or even conscious forecasts. They are mere unreasoning carry-overs from the past, from what has been occurring. This type of theory contends that the longer a commodity price movement lasts the more do borrowers and lenders consciously or unconsciously adjust their dealings with one another to the assumption that the movement will continue, and interest rates therefore continue to rise (or fall) as long as commodity prices continue to rise (or fall). This contention does not involve the proven absurdity of assuming good forecasting to be habitual or even usual, but the theory fails as a general explanation of the facts, though the consideration it stresses may often be a minor and sometimes, under peculiarly exceptional circumstances, a major factor in the determination of rates.⁶⁰

Forecasts that prevailing price movements will continue tend to be better than would be those based on the mere flips of a coin, only because commodity price movements so often gather very considerable

⁶⁵ Of course, even the near future of short term rates is, as we have shown in Chapter II, seldom foreseen with much accuracy. The 'adjustment' of bond yields to short term rates is usually an adjustment to present or past rates. As an adjustment to future rates, it is almost invariably overdone—as though the forecast were that a present high level of short term rates was an important indication that those rates would permanently or at least for a long time be much higher than had been expected before they rose.

⁶⁶ For example, in a period of pronounced and increasing currency inflation.

momentum. They never last forever but they often last a considerable time. Innumerable minor fluctuations may be superposed on major swings but the picture is usually like stormy waves on the open sea or rolling hills and surface irregularities in a mountainous country rather than like ripples on the flat surface of a small pond or ups and downs in a ploughed field. As the crest or trough of a great wave is reached, in other words when the future is no longer to be as the past has been, the forecasting is almost always exceedingly bad; that it is usually a mere straight-line projection of past price movements soon becomes all too evident. In the absence of startling occurrences whose economic significance seems fairly plain (such as war or a runaway currency inflation), rational as opposed to such mere projective forecasting is rare.⁶⁷

At this stage of the discussion it is desirable to introduce and examine an assumption that is implicit in most of the theories that stress the importance of conscious or unconscious commodity price forecasting. That assumption is that the only, or at least the overwhelmingly important, reason why anyone should value a promise to pay money in the future is that future money can be used, in the future, to buy commodities. Indeed, the suggestion has often been made that 'money' interest was a mere artificiality and 'commodity' interest the only 'real' interest.⁴⁸

et Professor Fisher, though he continues to strike the conscious-forecasting note, tends to press down more and more resolutely on the soft pedal. And that seems wise. The third sentence of Ch. XIV of The Rate of Interest (1907) states: "The object will be to ascertain the extent to which, in the actual world, the appreciation or depreciation of the monetary standard is foreseen by borrowers and lenders, and provided for in the rates of interest upon which they agree." The corresponding sentence of the corresponding chapter (XIX) of The Theory of Interest (1930) runs: "The main object of this chapter is to ascertain to what extent, if at all, a change in the general price level actually affects the market rates of interest." In many parts of the chapter of the later book, the language of forecasting persists but it often seems to be a mere hang-over from the earlier book. The theory of the "distributed lag" (presented in the later book) explains the movements of interest rates exclusively in terms of past commodity price movements.

**Scompare Irving Fisher, The Theory of Interest, p. 42.

"Is there, then, no absolute standard of value in terms of which real interest should be expressed? Real income, a composite of consumption goods and services, in other words, a cost of living index in accordance with the principles set forth in Chapter I, affords a practical objective standard. By means of such an index number we may translate the nominal, or money rate of interest, into a goods rate or real rate of interest, just as we translate money wages into real wages."

In recent years, this idea has gained considerable currency. Indeed. many buyers of bonds rather sententiously assert that, before investing. they attempt to forecast the cost of living. They insist upon the importance of future 'corned beef and cabbage' as opposed to future money. However, even the briefest interrogation will quickly disclose the fact that in almost every instance they are not talking about their own corned beef and cabbage but some one else's corned beef and cabbase. They personally are concerned only with future money. They want money interest and if possible a money profit on the purchase price of the bond. Even those investors 69 for whom the importance of future money might seem to be fairly measurable by the future commodities and services that it could buy, almost always think and act in terms of money rather than in terms of its future purchasing power. With exceptions so rare as to be negligible, the only reason why bond buyers or sellers talk about commodity prices is that they believe commodity price movements are highly correlated with bond price movements. Why this is so they do not know. Introspection leads them nowhere. They themselves do not think in terms of commodities. 70 All the 'corned beef and cabbage' talk is purely impersonal. It circulates like gossip without serious scrutiny or even clear formulation.

Corned beef and cabbage theories grossly underestimate the importance of money as undifferentiated purchasing power. Unless a potential lender of money who intends to use the resulting income for the purchase of consumers' commodities knows that he will, in the future, want only commodities that, because they do not deteriorate with time, can be bought in the present, and, unless he also knows exactly what commodities he will then want, he cannot forestall his future needs by present purchasing. To the extent that his future of Such as retired business and professional men who are free from debt and are living on the returns from their investments.

⁷⁰ This is, of course, not true when, as in the midst of an uncontrolled paper money inflation accompanied by rapidly increasing distrust in the currency as such, the

probability of an extremely violent price movement seems great.

¹¹ And he cannot advantageously forestall his future needs for even commodities that will not appreciably deteriorate, unless the market price of such commodities is to advance more rapidly than would money accumulate if placed in a superlatively secure investment maturing at the time he will wish to use the commodities. For instance, if the 'lender' discussed by Mr. Keynes (see note 64) were unwilling to accept 5 per cent money interest for a year because commodity prices were to rise 2 per cent during the year, he could not better himself by buying commodities and selling them at the end of the year with a profit of 2 per cent.

wants will be for perishable goods, he will want future purchasing power; and, to the extent that he does not now know what those wants will be, he will want not a ticket good merely for particular commodities but undifferentiated future purchasing power. He may, of course, obtain this undifferentiated purchasing power by speculating in commodities that he does not want to use or by engaging in a business that would be advantageously affected by a rise in the general price level. But the fact remains that what he wants and should want is undifferentiated future purchasing power—in other words, money not commodities.

And, for every dollar lent by such an individual who thinks in terms of future purchasing power (even if undifferentiated), there are many many dollars lent by institutions whose managers do not and should not so think. The corned beef and cabbage theory forgets that future money can be used to discharge future money obligations as well as to buy future commodities. The largest buyers of bonds are the banks and insurance companies. To liquidate their future money obligations, they clearly will need future dollars and not future commodities. If the managers of such institutions are interested in what happens to the market value of their bond portfolios, and if they believe that the movements of commodity prices affect the movements of bond yields, they will, of course, be interested in the future of commodity prices; just as they will be interested in the future of business activity. But their direct concern is with dollars and not with corned beef and cabbage. The same is true of borrowers. Though, like lenders, they may be affected indirectly by their intelligent or unintelligent pondering over the possible influence that future commodity price movements may have on future interest rates, they certainly do not, in their own business calculations, usually measure or even think of future interest payments in terms of relinquished future purchasing power. Unless they expect a gigantic rise or a gigantic fall in commodity prices, both borrowers and lenders tend to think in terms of money rather than in terms of commodities.

And thinking in terms of gold rather than paper is only partially an exception to this rule. Though, when such thinking occurs, the relatively stable purchasing power of gold may be stressed, the gold is not thought of as a commodity that, because of its physical characteristics, is desirable for its own sake; but as another and better money. It is

not wanted because it can be used to manufacture jewelry or tone photographs, but because of its undifferentiated purchasing power. It has been, and to a considerable extent still is, 'the money of the international republic'. It can be used as such or (at least till recently) converted into a larger or smaller number of paper dollars. But, whether to be converted or to remain unconverted, it is thought of as the supreme type of undifferentiated purchasing power.

If serious doubt arises as to the monetary soundness of the home currency, a foreign money, especially if it be gold, may be thought of as a more 'real' money. But, in the absence of any such doubt, the purchase of a bond payable in the foreign money will tend to be thought of by all, except those to whom for one reason or another the foreign currency is really 'money', as a speculation rather than an investment. During the long period in which the commodity purchasing power of silver was more stable than that of gold, there was no visible tendency for the inhabitants of countries on a gold basis to think of bonds payable in silver as more conservative and less speculative 'investments' than those payable in gold.

that the price of a foreign money in terms of the home money is to rise or fall, and if there be in that market two bonds similar in all respects save that the one bond is payable in the money of the market and the other bond in the foreign money, then the *relation* between the promised yields of the two bonds (calculated for each bond in terms of the money in which its promises are made) will tend to be affected by this forecast.⁷² The anticipated change in the price of the one money in terms of the other money may, of course, be expressed in terms of anticipated changes in the general purchasing powers of the

Of course if, in a particular market, there exist a general forecast

two moneys. But the introduction of these new (and presumably unknown) variables is quite unnecessary. In determining the *relation* between the two yields, borrowers and lenders are concerned with the present and future prices of a unit of the one money in terms of a ⁷² Compare Professor Fisher's table giving, annually for the period 1865–1906 in-

⁷² Compare Professor Fisher's table giving, annually for the period 1865-1906 inclusive, the gold yield of British India bonds payable in gold and the silver yield of British India bonds payable in silver, both yields being calculated from prices in the London market. The Rate of Interest, pp. 266-68 and The Theory of Interest, p. 404.

The relations between the yields of the table are far different from what they would have been had they been controlled by good price forecasting.

unit of the other money, entirely divorced from anticipated changes in the general purchasing power of a unit of either money. It is not necessary for them to forecast whether general purchasing power will be increasing for one money and decreasing for the other or increasing or decreasing for both.

Because of the desire for future 'money' there will, in any market, tend to be a factor favoring bonds payable in the money of that market. But this factor is of a monetary rather than a commodity nature. It exists whether the money of the market be appreciating or depreciating in terms of commodities or of another money. Only if the purchasing power of the market money declines so rapidly and far as to affect radically the essential monetary characteristics of the market money will the influence of this factor disappear or become reversed. In the past, its importance seems usually to have been definitely on the wane when the inhabitants of a country in the threes of a currency inflation have begun to stop ascribing their troubles to a rise in the currency price of gold and to talk about a fall in the gold price of the currency. By the time that most important contracts are being made in terms of gold or some foreign currency, the influence of this 'home market' factor has become reversed. The 'flight' from the old money is then nearly complete. No longer is it the money of the country. 'At long last' has come recognition that the trouble is with the paper and not with the gold. "'It is not I who am ailing', said the wizard; 'but there is one here very sick'."

But, in the absence of radical inflation and assuming, as we have been doing, that the monetary obligations of the buyers and sellers are predominantly in terms of the money of the market in which the bonds are being bought and sold, it would seem that the importance of the factor favoring bonds promising payment in that money would not usually be appreciably affected by a change in the forecast of the future price relations between it and some other money. The factor exists not because of the nature of such forecasts but because of their uncertainty. Its influence is usually therefore to a high degree independent of the influence of those forecasts.

If, in the seventies or eighties of the last century, a retired London banker, who neither had nor expected to have monetary obligations payable in rupees, had been weighing the relative investment attractiveness of the gold and silver bonds of British India, he would not have bought a rupee bond if he expected rupees (in terms of pounds sterling) to depreciate over the life of the bond, unless the sterling price of the bond when converted into rupees was such as to give a higher rupee yield than the gold yield of an otherwise identical British India bond payable in gold. But, in addition to the extra silver vield he would have demanded because of his expectation of a fall in the gold price of rupees, he would have insisted upon a further premium for the uncertainty of the (future) value of his (future) rupee pavments in terms of (future) pounds sterling-or (future) English 'money'. If, on the other hand, he had been a retired Calcutta banker having and expecting to have only rupee obligations, he would have been willing to accept a smaller silver yield than his forecast of a depreciation of rupees in terms of sterling would warrant. Because, in actual fact, the primary market for the sterling bonds was England and that for the rupee bonds was India and because of the peculiar monetary and trade relations between England and India, it is very hard to estimate how much or how little the 'spread' between the two yields was increased or decreased by the combined operation of the two factors, one favoring bonds payable in silver and the other favoring bonds payable in gold.

But although the case for believing in the importance of the moneyof-the-market factor be extremely strong, we do not always find unequivocal statistical assurance of even its algebraic sign. It is therefore only natural that statistical evidence of the influence of the often almost supposititious forecasting factor (whether of the price of gold, of commodities in general or of a foreign money) should seldom be clear cut and unmistakable. To assume, tempting as in any particular instance it may be to do so, that the influence of price forecasting can be discovered from past rates and succeeding prices (as they actually materialized) may be quite unwarranted. To reason that, because the rates and the succeeding prices do not seem incompatible with an assumption of good forecasting, the forecasting was good and the rates were so determined may be to introduce merely a grossly ad hoc fictional 'as if'. But to argue that, when rates (in the light of succeeding prices) give no suggestion of good forecasting, they must neecessarily have been determined by bad forecasting may well amount to the crassest of circular reasoning.

And, if to discover (except in periods of pronounced currency in-

flation) unequivocal statistical evidence of the mere existence of this clusive factor is often difficult, to *measure* its influence (even in such periods of pronounced inflation) is commonly found to be virtually impossible. How large or small an influence forecasting of the (paper) prices of gold and commodities (together with an almost certainly varying degree of preference for bonds payable in paper) may have had, for example, upon the (paper) prices and yields of American railroad bonds during the Civil War years of the 1862–79 inflation is certainly a 'puzzling question' even if not 'beyond all conjecture'.

Only a pale and flickering light is thrown on this question by the relative prices of gold and paper bonds. Even if we completely ignore differences in coupon rates and are extremely liberal as to differences in time to maturity, we still find it virtually impossible to discover pairs of important bonds identical or nearly identical in all respects save their media of payment. They fail to fulfill one or both of the two fundamental requirements of direct statistical comparison, identity of

markets and equality of confidence in future payments.

Almost no instances occur of pairs of otherwise similar gold and paper bonds that were traded in exclusively or even nearly so on one and the same monetary market and that market alone; not merely were they bought and sold on two or more monetarily different markets but the relative importance of the various markets was usually not even approximately the same for the two bonds. Indeed, in many instances, it seems that neither bond was traded in to more than a negligible extent on the primary market of the other bond; the primary market for the paper bond being Boston or New York and the primary market for the gold bond London. The differences in assurance that the promised future payments would be met as promised seem to have been great though almost certainly unmeasurable. Contemporary newspaper and magazine articles suggest strongly that both domestic and foreign confidence that the promised gold payments of almost any specific American gold bond would be met (in gold) fell appreciably short of the confidence that promised paper payments of paper bonds of the same obligor would be met (in paper). This was unmistakably true not only of Federal bonds but also, though to a less extent, of the best New England municipal bonds.

The relative yields of such gold and paper bonds as were otherwise at all comparable seem seldom to have been grossly incompatible with such market opinion as pictured by the financial commentators. But there were so many unmeasured if not unmeasurable factors that it is usually difficult to draw any very definite conclusions from the quoted prices. In March 1864, the Federal Government issued the '5 per cent Ten-Forties'. These bonds were payable at the pleasure of the Government after any period not less than ten years and not more than forty years from date. Both principal and interest were, by the Loan Act of 1864, payable unequivocally in gold. But, though the bonds were offered to the public at par (100) in paper, on the first day of offering (March 26, 1864) only \$875,000 was subscribed, the second day \$130,-000 and the third day \$430,000.73 On March 26, 1864, the price of greenbacks in gold ranged from 58.91 to 59.00 per 100. The gold yield of these bonds was therefore, even if they were to remain outstanding for the entire forty years, more than $8\frac{1}{2}$ per cent per annum; if paid in gold at the end of ten years, the gold yield would be over 12 per cent per annum. Later, in the summer of 1864, the paper price of the Ten-Forties was only 109 at a time when the paper price of gold was 250. The gold price was, therefore, at that time less than 44 and the gold yield, even to the forty year maturity, more than 11½ per cent per annum.74 The paper yields of Federal paper bonds were running high but at no such levels as these. Under the circumstances, it is difficult to say what part of the spread between the gold and paper yields was caused by distrust of the gold promises and what part (if any) was caused by the market's forecasting a rise in the gold price of paper. We must not forget that, even as late as 1869, there was no great assurance that even the 5 per cent Ten-Forties would have their principal paid in gold.75 The yields of gold and paper municipal and railroad bonds present similar difficulties.

During such a disturbed period as the year 1865, for example, fluctuations in the paper price of gold, because they affected confidence in the gold promises of the government, did not affect the paper prices of Federal gold bonds in the manner in which they might theoretically be expected to do. If the yield in gold of a gold perpetuity were to 13 Hunt's Merchants' Magazine, April 1864, p. 303.

⁷⁴ The complete lack, at this time, of British confidence that the American Government gold bonds would actually be paid in gold is seen in the fact that, in July 1864, the gold 6 per cent Five-Twenties of 1882 were offered in London at 49 gold while 50 gold was being bid for New York Central 6 per cent paper bonds of 1883.

⁷⁵ See Commercial and Financial Chronicle, March 20, 1869, p. 257, column 2.

remain constant, its price in gold would remain constant and therefore its price in paper would be a constant multiple of the paper price of gold. But if, whenever the paper price of gold declined, confidence that the bond would remain on a gold basis increased, the paper price of the bond would not decline as much as the paper price of gold; indeed, if the increase in confidence were sufficiently great, the paper price of the bond might even advance. Now the year 1865 was a year of rapidly declining paper prices of paper bonds and rapidly, though less uniformly, declining paper prices of gold, But from December 31, 1864 to March 1, 1865 the paper price of the Ten-Forties rose from 1013/4 to 1023/4 while the greenback price of gold was declining from 226 to 200. And, though the price of the bonds declined from 1023/4 on March 1, 1865 to 911/2 on March 22 while the greenback price of gold was declining from 200 to 157, it advanced to 95 on May 17 though the greenback price of gold had in the meantime declined further to 130. By November 25, the paper price of the bond had declined to 91 though the paper price of gold had advanced to 147. But, even after this decline, it was, relatively to the paper price of gold, much higher than it had been at the beginning of the year. The paper yields of American railroad bonds were during the year 1868 only a shade lower than the peak yields of 1865, but confidence that the Ten-Forties would be paid and paid in gold had increased so much (it would seem) that during that year they sold as high as 1091/8 (paper) and never below 100 (paper) even though the greenback price of paper went down as low as 1321/4.76

The movements of the prices of many Federal bonds suggest that confidence that promised payments of principal in gold would actually be kept tended to increase as maturity approached and no adverse governmental action occurred. On January 26, 1866, the Federal gold 6's of 1847 (due in 1867) sold at 123½ in paper with gold at 139¾, but thirteen months later (February 27, 1867), with gold at the same price, the paper price of the bonds had risen to 135.

It is, of course, in a case like this, extremely difficult if not quite impossible to estimate at all accurately the separate effects of increasing confidence in the gold promise, possible (bad) forecasting of the price of gold, preference and possibly changing preference for bonds payable in the money of the market, varying relative influence of the New York and London markets, etc.

We must remember that an American who wished paper rather than its gold equivalent but who bought the bonds because he expected the paper price of gold to advance or at least not decline appreciably would have faced a very serious paper loss if the premium on gold had virtually disappeared before the maturity of the bond; though an English purchaser would have been completely unperturbed by such an eventuality.

The great fall in the (paper) yields of American railroad paper bonds during 1862 and the abnormally low levels of those yields during 1863 and 1864 might easily suggest that the railroad bond market was at that time forecasting an imminent and prolonged fall in the paper price of gold, or commodities, or both gold and commodities. But one of the difficulties of this assumption is that, during the period in which the paper price of gold (and of commodities) was rising most rapidly and a forecasting of an imminent decline would therefore seem psychologically most improbable (paper) yields were falling-reaching their lows in July 1864, the peak month for the paper price of gold (six months before the peak month for commodity prices). Of course, it is barely possible that, unwarranted as it may seem to have been, the financial community was, during this period of rapid depreciation of the currency, actually expecting a speedy fall in the paper price of gold (and commodities) and operating on that expectation.77

But, if this were true, why did (paper) yields begin to rise sharply as soon as the peak in the paper price of gold was passed and the expectation of a fall in its price became really warranted? It would, of course, be quite understandable that they should have risen if the impending fall in the prices of gold and commodities had all along been fairly accurately foreseen. And, in the sense that the price future proved not inconsistent with a probably unwarranted but possibly existent general expectation, they may have been 'foreseen'. But even this seems rather hard to believe—much like being asked to take seriously the prophecies of Nostradamus.*

77 See Wesley C. Mitchell, A History of the Greenbacks, pp. 369 and 370.

"Nor... is it surprising that business men failed to see what was coming; for the course of prices depended chiefly upon the valuation set upon the greenbacks, and this valuation in turn depended chiefly upon the state of the finances and the fortunes of war—matters that no one could foresee with certainty. Indeed, there was much of the time a very general disposition to take an unwarrantedly optimistic view of the military situation and the chances of an early peace. Many members of the business community seem to have felt that the premium on gold was artificial and must soon drop, that prices were inflated and must collapse."

78 The yields of some of the bonds in our list would seem to suggest that there possibly was a real forecast of an even more rapid return of paper to a par with gold than actually occurred. For example, the Pennsylvania Railroad Second Mortgage 6's due in 1875 (Bond Number 9) sold at lower yields than the First Mortgage 6's of the same road due in 1880 (Bond Number 10) every month from March 1864 to August 1864 inclusive. Though, of course, all that this fact could logically be

Before leaving these puzzling Civil War years, it is desirable to remind the reader that, even if it could be known that the movements of American railroad bond yields during the years 1862–65 inclusive were as they were largely because of conscious gold or commodity price forecasting (which, whether accidental or not, would have been good forecasting); that fact would not help us to explain why, as for example during the period 1916–21 for commodity prices and 1917–22 for railroad bond yields (see Chart 18), bond yields and commodity prices should ever be positively and not negatively correlated—unless we are willing to introduce the deus ex machina of bad forecasting.

But 'much study is a weariness of the flesh. Let us hear the conclusion of the whole matter'. In the first place, the absence of a really persistent and uniform statistical relation between the series suggests strongly that, even if the one series be to a greater or less extent dependent on the other, the very nature of that dependence may vary. For example, forecasting may be a negligible or an important factor and, if important, may be good or bad. Thus, it is at least possible that railroad bond yields were low during the high gold and commodity prices of the Civil War because a great fall in prices was, whether warranted or not, being commonly expected; and high during the high commodity price period centering round 1920 because of conditions caused by the rise of prices but quite unrelated to (bad) forecasting.

Of course, even in a period of uncontrollable inflation, high rates and yields may be only partly the result of a sheer 'corned beef and cabbage' complex. We must remember, for example, that during the panic of such a period, with the increasing rapidity of circulation, commodity prices rise faster than the volume of the circulation and an intense money shortage therefore occurs. But, even with such refinements, it is not very difficult to understand why rates and yields should be high in such a period. If forecasting be assumed to occur, (Footnote 7s concluded)

made to signify, if (in spite of the results of our examination of the relative yields of serial bonds in the present century) we assumed that the relation between the yields of the two bonds was methodically considered, is that buyers and sellers felt that the paper yield of the bond with the shorter maturity should, for the period terminating March 31, 1875, be lower than the paper yield of the bond with the longer maturity for the period March 31, 1875 to December 31, 1880. But, in view of the bond with the longer maturity being a First mortgage bond and the bond with the shorter maturity only a Second mortgage bond, even this is curious enough.

both its direct and its indirect influences can be relatively easily analyzed.

But it is much more difficult to see why and how rates or yields should be affected by price levels or price changes during periods in which forecasting would seem to be a quite unimportant factor. The suggestion that, though there be periods in which conscious forecasting is negligible, there are no periods in which unconscious forecasting is unimportant, that when prices are rising the common though unconscious forecast is that they will continue to rise, is not as helpful as one might expect it to be. At best it offers an explanation of a usually non-existent condition. To the extent that the problem suggested by the statistics may be a real problem at all, it is why, in spite of numerous and glaring exceptions, rates to some extent and yields to a much greater extent are so often high when prices are high and low when prices are low or rise and fall with prices, not why they are high when prices are rising and low when prices are falling. And no questionbegging description of rates or yields as 'viscid' or 'sticky' is more enlightening than the old explanation that a body was hot because it contained much phlogiston. Even if such a physical analogy as the concept of 'stickiness' were thoroughly warranted, the question would still remain, why are rates and yields sticky?

If the movements of commodity prices ever affect the movements of interest rates and bond yields directly, in other words if the two series are ever, in the absence of conscious forecasting, more closely related to each other than as two aspects of some more fundamental condition, I suspect that the mere existence of long term debts (such as are represented by bonds), with rigid future interest obligations, is an extremely important factor in bringing about this result.

During a pronounced rise in commodity prices, though it may lead to an increased logarithmic 'scatter' among the prices, there is a pronounced tendency for the prices of nearly all things to rise. Though wages lag, even they eventually rise. But (aside from the resumption of payments on debts in default) interest payments on unmatured debts do not rise. Now this condition may possibly have an extremely important influence on rates and yields. After a rapid commodity price rise of one hundred per cent, the prices of the products of industry (except of those industries in which selling prices are determined by law) will, in general and as an average, have

doubled, but the burden of debt will remain virtually unchanged. Relatively to prices that burden will, therefore, have been halved. The market value of all plants (that do not have the prices of their products determined by law or custom) will, therefore, in general (ignoring depreciation and obsolescence) have at least doubled and that of going businesses more than doubled. The ability of business to borrow will be greatly increased—much more than doubled. And the urge to borrow will also be greatly increased; not merely because the volume of new loans necessary to continue the business at its old pace will have risen with the price level but also because the price rise will probably be associated with a rise in the prospects for profits and hence few businesses will be satisfied to continue operating at the old pace.

But there will be no corresponding increase in the ability and will-ingness to lend. Not merely will the bond income of existing bond holders remain unchanged but the prices of those things for which they used to spend that part of their income which they did not invest will have doubled. This great source of demand for new bonds will therefore, instead of increasing, actually decrease. Similarly with the (of course less important) demand for bonds from wage and salaried persons. Their incomes will not have kept pace with prices. There remains the great class of stockholders and business entrepreneurs. But the business entrepreneur will, during such a period, be expanding his business. And his silent partner, the stockholder, will tend indirectly to do likewise. An even larger percentage of his income than usual will go back into 'the market'. Either directly or indirectly, both the active and the silent partners will be increasing their borrowing more than their lending.

Moreover, as commodity prices rise and the burdensomeness of corporation debt declines, second and third grade bonds become first grade. The volume of bonds of the highest grade therefore increases even more rapidly than the increase that results merely from new issues. And it is the possible relation between commodity prices and the yields of these highest grade bonds that the hypothesis would attempt to explain.

But 'intriguing' as this all sounds, the hypothesis is almost as difficult to reconcile with parts of the record of actual rates and prices as are some of the theories upon which we have so adversely commented. If the long time major movements of prices and rates are ever causally related, the 'mere existence of long term debts' may, as I am inclined to suspect, be an extremely important factor—without being the only factor needed for a complete solution of the problem of why and how they are related. *Entia non sunt multiplicanda practer necessitam* rules only that causes are not to be multiplied beyond what is necessary.

CHAPTER VII

FACTUAL LEADS AND LAGS AND EMPIRICAL FORECASTING

The movements of the various individual series from 1856 to the present, and the similarities and dissimilarities of those movements are graphically presented in the charts scattered through this volume. The figures there depicted are presented in Appendix A. Better than in any mere text the reader will find in the tables, and especially in the charts, a clear picture of what has happened to short term interest rates, bond yields, stock and commodity prices and physical and monetary trade volumes in the United States during the last seventy-nine years.

The different trends are collected and presented in Chart 29. An examination of it and of the various charts on which data and trend curves appear together shows that the trends differ noticeably with respect not only to the rates of advance or decline but also to the possibility of their being adequately described by a mathematical equa-

tion representing a curve of clean-cut sweep.

Pig iron production and deflated bank clearings outside New York City suggest that their long movements could be represented by 'growth' curves of some kind or other;' railroad stock prices give a much less definite mathematical suggestion. The periods during which the line joining the data points does not intersect the trend line are much longer and the arrangement of its deviations around the trend line is much more irregular. Finally, in the collapse that began in 1929 those prices acted in such a manner as to suggest that they may never again even touch the old trend line. The trends of short term interest

¹ The mathematical equation used to describe the trend of pig iron production was fitted to the data fifteen or sixteen years ago. Upon taking up the series for the purposes of this book, we decided to use the curve already fitted, not only because it had remained so astonishingly good but also because of the interest attaching to it as an illustration of how growth curves seem sometimes to be more than mere fits to existing data.

rates, bond yields, and commodity prices are still less suggestive of any 'growth' or other simple mathematical curve. The trend lines were obtained by 'smoothing' and not by 'fitting', and the appearance of both the smoothings and the raw data suggests strongly that this was the only defensible procedure.

Chart 29 is presented to show the relations between the long term or 'trend' movements of the various series. It is composed of the various 'trend' graduations. The first thing that will strike the reader is, as we have said, that these lines do not appear to be true 'trends' at all. They do not have the single, simple sweep of such trend curves as are represented by the mathematical equations fitted to deflated bank clearings outside New York or to pig iron production. Each line, even those representing the deflated bank clearings and the pig iron series, shows more or less pronounced long term sinusoidal or wavelike movements. This is accounted for by the fact that, while the 'trend' graduation that we have used eliminates all the so-called ordinary 'business cycle'-ranging in length up to about four or four and a half years-it does not eliminate all the longer waves that appear in the data. The difficulty encountered in any such procedure as we have engaged in is to obtain a 'trend' line that will, as far as possible, show each 'cycle' as working definitely back and forth across such a line and, at the same time, eliminate as long cycles as possible. We may have erred in not choosing a formula that would have more of a dampening effect on the longer cycles-though such a formula has its own disadvantages. However, since we present the whole story not only graphically but also by means of tables, the reader may form his own opinion whether, in any particular instance, our conclusions might have been somewhat different if we had used a different 'trend' graduation. Call money, time money and commercial paper show the most pronounced of these long term wave movements-long term 'cycles' we might call them, if we did not wish to save that word for somewhat shorter movements. The amplitude of the long term wave movements becomes less as we pass from call money to rates on loans of longer duration, time money and commercial paper. In the bond yields line they almost disappear. That line is more like a typical 'trend'. The opposite movement in the trend lines for railroad stock prices and bank clearings in New York City from 1914 to about 1919 is rather striking, if we consider how closely the two curves move together

in other periods. The history of the railroads in that period was, of course, exceptional—as the chart indicates.

On examining Chart 21 the reader will notice that the 'cyclical' movements of the series have as marked peculiarities as their trends. The first difficulty he will encounter, although he is examining smooth curves and not raw data. is to decide what he should call a 'cycle'. He will soon see that it is not sufficient to define a cycle merely as a nortion of the curve that lies between two maxima (or minima). Not only will he note that maxima and minima may appear in a curve representing deviations from a trend when they do not appear in the original data but also he will begin to feel that the end points of a cycle are not necessarily either maxima or minima. In some instances the suggestion will be strong that, even though there be no maximum or minimum point, there is an end point that lies between two points of inflection. A point at which the second derivative is a maximum or minimum (the third derivative zero) often lies on a date that it would seem reasonable to take as a dividing line between two 'cycles'. Not only the appearance of the preceding and succeeding portions of the smooth curve itself but also the relation of the date to the dates of maxima or minima in other series may tend to confirm such a decision

However, the reader dare not allow any such mathematical considerations to outweigh his calm judgment concerning the type of 'cycle' he is interested in, or he may find himself with several 'cycles' each covering less than a twelve-month period. He must reject very short period cycles of negligible amplitude, especially if they occur between two points that are neither maxima nor minima even though their third derivatives equal zero. But he will find it very difficult, if not impossible, to formulate mathematical rules to guide him in the process of elimination.

The second difficulty he will encounter is closely related to the first. Even in the same series all 'cycles' are not equally clear cut, and even when equally clear cut, they are not equally important. The variation in amplitude between a cycle of pig iron production covering a period of world-wide industrial collapse and one that is revealed only through mathematical analysis may for most purposes be considered a difference in kind rather than merely in degree.

Finally, struggle as the observer may to decide what are the cycles

in his various series, he will find that some series undoubtedly have a larger number of definitely defined cycles than others. This is, of course, not surprising, though seldom recognized. Everyone knows that some economic series show pronounced seasonal cycles that are totally or almost totally lacking in others. And this brings up the subject of the attempts that have been made to discover mathematically regular 'business cycles'.

Virtually all 'cycle theorists' unconsciously assume that it is possible to discover the dates on which 'cycles' begin and end and also that, in any particular period, there are the same number of cycles for each

important economic series.

Nearly all the earlier and cruder efforts contained the further implicit assumption that there were no 'interferences' in the 'cyclical' movements. At any one time there was only one cycle. The picture was always that of a huge ground swell on a glassy sea rather than the choppy waves where two currents meet, or even the ordinary picture of small waves superimposed on larger ones.

The possibility that the amplitude of the cycles might vary was not discussed or even considered. Periodicity was the only concern of the writers. A ten-year cycle was a ten-year cycle if ten years intervened between two 'crises'. It mattered not whether, during the intervening years, there had occurred a boom that would go down in history, like the Mississippi Bubble, or merely such a negligible degree of prosperity that it was difficult to say when the terminating crisis began.

The proponents of rigid mathematical cycles early tended to base them on, or at least relate them to, astronomical periodicities. Two great astronomical cycles had been recognized before the dawn of history, indeed before the advent of man. The lives of even the lower animals were subject to the domination of day and night and the sequence of the seasons. It was almost inevitable that with the discovery of the 'sunspot' cycle, this longer solar cycle would soon be used by the economists. Its relation to terrestrial magnetism began to be investigated early in the nineteenth century; by the third quarter of that century 'sunspottery' was breaking out in economic circles. It was a period in which the cyclic idea was budding everywhere. The files of the English periodical *Nature* are full of suggestions; 7-day, 30-day weather cycles, 4-year, 8-year, 10-year, 16½-year, 19-year, 19-year,

21-year, 33-year, 35-year, and 400-year weather cycles were all to appear.

About 1862 Professor W. Stanley Jevons came to the conclusion that the dates of the preceding five English economic disturbances (1815, 1825, 1836–39, 1847 and 1857), which averaged 10.5 years apart and in each instance were extremely close to this normal interval, contained the clue to some mathematically exact nature cycle. His first attempts to correlate these figures with sunspot maxima and minima were disturbed by the fact that the sunspot cycle was at that time held to be about 11 years and not 10.5. When, however, Mr. J. A. Broun in 1877 came out with the statement that the true mean interval was 10.45 and not 11.1, Jevons' fate was sealed. He seized upon Broun's 10.45 figure with highly unscientific avidity and from that time (1877) became almost unbalanced in the ardor with which he fitted facts to his theory.

A couple of years previous, in 1875, he had examined and discussed the data in Thorold Rogers' History of Agriculture and Prices in England since 1259. He then believed, he tells us somewhat naively, that "he had discovered the solar period in the prices of corn and various agricultural commodities", and he accordingly read a paper to that effect at the British Association in Bristol. "Subsequent inquiry, however, seemed to show that periods of 3, 5, 7, 9 or even 13 years, would agree with Professor Thorold Rogers' data just as well as a period of eleven years," to quote Jevons' own words, and in disgust at this result he withdrew the paper from further publication.

J. A. Broun's 10.45 mean interval, however, prevented any such continued discouragement with the theory, as we witness in 1875. By November 1878 we have an article by Jevons in *Nature* (November 14, 1878, pp. 33–7) on Commercial Crises and Sun-spots, another article early in 1879 on the same subject, and in February 1879 we have a serious attempt at correlating *Sun-spots and Plague* which exhibits almost pitiably the extent to which Jevons was then outraging his own great intelligence.

An interesting feature of his article on Sun-spots and Plague is that Jevons suggests the correlation of plague and Asiatic famine. In view of this suggested correlation it is of some significance to note that in this article the incidence of plague (and hence of Asiatic famine) is

² 11.1 is closer to the modern figure than is 10.45.

supposed to coincide with sunspot maxima, whereas in his later articles on sunspots and commercial crises, commercial crises are synchronized with sunspot minima and at the same time with Asiatic famine.

In general, Jevons compared imagined or real crises not with sunspot maxima or minima but with dates, when, under Broun's discredited average, sunspot maxima or minima should have occurredbut did not-and this in the face of the fact that he had access to the data of actual observations tabulated by Wolf. Taking Jevons' own list of crises in order and comparing them with the closely-known epochs of maximum and minimum sunspot frequency, we obtain the following results: The doubtful (we should say 'assumed') crisis of 1701 followed a spot minimum by three years and preceded a maximum by four and one-half; the crisis of 1711 (predicated by Jevons merely because the South Sea Company had been founded in that year) followed a minimum by five and one-half years and preceded a maximum by one year; the South Sea Bubble of 1720 (Jevons places the date at 1721) followed a maximum by one and one-half years and preceded a minimum by three and one-half; the imagined crisis of 1731–32 preceded a minimum by two years; 1742 (no crisis known) preceded a minimum by three years (the joker here is that 1745 was a year of both minimum sunspots and panic—December 6, 1745, when there was a run upon the Bank of England due to fear engendered by the progress of the army of the Young Pretender-but Jevons refuses to notice this because he refused to accept Wolf's sunspot figures, seemingly because they did not check with his preconceived ideas); 1752 (no crisis) followed a maximum by two years and preceded a minimum by three; 1763 came exactly half way between a maximum and a minimum; 1772 came two and one-half years after a maximum and three and one-half years before a minimum; 1783 preceded a maximum by two years; 1793 came just half way between a maximum and a minimum; 1804-05 (no known crisis) coincided with a maximum (not a minimum); 1815 preceded a maximum by one and one-half years; 1836-39 included the year 1837 of maximum solar activity, that being also a year of panic in the United States); 1857 followed a minimum by one year; 1866 preceded a minimum by one year; 1878 was a minimum sunspot year. The dates of later crises reveal similar lack of agreement with the sunspot cycle.

The nadir of sunspottery was soon reached. In an article in the

May 1872 issue of Nature we find a certain B. C. Jenkins stating that "cholera epidemics have a period equal to a period and a half of sun-spots"! Henry Jeula in 1877 made a careful and laborious attempt to correlate sunspots and the number of wrecks posted each year in Lloyd's loss book-(based upon the assumed correlation of sunspots and East Indian hurricanes). By March 1879 he came to his senses, however, and in the Journal of the London Statistical Society of that date we have an oasis in the desert of nonsense that was being written by unscientific 'country gentlemen'. He made a most brilliant success of correlating Oxford-Cambridge boat races and sunspot maxima and minima. To quote from his article: "A cycle is believed to consist, as nearly as can at present be ascertained, of about eleven years, of which the 1st, 2d, 10th, and 11th form the minimum sunspot group, the 3d, 4th, 8th, and 9th the intermediate groups; and the 5th, 6th and 7th the maximum group. Of 12 races rowed in the minimum group, Oxford won 66 per cent; of 10 races rowed in the maximum group, Cambridge won 60 per cent; while of 16 races rowed in the intermediate sun-spot group of years, each university won exactly half."

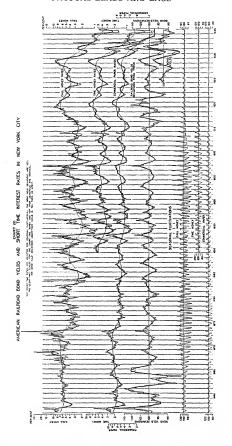
Modern cycle theory has availed itself of the mathematical apparatus of harmonic analysis. The flexibility of a Fourier series is as great as that of a power curve or higher parabola but, unless the essential nature of the data is periodic as is the case with such physical phenomena as heat, light, sound and electricity, the resulting mathematical descriptions or 'fits' are purely empirical. It is extremely easy to describe almost any time series by means of a set of superimposed sine curves of different periods and amplitudes but it is quite another matter to be able to describe data (whether future or not) that were not used in obtaining the constants. What shall we say of a mathematical 'law' that by its nature can be used to describe only those observations from which it was itself derived?

The mathematically exact economic cycles presented—before the onset of the depression of the 1930's—by some modern economists and accepted by many modern business men merit little if any more favorable consideration than we have given to the pronunciamentos of Jevons. We intend to save space and preserve friends by not discussing them. In the charts of this book the reader has before him abundant material to come to a conclusion about any of them—if he

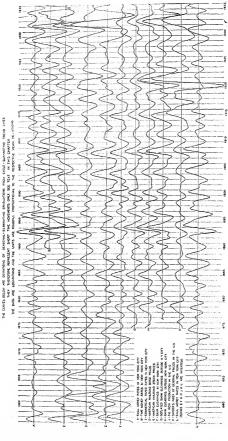
does not do what Jevons and so many of his modern representatives tend to do, call a rain storm a flood if by so doing it will seem easier to float a theory.

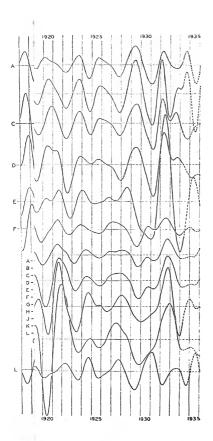
While but few economists believe that business prosperity comes and goes like day and night, or even rises and falls with the regularity of the tides—complicated as are the mathematics involved in lunar theory—there are probably even fewer who believe that either prosperity or depression is an accident that befalls the body politic. Dr. Mitchell's theory that the essence of 'business cycles' is to be found in the fact that the conditions attendant on each phase of the 'cycle' tend to bring on, sooner or later, the next phase has become almost universally accepted. That theory is sharply separated from the mathematically exact cycle theories by its emphasis on the indefiniteness of the timing, and from the accident theories by its emphasis on internal causation.

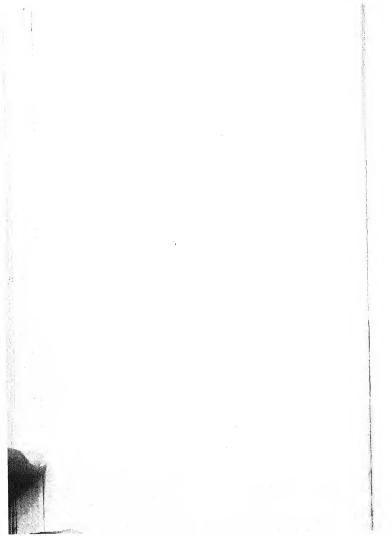
And this internal causation tends to show itself in leads and lags among important economic series. But the reader must not expect always to find a high degree of regularity in the relations among the various series or he will be badly disappointed. The uniformity is often rather specious. It sometimes amounts almost to an optical illusion. The general rule is that there is no rule. In all cases (aside from such essentially similar data as the various short term money series) irregularity is an outstanding characteristic. Often it is the outstanding characteristic. While a cursory examination of such a chart as number 21 might give the impression of extreme regularity in the sequences of and relations among the various series, more careful study will disclose a high degree of irregularity. For example, if the series should be thought of as having typical time lags, it is extremely difficult to say what they are. Sometimes a maximum or minimum sweeps across the chart in a startling manner, the various lags being clear cut and unmistakable. On the other hand, the entire picture is often quite obscure. Arithmetic averages of the amounts of lag are very treacherous. The inclusion of a single doubtful case may appreciably affect the result. Medians might be thought to be more suitable than arithmetic averages in such a case, but the essential feature of the data is that any type of average will involve making some questionable decisions. Moreover, the 'scatter' around the average-the 'deviations' from the average or typical lag-are extremely large in all



CYCLICAL MOVEMENTS OF INTEREST RATES AND OTHER ECONOMIC SERIES 78 times ratio and or session-terminal qualitation from critic all manifesting ratios.







but closely related series. Any great degree of confidence in the 'accuracy' of any averages is entirely unwarranted. They may well be more misleading than enlightening.

Even series A, C, D and E (of Chart 21),3 which are quite closely related, show many startling irregularities, as the reader may see if he will check up the following 'average' lags with individual instances. The average lags in these four series run roughly 5 as follows. A high in call money rates precedes a high in commercial paper rates by about 2 months, a high in railroad bond yields by about 4 months and a low 6 in railroad stock prices by about 5 months. A high in commercial paper rates precedes a high in bond yields by about 2 months and a low in stock prices by about 3 months. A high in bond yields precedes a low in railroad stock prices by about 1 month. The lows do not show the same set of lags. A low in call money rates precedes a low in commercial paper rates by about 2 months, but a low in bond yields by about 6 months and a high in stock prices by about 9 months. A low in commercial paper rates precedes a low in bond yields by about 4 months and a high in railroad stock prices by about 7 months. A low in bond yields precedes a high in stock prices by about 3 months.

The characteristics of the various lags are clear on Chart 21, which presents the cyclical movements of ten of the most important series presented in this book:

- A Call money rates, January 1857 to January 1936
- B Time money rates, January 1890 to January 1936
- C Commercial paper rates, January 1857 to January 1936
- D Railroad bond yields ('lowered' index), January 1857 to January 1936
- E Railroad stock prices, January 1857 to January 1936
- F Bank clearings in New York City, January 1857 to January 1936
- G Deflated bank clearings outside New York City, January 1875 to January 1936
- $^{\mathtt{s}}$ Series B—time money rates—is here omitted because it has been used only as far back as January 1890.
- 4 The condition is only slightly improved if the long period from January 1857 to January 1936 be broken up into shorter periods. Moreover, where improvement is possible it is often artificial and unreal—resulting from fitting to too few cases.
- 5 Greater 'accuracy' than here presented is merely misleading.
- ⁶ On the chart, series E is inverted. We are discussing it as though it were not inverted.

- H Bank clearings outside New York City, January 1875 to January 1936
- I Pig iron production in the United States, January 1877 to January 1936
- J Carl Snyder's index of general prices, January 1875 to January 1936
- K Call money rates, January 1857 to January 1936

Series E to K inclusive are inverted on the chart. The relations among the various series stand out sharply. Indeed, the reader may, as we have already said, easily be tempted to believe the regularity of movements and sequences greater than it really is. While the first three series (call money, time money and commercial paper rates) are very closely related, even here the lags are less uniform than a cursory inspection of the chart might lead one to suppose. For example, while commercial paper maxima on the graduations tend to occur about two months later than call money maxima, the range is all the way from two months earlier to ten months later. Similarly, while the commercial paper minima tend to occur about two months later than the call money minima, the range is from two months earlier to eight months later. A similar analysis of series that are less closely related shows even less regularity of movements and lags. The technical reasons for this condition are traceable not merely to the fact that the amounts of lag between definite maxima or minima, which on the chart appear unmistakably related, vary considerably, but also to the fact that it often is rather difficult to say just which maxima or minima should be considered together. The actual number of maxima or minima is not the same for each series. Call money rates have more maxima and minima, and hence more 'cycles', than railroad bond yields. Sometimes we have no actual maximum or minimum but do have a distinct pair of 'points of inflexion'. Shall these be used as though they contained a maximum or minimum point (we have not done so), and if so, what procedure should be followed to date such a point? Sometimes a maximum or minimum that appears distinctly on one series appears on another series as only a 'bulge' between two points of inflexion. In still other series it may not appear at all. For example, the minor maximum in call money rates in 1901 is suggested in time money. absent in commercial paper and railroad bond yields, suggested in railroad stock prices, clear cut in New York bank clearings, absent in deflated bank clearings outside New York, suggested in undeflated bank clearings outside New York, present in pig iron production and clear cut in Snyder's index of general prices. The reader can easily spot similar and even more startling irregularities. Interesting and instructive as Chart 21 may be, to discuss its mere graphic peculiarities in any lengthy manner seems unnecessary. It speaks for itself.

However, there is one series whose order in the chart may disturb the reader—bank clearings in New York City. In general the order of movement of the series, as presented in the chart, is:

- (1) Short time interest rates decline.
- (2) Long time interest rates decline.
- (3) Stock prices advance.
- (4) Physical volume of business advances.
- (5) Monetary volume of business advances.
- (6) Commodity prices advance.
- (7) Short time interest rates advance, etc.

Now bank clearings in New York City move earlier than the physical volume of business as represented by such series as deflated bank clearings outside New York City or pig iron production. The reason for this condition may be found in the fact that such a large percentage of the New York clearings are of a financial origin—tied up with groups 1, 2 and 3 above. The volume-of-business series that contain the price element move later than truly corresponding series that do not contain it. This is illustrated by bank clearings outside New York City—deflated and undeflated. Finally, we must remember that all the sequences may be reversed. This is illustrated by call money which is presented as the top of the chart and also as the bottom line—in the latter case inverted.

The reader who wishes to examine the actual series rather than the graduations may do so in other charts and in the tables in Appendix A. After all is said and done, the graduations are intended merely to make the interpretation of the series easier, not to replace them. The

7 At the end of 1901.

⁸ Our method of deciding which sequence was best for graphic presentation has already been described. It was based on the two considerations of length of lag and contour of the graphs. Similarity of contour would suggest that the sequence was more important when so lagged than when lagged in an opposite sense.

raw data for the first three graduations of Chart 21 (call money, time money and commercial paper) may be examined in Chart 20. On that chart are presented the raw data (after adjustment for seasonal fluctuation), and 'cyclical' and 'trend' graduations; also the deviations of the data and of the 'cyclical' graduation of bond yields from the 'trend' graduation of the same series. The seasonal fluctuations of the three short term rates are presented at the bottom of the chart.⁹

The raw data for the fourth and the fifth graduations presented in Chart 21 (railroad bond yields and railroad stock prices) are presented in Chart 14, which gives, for each series, the raw data and the 'cyclical' graduation. The figures are given in Appendix A, Table 10. Columns 5 and 6.

The raw data for the fourth, sixth, seventh, eighth and ninth graduations of Chart 21 (railroad bond yields, bank clearings in New York City, deflated bank clearings outside New York City, undeflated bank clearings outside New York City, and pig iron production) are presented in Charts 22, 23 and 24.10 Chart 23 gives each of these series in the form of the data and their 'cyclical' graduation. Mathematical curves fitted to deflated bank clearings outside New York City and pig iron production are given to illustrate how well the 'trends' of such series may be represented by ordinary mathematical equations (see Chart 22 and Chart 23). Chart 24 presents (for deflated bank clearings outside New York and pig iron production) the deviations of the data and of the 'cyclical' graduations from such fitted mathematical curves. This chart also presents railroad bond yields in the form of (1) the raw data, (2) the 'cyclical' graduation, (3) the 'trend' graduation, (4) the deviations of raw data and of the 'cyclical' graduation, from the 'trend' graduation. The reader will find it interesting and instructive to compare the deviations of deflated bank clear-

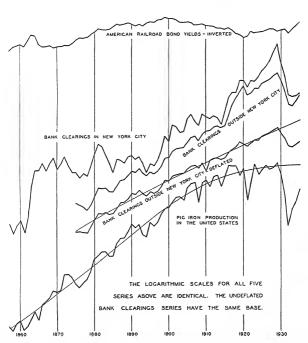
The figures for call money, time money and commercial paper rates, unadjusted for seasonal fluctuations, are given in Table 10 in Appendix A. Graduations and seasonals for these series are presented in Tables 21, 22 and 23.

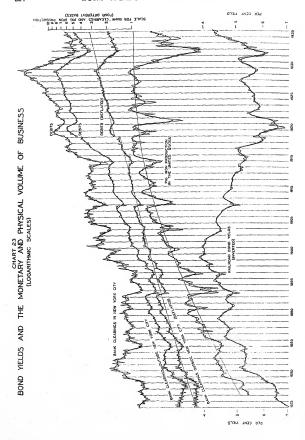
¹⁰ The figures for bank clearings in New York City, deflated bank clearings outside New York City, (undeflated) bank clearings outside New York City, pig iron production and wholesale prices, unadjusted for seasonal fluctations, are given in Appendix A, Table 27. The graduations and seasonals of these series are presented in Appendix A as follows: bank clearings in New York City, Table 28; (undeflated) bank clearings outside New York City, Table 29; deflated bank clearings outside New York City, Table 30; pig iron production, Table 31; wholesale prices, Table 32.

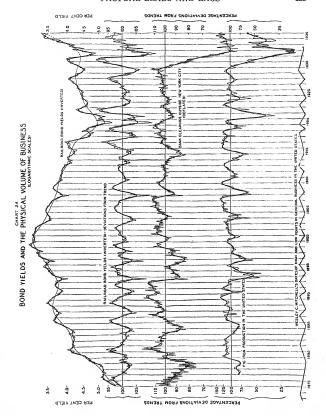
ings outside New York and of pig iron production from the fitted mathematical curves with the deviations of the same series from the 'trend graduations' (presented in Chart 21).

The raw data for Mr. Carl Snyder's index of general prices—the tenth graduation of Chart 21—are not shown on any chart presented in this book. The figures are given in Appendix A, Table 27. Monthly data (January 1890 to January 1936) for the United States

BOND YIELDS AND THE VOLUME OF BUSINESS

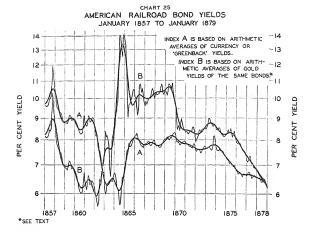






Bureau of Labor Statistics index of the price of commodities at wholesale are compared with bond yields in Chart 18—the data and the 'cyclical' graduation being given for each series.

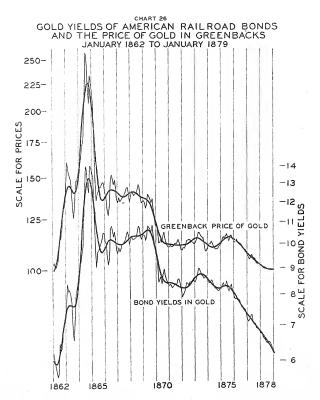
The reader who is interested in the distortions that are introduced



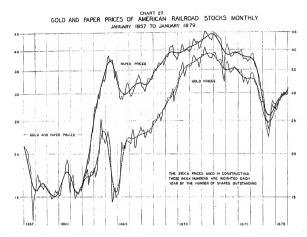
into some of the series by the paper inflation of 1862 to 1879 may examine Charts 25, 26, 27 and 28. An examination of these charts, together with the charts showing purely 'paper' data, will also illustrate how deceptive mere graphic appearances of lead and lag or correlation in general may sometimes be.

Such is the thorny path that must be trod by the professional 'forecaster'. He cannot operate on what the sequences and lags should be; he must operate on what they actually are—indefinite as a statement of that condition may be. He is interested in noting that a rise in short term interest rates or commodity prices so often precedes a rise in bond yields. He is very unlikely to be interested in hearing that if the future of short term interest rates or commodity prices were definitely known, the sequences might be different. However, such

knowledge might well be of some use to him. It would be well if he always remembered that the various sequences are as they are largely because of the inadequacies of human intelligence rather than because of its triumphs. For example, in a period when general forecasting



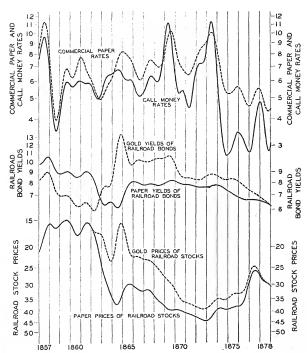
happens to be unexpectedly good the usual sequences will tend to be less rather than more reliable as indicators of the future. Economic forecasting that is based on 'leads' and 'lags' is almost necessarily extremely dangerous—though it often is almost the only way to handle



the problem. In attempting to forecast such a series as stock prices the professional 'forecaster' commonly assumes the continuation of illogical relations between it and certain other series, and attempts to predict the future of the latter—although if their future were really known the existing illogical relations would not continue. The forecasting of the future of the 'other' series is very often attempted by means of implicit assumptions concerning the timing of a reversal in their cyclical movements, the timing of this reversal being itself dependent on assumptions concerning regularity of amplitude in the 'swing' of these 'other' series. In such methods an extremely bad condition is assumed to be a good sign, and vice versa. The injunction to 'buy stocks when the percentage of pig iron furnaces in blast falls below sixty'—not when the percentage is more than sixty but when

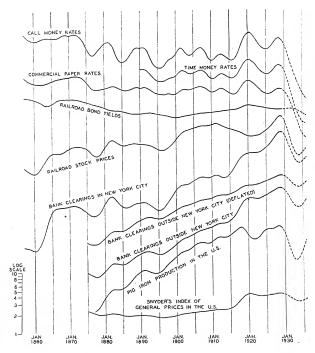
INTEREST RATES AND SECURITY PRICES IN THE UNITED STATES JANUARY 1857 TO JANUARY 1879

(IDENTICAL LOGARITHMIC SCALES)



LONG TIME MOVEMENTS OF THE VARIOUS SERIES
AS SHOWN BY CYCLE-ELIMINATING TREND LINES





it is *less*—involves the assumption that when the iron industry reaches a specified degree of *badness*, the outlook for general business (including the iron industry, of course) is, or at least in the near future will be, good. Other indices of the activity of business are used in a similar manner. When business is sufficiently bad, buy stocks; when it is sufficiently good, sell them. Even instructions such as 'sell stocks when commercial paper rates rise to 4½ per cent', or 'sell stocks when commercial paper rates have risen 1¼ per cent', are not given primarily because of any belief that such conditions will *cause* a decline in business but simply because such a movement of rates is considered a symptom—a good indication—that business has advanced far enough to be approaching the region of reversal. The chief proponent of the 1¼ per cent rise rule adds 'when business activity is increasing'.

However, the study of relations among economic series is at least more promising than the attempt to develop rigid cyclical formulas on the basis of one or more individual series. The 'lags' of the various series are less irregular than their cycle lengths though even here we find anything but mathematical regularity. The irregularities seem traceable to two causes. In the first place the relationship between any two series is seldom self-contained. Movements of pig iron production are not determined by movements of general commodity prices alone. In the second place, in so far as logical relations should exist, as between long and short term interest rates, the logical adjustment of the one series to the other so often requires more than a mere knowledge of the past and present. Logically, as we have shown, long term interest rates should be adjusted to future short term rates. But this is quite impossible not only because the future is not known but also because, in the stress of deflation, it could not be acted on if it were known 11

Few economic series are like long and short term interest rates, which logically would depend on one another alone, unaffected by what happens to all other series. The reason in this case is, as we have ¹¹ This would not be strictly true in a hypothetical society where all was known. In such a society 'deflation' would not occur. However, this merely illustrates that the economic cycle is a phenomenon of a society in which all is not known. Of course, the hypothesis of a society where 'all is known' becomes a metaphysical concept hardly to be distinguished from the nineteenth century mechanistic philosophy which would suggest that if, at the birth of Christ, the exact position and motion of every atom in the universe were known to a sufficiently skillful mathematician, he could have stated that beer would come back to America in April 1933.

seen in Chapter II, that logically they are the same thing. The relation would be what the logicians term an 'essential' relation. Long term interest rates would be absolutely rigidly related to short term rates because they would be an average of a particular form of future short term rates. They would be related to short term rates in much the same manner as an index number of commodity prices is related to the prices of the individual commodities.

To the extent that adjustment requires a knowledge of the future, economic relations tend to depart from what they logically would be. 'Present' adjustments, such as those concerned with the making in a market of a price for a perishable consumers' good, may approach a rational norm similar to that presented by the more rigid and arithmetic of the members of the Austrian school, for example, Philip H. Wicksteed, but adjustments involving forecasts of the future cannot do so.

In our discussion of the relation of bond yields to short term interest rates and to commodity prices we drew attention to the inadequacy of adjustments requiring knowledge of the future. The relation of bond yields to the general level of profits and to changes in the monetary and physical volume of business-the 'other' series that we present and discuss in this volume—is of a similar type. To be at all adequate as an adjustment, the relation would necessitate a complete knowledge of all the relevant future. Indeed knowledge of the future is, in each of these relations, the fundamental requirement. In the case of business profits this is immediately apparent. After correction for the element of risk, future profits (if they could be adequately forecast) would be a factor to which bond yields would have to adjust themselves. Fluctuations in the monetary volume of business do not appear to be so directly related to bond yields unless we remember their usual close relation to profits. Periods of high volume (physical or monetary) of production are usually periods of high rates of profit. Enforced liquidation may cause a sudden spurt in the monetary volume of trade and even stimulate production, undertaken to convert inventories into more salable products, but spurts due to enforced liquidation seldom last long. In general, both the physical and monetary volume of business is large when an increased demand has brought

about an increased output, then a rise in prices followed by a further increase in output. Usually the price rise remains or even continues

while the output is increasing. An increased physical volume without any increase in the monetary volume can occur only when prices have been falling. This would be most likely to occur in the very early stages of a revival. However, the increased physical volume could not be great or it would lead to an increased monetary volume. Absolute figures (not deviations from trends) of monetary volume would, of course, be more closely related to monetary profit levels than would absolute figures of physical volume.

The relations of the larger deviations from long term trends (so-called cycles) would, under a condition of complete and adequate adjustment (on the assumption of complete knowledge of the future), be of almost the same kind as if there were no trends, because, if one series were adjusted to future values of the other, this adjustment could be broken down into two components: one an adjustment to the future trend and the other an adjustment to the 'cycles', or better say, the major deviations from the trends. Now the adjustment to the future trend would tend to have the same sort of long term 'sweep' that all trends have. Because the trend of the independent variable is a trend—in other words, changes its level and direction only very slowly—the dependent variable will do likewise. On the other hand, of course, when the theoretical adjustment is such that the dependent variable is merely a first derived function of the independent variable as it would be if call money were absolutely determined by the monetary rate of change in commodity prices—the curve tracing the course of the dependent variable would not have the clear-cut 'trend' characteristics of the independent variable. However, not only would we not expect—even under the hypothesis of complete knowledge of the future—call money to be related to commodity price movements in this manner, but even if it were, the movements of time money, and still more those of long term bond yields, would, so far as they were dependent on the trend of commodity prices, have themselves almost as much of the 'sweep' and 'trend' characteristics as would the commodity prices. If the duration of a bond were long enough, the 'trend' of the yield would, under the assumption of complete adjustment to the future trend of commodity prices, show an even more pronounced 'sweep' than the commodity price trend itself.

But, leaving these discussions of how things would occur if the future were known and if that knowledge were rationally used, we

must emphasize that all the relations among the various series tend to be of the same illogical, or at least non-logical, nature we have already found to exist in the actual relations between bond yields and short term interest rates and commodity prices. Moreover, as we have attempted to explain in Chapter I, the relations are not uniform, for they are always affected more or less by good or bad forecasting. They are a composite of the results of past and present facts, and forecasts of the future. Because the forecasts vary with respect to not only their goodness but also the importance of their effect as compared with past and present facts, the series show only a very moderate degree of uniformity in their relations from year to year and from decade to decade. In a period of prosperity the influence of forecasting (of further prosperity or even of a termination of prosperity) is more important as compared with the influence on past or present facts than in a period of depression or crisis. As we have already noted, when selling is 'forced' the element of forecast becomes quite negligible.

With the growth of knowledge the accuracy of forecasting will increase but this can bring about a pronounced decrease in the violence of economic disturbances only if it entails something more than mere 'speculative' forecasting. It must lead to a change in those present conditions that tend to produce untoward future results. In a period of over-rapid credit expansion it is not enough to foresee that when such expansion can go no further a collapse of prices will begin. It is not sufficient to sell securities and commodities or even sell them short in preparation for such a collapse. It is necessary to check the credit expansion. We must make the future and not merely foresee it. And that can be done only in the present. Mere knowledge is not sufficient. It can never be complete and it will always be human nature to gamble on whether if one buys at an inflated level he will be able to find a bigger fool than himself to buy from him at a still higher level. The primary reason for the variableness of the economic future to which man must adjust himself lies in man himself. Without knowing what the future effects of his present acts will be, and often apparently caring less, he proceeds to make a future to which he will find he cannot adjust himself.

It would, of course, be absurd for the *individual* speculator or entrepreneur to base his business operations naively and completely on an

attempted analysis of how the social present *should* be adjusted to the social future. If we have demonstrated anything in this book, it is that economic phenomena are, in fact, only accidentally so related. But it is strange indeed that economic theorists should so seldom have hinted at, let alone analyzed, the *social* import of the opposition of the logical and actual sequences. That present conditions, if they are not to contain the seeds of future disturbance, must be adjusted to future conditions would seem plain and obvious. But perhaps it is too plain. The very insolence of the obvious can easily prevent its being noticed. And, even if noticed, its significance can all too easily be missed.



TABLES

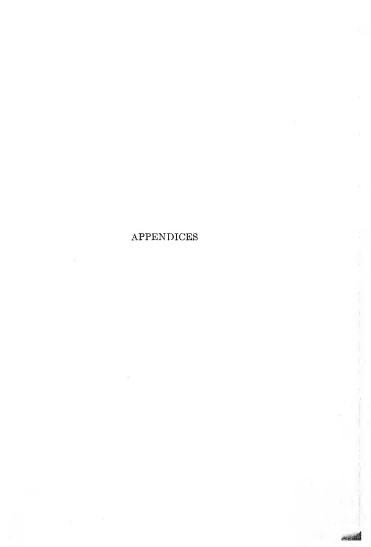
1	Identification Table of American Railroad Bonds	A5
2	Paper Prices of American Railroad Bonds, Monthly, January	
	1857-January 1879	A21
3	Yields of American Railroad Bonds, Monthly, January 1857-	
	January 1936	A33
4	American Railroad Bond Yields, January Index Numbers	A108
5	American Railroad Bond Yields, Six Index Numbers of Best 5	
	and Worst 5 Bonds	A110
6	Index Numbers of the Yields of American Railroad Bonds	
	Based on Sigma Equations	A113
7	American Railroad Bond Yields, Mathematical Functions and	
	Equations; Januaries 1857–1936	A131
8	Same, Quarterly	A134
9	Month to Month Slopes of 'Sigma Lines' Fitted to the Loga-	
	rithms of the Yields of American Railroad Bonds from January	
	1879 to January 1936	A139
10	Short Time Interest Rates, Bond Yields and Stock Prices	A141
11	An Adjusted Arithmetic Index Number of the Yields of Ameri-	
	can Railroad Bonds, Monthly, January 1857-January 1936	A162
12	New England Municipal Bond Yields, January Index Numbers	A172
13	New England Municipal Bond Yields, Arithmetic Average	
	Quarterly Index Number, January 1857-January 1914	A174
14	Railroad Common Stock Price Relatives, January 1857-Janu-	
	ary 1936	A181
15	Railroad Common Stock Weights, January 1857-January 1936	A193
16	Four Index Numbers of the January Prices of American Rail-	
	road Common Stocks	A204
17	An Arithmetic Average Index Number of the Prices of Ameri-	
	can Railroad Common Stocks, Weighted According to the	
	Number of Shares of Each Company Outstanding at the	
	Beginning of Each Year, Monthly, January 1857-January 1936	A206

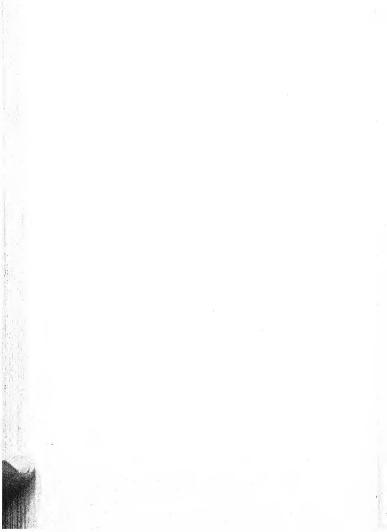
200	DOTTO TILLEDO TITEDO TORRES	
18 19	Price of Gold in Greenbacks, January 1862–December 1878 An Unadjusted Arithmetic Average Index Number of the Yields in Gold of American Railroad Bonds, Monthly, January	A21.
	1857-January 1879	A216
20	An Index Number of the Gold Prices of American Railroad Common Stocks, January 1862–December 1878	A219
21	Call Money Rates at the New York Stock Exchange, Monthly, January 1857–January 1936	A222
22	90-Day Time Money Rates in New York City, Monthly, January 1890-January 1936	A231
23	Commercial Paper Rates in New York City, Monthly, January	A237
24	1857-January 1936 Commercial Paper Rates in Boston, Monthly, 1831-1860	
25	(Martin) Commercial Paper Rates in Boston, Monthly, 1831–1860	A246
26	(Bigelow) Average Monthly Rates on 90-Day Prime Bankers' Accept-	A248
20	ances, January 1918–December 1935	A251
27 28	Bank Clearings, Pig Iron Production and Wholesale Prices Daily Average Bank Clearings in New York City, Monthly, January 1857–January 1919; Daily Average Bank Debits in	A252
29	New York City, Monthly, January 1919–January 1936 Daily Average Bank Clearings Outside New York City, Monthly, January 1875–January 1919; Daily Average Bank Debits for 140 Outside Cities, Monthly, January 1919–January	A271
	ary 1936	A281
30	Deflated Bank Clearings Outside New York City, Monthly, January 1875–January 1919; Deflated Bank Debits for 140	
31	Outside Cities, Monthly, January 1919–January 1936 Daily Average Pig Iron Production in the United States,	Λ289
22	Monthly, January 1877–January 1936	A297
32	United States Bureau of Labor Statistics Index Number of Wholesale Prices of Commodities, Monthly, January 1890-	1.204
33	January 1936 Dr. Wesley C. Mitchell's Dates of High and Low Points in	A304
	General Business in the United States	A308

CHARTS

1	American Railroad Bond Yields, Index Numbers for Each	
	January, April, July, and October, 1857-1936	91
2	Four Index Numbers of the Yields of American Railroad	
	Bonds, January 1857-January 1936	93
3	Four Index Numbers of the January Yields of American Rail-	
	road Bonds, Each January, 1857-1936	95
4	Four Index Numbers of the January Yields of American Rail-	
	road Bonds, the 4.50 Sigma and Three Index Numbers Based	
	on Averages of the Five Bonds Having the Highest Yields	
	Each January, 1857-1936	96
5	American Railroad Bond Yields, Scatter Diagrams of Three	
	Identical Groups of 41 Bonds	102
б	American Railroad Bond Yields, Scatter Diagrams, January	
	1857-January 1936	104
7	New England Municipal Bond Yields and American Railroad	
	Bond Yields, Index Numbers for Each January, April, July,	
	and October, 1857-1914	118
8	The January 1903 and January 1904 Yields of Bonds and Pre-	
	ferred Stocks on the New York Stock Exchange	124
9	American Railroad and Public Utility Bond Yield Scatter	
	Diagram	125
10	American Municipal and Railroad Bond Yields, January 1900-	
	January 1936	126
11.	Different 'Drifts' Shown by Index Numbers of Public Utility	
	Bond Yields, Railroad Bond Yields, and Municipal Bond	
	Yields	127
12	Frequency Distributions of Railroad Stock Price Relatives	140
13	Four Index Numbers of the Prices of American Railroad	
	Stocks, January Each Year, 1857–1936	149
14	American Railroad Stock Prices and American Railroad Bond	
	Yields, January 1857-January 1936	155

15	American Railroad Stock Prices and a Cumulated Product of the Slopes of the 'Sigma' Lines Fitted to the Yields of American	
16	Railroad Bonds	160
16	British and American Bond Yields and Commodity Prices, Annually	165
17	American Railroad Bond Yields and Commodity Prices, a Scatter Diagram	175
18	American Bond Yields and Commodity Prices, Monthly, January 1890-January 1936	178
19	British Consols and Commodity Prices, Monthly, January	
20	1890-January 1936 American Railroad Bond Yields and Short Time Interest Rates	181
21	in New York City, January 1857–January 1936 Cyclical Movements of Interest Rates and Other Economic	217
22	Series Bond Yields and the Volume of Business, 1857-1935—Long	218
	Time Trends	223
23	Bond Yields and the Monetary and Physical Volume of Business, January 1875-January 1936	224
24	Bond Yields and the Physical Volume of Business, January 1875-January 1936	225
25	American Railroad Bonds, Gold and Currency Yields, January	
26	1857-January 1879 Gold Yields of American Railroad Paper Bonds and the Price	226
27	of Gold in Greenbacks, January 1862–January 1879 Gold and Paper Prices of American Railroad Stocks, January	227
28	1857-January 1879 Interest Rates and Security Prices in the United States, January	228
	1857-January 1879	229
29	Long Time Movements of the Various Series as Shown by Cycle-Eliminating Trend Lines	230
30	American Railroad Bonds Used in Constructing Index Numbers and the Periods During Which Quotations Were Used	A17
31	New England States, Counties and Cities Whose Bonds Were	7117
	Used in Constructing Index Numbers and the Periods During Which Quotations Were Used	A171
32	American Railroads: the Periods During Which Their Common Stock Prices Were Used in Constructing Index Numbers	A178
	mon brock rivers were obed in constructing index reminers	211/0





APPENDIX A

The figures for the cyclical and cycle-eliminating curves and other mathematical material presented in Appendix A are, in most instances, given to at least one more decimal place than are the original data on which they are based.

In some of the mathematical material (such as the sigma equations of Tables 7 and 8 and the sigma 'slopes' of Table 9) extra decimals are given because cumulative multiplication was one of the purposes for which the material was calculated and, with such cumulation, if the number of decimals be too small, accuracy decreases rapidly. But the primary defense of such a procedure as calculating and printing one more decimal in a graduation (and in the deviations of the data from that graduation) than occur in the original data is that some readers may be interested in the graduation from a purely mathematical standpoint. While the economist might ask (particularly as to deviations) why more decimals were included than are warranted by the accuracy of the data and the adequacy of the graduation formula, the student of graduation ber se might as reasonably inquire why the extra decimal was dropped. He might well be primarily interested in studying the significance and mathematical peculiarities of the results obtained by using the formula; and, for most phases of such a study, the complete accuracy and even representativeness of the data would be assumed-if not considered irrelevant. For most of his analytic problems, the data are mere mathematical premises and not economic observations.

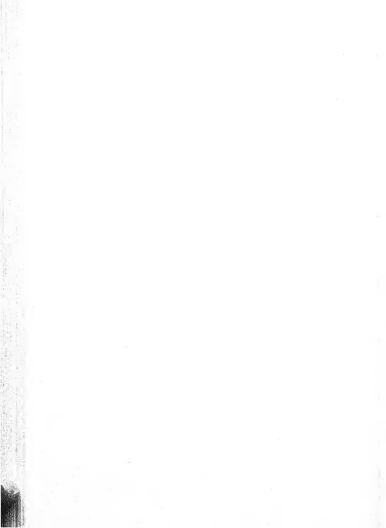


TABLE 1

IDENTIFICATION TABLE OF AMERICAN RAILROAD BONDS

This is a table to be used with Tables 2 and 3. Table 3 contains the identification numbers of Table 1, and also an abbreviated descrip-

tion. In Table 2 identification numbers only are given.

Table 1 consists of the exact name of each bond and information concerning security, medium of payment (gold or currency), date of issue, date of maturity, amount and dates of interest payments, whether bond is registered or coupon, and convertible or callable features.

(All bonds are coupon bonds unless designated registered)

Hudson River Railroad 1st mortgage 7s currency.

Dated Feb 1, 1849; due Feb 1, 1869. Interest paid Feb 1 & Aug 1. Registered.

Chicago and Rock Island Railroad 1st mortgage 7s currency Dated July 10, 1850; due July 10, 1870.

Interest paid Jan 10 & July 10.

Convertible into common stock of Chicago and Rock Island Railroad at par on any interest date on or before the 10th of July, 1858.

3. Lehigh Coal and Navigation Company general mortgage and deed of trust 6s currency.

Dated Mar 7, 1842; due Mar 1, 1870. Interest paid quarterly Jan 1, Apr 1, July 1 & Oct 1.

Philadelphia and Reading Railroad 2nd mortgage 6s currency 4. Dated Apr 1, 1849; due Apr 1, 1870. Interest paid Apr 1 & Oct 1.

5. New York and Harlem Railroad 1st mortgage 7s currency. Dated May 1, 1853; due May 1, 1873. Interest paid May 1 & Nov 1.

Lehigh Valley Railroad 1st mortgage 6s currency. Dated May 1, 1853; due May 1, 1873.

Interest paid May 1 & Nov 1.

7. Morris Canal and Banking Company 1st mortgage 6s currency. Dated Oct 1, 1856; due April 1, 1876. Interest paid Apr 1 & Oct 1.

Eastern Railroad (Massachusetts) 6s currency. 8.

Dated Aug 1, 1854; due Aug 1, 1874.

Interest paid Feb 1 & Aug 1.

9. Pennsylvania Railroad 2nd mortgage dollar bonds 6s currency. Dated June 1, 1854; due Mar 31, 1875. Interest paid Apr 1 & Oct 1.

Pennsylvania Railroad 1st mortgage dollar bonds 6s currency. 10. Dated Oct 14, 1852; due Dec 31, 1880. Interest paid Jan 1 & July 1.

Camden and Ambov Railroad 6s currency. 11. Dated Jan 1, 1854; due Jan 1, 1889.

Interest paid June 1 & Dec 1.

Camden and Ambov Railroad 6s currency. 12

Dated July 1, 1833; due Feb 1, 1883. Interest paid Feb 1 & Aug 1.

13. New York Central Railroad debt certificates or "premium bonds" 6s currency.

Dated Aug 1, 1853; due May 1, 1883.

Interest paid May 1 & Nov I.

Note:-The term "premium bonds" does not refer to the principal of the bond. These bonds promised to pay \$1,000 on May 1, 1883.

14. New York Central Railroad "bonds for debts assumed" 7s cur-

rency.

Dated Aug 1, 1856; due Aug 1, 1876.

Interest paid Feb 1 & Aug 1.

15. Chicago, Burlington and Quincy Railroad 1st mortgage 8s curren-Dated Jan 1, 1858; due Jan 1, 1883.

Interest paid Jan 1 & July 1.

16. Hudson River Railroad 2nd mortgage 7s currency.

Dated Dec 16, 1850; extended Dec 16, 1860; due June 16, 1885. Interest paid June 16 & Dec 16.

17. Chicago and Northwestern Railway "preferred sinking fund" (1st mortgage, Chicago to Oshkosh) 7s currency.

Dated July 1, 1859; due Aug 1, 1885. Interest paid Feb 1 & Aug 1.

18. Philadelphia and Eric Railroad 1st mortgage 6s currency. Dated Mar 31, 1861; due Mar 31, 1881.

Interest paid Apr 1 & Oct 1.

Galena and Chicago Union Railroad 1st mortgage 7s currency. 19. Dated Feb 1, 1852; extended Feb 1, 1862; due Feb 1, 1882. Interest paid Feb 1 & Aug 1 Callable at 105 on Feb 1, 1877.

Michigan Southern and Northern Indiana Railroad 1st mortgage 20. 7s currency.

Dated May 1, 1855; due May 1, 1885. Interest paid May 1 & Nov 1.

21. Cleveland and Toledo Railroad 1st mortgage 7s currency. Dated July 1, 1855; due July 1, 1885, Interest paid Jan 1 & July 1.

22. Connecticut and Passumpsic Rivers Railroad 1st mortgage 6s currency.

Dated Dec 1, 1856; due Dec 1, 1876.

Interest paid June 1 & Dec 1.

23. Buffalo, New York and Erie Railroad 1st mortgage 7s currency. Dated Oct 29, 1857; due Dec 1, 1877. Interest paid June 1 & Dec 1.

Chicago and Alton Railroad 1st mortgage 7s currency. 24.

Dated Dec 1, 1862; due Jan 1, 1893.

Interest paid Jan 1 & July 1.

25. Pittsburgh, Fort Wayne and Chicago Railway 1st mortgage 7s Series A currency. Dated Mar 1, 1862; due July 1, 1912.

Interest paid Jan 1 & July 1.

Camden and Amboy Railroad mortgage 6s currency. 26. Dated Nov 1, 1862; due Nov 1, 1889.

Interest paid May 1 & Nov 1.

Toledo and Wabash Railroad 1st mortgage 7s currency. 27. Dated Aug 1, 1853; extended Aug 1, 1865; due Aug 1, 1890. Interest paid Feb 1 & Aug 1.

28. St. Louis, Alton and Terre Haute Railroad 1st mortgage 7s Series

A currency.

Dated June 30, 1862; due July 1, 1894. Interest paid Jan 1 & July 1.

29. New York Central Railroad renewal bonds 6s currency.

Dated June 15, 1854-7s; extended June 15, 1864-6s; due Dec 15, 1887.

Interest paid June 15 & Dec 15.

30. Morris and Essex Railroad 1st mortgage 7s currency. Dated July 1, 1864; due May 1, 1914.

Interest paid May 1 & Nov 1.

31. New York and Erie Railroad 1st mortgage 7s currency. Dated July 1, 1847; extended May 1, 1867; due May 1, 1897. Interest paid May 1 & Nov 1.

32. Milwaukee and St. Paul Railway (Prairie du Chien Division) 1st mortgage 8s currency.

Dated Feb 1, 1868; due Feb 1, 1898. Interest paid Feb 1 & Aug 1.

Lehigh Valley Railroad 1st mortgage 6s currency. 33. Dated June 1, 1868; due June 1, 1898.

Interest paid June 1 & Dec 1.

Central Railroad of New Jersey "new bonds" later 1st mortgage 34. 7s currency. Dated 1869; due Feb 1, 1890.

Interest paid Feb 1 & Aug 1.

35. Lehigh Coal and Navigation Company "railroad loan" 6s currency. Dated 1867; due Feb 1, 1897.

Interest paid quarterly Feb 1, May 1, Aug 1 & Nov 1.

36. Chicago and Milwaukee Railroad 1st mortgage 7s currency. Dated 1863; due July 1, 1898. Interest paid Jan 1 & July 1.

Lake Shore Railway "dividend bonds" 7s currency. 37. Dated Apr 1, 1869; due Apr 1, 1899.

Interest paid Apr 1 & Oct 1.

Cleveland, Columbus, Cincinnati and Indianapolis Railway 38.

1st mortgage 7s currency.

Dated 1869; due May 1, 1899 Interest paid May 1 & Nov 1.

 Lehigh Valley Railroad 2nd mortgage 7s currency. Dated July 1, 1870; due Sept 1, 1910.

Interest paid Mar 1 & Sept 1. Registered.

40. Chicago and Northwestern Railway consolidated 7s currency.

Dated Jan 16, 1865; due Feb 1, 1915. Interest paid quarterly, Feb 1, May 1, Aug 1 & Nov 1.

41. Lake Shore and Michigan Southern Railway consolidated 1st mortgage 7s currency.

Dated July 1, 1870; due July 1, 1900.

Interest paid Jan 1 & July 1.

 Pennsylvania Railroad general mortgage 6s currency. Dated July 1, 1867; due July 1, 1910. Interest paid Jan 1 & July 1

 New York and Harlem Railroad consolidated (later 1st) mortgage 7s currency.

Dated May 1, 1872; due May 1, 1900. Interest paid May 1 & Nov 1.

44. New York Central and Hudson River Railroad 1st mortgage 7s currency.

Dated Jan 15, 1873; due Jan 1, 1903.

Interest paid Jan 1 & July 1.

 Chicago, Burlington and Quincy Railroad consolidated mortgage 7s currency.

Dated July 1, 1873; due July 1, 1903.

Interest paid Jan 1 & July 1.

46. Cleveland and Pittsburgh Railroad consolidated mortgage 7s currency.

Dated 1867; due Nov 1, 1900. Interest paid May 1 & Nov 1.

 Michigan Central Railroad consolidated mortgage 7s currency. Dated May 1, 1872; due May 1, 1902. Interest paid May 1 & Nov 1.

 Central Pacific Railroad 1st mortgage 6s Series A gold. Dated July 1, 1865; due July 1, 1895.

Interest paid Jan 1 & July 1.

 Chicago, Rock Island and Pacific Railroad 1st mortgage 6s currency.

Dated May 1, 1877; due July 1, 1917. Interest paid Jan 1 & July 1.

 Interest paid Jan I & July I.
 Chicago and Northwestern Railway consolidated mortgage 7s gold. Dated Nov I, 1872; due Dec I, 1902. Interest paid June 1 & Dec I.

 Chicago, St Paul and Minneapolis Railway 1st mortgage 6s gold. Dated May 9, 1878; due May 1, 1918.

Interest paid May 1 & Nov 1.

52. St. Paul, Minneapolis & Manitoba 2nd mortgage 6s gold.

Dated Oct 1, 1879; due Oct 1, 1909. Interest paid Apr 1 & Oct 1.

53. Nashville, Chattanooga and St. Louis Railway 1st mortgage 7s currency. Dated July 1, 1873; due July 1, 1913.

Interest paid Jan 1 & July 1.

St Paul and Sioux City Railroad 1st mortgage 6s gold. 54. Dated July 1, 1879; due Apr 1, 1919.

Interest paid Apr 1 & Oct 1.

55. Chicago, Milwaukee and St Paul Railway (Southern Minnesota Division) 1st mortgage 6s currency. Dated Jan 1, 1880; due Jan 1, 1910. Interest paid Jan 1 & July 1.

Canada Southern Railway 1st mortgage 5s Canadian currency. 56. Dated Oct 31, 1877; due Jan 1, 1908.

Interest paid Jan 1 & July 1.

57. Chicago, St Paul, Minneapolis and Omaha Railway consolidated 6s currency. Dated June 1, 1880; due June 1, 1930.

Interest paid June 1 & Dec 1.

St. Paul, Minneapolis and Manitoba Railway (Dakota Extension) 58. 1st mortgage 6s gold. Dated Nov 1, 1880; due Nov 1, 1910.

Interest paid May 1 & Nov 1.

Philadelphia and Eric Railroad general mortgage 5s gold. 59. Dated July 1, 1869; due July 1, 1920 Interest paid Apr 1 & Oct 1. Registered.

Chicago, Milwaukee and St Paul Railway (Chicago and Pacific 60. Western Division) 1st mortgage 5s gold.

Dated Jan 1, 1881; due Jan 1, 1921. Interest paid Jan 1 & July 1.

Chicago, Milwaukee & St Paul Railway (Wisconsin and Minnesota 61. Division) 1st mortgage 5s gold Dated July 1, 1881; due July 1, 1921.

Interest paid Jan 1 & July 1. Chicago, St Louis and New Orleans Railroad consolidated mort-62. gage 5s gold. Dated Mar 15, 1881; due June 15, 1951.

Interest paid June 15 & Dec 15.

Pennsylvania Company 1st mortgage 4½ gold. 63. Dated Apr 1, 1881; due July 1, 1921.

Interest paid Jan 1 & July 1. New York, Lackawanna and Western Railway 1st mortgage 6s 64. gold.

Dated Dec 1, 1880; due Jan 1, 1921.

Interest paid Jan 1 & July 1.

65. Hannibal and St Joseph Railroad consolidated mortgage 6s currenev.

> Dated Apr 30, 1881; due Mar 1, 1911. Interest paid Mar 1 & Sept 1.

66. New York Central and Hudson River Railroad debenture 5s currency.

Dated Sept 1, 1884; due Sept 1, 1904. Interest paid Mar 1 & Sept 1.

 Baltimore and Ohio Railroad 5s gold. Dated Jan 31, 1885; due Feb 1, 1925. Interest paid Feb 1 & Aug 1.

68. Chicago, Milwaukee and St Paul Railway, terminal mortgage 5s gold.

Dated July 1, 1884; due July 1, 1914.

Interest paid Jan 1 & July 1.

Chicago and Northwestern Railway debenture 5s currency. 69. Dated July 1, 1884; due Nov 1, 1909. Interest paid May 1 & Nov 1

West Shore Railroad 1st mortgage 4s currency.

Dated Dec 5, 1885; due Jan 1, 2361.

Interest paid Jan 1 & July 1. Chicago and Northwestern Railway debenture 5s currency.

Dated May 1, 1883; due May 1, 1933. Interest paid May I & Nov I.

72. Chicago and Northwestern Railway extension 4s currency. Dated Apr 15, 1886; due Aug 15, 1926.

Interest paid Feb 15 & Aug 15.

St Paul, Minneapolis and Manitoba Railway consolidated mortgage 41/2s (originally 6s) gold. Dated May 1, 1883; due July 1, 1933.

Interest paid Jan 1 & July 1.

74. Cincinnati, Indianapolis, St Louis and Chicago Railway general 1st mortgage 4s gold Dated Aug 2, 1886; due Aug 1, 1936.

Interest paid quarterly Feb 1, May 1, Aug 1 & Nov 1.

75. Pacific Railroad (of Missouri) 1st mortgage extended 4s gold. Dated Aug 1, 1868; due Aug 1, 1888 (6% coupon); extended Feb 1, 1887; due Aug 1, 1938 (4% coupon). Interest paid Feb 1 & Aug 1.

Illinois Central Railroad collateral trust 4s gold.

Dated Mar 31, 1888; due Apr 1, 1952. Interest paid Apr 1 & Oct 1.

77. Lake Erie and Western Railroad 1st mortgage 5s gold. Dated Feb 21, 1887; due Jan 1, 1937. Interest paid Jan 1 & July 1.

78. Wabash Railroad 1st mortgage 5s gold. Dated May 1, 1889; due May 1, 1939. Interest paid May 1 & Nov 1.

79. Chesapeake and Ohio Railway (Eastern Extension) 1st mortgage 6s gold.

Dated Jan 1, 1881; due Jan. 1911. Interest paid Apr 1 & Oct 1.

80. Rome, Watertown and Ogdensburg Railroad consolidated mortgage 5s gold.

Dated July 1, 1874; extended July 1, 1882 (gold); due July 1, 1922.

Interest paid Apr 1 & Oct 1 and a 11/4% coupon on July 1, 1922. New York, Chicago and St Louis Railroad 1st mortgage 4s gold. 81. Dated Oct 1, 1887; due Oct 1, 1937. Interest paid Apr 1 & Oct 1.

82. Chesapeake and Ohio Railway 1st consolidated mortgage 5s gold. Dated Jan 1, 1889; due May 1, 1939.

Interest paid May 1 & Nov 1. Illinois Central Railroad collateral trust (Louisville, New Orleans 83. and Texas Railway collateral) 4s gold. Dated Sept 1, 1892; due Nov 1, 1953.

Interest paid May 1 & Nov 1.

84. Chesapeake and Ohio Railway (Richmond and Alleghany Railway Division) 1st consolidated mortgage 4s gold. Dated Jan 20, 1890; due Jan 1, 1989.

Interest paid Jan 1 & July 1.

Cleveland, Cincinnati, Chicago and St Louis Railway (St Louis 85. Division) 1st collateral trust mortgage 4s gold. Dated Nov 1, 1890; due Nov 1, 1990. Interest paid May 1 & Nov 1.

86. East Tennessee, Virginia and Georgia Railway consolidated 1st mortgage 5s gold.

Dated July 5, 1886; due Nov 1, 1956.

Interest paid May 1 & Nov 1.

Chicago, Milwaukee and St Paul Railway general mortgage 4s 87. Series A gold. Dated May 1, 1889; due May 1, 1989.

Interest paid Jan 1 & July 1.

88. Lake Shore and Michigan Southern Railway 1st mortgage 31/2s gold.

Dated June 1, 1897; due June 1, 1997. Interest paid June 1 & Dec 1.

89. St Paul, Minneapolis and Manitoba Railway (Montana Extension) 1st mortgage 4s gold. Dated June 1, 1887; due June 1, 1937.

Interest paid June 1 & Dec 1.

90. Baltimore and Ohio Railroad 1st mortgage 4s gold. Dated July 1, 1898; due July 1, 1948.

Interest paid Apr 1 & Oct 1.

Callable at 105 after June 30th 1923 upon three months' notice. 91. Union Pacific Railroad 1st mortgage railroad and land grant 4s gold.

Dated July 1, 1897; due July 1, 1947.

Interest paid Jan 1 & July 1.

Chicago and Northwestern Railway general mortgage 31/9s gold. 92. Dated Nov 1, 1897; due Nov 1, 1987. Interest paid May 1 & Nov 1.

93. Chicago, Rock Island and Pacific Railway general mortgage 4s gold.

Dated Jan 1, 1898; due Jan 1, 1988. Interest paid Jan 1 & July 1.

94. Atchison, Topeka and Santa Fe Railway general mortgage 4s gold.
Dated Dec 12, 1895; due Oct 1, 1995.
Interest paid Apr 1 & Oct 1.

 New York Central and Hudson River Railroad refunding mortgage 31/s gold.

Dated June 1, 1897; due July 1, 1997.

Interest paid Jan 1 & July 1.
96. Scioto Valley and New England Railroad 1st mortgage 4s gold.
Dated Nov 1, 1889; due Nov 1, 1989.
Interest paid May 1 & Nov 1.

97. Lehigh Valley Railway (of New York) 1st mortgage 4½ gold.

Dated June 23, 1890; due July 1, 1940. Interest paid Jan 1 & July 1.

98. Louisville and Nashville Railroad unified mortgage 4s gold.
Dated June 2, 1890; due July 1, 1940.

Interest paid Jan 1 & July 1.

99. Oregon Railroad and Navigation Company consolidated mortgage

4s gold. Dated Aug 17, 1896; due June 1, 1946.

Interest paid June 1 & Dec 1.

100. Chicago, Burlington and Quincy Railroad (Illinois Division) 1st mortgage 31/25 currency.

Dated July 1, 1899; due July 1, 1949.

Interest paid Jan 1 & July 1.

Callable as a whole at 105 and interest on any interest date after July 1, 1929 on six months' notice.

101. Central Pacific Railway 1st refunding mortgage 4s gold.

Dated Aug 1, 1899; due Aug 1, 1949. Interest paid Feb 1 & Aug 1.

 Northern Pacific Railway prior lien railroad and land grant mortgage 4s gold.
 Dated Nov 10, 1896; due Jan 1, 1997.

Interest paid quarterly Jan 1, Apr 1, July 1 & Oct 1.

 Norfolk and Western Railway 1st consolidated mortgage 4s gold. Dated Oct 22, 1896; due Oct 1, 1996. Interest paid Apr 1 & Oct 1.

 Central Railroad Company of New Jersey general mortgage 5s gold. Dated July 1, 1887; due July 1, 1987.

Interest paid Jan 1 & July 1.

105. Hocking Valley Railway 1st consolidated mortgage 4½s gold. Dated July 1, 1899; due July 1, 1999. Interest paid Jan 1 & July 1.

106. Norfolk and Western Railway divisional first lien and general mortgage 4s gold.

Dated July 1, 1904; due July 1, 1944.

Interest paid Jan 1 & July 1.

Callable at 105 and interest on any interest date after January 1, 1929 upon three months' notice.

Oregon Short Line Railroad consolidated 1st mortgage 5s gold. 107. Dated Mar 1, 1897; due July 1, 1946. Interest paid Jan 1 & July 1.

Southern Pacific Railroad (California) first refunding mortgage 4s 108. gold.

Dated Jan 3, 1905; due Jan 1, 1955.

Interest paid Jan 1 & July 1.

Callable at 105 and interest on Jan 1, 1910 or on any interest date thereafter at not less than three months' notice.

Atchison, Topeka and Santa Fe Railway adjustment mortgage 4s 109. gold, stamped. Dated Dec 12, 1895; due July 1, 1995.

Interest paid May 1 & Nov 1.

110. Northern Pacific Railway general lien 3s gold. Dated Nov 10, 1896; due Jan 1, 2047. Interest paid quarterly Feb 1, May 1, Aug 1 & Nov 1.

Atlantic Coast Line Railroad 1st consolidated mortgage 4s gold. 111. Dated July 1, 1902; due July 1, 1952. Interest paid Mar 1 & Sept 1.

112. Delaware and Hudson Company first and refunding mortgage 4s

Dated May 1, 1908; due May 1, 1943.

Interest paid May 1 & Nov 1.

Callable as a whole at 1071/2 and interest on May 1, 1918 or on any interest date thereafter upon thirteen weeks' notice.

113. Central of Georgia Railway consolidated mortgage 5s gold. Dated Nov 1, 1895; due Nov 1, 1945. Interest paid May 1 & Nov 1.

Pennsylvania Railroad consolidated mortgage 4s gold. 114. Dated May 1, 1908; due May 1, 1948. Interest paid May 1 & Nov 1.

115. Kansas City Southern Railway 1st mortgage 3s gold. Dated Apr 2, 1900; due Apr 1, 1950

Interest paid Apr 1 & Oct 1.

Louisville and Nashville Railroad (Atlanta, Knoxville and Cin-116. cinnati Division) mortgage 4s gold. Dated Apr 1, 1905; due May 1, 1955. Interest paid May 1 & Nov 1.

Illinois Central Railroad refunding mortgage 4s gold. 117.

Dated Nov 1, 1908; due Nov 1, 1955.

Interest paid May 1 & Nov 1.

Callable as a whole at 107½ and interest on Nov 1, 1918 or on any interest date thereafter upon not less than thirteen weeks' notice.

118. Chicago, Burlington and Quincy Railroad general mortgage 4s currency.

Dated Mar 2, 1908; due Mar 1, 1958.

Interest paid Mar 1 & Sept 1.

Southern Railway 1st consolidated mortgage 5s gold.

120.

Dated Oct 2, 1894; due July 1, 1994.

Interest paid Jan 1 & July 1. Union Pacific Railroad 1st lien and refunding mortgage 4s gold.

Dated June 1, 1908; due June 1, 2008.

Interest paid Mar 1 & Sept 1.

Callable as a whole at 107½ and interest on Sept 1, 1918 or on any interest date thereafter upon three months' notice.

 Atlantic Coast Line Railroad collateral trust (Louisville and Nashville Railroad collateral) 4s gold.

Dated Nov 1, 1902; due Oct 1, 1952.

Interest paid May 1 & Nov 1.

Callable on any interest date in amounts of not less than \$100,000 at 105 and interest.

122. Norfolk and Western Railway Pocahontas Coal and Coke joint mortgage 4s gold.

Dated Dec 2, 1901; due Dec 1, 1941.

Interest paid June 1 & Dec 1.

Callable at 105 and interest after Apr 1, 1906 from charges against coal mined.

 Great Northern Railway 1st and refunding mortgage 4¼s Series A gold.

Dated May 1, 1911; due July 1, 1961.

Interest paid Jan 1 & July 1.

Callable as a whole at 105 and interest on or after Jan 1, 1941 upon ninety days' notice.

124. Canada Southern Railway 1st and refunding consolidated mortgage 5s Series A gold.

Dated Oct 1, 1912; due Oct 1, 1962. Interest paid Apr 1 & Oct 1.

125. Morris and Essex Railroad 1st refunding mortgage 3½s gold. Dated Dec 1, 1900; due Dec 1, 2000. Interest paid June 1 & Dec 1.

 Pennsylvania Railroad consolidated mortgage 4½s gold. Dated Feb 1, 1915; due Aug 1, 1960.

Interest paid Feb 1 & Aug I.

27. Canadian Northern Railway sinking fund debenture 6½s gold.

Dated July 1, 1921; due July 1, 1946.

Interest paid Jan 1 & July 1.

128. Great Northern Railway general mortgage 5½s Series B gold.

Dated Jan 1, 1922; due Jan 1, 1952.

Interest paid Jan 1 & July 1.

 Atlantic Coast Line Railroad general unified 4½s Series A gold. Dated June 1, 1914; due June 1, 1964. Interest paid June 1 & Dec 1.

Pennsylvania Railroad general mortgage 4½s Series A gold.
 Dated June 1, 1915; due June 1, 1965.
 Interest paid June 1 & Dec 1.

131. Pennsylvania Railroad general mortgage 5s Series B gold.
Dated Dec 1, 1918; due Dec 1, 1968.
Interest paid June 1 & Dec 1.

Great Northern Railway general mortgage 5s Series C gold. 132.Dated Jan 1, 1923; due Jan 1, 1973. Interest paid Jan 1 & July 1.

St Louis Southwestern Railway 1st mortgage bond certificates 133. (issued by the Central Trust Company) 4s gold. Dated Nov 1, 1890; due Nov 1, 1989.

Interest paid May 1 & Nov 1.

Missouri, Kansas & Texas Railway 1st mortgage 4s gold. 134. Dated June 1, 1890; due June 1, 1990. Interest paid June 1 & Dec 1.

Chesapeake and Ohio Railway general mortgage 41/2s gold. 135. Dated Feb 23, 1892; due Mar 1, 1992.

Interest paid Mar 1 & Sept 1.

136. Cleveland, Cincinnati, Chicago and St Louis Railway general mortgage 4s Series A gold. Dated May 15, 1893; due June 1, 1993.

Interest paid June 1 & Dec 1.

137. New York Central Railroad consolidation mortgage 4s Series A gold. Dated Aug 1, 1913; due Feb 1, 1998.

Interest paid Feb 1 & Aug 1.

Texas and Pacific Railway 1st mortgage 5s gold. 138. Dated Feb 1, 1888; due June 1, 2000. Interest paid June 1 & Dec 1.

139. Lehigh Valley Railroad (Pennsylvania) general consolidated mortgage 4s gold.

Dated Sept 30, 1903; due May 1, 2003.

Interest paid May 1 & Nov 1.

Canadian Pacific Railway 4% irredeemable debenture stock (a bond 140. without maturity). Issue authorized by an act of Parliament of the Dominion of Canada, passed in 1889, and subsequent acts. Issue of stock may be made from time to time. Interest paid Jan 1 & July 1

141. Southern Railway development and general mortgage 4s Series A gold.

143.

Dated Apr 18, 1906; due Apr 1, 1956. Interest paid Apr 1 & Oct 1.

Chicago and Western Indiana Railroad Company consolidated 142. mortgage 4s gold. Dated July 1, 1902; due July 1, 1952.

Interest paid Jan 1 & July 1. Pittsburgh, Cincinnati, Chicago & St Louis Railroad general mort-

Dated Apr 1, 1925; due Apr 15, 1975.

gage 5s Series B gold. Interest paid Apr 1 & Oct 1.

Great Northern Railway general mortgage 41/2s Series D gold. 144.

Dated July 1, 1926; due July 1, 1976. Interest paid Jan 1 & July 1.

 Chicago, Milwaukee and St Paul Railway general (now 1st) mortgage 4s Series A gold.
 Dated May 1, 1889; due May 1, 1989.

Interest paid Jan 1 & July 1.

Remain undisturbed under plan of reorganization.

146. Erie Railroad Company 1st consolidated prior lien 4s gold. Dated Dee 10, 1895; due Jan 1, 1996. Interest paid Jan 1 & July 1.

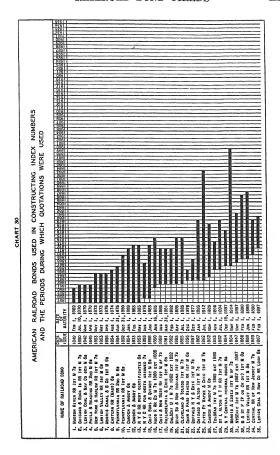
147. Pennsylvania Railroad general mortgage 4¼s Series D gold. Dated Apr 1, 1931; due Apr 1, 1981. Interest paid Apr 1 & Oct 1.

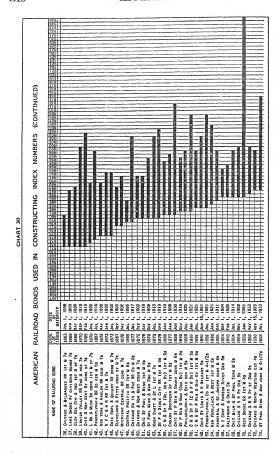
148. Chicago and Erie Railroad 1st 5s gold.
Dated Aug 21, 1890; due May 1, 1982.
Interest paid May 1 & Nov 1.

Chesapeake and Ohio Railway (Richmond and Alleghany Division)
 1st 4s gold
 Dated Jan 20, 1890; due Jan 1, 1989.

Interest paid Jan 1 & July 1.

150. Cleveland, Cincinnati, Chicago and St Louis Railway (St Louis Division) 1st collateral 4s gold Dated Nov 1, 1890; due Nov 1, 1990. Interest paid May 1 & Nov 1.





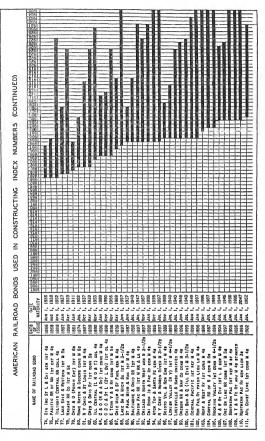


CHART 30

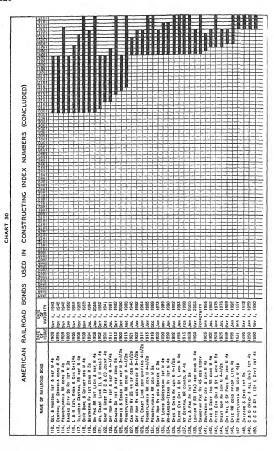


TABLE 2

Paper Prices of American Railroad Bonds, Monthly, January 1857—January 1879

This table is intended to aid students who wish original data on railroad bond prices in the paper ('greenback') money period. Gaps in this table occur in months when no sales were made. For identification

of the bonds refer by numbers to Table 1.

With the exception of Bond Number 8, all prices in this table are 'flat'. 'Flat' prices are given because that is the form in which they were quoted during the period covered by the table. Since January 1, 1909, it has been the almost universal practice in the United States to quote bonds at 'and interest' prices. In the period from January 1857 to December 1862, inclusive, the quotations for Bond Number 8 are 'and interest' prices for one day in the month. From January 1862 to January 1866 the quotations for Bond Number 8 are 'flat'.

The 'flat' price of a bond is the actual amount of money which changes hands when the bond is sold. The 'and interest' price equals the 'flat' price less the allowance for the accrued portion of the current coupon. Except on interest dates, the 'flat' price is, of course, greater than the 'and interest' price. For a simple discussion of 'flat' and 'and interest' prices, see Justin H. Moore; Handbook of Financial

Mathematics, pages 434 and 435.

PRICES OF RAILROAD BONDS IAN, 1857-IAN, 1858

	ż	High	828272748828 236588877774828
	JAN.	Low	\$200 \$200 \$200 \$200 \$200 \$200 \$200 \$200
	ن	High	828204228 82820428 82820428
	DEC.	Low	882744278 8827444 8627477774 8608 8608 8608 8608 8608 8608 8608 860
	NOV.	High	98287 775 827 775 827 827 827 827 827 827 827 827 827 827
		Low	88888888888888888888888888888888888888
	OCT.	High	80 82 64 73 87 87 80 80 80 80
	9	Low	200 200 200 200 200 200 200 200 200 200
	7.	High	90 84 17 17 17 10 17 10 10 10 10 10 10 10 10 10 10 10 10 10
	SEPT.	Low	90 844 844 70 70 82 82 82 82 83 65 65
	ن	High	95 17872 17872 173 17175 811 8572 171
	AUG.	Low	94½ 89% 73 73 711 81 85½ 85%
AN. 1637 JAN. 1636	JULY	чŝін	9835 7787 778 771 771 771 880 85 85 87 74 74 74 74 74 74 74 74 74 74 74 74 74
		Low	95 91 71877 71277 71277 80 85 85 87 7277 7477 84
100	JUNE	High	983/2 933/2 776/3/2 7121/3 7121/3 7121/3 80 85 98 98 98 98 98 98 98 98 98 98 98 98 98
2		Low	98 90 92 72 72 72 80 80 95 95
	MAY	High	987.7 179.7 170.7
		Low	971/2 96 91 91 77 77 7034 801/2 86 86 771/4
	E	High	201 / 202 /
	APR.	Low	8887 1888 1888 1888 1988 1987 1987 1987
	R.	High	977 102 881 724 724 891 761 761 761
	MAR.	Low	88 88 88 88 88 88 88 88 88 88 88 88 88
	FEB.	High	25 88 82 7 7 7 2 7 7 8 8 8 8 8 8 8 8 8 8 8
		Low	95.8 11.1
	ż	High	8807: 8 227 27 27 27 27 27 27 27 27 27 27 27 27
	JAN.	Low	8897.7 200 :0880.7 200 :0888.7 200 :0888.7
	ž	-	12 10 12 13 13

PRICES OF RAILROAD BONDS JAN. 1858—JAN. 1859

	11		1.00.00.40.40 \4 \70
	JAN.	High	101 101 101 101 101 101 101 101 101 101
		Low	7 27 27 27 27 27 27 27 27 27 27 27 27 27
	ı,	High	101 101 101 101
	DEC.	Low	103 988 888 888 883 882 100 100 100 100 100 100 100 100 100 10
		High	103% 998% 888 871% 871% 991% 104
	NOV.	Low	885 8727 8727 8727 8727 8727 8727 8727 8
	H	High	2027/2 2 2027/2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	OCT.	Low	933 953 953 953 953 950 950 950 950 950 950 950 950 950 950
	T.	High	101 95 9714 88 88 88 89 100 100 85 88 88 88 88 88 88 88 88 88 88 88 88
	SEPT.	Low	100 4 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
	ıj	High	101 955 977 885 887 874 874 874 874 874 874 874 874 874
1001	AUG.	Low	001 044 047 047 047 047 047 047 047 047 047
	Y.	High	25.5 27.7 27.7 28.5 28.5 27.7 27.7 28.6 28.6 27.7 27.7 27.7 27.7 27.7 27.7 27.7 27
- 1	JULY	Low	24047888822 24047888882 25088887 2777 2777 2777 2777 2777 2777 277
	司	High	2007 2747 2747 277 277 277 277 277 277 277
	JUI	Low	201 98 7474 880 880 880 880 747 747 87 87 87 88 89 96
	Ϋ́	High	101 19 19 19 19 19 19 19 19 19 19 19 19 19
	MAY	Low	20:00:00:00:00:00:00:00:00:00:00:00:00:0
	2	High	000001 40000000000000000000000000000000
	APR.	Low	96 92 92 73 73 92 92 74 77 77 77 77 77 77 77 77 77 77 77 77
	F.	High	98 95 95 77 77 77 77 75 75 95 95 97 97 97 97 97 97 97 97 97 97
	MAR.	Low	96 941% 9243% 177 777 88 88 88 99 773 99 97 97 97
	69	High	983/4 922/4 94-94-76 76-77-7 889-96-77-7 90-97-77-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7
	FEB.	Low	72777777777777777777777777777777777777
	z	High	882 8477 447 447 447 447 447 447 447 447 44
-	JAN.	Low	95 89 89 645 6445 7244 811 821 821 821 9332 9332 9332 9332 9332 9332 9332 93
	Š		12242000112242

PRICES OF RAILROAD BONDS JAN. 1859—JAN. 1860

JAN.	High	1006 1002 1002 1002 1003 1003 1003 1003 1003
JA	Low	106 1090 1090 1090 1090 1090 1090 1090 1
DEC.	High	104 1001 1001 103 103 103 103 103 103 103 1
D	Low	2037 2038 2038 2037 2038 2037 2038 2037 2038 2037 2038 2037 2038 2038 2038 2038 2038 2038 2038 2038
NOV.	High	103 2 49 2 87 2 87 2 87 2 87 2 87 2 87 2 87 2 87
Z	Low	200 200 200 200 200 200 200 200 200 200
CT.	High	103 93 97 97 97 87 87 85 94 94 94 94 94 94 94 94 94 94 94 94 94
0	Low	102 ½ 91 95 ½ 93 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
SEPT.	High	993777 993777 9937777 9937777 9937777
SI	Low	101 14 14 14 14 14 14 14 14 14 14 14 14 14
AUG.	High	100 889 881 881 881 881 882 883 883 883 883 883 883 883 883 883
V	Low	890 877 877 877 877 883 863 877 881 877 881 877 877 877 877 877 877
JULY	High	105 89 81 81 82 87 87 87 87 87 87 87 87 87 87 87 87 87
	Low	886 98 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
UNE	High	93 93 95 87 87 87 87 87 87 87 87 80 80 80 80 80 80 80 80 80 80 80 80 80
DÍ.	Low	901/2/4/8 89 88 89 88 94 88 94 88 98 88 98 88 98 88 98 88 98 88 98 98
MAY	High	105 97 97 8434 8434 8934 95 103 103 103 103 103 103 103 103 103 103
W.	Low	105 881 881 881 881 881 881 881 881 883 883
APR.	High	104 977 8537 893 95 95 103 853 853 853 853 853 853 853 853 853 85
AI	Low	102 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
MAR.	High	102 96 96 96 95 95 95 95 95 95 95 95 95 95 95 95 95
W	Low	202 202 202 202 202 202 202 203 203 203
FEB.	High	86 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
FE	Low	2000 2000 2000 2000 2000 2000 2000 200
JAN.	High	01 02 04 05 05 05 05 05 05 05 05 05 05
JA	Low	7 27 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
:	o V	-22420r800111242

PRICES OF RAILROAD BONDS Jan. 1860—Jan. 1861

, N	High	1003 1003 1003 1003 100 100 100 100 1033 103 10
JA	Low	88 83 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
DEC.	High	102 95 10014 81 90 90 90 77 77 77 77 77 77 77 77 77 77 77 77 77
ā	Low	101 89 77 77 85 85 85 85 85 85 85 85 85 85 85 85 85
NOV.	High	106 2037 2037 2000 101 101 103 103 103 103 103 103 103
ž	Low	508898 :078988888888888888888888888888888888888
OCT.	High	20:101 20
ŏ	Low	105% 84 988 96% 93 100% 88% 88% 97 97
SEPT.	High	106 87.2% 98.2% 101.3% 101.3% 102.4% 87.2% 102.4% 87.2% 102.4% 87.2% 102.4% 103
SE	Low	106 877 971 101 101 101 101 101 101 101 101 101 1
AUG.	High	106 98 101 1/2 95 2/2 95 2/2 101 3/2 101 3/2 86 1/2 100
A	Low	106 98 100 85 97 97 97 103 103 101 86 12 86 12 86 12 86 13 86 14 86 15 86 16 86 16 86 16 86 86 87 87 87 87 87 87 87 87 87 87 87 87 87
IULY	High	110 98 ¼ 101 84 ¾ 100 95 ¼ 90 90 90 97 ¼ 104 ¾ 104 ¾
K	Low	105 100 100 84 99 95 95 95 95 95 96 88 88 88 94 104 104 104 104 104 104 104 104 104 10
UNE	High	107 85 100 95 95 90 101 103 86 95 95 95 95
2	Low	106% 84 98% 93 93 93 92 101 89% 101 86 87 93
MAY	High	107 83 83 99 99 99 92 101 87 87 92 92 92 92 92 92 92 92 93
×	Low	1001 1000 1000 1000 1010 1010 1010 101
APR.	High	2000 2000 2000 2000 2000 2000 2000 200
A	Low	201 202 202 203 203 203 203 203 203 203 203
MAR.	High	001 002 002 002 002 003 003 003 003 003 003
Ä	Low	2008 2008 2008 2008 2008 2008 2008 2008
FEB.	High	24 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
-	Low	2001 2007 84 84 74 74 74 74 75 76 76 76 76 76 76 76 76 76 76 76 76 76
JAN.	High	7, 200 100 100 100 100 100 100 100
J. P.	Low	0001 0001 0001 0001 0001 0001 0001 000
:	ģ	122420180012242

PRICES OF RAILROAD BONDS JAN. 1863—JAN. 1864

PRICES OF RAILROAD BONDS JAN. 1861--- TAN. 1862

1		ųž	800 800 800 800 800 800 800 800 800 800
	JAN.	High	14 /4 /4 /4 /4 /4 /4 /4 /4 /4 /4 /4 /4 /4
İ	-	Low	97 1000 860 981 981 97 97 97 97 97 97 97 97
1	Ö.	High	100 100 100 100 100 100 100 100 100 100
	DEC.	Low	958 88127 900 957 957 957 957 957 957 957 957 957 957
1	Υ.	High	93 83 83 961 91 99 97 88 83 92 93 93 93
	NOV.	Low	93 97 880 933/2 90 83 823/2 90 923/2
	T.	High	94 100 80 9954 9174 9674 9634 9634 9634
ı	OCT.	Low	94 9993 94 91 91 92 92 92 92 92 92 92 92 93 92 93 93 95 95 95 95 95 95 95 95 95 95 95 95 95
1	T.	High	92 103 84 95 92 100 88 94 81 82 92 101 92 92 101 92 92
1	SEPT.	Low	92 83 83 92 92 92 86 92 87 100 92 92 92 92
Ì	G	High	102 85 98 91 91 100 96 81 81 81 81 93 92 92 96 96 96 96
202	AUG.	Low	101 82 96 91 100 863 787 80 80 100 92 92
JAN. I	Y.	High	94 8334 9732 9732 9732 9634 79 9634 102 9732 9732
JAN. 1801-JAN. 1802	JULY	Low	94 100 83 96 96 101 101 92 101 91
AN.	JUNE	High	95 1000 1000 1000 1000 1000 1000 101
		Low	95 981/2 80 95 95 851/2 87 100 77 100/2 93
	APR. MAY	High	92 10034 97 97 97 98 87 87 87 100 78 78 78 78 79 94 77 94 77
1		Low	913/ 999/4 76 955 877/8 877/8 877/8 76 76 76 97/4 99/4 99/4
		High	96 101 1/2 101 1/2 101 1/2 100 88 100 83 83 83 95 101 101 101 101 101 101 101 101 101 10
		Low	96 1001/2 80 991/2 901/2 82 80 80 951/2 951/2 951/2 951/2 951/2
	2	High	100 1023% 10075 100 100 91 100 83 84 84 84 84 97 101
	MAR.	Low	101 101 101 102 100 100 100 100 100 100
	ig.	High	101 883 100 100 100 100 100 100 100 100 100 10
	FEB.	Low	100 827% 827% 100 100 100 100 100 100 100 100 100 10
	ż	High	28 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
	JAN.	Low	995 100 100 100 100 80 83 83 96/2
	1	9	264200000000000000000000000000000000000

PRICES OF RAILROAD BONDS JAN. 1862—JAN. 1863

1 1 1 1 1 1 1 1 1 1		ó	220287654222008765
## APA APA APA APA JUNE JULY AUG. SEPT. OCT. NOV. DEC. IA the Low High Low	JA)		h h h
F.B. MAR. APR. AAR. JUNE JULY AUG. SEPT. OCT. NOV. DEC. IAA IAA IAA JUNE JULY AUG. SEPT. OCT. NOV. DEC. IAA IAA IAA JUNE JULY AUG. SEPT. OCT. NOV. DEC. IAA	ż	High	1000 1000 1000 1000 1000 1000 1000 100
High Low High High Low High High Low High	14		
Low High Low Hig	EB.		/01/01 /H /01 /H/01
High Low High High Low High Hi	_	_	<u> </u>
APR. MAY JUNE JULY AUG. SEPT. OCT. NOV. DEC. IA LOW High High Ling High Ling High Ling High Low High L	LAR.		·/8/8/2 /8 /8 /8/8/9
High Low High High Low High High Low High Low High Low High Low High Low High Low High High Low High High Low		-	101-101/01 101 101/01/11/01
MAY JUNE JULY AUG. SEPT. OCT. NOV. DEC. IA	APR		A 10 10 10 10
High Low H	.;	-	100 14/4 100,00/4 100
JUNE JULY AUG. SEPT. OCT. NOV. DEC. IA Low High	M		88888888888888888888888888888888888888
Low High		High	103 100 100 100 100 100 100 100 100 100
High Low High			2001 2001 2001 2001 2001 2001 2001 2001
JULY AUG. SEPT. OCT. NOV. DEC. IA			900 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
High Low High Lo			79 70 70/0/0 70
AUG. SEPT. OCT. NOV. DEC. IA In Low High Low Hi	ULY		12/2 /u · 1/2/4 /u
Co.		_	74/4/4/4 · /# /4/4
SEPT. OCT. NOV. DEC. IA Ia Low High Low High Low High Low Ia Low High Low High Low High Low Ia Low High Low High Low High Low Ia Low Low Low Low Low Low Low Low Low Ia	AUG		-701/0 701 701 701 74 701/0
High Low H		_	/m -/37/01 /m /m/59 /m /m
OCT. NOV. DEC. JA	SEI		033% 023% 023% 023% 023% 023% 023%
High Low High Line Hi	Ę.	High	103 100 100 100 100 100 100 100 100 100
High Low High Line Hi	ŏ	Low	101 101 101 101 101 100 100 100 100 100
NOV. DEC. 1A Low High Line High	CT.	High	1110 1110 1110 1110 1110 1100 1100 110
NY. DEC. 1A High Low High Ligh High Low	2.		100 100 100 100 100 100 100 100 100 100
DEC. 1A DEC. 1B DEC. 1	V	v Hig	A . 64 64 64 64
DEC. JA HIGH LOW W HIG			4. 22
1A 1	DEC.		Testes to 74 To 12 To 164
		_	Z
	JA		74.74 74 74 7

JAN.	High	1008 1004 1004 1007 1007 1008 1008 1008 1009 1009 1009 1009 1009
	Low	104 104 104 104 104 104 104 104 104 104
DEC.	High	100 1 100 1
Д	Low	1008 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2
NOV.	High	100 100 100 100 100 100 100 100 100 100
z 	Low	108 106 106 106 107 107 108 109 100 100 100 100 100 100 100 100 100
OCT.	High	1112 1000
•	Low	1112 1005 4 1011 132 1011 132
SEPT.	High	112 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
SE	Low	112 12 12 12 12 12 12 12 12 12 12 12 12
AUG.	High	112 100 101 101 101 101 100 100 100 100
A	Low	111 100 100 100 100 100 100 100 100 100
TULY	High	114 1108 1108 1108 1108 1108 1108 1109 1109
H	Low	113 1111 1108 1108 1108 1109 1109 1109 1109
JUNE	High	114 108 115 115 116 110 110 110 110 110 110 110 110 110
DE.	Low	112 108/21 110 113 113 113 116 116 110 110 110 110 110 110 110 110
MAY	High	112 14 15 15 15 15 15 15 15 15 15 15 15 15 15
M	Low	110 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
gi	High	112/2 112/2 110/2 115/2 110/2 110/2 110/2 110/2 110/2 110/2 110/2 110/2 110/2
APR.	Low	1112 1105 1112 1112 1112 1112 1112 1112
MAR.	High	1115 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
M	Low	1117 1117 1117 1117 1117 1117 1117 111
ej.	High	1119 1119 1119 1119 1119 1119 1119 111
FEB.	Low	1117 1117 1117 1117 1117 1117 1117 111
JAN.	High	11111111111111111111111111111111111111
Ϋ́	Low	113 / 100 /
ź	Ġ	22222222222222222222222222222222222222

PRICES OF RAILROAD BONDS JAN. 1864—JAN. 1865

PRICES OF RAILROAD BONDS JAN. 1865—JAN. 1866

IAN. FEB. MAR. APR.	FEB. MAR.	FEB. MAR.	MAR.	MAR.	MAR.	MAR.	MAR.	-	-	-	-	APR.	APR.	APR.	P.R.	.,	-			Z	MAY	51	\neg	7	21	B	1	!		_	JULY	11	> 1	1		~ (コー	AUG	. 1		**	S	片급	SEPT.	. 1		~	50	H				žĪ	NON	. 1		-	51	DEC.	. 1	_	-	đ t	Y N	. 1
High Low High Low High Low High Low High	Low High Low High Low High Low	Low High Low High Low High Low	Low High Low High Low High Low	High Low High Low High Low	High Low High Low High Low	High Low High Low High Low	Low High Low High Low	Low High Low High Low	High Low High Low	High Low High Low	Low High Low	Low High Low	High Low	High Low	High Low	Low	Low	Low			ligh	4		ĭ	Low		High	4g	-	3	Mor	Ξ.	High	g	ш	OW	2	Ξ	High	-	ĭ	Low		High	5	H	Low		High	gp	-	7	Low	High	45	H	NO.		High	5	귀	MO	_	田	High
105 99 103 99 99% 99% 99% 99% 99% 99%	99 103 99 1 99 1 99 1 99 1 99 1 99 1 99	99 103 99 1 99 1 99 1 99 1 99 1 99 1 99	99 103 99 1 99 1 99 1 99 1 99 1 99 1 99	103 99½ 99¾ 99¾ 99¾ 99¾	103 99½ 99¾ 99¾ 99¾ 99¾	2 99% 99% 99% 99% P	2 99% 99% 99% 99% P	2 99% 99% 99% 99% P	2 99% 99% 99% 99% P	2 99% 99% 99% 99% P	% 66 % 66 % 66 % 66 % 66 % 66 % 66 % 6	% 66 % 66 % 66 % 66 % 66 % 66 % 66 % 6	7 89% 99% 1 99%	7 89% 99% 1 99%	4 99%	4 99%	4 99%	266 7666	266 766	993	298	741	-	993	%	148	66	8/1		88	- 8		88	01	_	60	-	==	88		94	4;	;	95	77.	00	931	141	6,0	931	14	60		93	22	00	943	14	943	100	0.0	940		0,0	95
1061/5 107 1017/5 106 1011/5 102 1021/5	1061/5 107 1017/5 106 1011/5 102 1021/5	1061/5 107 1017/5 106 1011/5 102 1021/5	1061/5 107 1017/5 106 1011/5 102 1021/5	4107 1017/106 1013/102 1021/1	4107 1017/106 1013/102 1021/1	106 1013 102 102 102 102 141	106 1013 102 102 102 102 141	106 1013 102 102 102 102 141	106 1013 102 102 102 102 141	106 1013 102 102 102 102 141	1011/2/102 1021/1	1011/2/102 1021/1	2102 1023/1	2102 1023/1	1023/1	1023/1	1023/1	₹	₹	1037	33	1.	2150	10,	o m	-	25	:7		22	12		58		-	2		==	32		20	4		ó	77	0	£	듄	6	0 44	_	8	70	ĕ		0	60	730	38		9	٠Ŧ	100	ó	67
99% 99%	99% 99%	99% 99%	99% 99%	4 991/2 103 103	4 991/2 103 103	72 103 103	72 103 103	103 103	103 103	103 103	103 103	103 103	103	103	:	:	:	÷	÷		:			α	io e		88			85	7,		88	00	_	8		~	8	_	ő	00	-	8		30	<u>6</u>	160	5	0		8	Ξ	ō.;	٥.	900	33	70	00		000	3	5.70	000	33
1011/1021/ 001/102	10112101212 0012102 06 0012 00	10112101212 0012102 06 0012 00	10112101212 0012102 06 0012 00	710212 0812102 06 0812 00	710212 0812102 06 0812 00	90 26 89 89 89 89 89 89 89 89 89 89 89 89 89	90 763 89 90 89%	9672 89 90 8974	9672 89 90 8974	9672 89 90 8974	89 90 89%	89 90 89%	90 89%	90 89%	× 68	× 68	× 68	₹	₹	32	25			ŏŏ	200		ŝŝ	22		25		-	56	-	_	žõõ	.		200	-	x c	0 <	-	29	_	20	25	_	20	ဝင်	7	29	7	2.9	٥.	w 0	χō		õõ	37	200	22		xi o	0 00
108 100 100 1001/102 104	108 100 100 1001/102 104	108 100 100 1001/102 104	108 100 100 1001/102 104	108 100 100 1001/102 104	108 100 100 1001/102 104	100 1001/2102 104	100 1001/2102 104	100 1001/2102 104	100 1001/2102 104	100 1001/2102 104	1001/2 104	1001/2 104	7 102 104	7 102 104	200	200	200	-	-	105	32		70	.0	۰,		8			8			8		-	; ;	. :	_	: :	-	5	* 01		0	H 01	10	2	7	.0	,	7	ğ		ő	. ~	2	É	14	₹	17	5	3 5		ď	00
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105 109 106 107 103/2103/2105	105 109 106 107 103/2103/2105	105 109 106 107 103/2103/2105	105 109 106 107 103/2103/2105	109 106 107 103/2103/2105	109 106 107 103/2103/2105	106 107 103/2103/2105	106 107 103/2103/2105	107 103/2/103/2/105	107 103/2/103/2/105	107 103/2/103/2/105	103/2103/2105	103/2103/2105	210372105	210372105	2105	2105	2105	-	-	105	9			ខ្ល	٠,		88	.;		00		-	38	44.2	-	ő		Ξ.	22	-	9	7	(N	ĕ	7	ĭ,	72,	64	2	2	Ξ	≝	ζ.	Ď	~	=	ŝ	-	ĕ	_	30	= :	-	26	- 0
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103 100 103	1031/2 104 103 103 100 103 98	1031/2 104 103 103 100 103 98	1031/2 104 103 103 100 103 98	2 104 103 103 100 103 98	2 104 103 103 100 103 98	103 103 100 103 98	103 103 100 103 98	103 100 103 98	103 100 103 98	103 100 103 98	100 103 98	100 103 98	103 98	103 98	86	86	86	_	_	8	8		_	õ	9		8	₹		6			6	7	14	96		-	97	_	6	96	79	0	26	<u>~</u>	33	_	6	œ		6	-4	95	2		87	_	6		_	*	_	0	o
104 104 95 100 98 100 96 1	104 104 95 100 98 100 96 1	104 104 95 100 98 100 96 1	104 104 95 100 98 100 96 1	104 95 100 98 100 96 1	104 95 100 98 100 96 1	05 100 98 100 96 1	05 100 98 100 96 1	100 98 100 96 1	100 98 100 96 1	100 98 100 96 1	98 100 96 1	98 100 96 1	100	100	96	96	96	=	=	9	8		_	õ		_	ğ	0		6	_ :	-	ò	-	-	ő			8		0	'n		á		:	:	Ŧ	:	:	÷	õ	.	6	6	5	200	_	Š. 9	_		-	:	:	:
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100 101 98 100 95	100 101 98 100 95	100 101 98 100 95	100 101 98 100 95	101 98 100 95	101 98 100 95	98 100 95	98 100 95	100 95	100 95	100 95	95	95	95	95	: 95	: 95	: 95	-	-	95	95		_	:	:	÷	÷	:	÷	ó	~	_	6	8	_	6	~	_	93	-	ó	*	_	6	۰	~	95	_	6	5,	54	á		à		-	3		3	Ž,	2,1	4	_	٠.	4
10372105 99 100 98 100 98	10372105 99 100 98 100 98	10372105 99 100 98 100 98	10372105 99 100 98 100 98	2105 99 100 98 100 98	2105 99 100 98 100 98	86 100 88 100 66	86 100 88 100 66	100 98 100 98	100 98 100 98	100 98 100 98	86 100 86	86 100 86	100	100	86	86	86	-	-	66	66			ŏ	۰	-	8	œ	-	6		_	õ	œ	-	ŏ		-	96	_	0	53	201	ó	5,7	2	9	_	ď	œ	_	ó		٥	٥	٠,	9	_	5		5	2		2	4
2108 110 100 10832100 104 100 1	2108 110 100 10832100 104 100 1	2108 110 100 10832100 104 100 1	2108 110 100 10832100 104 100 1	110 100 108 100 104 100 1	110 100 108 100 104 100 1	100 1081/2100 104 100 1	100 1081/2100 104 100 1	1081,5100 104 100 1	1081,5100 104 100 1	1081,5100 104 100 1	12 100 104 100 11	12 100 104 100 11	104 100	104 100	100	100	100	=	=	1047	4	4	701	ğ	8	=	9	13	7	ತ	_	=	9	3	7	õ	7,	7	03		9	33	Ť	õ		=	5	-	2	2	-	5	~	2	3	=	22		2		=	8		2	8
1041/2/105 06 104 08 1102	100 000 000 000 000	17 100 1 00 1 00 1 00 1 00 1 00 1 00 1	100 000 000 000 000	200	17100 001 00 101	200	200	100	100	100	200	200																																																					

PRICES OF RAILROAD BONDS JAN. 1866—JAN. 1867

	z	High	72 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	JAN	Low	97 99 99 99 99 99 99 99 99 99 99 99 99 9
1	ن	High	98 102% 102% 103% 103 100 100 100 100 100 100 100 100 100
	DEC.	Low	97.7 92.2 92.2 92.2 93.7 7.7 90.2 10
	ν.	High	97.7. 102.7. 102.7. 102.7. 102.7. 102.7. 103
1	NOV.	Low	97 93 93 105 97 92 92 96 103 96 104 104 104 97 97 96 97 97 97 97 97 97 97 97 97 97 97 97 97
	OCT.	High	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7
i	8	Low	201 201 201 201 201 201 201 201 201 201
	T.	High	100 100 100 100 100 100 100 100
	SEPT	Low	98 7 100 100 100 100 100 100 100 100 100 1
	AUG.	High	101 101 101 101 101 101 101 102 103 103 103 103 103 103 103 103
1867	AL	Low	788888 78784 100 100 100 100 100 100 100 100 100 10
JAN.	MILY	High	901 901 103 103 103 101 101 101 103 103 103 1
AN. 1866—JAN. 1867	E	Low	888 888 881 101 101 100 100 100 100 100
JAN.	JUNE	High	2010 2010 2010 2010 2010 2010 2010 2010
	P.	Low	2000 2000 2000 2000 2000 2000 2000 200
	MAY	High	90 90 90 90 90 90 90 90 90 90 90 90 90 9
	M	Low	2008 2007 2007 2007 2007 2007 2007 2007
	APR.	High	201 201 201 201 201 201 201 201 201 201
1	AF	Low	884 1001 101 101 101 103 101 103 101 103 103
	MAR.	High	288883 201011 20101 201
	W.	Low	882 100 100 100 100 100 100 100 100 100 10
	FEB.	High	93 74 88 84 74 88 84 74 88 84 74 88 84 74 88 84 74 84 84 84 84 84 84 84 84 84 84 84 84 84
	E	Low	884 884 1000 1000 1000 1000 1000 1000 10
	JAN.	High	883 885 886 100 100 100 100 100 100 100 100 100 10
	JA	Low	92 83,12 83,12 85,12 103 101 94 94 94 96 100 900 900 900 900 900 900 900 900 900
	ž	9	00112111111111111111111111111111111111

PRICES OF RAILROAD BONDS JAN, 1867—JAN, 1868

		'm 'm' 'm 'm
JAN.	High	93.75 93.75 93.75 93.75 93.75 93.75 93.75 93.75 93.75 93.75 94.75 95.75 95.75 95.75 95.75 95.75 95.75 95.75 95.75
JA	Low	2000 : 00025 : 12000 :
	High	101 111 102 103 103 103 103 103 103 103 103 103 103
DEC.	Low	100 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	High L	1 74 74 : 75 : 75 75 75
NOV.		
	Low	85 103 1111/2 103 1111/2 1103 1103 1103 1103 1103 1103 1103 110
OCT.	High	98 8 8 8 1 1 1 0 0 2 2 8 8 8 8 8 8 1 1 0 0 0 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0
ŏ	Low	98 8 8 6 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
F.	High	88888 88917 96 5200 97 5000 97
SEPT.	Low	8886 % 888 %
	High 1	100 889 889 899 100 100 100 100 100 100 100 100 100 1
AUG.	Low H	288888 40 40 40 40 40 40 40 40 40 40 40 40 40
-	-	/43 /53 · /21/61/63 ·
JULY	w High	82 25 27 74 75 75 75 75 75 75 75 75 75 75 75 75 75
_	Low	288940110299 :80122699 :8
JUNE	High	86 25 25 25 25 25 25 25 25 25 25 25 25 25
Jū	Low	98 92 77 100 100 100 100 100 100 100 100 100
×	High	2000 2000 2000 2000 2000 2000 2000 200
MAY	Low	288824 2002022488884 2002022488884
_	High 1	2000 000 000 000 000 000 000 000 000 00
APR.	Low H	200 000 000 000 000 000 000 000 000 000
-		1 100 1 100 110
MAR.	v High	· · · · · · · · · · · · · · · · · · ·
rici.	Low	6/6/2/20
FEB.	High	001 0088 4401 1110 1110 1110 1110 1110 1
E	Low	997. 101. 101. 100. 100. 100. 100. 100. 10
rj.	High	25 24 27 27 27 27 27 27 27 27 27 27 27 27 27
JAN.	Low	2000 2000 2000 2000 2000 2000 2000 200
		2221001122110 222222011221122110 22222210011221110

PRICES OF RAILROAD BONDS JAN. 1868—JAN. 1869

	l a	%:
JAN.	w Hig	98.74 91.12 91.12 91.10 91.74 92.10 93.74
_	Low	8 : 8 : 0 : 0 : 0 : 0 : 0 : 0 : 0 : 0 :
DEC.	High	10034 112 112 100 100 103 103 103 103 103 103 103 103
н	Low	100 1111 1
NOV.	High	101 ½ 89 94 ½ 112 112 112 112 112 112 112 112 112 1
ž	Low	889 894 111 111 100 100 100 100 100 100 100 10
OCT.	High	101 102 102 103 103 103 103 103 103 103 103 103 103
00	Low	100151 88 877 88 877 88 877 88 877 89 97 1001 100 100
£.	High	1001 1005 1005 1005 1005 1005 1005 1005
SEPT.	Low H	100 100 100 100 100 100 100 100 100 100
		100 100 100 100 100 100 100 100
AUG.	Low High	1 1414100 141 100 1 101/01/00 101
		7 7 7 7 7 7 7 7 7 8 8 8 9 9 9 9 9 9 9 9
JULY	v High	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	Low	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
JUNE	High	103.7 95.7 95.7 1013.1 101
БĹ	Low	87.3 91.14 99.5 99.7 99.7 96.6 96.6 96.6 96.6 96.6 96.6
Z	High	100 5 100 100 100 100 100 100 100 100 10
MAY	Low	20027 20027
.,	High	102 103 103 103 103 103 103 103 103 103 103
APR.	Low	2888877 2888877 2010 1010 1010 1010 1010 1010 1010 1010
.:	High	1000 1000
MAR.	Low H	2001 2001
		2000 2000
FEB.	Low High	98888 98888 9888 9888 9888 9888 9888 9
		2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
JAN.	w High	7. 25. 25. 25. 25. 25. 25. 25. 25. 25. 25
	Low	88 88 100 100 100 100 100 100 100 100 10
2	2	011211211211211311211101110111011110111

PRICES OF RAILROAD BONDS JAN. 1869—JAN. 1870

JAN.	Low High	88.3 88.3 88.3 88.3 88.3 88.3 88.3 88.3
DEC.	High	883 884 100 100 100 100 100 100 100 100 100 10
Д	Low	28 8 2 2 4 8 2 2 2 2 2 2 2 2 2 2 2 2 2 2
NOV.	High	88 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
'Z	Low	72 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
OCT.	/ High	1001 1001 1001 1001 1001 1001 1001 100
	Low	25 25 25 25 25 25 25 25 25 25 25 25 25 2
SEPT.	w High	20 20 20 20 20 20 20 20 20 20 20 20 20 2
-S	gh Low	999 988 88 821 821 92 93 93 93 93 93 93 93 93 93 93 93 93 93
AUG.	Low High	888 886 888 888 888 888 888 888 888 888
	High L	88 88 88 88 88 88 88 88 88 88 88 88 88
JULY	Low H	88888888888888888888888888888888888888
8	High]	885 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
JUNE	Low	100 885 988 988 1112 101 101 100 98 100 100 100 100 100 100 100 10
MAY	High	88 88 88 88 88 88 88 88 88 88 88 88 88
M	Low	300: 22 22 22 22 22 20 20 20 20 20 20 20 20
APR.	High	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
۷	Low	8888912588 882828 74 74 75 15 15 15 15 15 15 15 15 15 15 15 15 15
MAR.	W High	74 74 74 74 74 75 75 75 75 75 75 75 75 75 75 75 75 75
	zh Low	2017888888888888888888888888888888888888
FEB.	Low High	988 885 35 98 88 85 35 98 98 98 98 98 98 98 98 98 98 98 98 98
_	High L	9875 9875 9875 9875 9975 9977
JAN.	Low Hi	988 3 8 8 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9
2	-	22222222222222222222222222222222222222

PRICES OF RAILROAD BONDS JAN. 1870—JAN. 1871

'n																				
	JAN.	High	94	92	103	9875	202	100	100%	766	102	7/96	94	95	88	102	86	1063/2	943%	!
	J.	Low	93	0.0	1023%	983	100	9814	66	766	100	6	94	62	88	100	95	10536	94	
	ن	High	93	913/2		86	100	973%	1001	103	103	95	941/4	:	87	1003/2	95	10514	9412	1021
	DEC.	Low	921%	8934		86	100	6	1001/2	102 1/2	103	94	9434	:	8634	9934	95	105	94	10212
		High	923/2			86	100%	86	991/2	102/4	104	95	9234	95	867%	100	9716	105	9812	102
	NOV.	Low	9212	189	i	97	200	9616	9912	102,4	104	93	91	95	895	993	97.16	104	9812	101
		High	92 1/2		:	:		1013%	100	102	104	9712	91)2	97.72	:	10315	100	1051/2	86	101
	OCT.	Low	9214	91	:	:		9912	100	102	104	951%	06	95	:	101	100	104	86	1001
1		High	92	161	104	:	\$8	9972	86	102	:	96	93	86	:	102		10519	26	101
	SEPT	Low	901/2	8=	104	:	* 8	9812	86	102	:	9415	91	6	:	100		10412	95	101
	ی	High	92	111	102	97	3	66		1000	102	96	9118	86	:	101	66	103	6	1001
	AUG.	Low	933%	10%	101	96	7.7%	86	:	90	101	95	911%	86	:	100	66	102	6	1001
	JULY	High	90	111	100	102 1/2	103	100	:	101	103	96	95	55		104	100	10814	96	103
	2	Low	94	133	100	102 1/2	103	766		100%	102	941/4	94	5	:	10332	100	108	9576	103
	E I	High	941/4	931/2	106	000	200	100	1031/2	:	105%	95	76	5	:	101 12	66	107	95	103
	JUNE	Low	88	92	103,	000	200	991/2	103 1/2	:	105	94	93	16	:	1001/8	66	107	32	102
1	٠,	High	9272		1053/2	86	993%	100	103	102/2	105	94	93	20%	:	101		107	66	1021/2
	MAY	Low	888%	8872	105	27.70	98%	86	101	10275	104	9314	93	S	:	100	:	1051/2	97.15	101
1	APR.	High	8837	933	106	60	28	102	101	102%	105	97.72	9314	3	913/2	103	10014	1053	97	66
	4	Low	88	923/2	104	95	88	101	101	101	5	95	93	9452	911/2	102	9934	10412	7696	66
	MAR.	High	8714	175	1051/2	96	36	102	103	203	10632	95	95	55%	90%	103	101	105	86	66 1
	M	Low	861%	_	=		8		_	-	-	-		_	_	=	₹.	=		
١,	FEB.	High	867.7	12	105	60	102	102	86	707	105	6	65	*	8	10	100%	103	9	8
	=	Low	83%																	
	JAN.	High	883	900	104	62	66	977	93	86	_	-	-	_		=	_	=		_
	7	Low	853%	_	-	-	<u>. </u>	196					200							
	Z		11	133	16	10	19	20	21	77	25	50	27	9 7	57	30	31	35	33	34

BONDS	377	
RAILROAD	LAN 1871 - LAN 1872	
PRICES OF	IAN	

11		g.	
	JAN.	High	25
		Low	1033 25 25 25 25 25 25 25 25 25 25 25 25 25
	DEC.	High	992 101327 10132
1	ā	Low	992 9012 9012 9012 9012 9012 9012 9012 9
1	>	High	93 7 7 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	NOV.	Low H	10 10 10 10 10 10 10 10 10 10 10 10 10 1
			14/4 . 14 . 14 Millia 14 Millia
	OCT.	v High	74
		Low	2010 1000
	SEPT.	High	201 101 102 102 102 103 103 103 103 103 103 103 103 103 103
	S	Low	927.7 1017.1 1017.1 1027.7 103
	AUG.	High	922 923 924 925 925 925 925 925 925 925 925 925 925
2	AU	Cow	20000000000000000000000000000000000000
JAN. 1812-JAN. 1013	>	High	93.75 110
į	JULY	Low H	14 . 100 lesta . 14 lesta . 14 100
18			M/4 /21/21 /21 /21 /21 /21 /21/21 /2/21
2	JUNE	v High	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	5	Low	8 103 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
1	MAY	High	222 222 222 222 222 223 223 223 223 223
	M	Low	911 911 106 % 100 100 100 93 % 99 % 99 % 99 % 99 % 99 % 99 % 99 %
	یہ	High	922% 1964% 1005% 1005% 1007% 1008% 1008% 1008% 1008%
	APR.	Low	991.7 1000.7 100
	2	High	923/4 105/4 106/4
	MAR.	Low H	9907 9907
			19/10 10 14 19/4 10/4 19/10 19/10
	FEB.	w High	10 /0 /0/0/ ·/0/0/0/0 /0/0/
		Low	124-124
	JAN.	High	93 105 105 105 105 105 105 105 105 105 105
	JA	Low	1011 1033; 1011 1011 1011 1011 1011 1011
1		ġ.	4383333333455255555555555555555555555555

PRICES OF RAILROAD BONDS Jan. 1873—Jan. 1874

	JAN.	High	100 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	
	JA	Low	101 102 103 103 103 101 101 101 100 100 100 100	881/2
	DEC.	High	1000 1000 1000 1000 1000 1000 1000 100	
	DE	Low	101 103 103 100 100 100 100 100 100 100	88
		High	100 100 100 100 100 100 100 100 100 100	88
	NOV	Low	96 100 100 100 100 90 98 88 88 88 88 90 90 90 90 90 90 90 90 90 90 90 90 90	878
	F	High	25 25 25 25 25 25 25 25 25 25 25 25 25 2	86
	OCT.	Low	100 100 100 100 100 91 91 101 101 101 10	83
	Ŧ.	High	· /4 · · · · /21/24/25 /24 : 74	90.
	SEPT.	Low	1013, 1013, 1053, 927, 927, 106, 106, 106, 106, 106, 106, 106, 106	897
	75	High	2000 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	923%
*101	AUG.	Low	004 005 005 005 005 005 007 007 007 007 007	200
4.7.	>	High	105 105 105 105 105 105 105 105 105 105	937
	JULY	Low	20100000000000000000000000000000000000	92
Dark Toro	ы	High	1016 1016 1016 1016 1016 1016 1016 1016	
1	JUNE	Low	2001 174 2008 100 200 100 200 100 200 100 200 100 200 2	100
	٧.	High	1000 1000 1000 1000 1000 1000 1000 100	8934
	MAY	Low	1011 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	10
		High	100 44. 100 44. 100 41. 100	
-	APR.	Low	100 100 100 100 100 100 100 100 100 100	
-	ر ا	High 1	100 4 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	_
	MAR.	Low	100 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
		High	1001 1001 1000 1000 1000 1000 1000 100	74
	FEB.	Low	1004 1005 1005 1006 1006 1006 1006 1006 1006	
1		High 1	103 104 105 105 105 105 106 106 107 108 108 108 108 108 108 108 108 108 108	
	JAN.	Low H	103 / 2 / 2 / 2 / 2 / 2 / 2 / 2 / 2 / 2 /	-
	1		50144232222222222222222222222222222222222	
1				

PRICES OF RAILROAD BONDS JAN. 1874—JAN. 1875

	r		
	ż	High	2001 000 000 000 000 000 000 000 000 000
1	JAN.	Low	74 : 24 : 24 : 24 : 24 : 24 : 24 : 24 :
	ij	High	8837 10101 100 100 100 100 100 100 100 100
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		Low	25 25 25 25 25 25 25 25 25 25 25 25 25 2
	SEPT.	High	1.001 242 25 25 25 25 25 25 25 25 25 25 25 25 25
	(3)	Low	105 105 100 100 100 100 100 100 100 100
	AUG.	High	103%; 101%;
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AN.	<u>ы</u>	High	1044 1044 1044 1007 1007 1008 1008 1008 1008 1008 1008
	JUNE	Low H	2000 2000 2000 2000 2000 2000 2000 200
		High	7 7 7 7 7 7 7 7 2 2 2 2 2 2 2 2 2 2 2 2
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		h Low	707/2 70% : 707/4 70
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	⋖	Low	1005 1005 1005 1005 1005 1005 1005 1005
	MAR.	High	105 105 106 100 100 100 100 100 100 100 100 100
	M	Low	201105 20
1	ai	High	2000 190 190 190 100 100 100 100 100 100
	FEB.	Low	890 20 20 20 20 20 20 20 20 20 20 20 20 20
		High I	2000 2000
-	JAN.	Low H	000 000 000 000 000 000 000 000
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	JAN.	Low High	112 104 104 105 105 105 105 105 105 105 105 105 105	
-	DEC.	High L	115 110 110 110 110 110 110 110 110 110	
	D	Low	115 1104 101 101 114 113 113 1103 14 1103 1103	
1	<u>۸</u>	High	1115 1105 1106 1106 1116 1117 1117 1106 1106 1107 1107	
1	NOV	Low	11100 1000 1000 1000 1000 1000 1000 10	
	OCT.	High	111274 110877 1000 1000 1000 1000 1000 1000 10	
-	_	Low	1112 1102 1103 1105 1107 1107 1107 1107 1107 1107 1107	
	SEPT.	v High	24 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	
-	_	h Low	7.2 7.2 7.4 7.4 7.5 7.4 7.4 7.5 7.4 7.4 7.5 7.4 7.4 7.5 7.4 7.4 7.5 7.4 7.5 7.4 7.5 7.5 7.5 7.5 7.5 7.5 7.5 7.5 7.5 7.5	
	AUG.	Low High	2011 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
-		High Lo	1110 1110 1110 1110 1110 1110 1110 111	
1	JULY	Low Hi	1109 1111 1121 1122 1123 1123 1123 1123 112	
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	JUNE	Low H	1113 1017 1017 1017 1017 1017 1017 1017	
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	APR.	High	11110101010101010101010101010101010101	
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-		gh Low	007 100 003 102 102 102 102 103 103 103 103 103 103 103 103 103 103	
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	ż	High	1110 1110
	JAN.	Low	21110 2717 2717 2717 2717 2717 2717 2717
	ن	High	1209 4 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	DEC.	Low	1111
ı		High	118 108 1177 1187 1187 1100 1100 1100 11
	NOV.	LOWE	1118 1107 1115 1115 1115 1100 1101 1107 1107
	· ·	High L	7 :4% 7 474 7 72%
١	OCT.	Low H	
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	SEPT.	w High	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7
Ì		h Low	2
١	AUG.	High	121 0665 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
18/	_ <	Low	10000000000000000000000000000000000000
AN. 18/6-JAN. 18/	JULY	High	1118 1005 1118 1107 1107 1108 1108 1108 1108 1108
18/6	25	Low	1117 1105;2; 1105;2; 1105;2; 1106;2; 1103;2; 1
ÀN.	JUNE	High	121: 105 125 125 125 125 125 125 125 125 125 12
	J.	Low	120
	×	High	110 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
	MAY	Low	1118 1000 1000 1000 1000 1000 1000 1000
	,	High	1: 12
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	-	High I	11108 6 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	MAR.	Low H	11157 27 111157
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	FEB.	Low High	/4/4 /4 /4/4/4/4 /4/4/4
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	JAN.	w High	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7
		Low	112
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SUNDA CLASSIFICATION PONDS

		High	1114 1114 1114 1114 1114 1114 1114 111
	JAN.	marine.	00 31 -731 A+ 30 /21/21/41 /4-44
		Low	008 00 00 00 00 00 00 00 00 00 00 00 00
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	ν.	High	1115 1107 1107 1107 1107 1107 1108 1107 1107
	NOV.	Low	114 110 007 110 008 008 008 009 107 107 118 118 118 119 119 119 119 119 119 119
		High 1	1112 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	OCT.	Low H	45.00 × 55.00 × 40.10 × 60.00
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Sall	(5	High	1118 1119 1119 1119 1118 1118 1118 1118
PRICES OF KALLROAD BONDS JAN 1877—JAN. 1878	AUG.	Low	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
4. 187	>	High	71000000000000000000000000000000000000
	JULY	Low E	14/10 14/4 24/4 74
1877	_		70 74 70 74/4/4/4
JAN	UNE	v High	14 14 14 14 14 14 14 14 14 14 14 14 14 1
E C	5	Low	1100 1100 1100 1100 1100 1100 1100 110
٠	×	High	1115 1118 1118 1118 1118 1100 1100 1100
	MAY	LOW	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7
	-	High	2000 2000
	APR.	Low H	<u> </u>
			7 1133 114 1153 114 116 116 116 116 116 116 116 116 116
	MAR.	High	8 5 4 4 8 4 4 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	A	Low	1004 1004 1004 1004 1004 1004 1004 1004
	mi	High	1115 1100 1100 1100 1100 1100 1100 1100
	FEB.	Low	1115% 109% 1100 1100 1000 1000 1000 1000 100
	1,2	High	100 100 100 100 100 100 100 100 100 100
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PRICES OF RAILROAD BONDS

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	JAN.	High	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
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	_	High	10 10 10 10 10 10 10 10
	NOV.	Low H	2214 2008 2008 2017 2017 2017 2017 2017 2017 2017 2017
		High L	70 . 4 . 14 /4 /4/4/4/4/4. 3
	OCT.	Low Hi	74 76 : : 14/4 24/4/4 14/4/4
			411.57
	SEPT.	v High	24
		Low	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	AUG.	High	11.25 11
1879	IV.	Low	111.2 111.2 111.2 111.2 111.2 111.2 111.2 111.2 111.2 111.2 111.2 111.2 111.2 111.2 111.2
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AN.	E	High	1112/2 1123/2 1123/2 1123/2 1123/2 1123/2 113/2 113/2
	JUNE	Low	10.00 10.00
	_	High 1	110 110 111 111 111 111 111 111 111 111
1	MAY	Low H	10.000
		High L	X: Y X: 22 2/22 2/2
	APR.	Low Hi	74 74 14 14 14 14 14 14 16 14 14 14 14 14 14 14 14 14 14 14 14 14
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	MAR.	, High	2 PA PA PAPER P P P P P P P P P P P P P P P P P P
1	- A	Low	28.9 :1-10 :10 :10 :10 :10 :10 :10 :10 :10 :10 :
	FEB.	High	11100 11110 1010 1010 1010 1010 1010 1
	E	Low	1118 1110 1110 1110 1110 1110 1110 1110
	ż	High	1114 1116 1116 1117 1117 1117 1117 1117
	JAN.	Low	11110 1110 1110 1110 1110 1110 1110 11
	1	3	480801284888888844444444

TABLE 3

YIELDS OF AMERICAN RAILROAD BONDS, MONTHLY, JANUARY 1857—JANUARY 1936

This table gives for each month the yield of each bond if held to maturity. The yields are based on the assumption that each bond is bought at the middle of the month and costs the arithmetic average of the highest and lowest prices of the month. The italicised yields are not based on actual price quotations but are interpolated. For a more com-

plete description of the bonds used in this table see Table 1.

This is a 'currency' or 'dollar' yield table. In other words all calculations have been based on the assumption that the buyers and sellers were interested only in legal tender without reference to its gold, 'commodity', or other exchange value. For example, if on Jan. 15th, 1863, an individual bought for \$1000 in greenbacks a one thousand dollar 6% bond maturing in exactly ten years and received as interest \$30 in greenbacks every 6 months until maturity and \$1030 in greenbacks at maturity, he would consider that he had received 6% on his investment throughout the ten years without any reference to how many ounces of gold he could have bought with the original 1000 greenback dollars or with any or all of the greenback interest payments or the 1030 greenback dollars received January 15, 1873.

The yields in this table therefore correspond to those which would be obtained by entering an ordinary bond yield table with the dollar (or 'greenback') purchase price. This was, of course, the form in which the

prices were actually quoted throughout the period.

VIELDS OF RAILROAD BONDS

		JAN	1857	AN. 1857-JAN. 1858	828										
Ref.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	
14321	Hudson River RR. 1st M. 78, 1869. Lichtago R. Roch is R.R. 1st M. 78, 1870. Lichtigh Coal R. Nar, 70, 70 mm M. 68, 1870. Link R. Reading N. 2 mm M. 68, 1870. New York & Harlom RR. 1st M. M. 78, 1870.	7.72 6.77 8.47 9.64	7.49 6.79 8.59 9.55	7.48 6.85 8.78 9.54	7.54 6.92 8.87 9.64	7.52 7.73 6.82 9.80	7.58 6.83 8.86 10.27	7.86 8.13 6.67 10.32	7.74 8.42 7.01 9.27	8.50 9.33 7.67 10.81	10.15 7.88 11.84 13.32	8.15 8.65 7.85 10.63	7.99 8.15 7.25 10.16 11.85	7.92 8.18 7.05 10.01 11.32	
20820	Lehigh Valley RR 1st M de 1873. Dergerin Gamp Se Deo 1st M de 1876 Esstern RK (Mass) og 1874. Esstern RK (Mass) og 1874. Permsylvania RN 1st M de 1880.	9.84 8.09 7.33	9.76 9.28 8.09 7.24 6.17	9.71 9.29 8.16 7.41	9.50 9.33 7.39 6.38	9.65 11.51 6.40	9.46 9.47 7.68 6.52	9.57 9.57 7.75 6.27	9.57 9.58 8.06 7.76	10.11 10.52 7.94 7.99 6.53	11.14 10.99 8.47 9.09 7.29	11.17 10.14 8.48 9.20 7.04	10.89 9.25 8.15 8.93 6.66	10.38 9.28 8.08 8.44 8.44 6.48	
1321	Camden & Amboy 6s Jan 1889. Camden & Amboy 6s 1883. IN Y C RR debt certificates 6s 1883.	8.18 8.09 7.18	8.21 8.04 7.13	8.31 8.16 7.05	8.33 8.29 7.18	8.33	8.68 7.37	8.89	8.90	9.78 9.85 8.90	9.95 10.24 9.11	10.09 9.73 7.44	9.60	9.08	211 2
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No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
40040	Hudson River RR 1st M 7a 1809 . Charlog & Rock 13 RR 1st M 7s 1870 Lehigh Ceal & Nav Co gen M 6s 1870. Lehigh Ceal & Nav Co gen M 6s 1870. New York & Harlem RR 1st M 1st 18 1833.	7.92 8.18 7.05 10.01	8.12 6.73 9.62	7.53 7.86 6.74 9.52 9.50	7.47 7.85 6.69 9.89 9.47	7.73 6.74 9.81 9.34	7.05	7.06 7.81 6.32 9.76	6.97 7.77 6.33 9.37	7.03 7.82 6.43 8.89 9.18	6.96 7.97 8.57 8.63	6.82 7.93 6.31 8.48 8.55	6.86 7.67 6.27 8.37 8.52	7.05 7.89 6.39 8.47 7.92
20870	Lehinh Valley RR 1st M 6s 1873. Morris Canal E Do 1st M 6s 1876. Eastern RK (Miss) 6s 1874. Eastern RK (Miss) 6s 1874. Permsylvania RK 1st M 6s 1890.	10.38 9.28 8.08 8.44 6.48		9.23 8.41 6.81 7.45 6.18	8.29 8.29 6.81 7.55 6.28	8.25 6.36 7.60 6.23	8.31 8.12 6.65 6.14	8.02 8.02 6.81 7.54 6.11	8.26 7.96 6.93 7.48 6.15	8.22 7.63 7.04 7.18 6.10	7.372	7.49 7.32 6.66 7.04 5.93	7.52 7.31 6.61 6.95	7.46 7.39 6.72 6.94 5.94
12222	Camden & Amboy 6s Jan 1889 Camden & Amboy 6s Jan 1889 Camden & Angoy 6s J883 Y C RR dote certificates 6s 1883 Nic Barl & Qiliqo'i sasumo 7s 1876 Nic Barl & Qiliqo'i sa N 8s 1883.	9.08 9.11 7.38 7.86 10.00	8.98 8.94 7.08 7.47 9.49	8.63 8.59 6.99 7.35 9.05	8.25 8.25 6.95 9.23	7.96 7.95 7.02 7.50 9.38	8.06 8.16 6.92 7.57	7.17 8.15 7.07 7.56 9.58		7.58 7.58 7.00 7.55 9.81	7.36 7.38 7.18 7.18 9.64	7.38 7.43 6.82 7.08 9.53	7.53 7.40 6.85 7.19 9.45	7.34 7.45 6.83 7.00 9.66

YIELDS OF RAILROAD BONDS JAN. 1859—JAN. 1860

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No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	
-004v	Hrdson River RR 1st M 7s 1869 Chicago & Rook 1s RK 1st M 7s 1870. Lchipt Cook Nav Co gen M 6s 1870. Linibi Cook Nav Co gen M 6s 1870. New York & Harlem RR 2sh M M 5s 1870. New York & Harlem RR 1st M M 7s 1873.	7.05 7.89 6.39 8.47 7.92	6.89 7.97 6.43 8.70 8.21	6.81 7.78 6.53 8.67 8.06	6.74 6.52 8.30 8.00	6.58 8.24 6.61 8.73 8.22	8.60 6.89 9.03 8.41	6.79 8.69 6.79 9.13 8.28	6.61 8.66 6.72 9.28 8.20	6.88 8.01 6.61 7.99	6.84 6.60 9.32 8.19	6.79 8.30 6.32 8.09	6.84 8.29 6.21 7.93	6.58 8.30 6.09 9.50 7.97	
92890	Lehigh Valley RR 1st M 6s 1873. Parir Ganal R E Co 1st M 6s 1876. Eastern RK (Mass) 6s 1874. Pemisylvana RX Znd M 6s 1875. Pemisylvana RX 1st M 6s 1880.	7.46 6.73 6.94 5.94	7.36 6.51 6.97 5.95	7.46 7.08 6.40 6.94 6.00	7.28 7.06 6.51 7.01 5.98	7.83 7.12 6.51 7.27 6.02	7.61 7.60 6.62 7.52 6.19	7.73 7.50 6.62 7.62 6.13	7.68 7.48 6.52 7.63 6.07	7.44 7.32 6.30 7.43 6.11	7.40 7.34 6.31 7.54 6.15	7.53 6.47 7.53 6.19	7.64 7.57 6.31 7.60 5.98	7.59 6.26 7.67 6.05	
12222	Camden & Amboy 6s Jan 1889. Canden & Amboy 6s 1883. N Y C RR debt certificates 6s 1883. N Y C RR for debt assumed 4s 1876. Chic Burl & Quincy 1st M 8s 1883.	7.34 7.45 6.83 7.00 9.66	7.13 6.84 7.08 9.74	7.43 6.85 6.86 9.82	7.47 7.48 6.76 9.79	7.63 7.54 6.72 7.08 9.74	7.75	7.54 7.71 7.01 7.31 9.80	7.65 6.94 9.56	7.58 7.59 6.79 7.19	7.46 7.54 6.78 7.07 9.34	7.59 7.71 6.77 7.11 9.45	7.60 7.81 6.81 9.52	7.63 7.64 6.89 7.04 9.60	
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Ref.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
-14m4m	Hudson River RR 1st M 7s 1869. Chingto & Rock 1s RR 1st M 7s 1870. Chingh Coal & Nav Co gern M to 1870. Linish Coal & Nav Co gern M to 1870. Linish & Reading RR 2nd M to 1870. New York & Hatlem RR 1st M M 7s 1873.	8.30 6.09 7.97	6.67 8.04 9.44 7.93	6.65 8.33 6.13 7.86	6.82 6.09 7.55	6.48 7.91 6.08 8.89 7.28	6.34 7.61 6.18 8.54 7.19	6.35 7.38 6.01 8.68 7.23		6.20 7.62 6.01 8.38 7.59	6.27 7.86 5.91 8.52 7.55	6.69 8.43 6.08 8.85 7.90	8.71 6.32 9.45 8.09	6.71 8.08 6.10 9.05 7.50
	Lehigh Valley RR 1st M 6s 1873 Morris Canal & Do 1st M 6s 1856. Eastern RK (Mass) 6s 1874 Pennsylvania RK 1st M 6s 1850.	7.59 7.45 6.26 7.67 6.05	7.42 7.25 6.31 6.06	7.24 7.10 6.31 7.42 6.05	7.13 6.97 6.26 7.42 6.02	7.04 6.93 7.27 6.08	6.80 6.96 7.26 6.07	6.73 6.69 5.73 7.36 6.01	6.76 6.75 5.68 7.22 5.92	6.77 6.77 5.81 7.10 5.93	6.75 6.76 7.20 5.90	7.27 7.16 5.88 7.39 6.19	7.66 7.47 6.21 7.78 6.34	7.38 7.28 6.00 7.72 6.02
122243	Camden & Amboy 6s Jan 1889. Canden & Amboy 9s 1883. N Y C RR debt certificates 6s 1883. N Y C RR to debt seamed 7s 19%. Chik Burl & Ohiney 1st M 8s 1883.	7.63 7.68 7.08 6.89 6.89	7.51 6.88 7.02 9.63	7.46 7.44 6.83 7.06 9.72	7.39 7.47 6.78 7.00 9.12	7.27 7.15 6.72 9.07	7.16 7.19 6.57 8.57	7.19 7.20 6.56 8.33	7.22 7.22 6.53 6.81 8.20	7.24 7.27 6.40 6.77 8.27	7.32 6.46 6.75 8.45	7.57 7.75 6.72 7.05 8.94	8.10 8.00 6.82 7.15 9.42	7.81 7.84 6.67 7.28 9.06

BONDS	25
IELDS OF RAILROAD	JAN. 1861-JAN. 180

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Ref.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	
20420	Chicago & Rock Is RR 1st M 7s 1870. Lehigh Codi & Nav Vo gren Me 98 1870. Pulla & Reading RR 2nd M 68 1870. New York & Hafriem RR 1st M 7s 1873.	8.08 6.10 7.50 7.38	7.9 9.19 7.35 4.7	7.19 8.93 7.33	7.91 7.37 7.37 7.37	8.70 6.17 7.55 7.55	8.28 6.33 7.72	7.99 6.01 9.13 7.61	8.17 5.93 7.66 7.37	8 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	8.28 6.10 7.86	8.54 6.52 9.36 7.71	8.23 6.38 7.63	7.43 5.89 8.52 7.12 6.91	
- 2001T	Morrie Canal & B Co 1st M 6s 1876. Morrie Canal & B Co 1st M 6s 1876. Pennsylvania (RR 2nd M 6s 1875. Pennsylvania (Rt 2nd M 6s 1880. Candensylvania (Rt 1st M 6s 1880. Candensylvania (St 2nd M 1880.				7.27 5.83 7.68 6.18	7.54 6.00 8.15 6.35 8.40	7.42 6.00 8.11 8.20	7.18 7.91 6.47	7.26 6.00 7.64 7.93	7.17 6.00 7.90 6.73 7.85	7.21 6.22 8.07 8.01	8.03 8.03 8.04 8.04	7.05 8.10 8.03		
1134112	Camden & Amboy 6s 1883. W V R R delve bertificates 6s 1883. N V C RX for dobts assumed 7s 1876. Hoffen Buf & Quoro; 1st M 8s 1883. Hudson River RR 2d M 7s 1885.	7.84 6.67 7.28 7.25	7.91 6.43 7.00 8.79	7.63 6.52 6.88 9.48 7.16	7.91 7.05 7.21 7.21	8.64 6.73 7.20 7.25	8.39 6.91 7.21 9.14	7.91 6.55 7.19 8.99 7.35	7.88 6.81 6.98 7.45	7.87 6.92 7.02 9.00 7.48	8.10 6.99 7.12 9.00 7.59	7.84 6.82 7.04 7.54	7.93 6.86 7.10 7.44		
		VIELDS OF RAILROAD BONDS	OF F	MILEC	AD BC	NDS									

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No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	
201-80	New York & Harlem RR 1st M 7s 1873 Lehigh Valley RR 1st M 6s 1873 Morris Canal & B Co 1st M 6s 1876 Bastern RR Klass 96s 1874 Pennsylvanis RR 2nd M 6s 1885	7.12 6.91 6.89 7.64	7.20 6.42 6.50 5.88 7.19	7.35 6.58 6.63 7.09	7.17 6.48 6.57 6.00 6.87	6.88 6.04 6.39 6.43	6.69 6.10 6.26 5.65 6.32	6.54 6.05 6.27 5.59 6.38		5.23 5.97 5.97 5.99	5.73 5.73 5.09 5.53		5.95 5.67 5.49	5.17 5.03 5.03 5.07	
12224	0 Pennaylvania RR 1st M 6s 1880. 1 Canden & Amboy 6s Jan 1889. 2 Canden e R. Amboy 6s 1889. 3 N Y C RR dolt certificates of 1889. 8 N Y C RR for debts assumed is 1879.	6.14 7.73 6.69 6.87	6.06 7.33 7.55 6.44 6.47	6.18 7.39 6.55 6.77	6.10 7.29 7.24 6.56 6.81	5.90 6.70 6.22 6.58	5.75 6.47 6.02 6.44	5.80 6.21 5.99 6.40	6.72 6.73 5.86 5.98	5.47 6.33 5.75 5.84	5.12 6.08 5.49 5.74	55.577	5.36 6.02 5.30 5.30 5.68	5.62 5.00 5.00 4.93	
15 17 18 19	Chite Burl & Quinoy 1st M 8s 1883 Chitekon River RZ JM N 18 1885 Chite & Nor West By 1st M st N 885 Haldedpink & Prete st M 6s 1881 Gall & Chit U RR 1st M 7s 1882	8.56 7.06 8.72 7.21	8.20 6.95 8.29 7.97 7.00	8.25 7.20 8.30 7.84 7.10	8.48 7.21 8.41 7.35	8.01 7.80 6.90 6.90	7.56 6.77 7.54 6.84 6.94	7.42 6.79 7.91 6.87	7.27 6.58 6.50 6.65	6.93 6.05 6.36 6.36 6.63	6.70 6.57 6.58 6.58	6.80 6.16 7.00 5.81 6.32	6.68 6.06 7.06 5.86 6.11	5.52 5.52 5.55	
20	Mich So & Nor Indiana 1st M 7s 1885. Cleveland & Toledo 1st M 7s 1885.	8.79	8.33	8.53	8.10	7.55	7.13	7.16	7.07	6.82	6.64	6.93	6.79	6.31	

YIELDS OF RAILROAD BONDS JAN. 1863-JAN. 1864

														1
Ref.	Name of Bond	Jan.	Feb.	Mar.	April	May	Эппе	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
100-80	New York & Harlem R.R. 1st M. 7s 1873. Lagh Yalloy R.R. 1st M 6s 1875. Morris Caml & B. Co. 1st M 6s 1876. Lagracem R.R. (Mass 96s 1874. Pennsylvania R.R. 2nd M 6s 1875.	5.17 4.87 5.03 5.07 5.07	4.96 4.41 4.69 4.65	5.28 4.57 5.02 4.63	5.75 4.86 5.32 4.73 5.09	5.54 4.93 5.28 5.17	5.38 4.99 5.32 5.17	5.38 5.22 5.22 5.22 5.27	5.70 5.04 5.15 5.15 5.30	5 4 9 9 9 7 9 9 9 7 9 9 9 7 9 9 9 7 9 9 7 9 9 7 9 9 7 9 9 7 9 9 7 9	5.74 5.41 5.41 5.35	5.35 5.35 5.35	55.35	5.54 5.68 5.61 5.49
51124	Pennsylvania RR 1st M 6s 1880. Candem & Mando 9s Jan 1889. Candem & Amboy 9s Jan 1889. Candem & Amboy 9s 1881. V C RR Greberstiffacts of 1883. N Y C RR for debts assumed 7s 1876.	5.62 5.79 5.00 5.00 5.00	5.63 5.63 4.71	5.70 5.70 5.14 4.91	5.87 5.83 5.25 5.17	5.70 5.22 5.04	5.74 5.74 5.55	5.06 5.75 5.81 5.62 5.56	5.26 5.67 5.58 5.31	5.13 5.72 5.64 5.64	5.13 5.76 5.40 5.40	55.55 5.47 7.47 7.47	55.55 5.50 5.50 5.50	5.36 5.98 5.96 5.41
15 17 18 19	Chic Burl & Quincy 1st M & 1883 Huston River 1X 20 M 18 1885 Chic & Your West Ry 181 M 17 18 1885 Thinkelphin & Frei et M 68 188 Gai & Chi U RR 1st M 78 1882	6.01 6.51 5.52 5.56	5.33 5.34 5.35 5.35	5.70 5.21 6.21 5.33	5.01 5.69 5.55 5.62 5.72	6.66 5.93 5.93	5.35 5.65 5.05 6.04	6.29 6.78 6.78 6.19	6.25 5.36 6.92 6.02	5.00 5.82 5.79 5.88	5.64 5.68 5.68 5.82	5.92 5.92 5.95	5.88 6.88 6.05 6.05	6.37 6.94 5.89 5.89 6.20
22222	Mitch So & Nor Indiana 1st M 7s 1885. Comn & Pass Rivers 1st M 7s 1885. Comn & Pass Rivers 1st M 7s 1876. Chindlo N Y & Edic 1st M 7s 1877. Chingao & Alton 1st M 7s 1893.	6.31 6.20 5.42 6.62	6.11 6.12 6.26 6.34	6.20 6.23 5.47 6.10	6.20 6.36 5.76 6.32 6.51	6.12 5.85 6.09 6.56	6.32 6.32 6.22 6.22	6.49 6.47 5.81 6.12	6.37 6.17 5.81 6.40 6.83	6.22 6.06 5.85 6.31 6.88	5.88 5.90 5.88 6.85	6.24 5.86 6.37 6.89	6.63 8.93 8.03 8.03 8.03	6.44 6.37 5.97 7.27
25	Pitts Ft Wayne & Chic 1st M 7s 1912	6.15	5.94	00.9	6.58	6,43	6.65	69.9	6.58	6.62	6.45	6.53	6.69	6.64

VIELDS OF RAILROAD BONDS JAN, 1864—JAN, 1865

		AFFEI	NDIA		
Jan.	6.60 6.16 6.08 5.50 5.50	5.43 6.09 5.80 5.46	6.82 6.88 6.03 6.45	7.14 6.58 6.48 6.42 6.78	5.64
Dec.	6.27 6.02 5.78 5.25	5.16 6.01 5.46 5.24	6.32 5.86 5.91 5.91	6.53 6.60 6.60 6.74	5.57
Nov.	55.73	5.01 6.00 5.25 5.37	5.36 5.54 5.62	6.35 6.60 6.90 6.73	5.50
Oct.	5.27 5.32 5.32 5.16	5.04 6.08 5.17 4.91	6.34 5.62 6.68 5.91 5.70	6.62 5.54 5.98 6.50 6.92	5.70
Sept.	5.53 5.04 5.11 5.11	5.67 5.67 5.69 3.92	6.12 5.25 5.25 5.25	5.95 5.95 6.83 6.83	5.88
Aug.	4.4.85 2.12 3.12 3.12	5.45 5.39 3.76	5.25 6.11 6.11 7.79	5.55.81 5.55.94 5.55.95	4.92
July	4.56 4.56 4.49 5.26 3.86	5.53 4.58 4.58	5.43 5.61 5.04 5.73	5.5.93	5.35
June	5.59 5.12 5.32 5.32 4.56	5.53 5.72 5.01 4.87	5.25 6.26 5.31 5.29	5.81 5.93 5.93	5.20
May	5.43 4.67 5.37 4.70	5.50 5.22 5.22	5.85 5.41 6.32 5.73	5.84 5.84 6.13 6.42	5.24
April	5.26 4.85 5.34 4.62	5.55 5.33 5.21	5.36 5.25 5.00 5.00	6.10 5.72 6.20 6.44	5.23
Mar.	5.79 5.28 5.67 5.54 5.00	5.92 5.92 5.47 5.40	6.00 5.77 6.72 5.57 5.72	6.16 5.97 5.84 6.24 6.50	5.38
Feb.	5.57 5.57 5.78 5.31	5.16 5.05 5.53 5.53	6.28 5.74 5.95 5.95	6.26 5.26 5.72 6.72 6.93	5.67
Jan.	5.68 5.68 5.68 5.49	5.36 5.98 5.96 5.67	6.37 6.80 6.20	6.37 5.97 6.67	5.65
Name of Bond	New York & Herine RR 1st M 's 1873 Libita Walley RR 1st M (se 1873 Morris Canal & B Co 1st M (se 1876 Bastern RR (Mass) (se 1876 Bennsylvania RR Zird M (s 1875)	Pennsylvania RR 1st M 6s 1880. Camden & Amboy 6s Jan 1889. Camden & Amboy 6s Jan 1889. V C RR del ceed riterate 8s 1883. N V C RR for debts assumed 7s 1876.	Chic Burl & Quincy 1st M & 1883. Little San River No. M is 1885. Chic & The World M is 1885. Chic & The Wrest Fy ist M is 1885. San Mandelpina & Perric ist M of 1881. San E Chic V R Ist M is 1885.	Mich & R. Vor Indiana 1st M 7s 1885. Cleveband & Diedo 1st M 7s 1885. Comn & Paga Kivers Kit st M 6s 1876. Comn & Page 1st M 7s 187. Chicago & Alton 1st M 7s 1897.	Pitts Ft Wayne & Chic 1st M 7s 1912. Camden & Amboy M 6s Nov 1889
Ref.	20000	31224	29286	22222	25 26 1

		JAZ	c. 1866-	Jan. 1866—Jan. 1867	1867									1
	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
ennsylv ennsylv amden amden	Pemisylvania RR 2nd M 6s 1875. Pemisylvania RR 1st M 6s 1880. Canden & Amboy 6s Jan 1889. Canden & Amboy 6s 1881.	7.44 6.51 7.59 7.90 6.88	7.56 6.65 7.91 6.91	7.84 7.98 7.05	7.03 6.16 7.92 7.20	6.72 6.08 7.18 6.78	6.97 6.89 7.27 6.81	6.96 6.11 7.14 7.36 6.57	6.70 6.14 7.12 7.22 6.78	6.94 6.99 6.99 6.68	6.90 6.92 6.93 6.71	6.54 6.87 6.90 6.61	6.01 6.05 7.06 6.63	6.73 6.93 7.12 6.78
N Y C R Chic Bur Hudson Chic & N Philadel	N. Y. C. RR, for debts assumed 7s 1876. Holdson River RR, 2d M. 7s 1853. Holdson River RR, 2d M. 7s 1855. Philadelphia & Efer Jst M. 6s 187 1885. Philadelphia & Efer Jst M. 6s 1881.	7.01 7.10 6.96 8.21 7.55	7.00 7.10 8.06 7.34	7.02 7.21 7.11 8.45 7.16	7.01 7.38 7.06 8.33 7.15	7.07 7.05 7.09 7.09	7.06 6.96 7.18 7.18	6.93 7.20 7.44 7.19	6.89 7.04 6.80 7.34	6.84 7.05 6.91 7.54 7.10	6.23 7.09 6.80 7.57	6.37 6.94 7.51 6.92	7.05 7.05 7.57 6.99	7.03 6.88 6.77 7.63
fich So levelan huffalo	Gaf & Chi U RR 1st M 7s 1882. Michic Se Wor Chafman 1st M 7s 1885. Cleveland & Tolicdo 1st M 7s 1885. Cleveland & Tolicdo 1st M 7s 1885. Cherga & Atton 1st M 7s 1897. Chicago & Atton 1st M 7s 1895.	7.15	7.82 7.82 7.99 7.63	7.49 7.83 7.75 8.15	7.48 7.81 7.66 8.16 7.63	7.59	7.74	7.35 6.98 7.78	7.22 7.61 6.75 7.87	7.07 7.36 6.95 7.20	7.16 7.33 6.90 7.98	7.16 7.33 6.95 7.78	7.29	7.36 7.59 7.79 7.15
Pitts Ft Camden Tol & W St L Alt	Pitts Ft Wayne & Chic 1st M 7s 1912. Camden & Amboy M 6s Nov 1889. Tol & Wasash 1st M 7s 1890. Set LAlton & TH RR 1st M 7s 1894.	7.00 6.90 8.15 7.77	7.14 6.99 8.27 7.78	6.81 8.41 8.01	6.71 8.24 8.08	7.09 6.71 8.18 8.18	7.11 6.62 8.20 8.15	6.91 6.58 8.16 7.92	6.92 6.56 7.82 7.97	6.92 6.42 7.77 7.94	7.10 6.38 7.78 7.90	6.85 6.36 7.89 7.82	7.03	6.95 6.55 7.96 7.82

VIELDS OF RAILROAD BONDS

	A4	0			APPE	ıIN.
-	Jan.	6.15 7.27 7.37 6.97 7.03	7.03 6.86 7.54 7.03 7.19	7.37 6.93 7.02 6.88	6.49 7.60 7.32	
	Dec.	6.23 7.60 7.03 7.10	7.20 6.93 7.10 7.20	7.49 6.98 8.60 7.04 6.84	8.29 7.66 6.87 7.41	
	Nov.	6.31 7.62 7.69 6.87 6.85	7.106	7.37 7.01 8.63 6.97	6.67 8.34 7.73 6.84 7.42	
	Oct.	6.25 7.59 6.90 6.88	7.04 6.79 7.62 6.94	7.33 6.92 8.59 6.94 6.79	6.54 8.21 7.67 6.69 7.36	
	Sept.	6.17 7.34 7.28 6.65 6.65	6.93 7.50 6.90 6.90	7.24 6.90 8.64 6.94 6.75	6.55 8.07 7.81 6.73	
	Aug.	6.17 7.13 7.24 6.65 6.55	6.84 7.56 7.56 7.03	7.28 6.89 8.38 6.89 6.74	6.52 8.09 7.94 6.89 7.38	
	July	6.25 7.38 7.26 6.62 6.45	6.76 6.76 7.64 6.96 6.98	7.25 6.78 8.42 7.04 6.83	6.54 7.91 6.68 7.38	
-	June	6.38 7.37 7.38 6.48 6.80	7.19 6.86 8.00 6.99 7.21	7.34 7.02 8.49 7.19	6.63 7.96 7.96 7.48	
	May	6.32 7.23 7.40 6.69 6.72	7.15 6.87 7.89 6.94 7.23	7.38 7.06 8.40 7.21	6.54 8.26 8.19 6.68 7.48	(DS
808	April	6.80 6.80 6.63	7.77	7.38 7.00 8.16 7.22 7.03	6.52 8.29 8.10 6.88 7.59	D BO
AN. 1867—JAN. 1868	Mar.	6.17 7.22 7.22 6.76	7.03 7.65 7.24 7.24	7.33 7.00 8.01 7.15	8.16 7.88 6.64 7.50	ILROA
N. 186/	Feb.	6.10 7.27 6.83 6.63	6.94 7.67 7.24 7.34	7.47	6.58 8.07 7.70 6.60	OF RA
JA	Jan.	6.93 7.12 6.78 7.03	6.88 6.77 7.10 7.30	7.59 7.12 7.79 7.15 6.95	6.55 7.82 7.82 7.42	VIELDS OF RAILROAD BONDS
	Name of Bond	Pennsylvania RR 1st M 6s 1880. Camelor & Amboy 6s Jan 1889. Camelor & Amboy 6s 1883. N Y C RR debt certificates 6s 1883. N Y C RR debt certificates 6s 1883.	Chie Burl & Quincy 1st M 8s 1883 Hadran River RZ 2M M"s 1885. Chie & New West RY 1st M si 7s 1885. Hadrelphia West Fix 1st M si 7s 1885. Gal & Chi U RR 1st M 1s 1885.	Mitch So & Nor Indiana 1st M 7s 1885. Cloredand & Todot 1st M 7s 1885. Infrato W. & Erle 1st M 7s 187. Pitrs & Wayne & Colo 1st M 7s 197. Pitrs & Wayne & Colo 1st M 7s 197.	Canden & Amboy M Gs Nov 1889. Jol & Withean 1st M 's 1889. M. L. Amon & T H H st M 's 1894. 'A Contral revensh bonds of 1887. Morris & Essex 1st M st 7s 1914.	IX
	Ref.	01224	120	25 25 25 25	320 230	

			N. 186	JAN. 1868-JAN. 1869	6981				1	ĺ				1
No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
13 13 15 15	Pennsylvania KR 1st M 6s 1880. Camden & Anboy 6s Jan 1889 Anboy 6s 1883. N'Y CR deby certificaties 6s 1883. Chite Burl & Quincy 1st M 8s 1883.	6.15 7.27 7.37 6.97	6.08 7.15 6.87 6.85	6.77 6.77 6.77	6.03 7.28 7.37 6.61 6.83	5.95 7.16 6.64 6.85	5.95 7.18 6.67 6.92	6.02 7.20 7.19 6.56 6.96	6.08 7.34 6.58 6.80	6.12 7.44 6.77 6.94	6.12 7.36 7.51 6.85 6.93	6.14 7.46 7.46 7.02	6.24 7.48 7.62 7.03	6.22 7.50 7.66 7.20 6.84
16 17 18 19 20	Hudson River RR 2d M 7s 1885. Think & You West My 1st Me 187 s Philadolphia & Eric Ha Me 187 s. Ref. & Chiu C Hast Ha Me 182. Mich So Wor Indiana 1st M 7s 1885.	6.86 7.54 7.03 7.37	6.83 7.61 7.15 7.23	6.73 7.62 7.08 7.11	6.68 7.94 7.11	7.58	6.98 7.35 7.20 7.01	6.77 7.39 7.30 7.30	6.62 7.34 6.92 7.13	6.75 7.30 7.07	6.75 7.20 7.00 7.25	7.56 7.56 7.18 7.18 7.35	7.99	6.61 7.69 8.04 7.31
21 23 24 25 26	Cleveland & Toledo 1st M 7s 1885. Chicato & Alton 1st M 7s 1857. Chicato & Alton 1st M 7s 1893. Charles F Wayne & Chic 1st M 7s 1912. Canden & Amboy M 6s Now 1889.	6.93 7.02 6.88 6.49	6.83 6.33 6.33	6.95 8.14 6.71 6.46	6.97 7.00 6.74 6.44	6.93 6.35	6.93 6.85 6.37 6.37	6.91 6.73 6.73 6.37	8.90 7.08 6.81 6.81	7.13 8.18 7.04 6.75 6.50	7.16 7.07 6.70 6.50	6.96 7.17 6.95 6.95	7.04 8.97 7.04 6.70	7.06 8.94 7.04 7.04 6.77
27 28 30 31	Tol & Wahnsh 1st M 7s 1800. St. LAIOn & T H RK 1st M 7s 1894. N Y Central removal bonds 6s 1887. Morisk Essex 1 H M ff 7s 1914. N V & Prie RR 1st M ff 7s 1914.	8.08 7.60 7.32 6.90	7.94 7.58 6.73 7.33 6.81	7.91 7.63 7.29 6.81	7.95	7.85 7.66 6.69 7.13	7.62	7.84 7.57 6.59 7.08 6.81	7.64 6.46 7.07 6.84	7.90 7.60 7.15 6.31	8.00 7.67 7.22 6.89	7.90	7.99 7.78 7.30 6.95	7.89 7.00 7.38 6.93

VIELDS OF RAILROAD BONDS JAN. 1869—JAN. 1870

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Jan.	6.39 7.86 7.55 7.07	6.80 7.93 7.90 7.50	7.82 7.25 6.89 6.78 8.29	7.76	6.58
Dec.	6.61 7.78 8.29 7.85 7.05	7.19 7.92 7.33 7.57	7.83 7.29 7.17 6.68 8.48	7.98 7.38 7.44 8.05	6.67
Nov.	6.61 7.77 8.19 7.48 7.40	7.30	7.62 7.21 7.20 6.57 8.41	8.00 7.24 7.34 7.46 8.16	6.72
Oct.	6.51 7.87 8.11 7.43 7.33	6.94 8.02 7.82 7.31	7.47 7.12 7.20 6.64 8.30	7.88 7.13 7.28 7.54 8.13	99.9
Sept.	6.32 7.77 7.85 7.35	6.95 7.72 7.37 7.37	7.22 7.15 7.03 6.71 8.20	7.73 7.27 7.39 8.05	6.63
Aug. S	6.25 7.78 7.16 7.15	6.86 7.47 7.48 7.38	7.15 6.95 6.68 8.12	7.86 6.89 7.35 7.92	6.56
July	7.98	7.03	7.24 7.05 6.93 6.71 8.21	7.71 6.99 7.32 7.88	6.52
	6.23 7.44 7.61 7.00 7.01	7.08 7.72 7.732 7.32 7.23	7.22 6.91 7.82 6.87 8.07 8.07	7.74 6.88 6.88 7.11 7.11 7.86	6.52 6
y June					
Мау	7.47 7.47 7.10 1 6.95	2 7.55 7.25 7.25 7.25	2 7.29 8 6.88 6.69 7.99	7.85 7.7.15 7.025 7.115 7.85 7.85	6 6.62
April	6.34 7.58 7.31 7.01	6.99 7.52 7.52 7.45	7.32 7.09 6.98 6.78	7.77 7.15 7.25 7.25 7.92	99.9
Mar.	7.28 7.21 7.21 6.92	6.94 7.63 7.36 7.69	7.19 6.96 6.85 8.01	7.73 7.28 7.28 7.07	6.64
Feb.	6.32 7.53 7.48 7.16 6.80	7.00 8.01 7.31	7.17 6.99 6.99 7.83	7.71	6.58
Jan.	6.22 7.50 7.50 7.20 6.84	6.61 7.69 8.04 7.31	7.04 7.04 7.04 6.77	7.73 7.00 7.38 6.93 7.93	6.54
Name of Bond	Pennsylvania RR 1st M 6s 1880. Candie & Alboy 6s 18al 889. Candien & Anboy 6s 18al 889. N Y C RR debte certificates 6s 1883. Chie Burl & Quitoy 1st M 8s 1883.	Hudson River RR 2d M 7s 1885 The R Now Week Y1 st M 77 1885. Philadelphia & Eric 1st M 6s 1881. Add & Chi U Rr 1st M 7s 1882. Mich Soe Now Indiana 1st M 7s 1885.	Cleveland & Toledo 1st M 7s 1885. Cleveland & Toledo 1st M 7s 1933. Pitts FV Wayne & Chic 1st M 7s 192. Pitts FV Wayne & Chic 1st M 7s 192. Toledmen & Ambony M 6s 100 V 1889. Tole & Wabani 1st M 7s 1890.	St. L Alton & T. H RR. 1st. M. 7s 1894. W. Central renoved bonds of 1887. Morris & Essen ist. M. 67 s 1914. W. & Eric RR. 1st. M. 7s 1907. M. & St. P. Cr. 1st. M. 7s 1908. M. & St. P. P. du. Ch. dv.) 1st. M. 8s 1898.	Lehigh Valley RR 1st M 6s 1898
Ref.	12222	20110	28222	33133	33

VIELDS OF RAILROAD BONDS JAN. 1870—JAN. 1871

April May June July Aug. 7437 7,187	April May June July Aug. Sept. 7.33 7.31 6.82 7.00 6.88 7.20 7.15 7.15 7.15 7.15 7.15 7.15 7.15 7.15	Ayril May Jume July Aug. Sept. Oct. 733 7.38 7.38 7.49 6.88 7.00 6.88 7.00 6.89 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 6.80 7.00 7.00 7.00 7.00 7.00 7.00 7.00 7	Ayril May Jume July Aug. Sept. Oct. 7, 231 7, 121 7	April May June July Aug. Sept. Oct. Nov. 1718 7718 7718 7718 7718 7719 688 770 689 770 699 7718 7718 7718 7718 7718 7718 7718 77	Name of Bond Jan. Feb. Mar	Turniden & Amboy 6s Jan 1889 7.67 7.47 7.47 1.47 1.47 1.47 1.47 1.47 1.4	The Chick Now West Ry is M of 1s 1885. 7.99 7.39 7.39 7.39 7.30 7.30 7.30 7.30 7.30 7.30 7.30 7.30	Chicago & Alton 1st M 7s 1893. C. 25 6.90 6.85 25 Pictor R. Warden Chicago & Alton 1st 75 6.90 6.77 6.05 26 Camedra Ramboy M 68 78 78 78 6.07 78 6.07 6.07 6.07 6.07 6.07 6.07 6.07 6.07	N V Central renewal bonds 6a 1887 7.20 7.20 7.00 Morbie Extern et al. 1887 7.21 7.21 7.21 7.21 7.22 Morbie Extern et al. 1887 7.23 Morbie Extern et al. 1887 7.23 Morbie Extern et al. 1887 7.23 7.23 Morbie Extern et al. 1887 7.23 7.23 7.23 7.23 7.23 7.23 7.23 7.2	The state of National Towns of the State of
May June July Aug. 7.11 0.88 7.74 0.	May June July Aug. Sept. 7.18 6.87 7.00 6.88 7.01 7.18 6.87 7.00 6.88 7.01 7.18 6.87 7.00 6.88 7.01 7.18 7.00 6.70 6.88 7.00 7.18 7.00 7.00 6.99 7.00 7.19 7.00 7.00 7.00 7.10 7.10 7.00 7.00 7.10 7.00 7.00 7.00	May June July Aug. Sept. Oct. 7,115 6,87 7,00 6,88 7,00 6,90 7,715 6,715 7,00 6,88 7,00 7,10 6,88 7,00 7,10 6,88 7,00 7,10 6,88 7,00 7,10 6,88 7,00 7,10 6,80 7,10 7,10 7,10 7,10 7,10 7,10 7,10 7,1	May June July Aug. Sept. Oct. 7, 131	May June July Aug. Sept. Oct. Nov. Doc. 7,118 (2) 88 7100 6.28 7.28 7.38 7.38 7.38 7.38 7.38 7.38 7.38 7.3	Mar. Apri	7.44 7.69 7.27 6.79 6.64 6.64	7.54 7.67 7.24 7.6.97 7.11	6.89 6.69 6.76 6.72 7.72 7.83 7.83	7.09 7.07	
June July Aug. 1.187 1.00 6.88 1.00	June July Aug. Sept. 10.00 (6.88) (6.80) (6.	June July Aug. Sept. Oct. 18, 20, 20, 20, 20, 20, 20, 20, 20, 20, 20	June High Aug. Sept. Oct. 1, 123 1, 124 1, 1	June July Aug. Sept. Oct. Nov. Dec. 6.18 (170) 6.88 (170) 6.88 (170) 6.89 (170) 6.89 (170) 6.89 (170) 6.89 (170) 6.89 (170) 6.89 (170) 6.99 (17		1				
Aug. Aug. Aug. Aug. Aug. Aug. Aug. Aug.	July Aug. Sept. 17.17.17.17.17.17.17.17.17.17.17.17.17.1	July Aug. Sept. Oct.	July Aug. Sept. Oct. 17,194 Aug. Sept. Oct. 17,194 G. St.	July Aug. Sept. Oct. Nov. Dec.		ĺ				
100000 00000 00000 00000	Sept. 200 200 200 200 200 200 200 200 200 20	Sept. Oct. 12.12.12.12.12.12.12.12.12.12.12.12.12.1	Sept. Sept	Fepr. Oct. Nov. Dec. 15.00	July	1				
	1 10 11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Oct. 7.22 7.72 8.00 8.00 8.00 8.00 8.00 8.00 8.00 8.0	Oct. 1.22.4.7.7.7.2.4.9.5.6.6.5.8.8.0.2.2.4.7.7.7.2.4.9.7.7.7.2.4.9.7.7.7.2.4.9.7.7.7.2.4.9.7.7.7.2.4.9.7.7.7.2.4.9.7.7.7.2.4.9.7.7.7.2.4.9.7.7.7.2.4.9.7.7.7.7.2.4.9.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7	Oct. Nov. Dec. 100 9 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		6.83 6.83 6.97	7.42 7.18 7.18 7.26	7.06 6.96 6.58 7.92 7.26	7.15 7.15 7.26 7.81 6.33	

VIELDS OF RAILROAD BONDS JAN. 1871—JAN. 1872

No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
13221	Camden & Amboy 6s Jan 1889. Camden & Amboy 6s 1883. V C RR debt certificates 6s 1883.	6.69	6.98	6.74 7.13	6.99 7.15	6.94 7.13 7.02 6.76	7.17	01.12	7.13	7.18	7.24	7.25	7.71	7.14 7.43 6.86 6.25
	Chie bull by Minh as In a 8885. Chie & Nor West Ry 1st M of 78 1885.			7.17	7.33	7.27	7.36	7.25	7.03				7.00.47	6.96
2022	Philadelphia & Erie 1st M 6s 1881 Cal & Chi U RR 1st M 7s 1882 Mich So & Nor Indiana 1st M 7s 1885	7.28	7.24	7.20	7.04	6.94	6.95	10.00	6.862	6.90	7.15	7.12	7.05	6.48
	Chrysland & Lyck M. 18 1893. Chicago M. 18 18 1893. Canden & Amboy M. 6 Nov 1889. Tri R. Warsel 1st M. 18 190.	7.09 6.95 6.57 7.93		7.00 6.92 6.61 7.86	6.98	6.94 6.82 6.53	6.93 6.81 6.50	6.8 7.53 8.60 8.60 8.60	6.81 7.57 7.46	6.63	6.67	6.93	6.76	6.68 6.56 7.26
	St. L. Alton & T. H. RR. 1st M. 7s 1894 N. V. Central renewal bonds 6s 1887 North & Essex 1st M. 8s 17s 1914 N. V. & Eric RR. 1st M. 7s 1897	7.48	6 7.63	7.96 6.96 7.35	7.52	6.87	7.16	6.87 7.06 7.06 7.06	7.02				7.01	6.83 7.01 7.41
	M & St. F (F du Ch dy') 18t M 88 1099. Lehigh Valley RR 18t M 68 1898. Central RR of New Jersey M 78 1890.	7.00		7.01	7.00	6.35	6.39	6.94					6.46	6.48

APPENDIX

VIELDS OF RAILROAD BONDS JAN. 1872—JAN. 1873

Jan.	7.37 7.20 6.45 6.74 6.75	6.96 6.88 6.74 6.53	7.00	6.48 6.73 7.70 7.70	6.98 6.86 7.83
Dec.	7.29 6.72 6.79 6.94	7.03 6.93 6.91 7.35	7.23 7.30 6.78 6.95 7.64	6.51 6.94 6.62 7.82 7.74	7.04 6.86
Nov.	7.26 7.41 6.74 6.98	7.01 6.92 6.91 6.50	7.15 7.50 6.88 6.88 7.58	6.37 6.96 6.57 7.84 7.64	7.03 6.83 7.63
Oct.	7.27 6.60 6.57 7.01	6.95 6.78 6.86 6.42 7.67	7.12 7.02 6.87 6.95	6.37 6.88 6.50 7.81	7.02 6.83
Sept.	7.14 7.55 6.39 7.08	6.93 6.78 6.41 7.69	7.14 6.96 6.96 6.97 7.47	6.29 6.82 6.36 7.54	6.99
Aug.	6.38	6.87 6.69 6.71 6.34 7.54	7.13 7.08 6.83 6.90 7.37	6.22 6.66 6.33 7.78	6.96
July	7.30 6.73 6.83 6.83	6.81 6.77 6.36 6.36 7.35	7.12 6.64 6.85 7.45	6.18 6.57 7.64 7.46	6.95
June	6.91 6.91 6.61 6.61 6.84	6.89 6.77 7.47 7.47	7.25 6.70 6.71 7.54	6.26 6.67 7.43	6.99
May	7.35 6.56 6.59 6.89	6.94 6.79 6.78 7.46	7.26 6.90 6.82 7.91 7.53	6.30 6.69 7.66 7.43	7.00
April	7.25 6.51 6.91 6.91	6.95 6.73 6.58 6.58 7.40	7.26 6.88 6.80 7.91	6.46 6.68 7.71 7.48	7.06
Mar.	7.25 7.15 6.41 6.81	7.17 6.70 6.76 6.56 7.32	7.42 6.88 6.99 7.44	6.47 6.68 6.68 7.77 7.45	7.06
Feb.	6.31 6.31 6.39 6.80	6.76 6.61 6.65 6.52 7.17	7.32 6.72 6.74 7.42	6.43 6.62 6.57 7.59	7.00
Jan.	6.86 6.25 6.43 6.77	6.65 6.65 7.26	6.83 6.77 7.01	6.64 6.64 7.61 7.61	6.98
Name of Bond	Candion & Amboy 6s, 1883. Chick R. Chucker certificates 6s, 1883. Chic Burl & Quinoy 1st Al. 8s, 1883. Hudson River REA 2d M. 7s, 1885. Mich So & Nor Indiana 1st M. 7s, 1885.	Chicareland & Toledo 1st M 7: 1885. Chicago & Manos M 18 1893. Plats R Wanne & Chic M 18 1893. Charden & Almoy M 68 1909 1899. Tole & Walanda 1st M 18 1890.	A Lone & T H RR. 1st M 7s 1894. V Central Frenewal bonds 6s 1887. V Central Frenewal bonds 6s 1887. V R. Elfer RR. 1st M 7s 1897. & S. E. P. Crut Cin (dy) 1st M 8s 1898.	Lichigh Valley Ri 1st M 6s 1888. Central RX of New Teres M 7s 1890 Lishigh Oral & New Crex Loan 6s 1897 Lichigh Oral & New CreX Loan 6s 1897 Lake & Millennier RX 1st M 7s 1898 Lake Sinor Sy Driviand bonds 7s 1899.	Cley Col Cin & Ind 1st M sf 7s 1899. Lehigh Valley RR 2nd M reg 7s 1910 Chic & Nor West Ry cons sf 7s 1915.
No.	SESSE SESSE	22 22 22 24 24 24 24 24 24 24 24 24 24 2	XXXXX 333338 333338	24888 70707	238 070

YIELDS OF RAILROAD BONDS Jan. 1873—Jan. 1874

								-						1	
4,0	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	
22720	Hudson River RR 2d M 7s 1885 Gleveland & Toledo 1st M 7s 1885 Cleveland & Toledo 1st M 7s 1885. Cleveland & Toledo 1st M 7s 1895. Pitts R Wayne & Calo 1st M 7s 192.	6.74 6.96 6.96 6.88 6.74	6.85 7.00 6.82 6.70	6.78 7.06 6.87 6.87	6.74 6.82 7.00 6.84 6.59	6.59 6.96 6.80 6.72	6.43 6.88 6.77 6.69	6.52 6.90 6.70 6.70	6.65 6.71 6.96 6.57 6.66	6.73 6.97 6.77 6.69	6.95 7.23 7.10 6.95	7.10	7.10 7.13 7.16 6.96 6.98	6.85 6.90 6.74 6.69	
328278	Canden & Amboy M 6s Nov 1889. St. L. Alton & T. H. Rt. 181 M 1879. St. L. Alton & T. H. Rt. 181 M 18189. W. Central travewal bodh 3s 1887. Morris & Essex 1st M 18 1914.	6.53 7.35 7.00 6.79	6.53 7.45 7.02 6.76	6.57 7.56 7.01 6.79	6.64 7.19 7.19 6.85	6.56 7.29 7.17 6.80	6.56 7.21 7.21 6.71	6.47 7.21 6.94 6.77	6.41 7.13 7.00 6.75	7.55 7.44 7.01 6.99	6.94 7.89 7.83	6.81 8.16 7.78 7.78	6.92 7.33 7.41 6.85	6.47 7.07 7.25 6.77	
333333333333333333333333333333333333333	N Y & Eric RR 1st M 7s 1897 Libit & St P (Pt Ur) Ld V1 st M 8s 1898 Libit Valley RR 1st M 6s 1893 Certarl RR of New Jessey M 7s 1890 Libits Cost & New Co RR Loan 6s 1897	7.01 7.63 6.48 6.73 6.73	6.99 6.49 6.76 6.62	6.95 6.78 6.06	7.00 7.53 6.34 6.84 6.76	6.36 6.36 6.77 6.77	6.89 7.48 6.46 6.77	6.85 7.46 6.47 6.58 6.81	6.82 6.51 6.51 6.77	6.55 6.55 6.99	7.13 7.88 6.69 7.54	7.16 8.15 7.24 7.13	7.08 7.85 7.08 7.08	6.98 6.31 6.77	
38 39 39 40	Chicago & Milwaubee RR 1st M 7s 1898 Les Shore W dividen bonds 7s 1899 Chev Col Cin & Ind 1st M st 7s 1899 Chev Col Cin & Ind 1st M st 7s 1899 Chev Col Cin & Ind 1st M st 7s 1990 Chev Col Cin & Ind 1st M st 7s 1990 Chic & Nor West R. And M reg 18 1915	7.70 7.76 6.98 6.86 7.83	7.64 6.97 6.79 7.80	7.69 6.99 6.77 7.86	7.75 7.67 7.02 6.78 7.94	7.69 7.70 6.90 7.95	7.65	7.67 7.53 6.77 6.86	7.70 7.62 6.77 7.74	7.78 7.07 6.92 7.97	8.14 8.41 7.00 8.53	8.11 8.45 7.34 8.57	8.08 8.08 8.08	7.72	
41	L Sh & Mich So cons 1st M sf 7s 1900	7.15	7.17	7.22	7.28	7.34	7.33	7.07	7.12	7.58	8.13	8.21	7.97	7.40	

YIELDS OF RAILROAD BONDS JAN. 1874—JAN. 1875

		ALLEI	ND121		
Jan.	6.47 6.43 6.43 6.55	5.89 6.24 6.46 6.74	7.46 5.90 6.39 7.64	7.14 6.62 7.90 6.94	6.31
Dec.	6.57 6.64 6.58 6.58	5.96 6.84 6.46 6.81	7.54 5.96 6.28 6.18	7.21 6.72 6.66 7.99 7.06	6.42
Nov.	6.29 6.55 6.43 6.46	6.03 6.29 6.52 6.80	7.53 6.04 6.37 7.85	6.72 6.72 6.98 6.98	6.59
Oct.	6.35	6.02 6.57 6.65 6.88	7.59 6.11 6.29 7.84	7.34 6.88 6.74 8.45 7.15	6.68
Sept.	6.54	6.09	7.70 6.09 7.88 7.88	7.47 6.95 6.71 8.42 7.26	6,63
Aug.	6.84	6.12 6.81 6.71 6.85	7.68 6.00 6.61 7.78	7.47 7.04 6.81 8.38 7.39	6.59
July	6.6933	6.99	7.65 6.06 6.61 7.84	7.50 6.70 6.70 7.40	6.69
June	6.35 6.90 6.04 6.77	6.13 6.64 6.70 6.70	7.67 6.06 6.41 6.48 7.75	7.51 7.14 6.67 8.19 7.45	6.77
May	6.08	6.18 6.94 6.94 6.85	7.66 6.12 6.54 6.54	7.54 7.07 6.79 7.42	6.94
April	6.53 6.78 6.57 6.57	6.33 7.10 6.91 6.75 6.85	7.49 6.14 6.36 7.72	7.49 7.94 7.37	98.9
Mar.	6.62	6.33 6.71 6.72 6.94	7.47 6.21 6.50 7.74	7.53 6.94 6.81 7.78 7.38	6.87
Feb.	6.69	6.40 7.15 6.84 6.70	7.51 6.14 6.57 7.63	7.54 7.00 6.92 7.63 7.38	6.81
Jan.	6.87 6.90 6.09 6.69	6.47 7.25 6.77 6.98	7.56 6.31 6.68 6.77 7.72	7.73 7.07 6.86 7.95 7.40	6.84
Name of Bond	Huston Kiver RK 24 M 7s 1885. Mint So & Nor Indiana 1st M 7s 1885 Cleveland & Toledo sta M 7s 1885. Chicago & Alton 1st M 1s 1885. Estis FV Wayne & Clitc 1st M 7s 1992.	Cauden & Anbon M of Nove 1889. 22. Alton & T. H. R. 1st M. 7s 1894. N. V. Catron & T. H. R. 1st M. 7s 1894. N. Order & Esser 1st M. of 1st 1914. More & Esser 1st M. of 1st 1914.	M. & Se. P. P. P. du. Ch. of v.) st. M. 8s. 1898. Chingh Valley R.R. Ita: M. 6s. 1898. Chingh Cand R. Mer. Co. R.L. Cann 5s. 1897. Chinggo & Milwaukee R.R. 181 M. 7s. 1897.	Lake Shore Rv dividend bonds 7a 1899 Chr O'Cl fin & Thi 18 M 81/19 1890 Chir O'Cl fin & Thi 19 18 19 19 19 19 19 19 19 19 19 19 19 19 19	Pennsylvania RR Co gen M 6s 1910
No.	25 24 20 E	33888	388888 38488	70202 70202	42 P

YIELDS OF RAILROAD BONDS JAN. 1875—JAN. 1876

Ref.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
22822	Chicago & Atton 1st M 7s 1893. Charles F Wayne & Chic 1st M 7s 192. Canden & Amboy M 66 Nov 1899. La Alton & TH RR 1st M 7s 1894. N Y Central renowal bonds 6s 1887.	6.43 5.89 6.56 6.24	6.23 6.47 5.86 6.64 6.20	6.25 6.43 5.90 6.21	5.97 6.42 5.86 6.62 6.12	6.00 6.34 5.76 6.68 5.99	6.01 6.30 5.71 6.77	6.11 6.21 5.73 5.89 5.89	6.08 6.18 6.39 5.86	6.00 6.17 5.64 5.78	6.04 6.18 5.61 5.99	5.05 5.09 5.64 8.64	5.89 6.14 5.59 5.91	5.88 5.99 5.58 5.48
82222	Morris & Essex 1st M st 7s 1914. Ve & Eric RM, st M N s 18388. M. & Er. P C fut Ch dv) 1st M 8s 1888. Chaffin Vallog YK 1st M st 1898. Central RK of Now Jersey M Ns 1898.	6.46 6.74 5.90 6.39	6.32 6.77 7.50 5.85 6.12	6.34 6.70 5.90 6.09	6.30 6.71 7.39 5.78 5.72	6.29 6.71 7.33 5.78 6.01	6.29 6.92 7.31 5.76 6.02	6.25 6.88 7.20 5.79 6.00	6.18 7.28 5.85 5.98	6.06 6.83 7.22 5.82 5.93	6.17 6.75 7.20 5.85 5.89	6.01 6.71 7.12 5.81 5.90	6.04 6.57 7.00 5.73 5.70	6.07 6.43 6.94 5.72 5.64
3833	Lehigh Coal & Nay Co RR Loan 6s 1897 Lakengo & Missaiber RR 18 x M 7s 1898 Lake Singe Ry dividend bonds 7s 1899 Lebe Col Cu & Man 1st M 1s 1899 Lehigh Valley RR 2nd M reg 7s 1899.	6.22 7.14 6.62 6.64	6.07 7.58 7.21 6.62	6.09 7.56 7.08 6.63 6.46	6.98 6.98 6.58 6.46	5.96 7.43 6.95 6.46 6.48	5.92 7.39 7.12 6.56 6.48	5.94 7.32 7.11 6.61 6.47	6.00 7.11 6.64 6.43	5.97 7.27 7.08 6.56 6.31	6.03 7.35 6.47 6.38	5.94 7.24 6.54 6.40	5.83 7.00 6.58 6.38	5.77 7.00 6.83 6.55 6.31
645 54	O Chie & Nor West Ry cons af 7s 1915. 1. Shi & Mich So one 1s M is 7s 1900. 1. Emmsylvania, RR. Co gen M of 1910 1. Pennsylvania, RH co gen M of 1910 1. New York & Harben RR com M 7s 1900 1. NY C & H R RR lst M 7s 1903.	6.34 6.34 6.34 6.31	7.94 7.04 6.13 6.34 6.09	7.97 6.97 6.14 6.10	7.70 6.93 6.27 6.10	7.58 6.92 5.99 5.23 5.96	7.52 7.37 5.98 5.23 5.98	7.37 6.86 5.90 6.24 5.87	7.24 6.78 5.99 6.21 5.87	7.22 6.95 6.02 6.13 5.60	7.43 6.97 6.04 6.18 5.68	7.31 6.99 6.00 5.70	7.18 6.89 5.99 5.99 5.49	7.05 6.79 5.94 5.85 5.52
45	Chic Burl & Quincy RR cons M 7s 1903	6.85	6.85	6.81	6.81	9.00	09.9	69.9	09.9	6.61	6.65	6.58	6.45	6.42

VIELDS OF RAILROAD BONDS JAN. 1876—JAN. 1877

Chesage & Alton 1st M 7s and of Bond June Peb Mar. April May June July 4ug. Sept. Oct. Nov. Dec. Jun. Chesage & Alton 1st M 7s 183. 12. 18. 18. 18. 18. 18. 18. 18. 18. 18. 18			APPER	IDIA		
Jan. Feb. Mar. Aug. Sept. Oct.	Jan.	5.54 5.08 5.25 5.25	6.00 6.28 5.29 6.46	5.77 6.59 6.61 6.36 6.12	6.84 5.59 5.70	6.24
Jun Feb Mar. April May June July Aug. Sept. Oct.	Dec.	5.54 5.13 6.54 5.80	5.82 6.11 6.73 5.37 6.23	6.02 6.37 6.37 6.99	6.85 6.70 5.57 5.65	6.28
Jan. Feb. Mar. Anti- July June July June July June July July June July June July June July	Nov.	5.53	5.94 6.29 6.69 6.44 6.12	5.93 6.71 6.62 6.34 6.17	6.88 6.60 5.60 5.73	6.29
Jun. Peb. Mar. Antil May June July Aug. Sept. Se	Oct.	5.50 5.50 5.50 5.50	6.00 6.00 5.56 6.18	6.10 6.67 6.37 6.29	6.83 6.54 5.76 5.76	6.22
Jan. Feb. Mar. May. Mar. May.		5.31 5.44 6.44 5.70	6.01 6.60 5.58 6.26	6.02 6.80 6.33 6.22	5.03 5.03 5.08 5.76	6.24
Jun. Feb. Mar. Anril May June July Systems of Systems o		5.23 5.44 5.32 5.37	5.78 6.27 5.60 5.65	5.90 6.76 6.42 6.34	6.71 6.53 5.65 5.49	6.22
Jan Reb Mar Abril May June Reb Abril May June Reb Abril May June Reb Abril May June Abril May	-	5.37 5.52 5.52 5.44	5.84 6.73 5.70 5.70	5.84 6.882 6.33 6.24	6.85 6.47 5.76 5.50	6.28
Jun. Feb. Mar. April Mar. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6.	-	5.47 5.86 5.54 5.61	5.98 6.83 5.52 6.05	6.96 6.32 6.32	6.89 6.57 5.76 5.77 5.77	6.29
Jun Feb. Mar. April		5.56 5.67 5.64 5.59	6.01 6.30 6.79 5.62 5.87	5.83 6.93 6.35 6.40	6.90 6.66 5.78 5.79	6.30
Jan. Go.		5.60 5.73 5.65	5.96 6.73 5.67 5.87	5.84 7.10 6.38 6.33	6.90 6.55 5.62 5.62	6.32
1 ma	-	5.91	5.96 6.33 5.65 5.65	5.81 6.96 6.34 6.23	6.86 6.34 5.78 5.46	6.35
1 m.		5.65 5.99 5.58 6.44 5.62	5.97 6.79 5.70 5.52	5.82 6.97 6.41 6.32	6.92 6.70 5.82 5.73 5.52	6.40
Name of Bond hiesge & Alton 14 M. 18 193. The F Wayne & Clin, is M. 18 192. The Alton & The M. 18 193. The Alton & The M. 193.	Jan.	5.588	6.07 6.943 5.72 5.64		7.05 5.94 5.85 5.52	6.42
	Name of Bond		ornis & Bearx 1st M st 7s 1914. Y & Eric RR 1st M 7s 1991. & St F (P on C. A of V) st M 8s 1898. & St F (P on C. A of V) st M 8s 1898. intral RR of New Jersey M 7s 1890.	high Coal & Nay Co RR Loan 6s 1897 Margo & Mirwahee RR 1st M 7s 1898 kte Shore & Virkderd bonds 7s 1899 the Col Ch & Marl 1st M 8f 1st 1899 high Valley RR Znd Mreg 1s 1990		iic Burl & Quincy RR cons M 7s 1903

YIELDS OF RAILROAD BONDS JAN. 1877—JAN. 1878

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a .o	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
44	Chicago & Alton 1st M 7s 1893.	5.54	5.58	5.77	5.80	1		i						5.70
3888	Camden & Amboy M 6s Nov 1889. St. L'Alton & TH RR 1st M 7s 1894. Ordris & Essex 1st M 8f 7s 1914.	5.08 6.25 6.00	6.09	5.27 6.36 6.09	5.47 6.40 6.10	5.36 6.49 6.06	5.93	5.21 6.05 5.98	5.05 6.09 6.07	5.01 6.11 6.04	6.14 6.08	5.20 6.26 6.04	6.00	5.08 6.33 6.02
333333333333333333333333333333333333333	M V & Eric RR 1st M 7s 1897 M & St P (P du Crdy 1st M 8s 1898 Lebith Valley RR 1st M 6s 1898 Central RR of New Greezy M 7s 1890 Lebith Coal & Nav Co RR Loan 6s 1897	6.28 6.74 5.29 6.46	6.28 6.74 5.50 6.60 5.87	6.08 6.69 6.13	6.02 5.69 6.44 6.18	5.98 6.55 6.20 6.13	5.90 6.67 6.17 6.13	5.94 6.71 5.38 5.91 6.00	5.94 6.70 5.41 5.91	6.05 6.83 5.94 5.94 5.81	6.17 6.83 5.44 6.00 5.71	6.11 6.75 5.45 5.94 5.94	6.05 6.59 5.36 5.96	6.15 6.49 5.34 5.78 5.90
338 336	Chicago & Milwautkee RR 1st M 7s 1898. Che Shore Ry dividend bond 7s 1899 Clev Con & Ind 1st M st 7s 1899 Cher Con R Ind 1st M st 7s 1899 Cher Con West R? and M reg 7s 1910 Chic & Nor West R? non st 7s 1915	6.59 6.36 6.12 6.84	6.51 6.36 6.34 6.34	6.61 6.56 6.52 6.40 6.75	6.61 6.52 6.52 6.58 6.74	6.57 6.56 6.52 6.69	6.48 6.21 6.45 6.63	6.29 6.28 6.31 6.65	6.38	6.45 6.25 6.63	6.52 6.59 6.21 6.65	6.50 6.42 6.15 6.59	6.45 6.39 6.14 6.57	6.85 6.41 6.37 6.15 6.55
44444	L Sh & Mich So cons 1st M sf 7s 1900. Whenyivania R NC O gen M of 8 1910 New York B Harden R St cons M 1900 Y C & H R R R R M 1900 Chie Bull & Quince R X cons M 7s 1903	6.29 5.70 6.24	5.35 5.35 5.39 6.29	5.52 5.67 5.97 6.50	5.64 5.63 5.87 6.41	5.53 5.64 6.40	5.66 5.71 5.72 6.38	5.65	5.72 5.72 5.71 6.32	5.06 5.72 5.78 6.37	6.32 6.32 6.32 6.32	6.40 5.69 5.58 6.27	5.30 5.70 6.24 6.24	5.24 5.55 5.55 6.27
		-	1											

VIELDS OF RAILROAD BONDS Jan. 1878—Jan. 1879

	Name of Bond	Jan.			4	~			-	w l	Oct.	-	-	Jan.	1
Chicago & Ahton 18t M ? 8 1893. Pitts Ft Wayne & Chic 1st M 7s 1912. Canden & Amboy M 6s Nov 1889. St L Alton & T H RR 1st M 7s 1894. Morris & Essex 1st M 8f 7s 1914.		6.0338	5.55.05 5.33.13	5.83 6.30 5.95	5.24 5.24 5.20 5.90	5.07 6.16 9.00 5.00	5.75 5.09 5.09 5.85	5.56 5.76 5.37 5.86	5.07 5.07 5.68 8.68	5.54 6.54 5.54	5.73	5.70 6.98 5.90 5.90	5.36 5.04 5.94 5.94		5.49 5.64 5.92 5.92
N. V. & Erie R.R. [45 M. 78 1897 & S. P. P. (Pr. 107 dy J.) 44 M. 85 1899 Length "Anley R.R. 187 M. 98 M. 98 1899. Length R.R. of Wer Teney "N. 78 1899. Length Coal & Nav Co R.R. Lean 98 1897.		6.15 6.49 5.34 5.78	5.29	6.09 6.52 5.31 5.79 5.91	6.04 6.53 5.85 5.96	6.00 5.83 8.83 8.83 8.83	5.89 6.29 5.33 5.64 5.78	5.73 6.33 5.52 5.73	55.25	5.82 6.44 5.18 5.47 5.64	5.80 6.39 5.17 5.54 5.69	5.76 6.31 5.14 5.50 5.61	5.73 6.30 5.17 5.64 5.63		5.63 6.15 5.32 5.37
Chicago & Milwaukee RR 1st M 7s 1898. Lake Shore Ry divident bonds 7s 1899. Cley Col Clin & Ind 1st As 17s 1890. Loingh Vallee RR 2nd M reg 7s 1910. Line & Nor West Ry cons si 7s 1915.		6.85 6.41 6.37 6.15 6.55	6.70 6.40 6.35 6.20 6.51	6.64 6.41 6.37 6.10 6.52	6.69 6.37 6.10 6.53	6.67 6.31 6.12 6.43	6.19 6.13 6.12 6.12	6.71 6.25 6.46 6.03 6.33	6.34 6.34 6.11 6.30	6.91 6.27 6.32 6.39	6.18 6.29 6.33 6.33	6.17 6.29 6.29 6.29	6.19 6.17 6.02 6.19		6.26 6.10 6.04 5.92 6.10
L. Sh & Mich Se, cons 1st M. st. 7s 1900. Pennsylvanis A. R. Co, gran M. os 1910. N. Y. & E. H. I. R. R. 1st M. st. 950. Like Burt & Guiney R. Cons M. 7s 1900. Like Burt & Guiney R. Cons M. 7s 1903.		6.5.55	5.24 5.53 5.53 6.29	5.23 5.54 5.54 5.54 6.32	5.54	5.52 5.53 6.28 6.28	6.15 5.53 5.50 5.62 6.21	5.54 5.48 5.48 5.63 6.10	6.07 5.56 5.51 6.02	5.58 5.54 5.69 6.03	6.55.56 6.05 6.05 6.05	5.48 5.48 5.46 6.02	5.40 5.40 5.95 5.95		5.36 5.36 5.89 5.80
Cleveland & Pitts cons sf M 7s 1900 Michigan Central RR cons M 7s 1902		6.28	6.29	6.38	6.30	6.35	6.14	6.15	6.18	6.20	6.18	6.11	6.16		5.94

VIELDS OF RAILROAD BONDS JAN. 1879—JAN. 1880

Jan.	55.27	5.84 5.10 5.10 5.85	5.50	5.09 5.01 5.17 5.57	5.18
Dec.	25.5.55 44.0.45 24.0.45	5.82 5.10 5.23 6.01	55.52	5.29 5.29 5.59	5.65
Nov.	5.32 5.42 5.96 5.59 5.17	5.94 5.39 5.25 5.25	5.75 5.85 5.85 5.79	5.09 5.30 5.57 5.63	5.24
Oct.	5.33 5.98 5.04 5.26	5.33 5.33 6.05	55.57 59.57 54.57 54.57	5.09 5.21 5.26 5.58 5.63	5.23
Sept.	2.00.37	5.91 4.92 5.31 5.28 6.00	5.67 5.87 5.86 5.56	5.55.27 5.55.29 5.55.85 5.55	5.24
Aug.	5.50	5 25 5 25 5 85 5 85	55.55	5.05 5.21 5.21 5.97	5.62 5.24 5.21
July	55.53	5.84 4.75 5.12 5.94	5.05 5.05 5.67 5.67	55.58	5.15
June	55.55	5.86 4.74 5.12 5.37 6.11	5.60 5.67 5.76 5.51	55555	5.60 5.12 5.21
May	5.54	5.90 5.21 5.21 6.17	55.55	55555	5.65 5.13 5.20
April	5.51	6.01 5.12 5.29 5.61 6.15	55555 55555 8657 8657 8657 8657 8657 865	5.38	5.85 5.20 5.28
Mar.	55.55.2	5.98 5.18 5.27 5.55 6.10	55.95	5.33	5.90 5.30 5.35
Feb.	5.19	5.96 5.15 5.13 5.46 6.05	58.83 66.83 66.83 66.83	5.31 5.31 5.71 5.70	5.67 5.21 5.27
Jan.	5.45 5.92 5.93 5.93	5.00 5.32 5.67 6.26	6.10 5.92 6.10 5.87	55.36 5.80 5.80 5.94 5.94	5.98 5.41 5.39
Name of Bond	Chicago & Alton 1st M 7s 1893. Chicago & Alton 1st M 7s 192 St. L Alton & T H RR 1st M 7s 192 Norsi & Essex st M st 7s 194 Norsi & Essex st M st 7s 194 N Y & Eric RR 1st M 7s 1891	M. &. St. P. (P. du Ch. dv.) 1st M. Ss. 1898. Central R. R. of N. 1818. Central R. R. of New Jersey, M. 78 1899. Central R. R. of New Jersey, M. 78 1899. Cinicago, &. Milwantee R. R. 1st M. 78 1898. Cinicago, &. Milwantee R. R. 1st M. 78 1898.	Lake Shore Ry dividend bonds 7s 1899 Cley Col Cin R. Into 1st M of 7s 1899 Librito Walley RR 2nd M veg 7s 1910 Chie R. Nor Weet Ry cons 8f 7s 1915 L. Sh & Mich So coms 1st M of 7s 1995	Pennsylvania R.R. Co gen M 6s 1910. N V V Sor H.R. R.R. 184 M 7s 1903. N V V Corle B.R. R.R. 184 M 7s 1903. Clorelb and R. Quincy R.R. come M 7s 1903. Cloreland & Pitta coms 8t M 7s 1903.	Michigan Central RR cons M 7a 1902. Central Pacific RR 1st M 6s 1895. Chicago Rk 1s & Pac RR 1st M 6s 1917
Ref.	28882	33.45.23	338 339 41 41		448 49

APPENDIX

VIELDS OF RAILROAD BONDS JAN. 1880—JAN. 1881

			111 1	222 (22 22	-	
1 2	Jan.	4.44 5.04 4.99 4.34	5.12 5.12 4.89 4.95	44.65 44.46 55.55	44.98 44.72 5.24 4.58	5.07 5.78 5.78 5.34
- 2	_	4.74 4.94 4.09 4.31	5.11 5.11 5.16 5.07	4.44.63 4.63 4.63 6.63	5.25 5.25 4.83 4.83	5.02 5.53 5.87 5.87
Log N	TAGA.	4.77 4.74 5.14 4.40	5.16 5.25 5.14 5.09	5.02 4.72 4.55 71	0.5.44 0.2.29 0.2.29 0.6.3 0.6.3	55.27 5.65 5.98 5.98
to	-	45.45.4 52.25.8 52.25.8 53.25.8	5.37 5.37 5.07	5.31 5.16 4.72 4.82	5.19 5.37 4.93 4.72	55.55 7.28 7.28 7.48
Sont	ochr.	45.45.4 57.27 10.4 10.4 10.4 10.4 10.4 10.4 10.4 10.4	5.37 5.37 5.37	5.45 4.82 4.82	5.25 5.39 4.97	5.06 5.06 5.36 5.36 5.36
Ang	-	58.85 5.04 5.36 5.36 6.36	5.42	5.24 5.09 4.80 8.80 8.80	5.25 5.23 4.90 85.85	56.33
Tule	oun's	5.13 5.40 5.40 4.54	5.54	82.29.44 82.29.88.	24.544 24.888 88.84	55.74
Tune		55.21 5.47 5.47 5.47 5.47	5.30 5.30 5.30	5.00 5.00 5.00 5.00	5.55.49 5.06 5.06	5.90 6.36 6.22 5.98
Mox	ran's	4 55.25 4 67.12	55.55 5.51 5.51 5.51 5.51	55.09	5.50 5.01 5.01	5.35 6.35 5.15 5.15
l line A	i d	5.30 5.30 5.24 5.67	55.53	5.66 5.42 5.11 5.11	5.55 5.59 5.97 6.97	5.83 5.86 6.41 5.93
Mor	nidi.	5.20 5.22 5.76 4.67	5.57	5.21 5.21 5.14 5.13	5.55 5.95 5.97 5.03	5.84 6.49 5.93
T est	T.CD.	55.26 55.26 57.71	5.82 5.82 5.62 5.62	5.25 4.97 5.06 5.11	5.62 5.62 5.02 5.02	5.80 6.52 6.10 5.99
i d	Jan.	55.23 47.84 47.74	5.26 5.56 5.56 5.50	5.06 5.09 5.01 5.17	5.57 5.61 5.18 5.18	5.82 5.90 6.58 6.40 6.20
Name of Road	reame or bond	2.5 Piter R twyne & Chic 18 M 's 1912. 30 Monts & Essox tet M 8 (7 8 1914. 31 N V & Eric RR 1 tet M '18 1897. 32 M & Est P C do Chic My 18 1893. 33 Left B V A Chic RX 1 tet M (8 1893.	Lehligh Coal & Nav. Co. RR. Loan. 6s. 1897. Christon & Milmunlers RR. 1st M. 7s. 1898. Cley. Co. Clin. R. Intelligent 1899. Cley. Co. Clin. R. Int. 1878. 1899. Lehligh Valley, RR. 2nd. M. reg. 7s. 1910.	Chie & Nor West Ry cons st 7s 1915. 18 % Mid 2 woons 1st M 1st 7s 1900. Formsy'rand R K Cons M 6s 1900. Formsy'rand R K F R 1900. N Y V C & H R R R Ist M 7s 1903.	Chic Burl & Quinoy RR cons M 7s 1903. Chicyand & Parks cons s M 7s 1900 Michigan Cerran IR Store M 7s 1902 Chichigan Cerran R 18th Store M 7s 1903. Chicago Rk 1st M	Chic St. Paul & Minn te. M. 62 1918. Chic St. Paul & Minn te. M. 62 1918. The Yeah Minn & Man 24d M. 62 1909. Nash Chart & St. L 1st M. 7s 1913. St. P & Stoux City RR 1st M 6s 1919.
Ref.	3	333	33833	84444	\$448 468 468 468	553250

YIELDS OF RAILROAD BONDS Jan. 1881—Jan. 1882

		101010100				
Jan.	4.74 4.82 5.02 4.29	5.15 5.05 5.05 5.06 4.60	4.33 4.33 4.98 4.87	5.17 4.64 4.55 5.10 5.42	5.71 5.91 5.74 5.31	6.09
	27,000	45500	22222	9895		
Dec.	4.32 4.32	5.14 5.01 5.01 5.16 4.80	4.33 4.49 4.96 4.72	5.16 4.68 5.17 5.17	5.50 5.24 5.24	6.01
· ·	4.74 4.88 4.63 4.21	55.08 7.08 7.08 7.08	4.58	5.22	5.62 5.96 5.68 5.68 5.19	5.95
Nov.						
Oct.	4.76 4.96 5.09 4.40	5.11 5.03 5.09 5.09	4.49 4.84 4.84 4.88	24425 7266 7868 7888 7888	55.55	5.97
ŏ						
Sept.	4.73 4.98 4.57 5.09	44.98 4.98 4.98	44.44 4.77 7.77	24425 4045 4045 4045 4045 4045 4045 4045	5.56 5.81 5.40 5.68 5.11	5.92
		1-1280m	04040			
Aug.	4.08 4.41 4.84 4.26	4.97 4.78 5.02 4.73	4.49 4.34 4.71 4.88	4.4.8 5.05 2.29	5.25.78	5.92
	4.68 4.64 4.30 4.23	5.01 5.01 4.65	44.44.44.44.37.77.44.43.77.44.44.44.44.44.44.44.44.44.44.44.44.	54.45 5.31 5.31	55.33 55.33 4.99	5.82
July	च च च च च	40404	यं यं यं यं यं	44440	NNNN4	s.
June	48.44 48.44 4.05 4.05	45.94 5.00 5.00 6.00	4.888.44.80	4.78 4.49 5.30	45.52 4.89 89	5.69
P.						
May	4.82 4.78 4.49 4.02	5.03 5.05 5.05 4.82	7.4.4.4.4.9.6.9.8.3.7.	5.34	4.94 1.05 1.05 1.05 1.05 1.05 1.05	5.78
April	5.03 5.03 5.03 5.03	55.18 5.22 4.76 4.91	4.47 4.63 4.71 5.07	5.45 5.27 5.45 5.45	55.83	5.89
			70101			
Mar.	8.44.80 77.73 5.25 7.25	5.10 4.84 5.18 4.89	4.52 4.63 4.71 5.27	5.13 4.86 5.24 5.44	5.82 5.88 5.44 5.02	5.84
	4.77 4.99 5.08 4.28	5.00 5.00 4.94 5.00 4.86	4.52 4.65 5.01 5.27	5.23 5.33	55.35 45.36 4.98	5.69
Feb.						
Jan.	4.74 4.99 4.57 5.07	5.16 4.89 4.95 5.00 4.65	4.4.4.4.5 5.2.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	5.07 5.07 5.07	5.35 5.34 5.47 5.47	5.66
, j						
			Pemsylvania RR Co gen M 6a 1910. Ney York & Harlen RR const. Ney C & HR RR 1st M 7s 1903. Che Bart & Quinche RR const. Che Bart & Quinche RR const. Cheveland & Pitts cons 8 fM 7s 1903.	k cons M 7s 1902 st M 6s 1895 RR 1st M 6s 1917 cons M 7s 1902. 1st M 6s 1918.	St. Paul Minn & Man 2nd M 6s 1909. Nash Chart & St. Li EM 7st 1913. St. P. Sounc City RR, Ist M 6s 1919. M. & S. P. (So Min Dy) 1 and M 6s 1910. Canada Southern Ry Ist M 5s 1908.	Chic St P Min & Omaha cons M 6s 1930
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71		9	161 18 1	913	. 65	193
Name of Bond	5 : 3 :	82625	10 10 10 10	190 181 18	88.19	89
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	E.5885.E	ದ್ದಿಗಳಿತ	BOX28	Stage	ada ada	š
	Pitts Ft Wayne & Chic 1st M 7s 1912 Morris & Essex 1st M sf 7s 1914 N V & Erie RR 1st M 7s 1897 M & St P (P du Ch dv) 1st M 8s 1898 Lehigh Valley RR 1st M 6s 1898	Lake Shore Ry dividend bonds 7s 1899 Clev Col Cin & Ind 1st M st 7s 1899 Lebigh Valley RY 2nd M reg 7s 1910 Chic & Nor West Ry cons at 7s 1915 L Sh & Mich So cons 1st M st 7s 1900	Pic Ven	Michigan Central RR cons M 7s 1902 Central Pacific RR 1st M 6s 1895 Chicago Rk 1s & Pac RR 1st M 6s 1917 Chicago & Nor West cons M 7s 1902 Chic St Paul & Minn 1st M 6s 1918	A NASA	hic
No.	333333 333333 3333333	70101	#5444 #5400	744688 NOOOO	55555	57
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YIELDS OF RAILROAD BONDS JAN. 1882—JAN. 1883

LET MORE THAN 1912. LET MORE
4.28 4.914 4.71 4.71 4.71 4.71 4.71 4.71 4.71 4.
5.50 4.198 4.198 4.206 5.50 5.50 5.50 5.50 5.50 5.50 5.50 5.
5.13 5.17 5.20 5.10 5.44 5.15 5.17 5.20 5.10 5.44 5.15 5.17 5.20 5.10 5.44 5.15 5.17 5.20 5.10 5.44 5.15 5.17 5.20 5.10 5.10 5.14 5.15 5.17 5.10 5.10 5.10 5.10 5.10 5.10 5.10 5.10
5.05 5.03 5.05 5.00 4.94 5.06 5.01 5.05 4.99 5.06 5.11 5.11 5.18 5.08 5.08 5.06 5.11 5.11 5.18 5.08 5.09 5.06 5.11 5.18 5.08 5.09 5.06 5.18 5.08 5.09 5.08 5.08 5.08 5.08 5.08 5.08 5.08 5.08 5.08 5.08
4.78 4.61 4.53 4.51 4.33 4.36 4.55 4.49 4.51 4.98 5.06 5.10 5.01
4.33 4.51 4.58 5.06
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Claredard & Diete cone of M 7s 1000

YIELDS OF RAILROAD BONDS Jan. 1883—Jan. 1884

કું <u>કું</u>	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	نہ ا
33333	Pitts Ft Wayne & Clic 1st M 7s 1912. Margis Elsen 1st M sf 7s 1912. M & St P P du Ch dv) 1st M 8s 1888. Margin Yallor XR 1st M 6s 1898. Lake Shore Ry dividend bonds 7s 1899.	5.08 4.28 4.28 5.16	4.76 5.04 5.22 5.22	4.76 5.05 4.24 5.20 5.20	4.62 4.88 5.09 5.21	4.85 4.85 5.13 4.26	4.86 5.15 5.22 5.22	4.86 4.86 5.02 4.30 5.16	4.91 5.17 4.36 5.10	4.88 5.18 5.18 5.13	4.82 5.15 4.42 5.13	5.03 5.03 5.13 5.13	4.87 4.99 4.30 5.04		4.67 5.08 5.08 5.02
888444	Clev Col Cin & Ind 1st M st 7s 1899. Chick Why The N Znd M vig 7s 1910. Chic & Nor West By come st 7s 1916. En & Mich Sooms 1st M 87 18 1905. Femsylvania RR Co gen M 6s 1910.	5.08 8.05 4.74 5.05 88 88 88 88 88	5.09 5.08 4.86 4.58	5.11 5.11 5.13 4.98 4.59	5.10 4.84 5.10 5.07 4.62	5.10 5.11 5.02 4.56	5.14 5.07 4.95 4.59	5.02 4.84 4.88 4.68	5.16 5.01 5.01 4.85	5.18 4.98 5.11 5.00 4.73	5.15 5.10 5.10 4.87	5.18 4.90 4.84 7.73	5.22 4.93 4.72 7.72		5.24 5.04 4.72 4.68
54444	New York & Harlem RR cons M 7s 1900 V C & H R R K 184 M 7s 1903. Chie Burl & Quincey R A 7s 1903. Glocebard & Pittes cons M 7s 1900. Michigan Central RR cons M 7s 1900.	4.62 4.94 4.94 5.07	4.62 4.73 4.99 5.11	4.64 4.75 5.01 5.13	4.64 4.74 5.01 5.11	4.78 4.78 5.09 5.12	4.76 4.93 5.05 5.10	5.06 5.06	4.60 4.81 5.00 5.22	4.75 4.75 5.12 5.21	5.73 5.13 5.13 5.11	5.03 5.03 8.03	4.53 4.99 5.03		4.47 4.53 5.00 5.05
52555	Central Pacific RR 1st M 6s 1895 Chicago Rk 1s & Pec RR 1st M 6s 1917. Chicago Rv 1st West coms M 7s 1902. Chicago Rv Mm 1st M 6s 1918. Sh Paul Minn & Man 2nd M 6s 1918.	5.03 5.32 5.32 5.32	5.10 5.44 5.52	5.24 5.25 5.24 5.57	5.25 5.38	5.15 5.15 5.42	5.15 5.15 5.15 5.48	4.70 5.20 5.21 5.55	5.23 5.24 5.24 5.24 5.24	5.22 5.22 5.26 5.40	5.15 5.16 5.18 5.47	5.05 5.05 5.14 5.14	4.45 5.05 1.05 1.05 0.05 0.05		55.04 5.04 5.07 5.04
52525	Naah Chatt & St. L 1st M 7s 1913. 2. Pe X Sounc ULVH RR 1st M 6s 1910. 3. M & St. P (3o Min Dv.) 1st M 6s 1910. Chand Southern Rv 1st M 8s 1908. Chic St. P Min & Omala cons M 6s 1930.	55.33	5.96 5.40 5.44 5.62	5.92 5.41 5.40 5.65	5.39 5.33 5.31	5.27 5.27 5.30 5.01	5.52	5.30	5.87 5.63 5.43 5.46	5.86 5.20 5.45 5.53	55.55 56.19 64.55 64.55	55.33 55.33 57.33 57.33	55.23		55.33
59 50 50 50 50	St. P. Min & Man (Dak Dv.) 1st M 6s 1910. M. B. P. Willer (B. M. B.) 1st M 8s 1921. M. & S. P. (W. W. Dv.) 1st M 8s 1921. M. & S. P. (Willer & Min Dv.) 1st M 5s 1921. Chic St. Louis & N Orleans 5s 1951.	5.49 5.55 5.55 4.83	5.58 5.58 8.83 48.83	5.55 4.85 4.85 4.85 4.88 8.88	54.83 48.83 48.83	4.8.8.8 5.69 8.80 8.80	5.49 5.37 5.65	5.50 5.39 5.64 8.78	5.53 4.90 5.48 5.71 4.81	5.49 5.47 5.54 8.80	5.45 5.46 5.69 4.81	5.42 5.47 4.62 7.47 7.75	5.38 4.83 4.557 4.65	5.42 5.43 5.57	42 79 57 71
83	Pennsylvania Co gu 1st M 4½s 1921	4.81	4.80	4.81	4.80	4.81	4.83	4.81	4.84	4.85	4.84	4.82	4.79	4.85	22

YIELDS OF RAILROAD BONDS JAN. 1884—JAN. 1885

				1			Ī	Ī			_	~	-		
	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	. Dec.	Jan.	
Morris M & S	Pitta Fr Wayne & Chite Jat M 7a 1912. Mornie & Esser Hat M 8f 7s 1914. M & St. P P din Chi dr) Hat M 88 1889. Lake Siner & Jyividend boulds 7a 1899. Lake Siner & Jyividend boulds 7a 1899.	4.67 5.08 4.25 5.02	4.62 4.97 4.24 4.92	4.63 4.94 4.94	44.44 4.96.4 4.000.0	4.61 5.02 4.13 5.13	4.73 5.04 5.04 5.18	4.71 4.85 5.00 4.13 5.22	4444 988 98.69	4.70 4.85 5.05 4.15 5.21	5.20 5.20 5.20 5.20 5.20	5 4 7 7 0 0 5 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	8 4.09 0 5.05 0 5.05 0 5.05	4.84 4.84 5.02 6.02	
Shic Shic Seng	Clev Col Cin & Ind 1st M sf 7s 1899. Lichigh Valloy RX 2nd Mre 25 1910. Chic & Riv West Ry coms sf 1s 195. 23 & Mich Sooms 1st 1st 1950. Pennsylvania RX Co gen M 6s 1910.	5.24 4.88 4.72 4.68	5.09 4.4.85 6.68 6.68 6.68	5.01 4.98 4.98 5.03 5.03	4.4.4.4 4.9.9.4 6.5.0 8.0.0	5.18 48.4 4.84 4.76	5.14 5.31 4.72	5.45 5.18 4.90 4.57	2.4.4.4 00.99.4 00.81.8	5.01 5.02 4.76	2 4.93 2 4.93 2 4.81 8 4.81	24.44 74.44 74.44 74.83 74.83 74.83	78 8 8 3 4 4 8 8 3 5 0 5 4 4 4 4 5 5 0 5 0 5 0 5 0 5 0 5 0	2.4.4.4.4 20.9.4.4.4.4.4.65	
Zhic Cleve	New York & Harlem RR cons M 7s 1900. Ye C & H R RR Ris M 7s 100s. Chic Burl & Quinor 7K Cons M 7s 1903. Which Burl & Quinor 7k Cons M 7s 1900. Michigan Central RR cons M 7s 1900.	4.47 4.73 4.73 5.00 5.05	44.44 4.751 4.855 5.95	44.44 4.83 88 88	4.20 4.50 4.86 7.87	4.4.4.4.6.1.0.2 14.8.2.0.2 10.0.2	4.54 5.05 5.02 5.02	4.61 5.00 5.03 5.03	4.4.4.4 05.9.4 7.9.9	4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	2 4 4.61 2 4 4.85 2 5.00 3 5.00	1.4.58 5.4.86 0.5.02	2 44.53 2 44.73 2 4.92 5 102	4.44 4.93 6.93 93	
Chicago J Chicago J Chicago S Chic St P St Paul N	al Pacific RR 1st M 6s 1895 ugo RR 1st R be The RR 1st M 6s 1917. ugo R Nord West cores M 7s 1902. Paul & Mirra Et M 6s 1918 ul Mirra & Man Znd M 6s 1909.	5.04 5.04 5.04 5.04 5.44	4.50 4.95 4.99 5.34	44.52 4.52 4.52 7.23 7.27	44.52 25.44.52 05.20	4.4.4.80 5.99 5.33	5.04 5.12 5.17 5.17	5.11 5.16 5.16 5.17 5.64	4.4.7. 6.0.0 6.0.0 7.00 7.00 7.00 7.00 7.00	5.05 5.05 5.05 7.47	74.87 25.02 25.03 25.03	8 5.00 8 5.00 8 5.00 8 5.00	00 4 4 92 00 4 4 89 00 5 5 0 0 1	5.00 5.35	
A P P P P P P P P P P P P P P P P P P P	Nash Chatt & St. List M 7s 1913 P. & Shour Chy RXT st M 6s 1910 C. M & St. P. Go. Min. Dry) set M 6s 1910 Channel Souther Ty List M 5s 1993. Chies St. P Min & Omala cors M 6s 1930.	5.512	5.80 5.08 5.37 5.21	5.78 5.00 5.00 5.38	5.64 5.21 5.21 5.35	5.76 5.31 5.17 5.49	5.64	5.93 5.72 5.41 5.47	5.87 5.20 5.27 5.27	5.92 5.04 5.32 5.45	52.55 5.55 5.55 5.55 5.55 5.55 5.55 5.5	53652	5.84 5.07 5.29 7.7 5.29	5.78 5.28 5.28 5.36	
hic Mala	Ps. P. Min & Man (Dak Dov) 1st M 6s 1910. Ps. Madelplan & Eriegen M 5 1970. C. M. & S. P. (W. & P. T. Dov) 1st M 5 1921. Ch. M. & S. P. (W. & M. M. Dov) 1st M 5 8 1921. Chic St. Louis & N. Orleans 5s 1951.	5.42 4.79 5.43 4.71	5.34 5.35 5.35 5.35	2.44.2.4 41.74 46.66	5.28 5.08 5.14 5.14 5.68	5.36 5.31 5.37 4.68	5.51 5.48 5.52 5.52 4.71	5.48 5.41 5.60 7.77	5.46 5.50 7.77	85.33 25.33 25.49 87	5 5.49 7 5.46 9 5.52 4 79	0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.0	26.5.35 2.4.35 2.4.35 2.4.35 2.8.45 3.35 3.35 3.35 3.35	5.42 5.42 7.74	
enns lew	Pennsylvania Co gu 1st M 414s 1921. New York Lack & West 1st M 6s 1921.	4.85	4.88	4.78	4.83	4.79	5.15	5.18	5.00	4.79	6 5.02	2 5.04	4.71	4.74	

VIELDS OF RAILROAD BONDS JAN. 1885—JAN. 1886

Name of Bond Jan Feb Mar April May June July Aug Sept. Oct. Nov. Doc. July E. Wayne & Clic 1st Mrs 1912 4.66 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.57 4.58 4.50		1 to to 10 to 0	60 min - min t-	00.01.01.01				
Philip Program & Chine In Name of Board Dam Pab Mart April May June July Aug. Sept. Oct. Nov. In His E. Wayne & Chine In His In 1912 4.68 4.66 4.50 4	Jan.	4.47 4.58 3.66 4.83	4.44 4.34 4.34 7.04	3.78 4.12 4.52 4.53 51	5.74 5.33 5.75 5.31	4.58 4.90 4.92 4.71	4.84.84.84.44.44.29	4.43
Name of Bond Jan. Feb. Mar. April May June July Aug. Sept. Oct. O	Dec.	4.47 4.49 3.60 4.90	44444 84444 7444 7444 7444 7444 7444 74	84444 85125 86428	5.40 5.40 5.40	4.24.4.4 0.00.00 0.00.00 0.00.00 0.00.00 0.00.00	44444 688 645 645 645 645 645 645 645 645 645 645	4.62
Part R P. Wayne & Chir Let M. T. Part B. Mar. April May June July Aug. Sept. Oct.	Nov.	4.50 4.46 3.72 4.92	44444 4644 19464 19464 19464	3.77 4.15 4.51 4.63	5.4.4.2 5.4.89 5.40	5.04 5.04 5.15 4.90	4.49 5.00 4.49 4.46	4.71
Patter F. Wayne & C. Chie, E. Mar. April May June July Aug. Sept.		4.49 4.523 4.523 4.533	4.50 4.50 4.47 4.47	8.84 4.17 6.66 6.66	54.44.61 54.92 54.88	4.95 4.95 4.94	5.06 5.06 4.46 5.09	4.74
Name of Bond Jan Peb Mar. April May June July Aug.			.84 .71 .75 .26	. 36 . 35 . 31 . 31 . 31	.71	84488	45.55	
Heits F. Wayne & C. Chie 1st M. 7st 1912.								
Pitts F Wayne & Chie in M s 1912. 4.68 4.75 4.60 4.50	Aug.	444.64	0.0044	8.4444		4.2.2.2.2 8.10.20	40044	9.4
Name of Board Jan Peb Mar. April May	July	4.57 4.86 3.80 4.97	4.4.93 4.4.65 4.4.88 4.22	6.44 4.24 4.67 4.67	4.24 4.47 5.07 5.62	5.10 5.33 5.10	5.11 5.17 4.52	4.65
Name of Bond Jan Peb Mar. April May Mar. April May Mayne & Clife 1st M Mayne &		4.59 4.85 3.86 4.99	5.00 4.4.4.6 1.25 1.25	3.95 44.26 4.77 4.91	4.29 4.81 5.04 5.04	55.25 5.35 5.08	45.23 4.54 4.54 5.27	4.79
Pitts P. Wayne & Chie it at M s 1912. 4.66 4.		4.57 4.49 3.89 5.04	44.95 4.75 4.20	4.4.4.4 4.4.4.9 91.91	5.14 5.14 5.14 5.68	25.55.25 27.27 27.27	54.61 5.33 5.39 5.45 5.45	4.87
Peter Pete			4444 80 252 82 82 82	44444	44422 648 947 947	55.25 5.25 5.25 5.25 5.25	45.55 4.65 4.65	4.81
Name of Bond Jun. Preb. Jun. Jun. Jun. Jun. Jun. Jun. Jun. Jun.					8.21 8.21 8.21 8.81	5.25 5.25 5.25	45.54 46.64 64.64 64.64	4.85
Name of Bond Jun. Fig.								
Name of Bond Name of Bond Morris & Eages, 14th M 71 51912. And S. P. (F. of Adv.) In M 71 51912. And M. S. P. (F. of Adv.) In M 71 51912. And M. S. P. (F. of Adv.) In M 71 5192. And M. M. S. (P. of Adv.) In M 71 5192. Cley Coll. R. Ind 11st M 61 78 1590. Cley Coll. R. Ind 11st M 61 78 1590. Cley Coll. R. Ind 11st M 61 78 1590. Cley Coll. R. Ind 11st M 61 78 1590. Cley Coll. R. Ind 11st M 61 78 1590. Cley R. M. (M. Seconda M 61 7900. Cley R. M. (M. Seconda M 71 5100. Cley Coll. R. M. (M. Seconda M 71 5100. Cley Coll. R. P. H. E. One M 71 5100. Cley Coll. R. P. H. E. One M 71 5100. Cley Coll. R. M. (M. Coll. M 71 5100. Cley Coll. R. M. (M. Coll. M 71 5100. Cley Coll. R. M. (M. S. P. Of R. R. M 61 1910. Cle M. S. R. (S. Coll. M. M. M. 19 18 M 61 1910. Cle M. S. R. (S. Coll. M. M. 19 18 M 61 1910. Cle M. S. R. (S. Coll. M. M. 19 18 M 61 1910. Cle M. S. R. (S. Coll. M. 19 19 19 19 19 19 19 19 19 19 19 19 19								
PHEF F. Wayne & Morrie E. Essey. It was not be a few as to be a fe	Ja	44440						
THE POOL WOODS WOODS ACCOUNT WOODS ACCOUNT			M ef 7s 1899. 4 reg 7s 1910 ms ef 7s 1915. L M ef 7s 1900. n M 6s 1910.	R. Harlem RR cons M I R. RR. 1st M. 7s 1903. 2 Quincy RR cons M. 7s 2 Pitts cons sf M. 7s 19 2 Petts cons M. 7s 19	217.	3: P & Sioux City RR 1st M 6a 1919. 2: M & St P (So Min Dv) 1st M 6s 1910. 2: and 6 Southern Ry 1st M 5s 1908. 3: Southern Ry 1st M 5s 1908. 3: P Min & Man M 6s 1910. 3: P Min & Man (Dak Dv) 1st M 6s 1910.	nhia & Erie gen M 5s 1920. st P (C & P W Dv) 1st M 5s 1921. st P (Wis & Min Dv) 1st M 5s 1921. oublis & N Orleans 5s 1951. ania Co gu 1st M 4½s 1921.	New York Lack & West 1st M 6s 1921 Hannibal & St Joseph cons M 6s 1011
	Ref.	33233				455555 8		4 5

VIELDS OF RAILROAD BONDS Jan. 1886—Jan. 1887

Jan.	4.44 3.57 3.57	4444. 60.11. 83.33	3.98 4.11 4.41 4.53	44.25 44.72 44.72	44.4.4.4.86 25.24.4.4.86 73.73	4 4 57 4 4 57 4 65 4 31 5 23	4.50 4.51 4.52 4.80	3.90
Dec.	4.4.4.8.4 26.62 26.62	24.44.4 20.03 20.03	44444 005 1544 531	5.44 5.05 5.05 5.05	5.4444 6.55 8.81 8.81 8.81 8.81	4.4.4.4.6.30 2.30 2.30 2.30	4.4.4.4.4.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6	3.91
Nov.	4.36 3.40 4.60 4.67	44.55 4.30 4.30 0.130	3.95 4.96 4.42 4.51	3.93 4.43 5.62 5.07	4.51 4.95 4.79 4.79	4.4.4.4.4.5.32 2.32 2.32 2.32	4.4.4.4.4.3.5 64.4.9	3.91
Oct.	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4.4.4.4.50 2.27.4.4.06.06	44444 90 144 144 144	5.44.45 5.70 5.00	4444 444 72 72 72	4.23 4.30 4.19	44444 655 645 645 645	3.98
Sept.	4.4.4. 3.30 3.50 7.70	24.44 8.25 8.25 8.25 8.25	3.99 4.45 4.51	3.99 4.26 4.42 5.77	44.68 47.44 75	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4 4 4 50 4 4 4 38 4 4 4 3 8 4 7 9	3.97
Aug.	4.29 3.45 4.64 4.64 5.66	44.10 3.24.42 3.85	4.35 4.35 4.35 4.35	44.44.6 44.44.6 5.03	4.4.4.4.4.6.0.0.0.0.0.0.0.0.0.0.0.0.0.0.	44444 28841 28842	4.28 4.29 4.39 4.39	3.92
July	4.42 4.42 3.46 4.65	344.28 34.42 37.14 37.18	3.85 44.02 44.44	5.03 5.03	4.52 4.61 4.75 4.70	4.54 4.54 4.17	4.29 4.39 4.39	3.88
June	4.30	4.26 4.26 4.26 4.05	3.83 3.96 4.16 4.38	6.15 4.4.41 5.25	4.47 4.78 4.76 4.70	4.54 4.54 4.24 4.24	4.35 4.35 4.40 6.60	3.92
May	4.4.4.4.4.3.0.4.9.0.4.0.0.4.0.0.4.3.0.0.4.3.0.0.4.3.0.0.4.0.4	4.60 4.30 4.25 4.12	3.83 4.02 4.27 4.39	4.12 4.10 4.41 4.71 5.30	4.51 4.83 4.83 7.4 4.81	44.44.67 67.67 68.33 42.44	4.39 4.49 4.49 7.6	3.95
April	4.38 3.58 4.74 4.74	4.47 4.35 4.25 3.98	3.86 4.25 4.44 4.44	4.21 4.23 4.42 4.70 5.16	44.88 4.94.4.99 4.91.69	44444	4.4.36 4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	3.94
Mar.	44.45 3.55 4.69	44446 42426 93246	3.83 4.21 4.21 4.44 4.84	54.4.20 54.4.18 5.18	4.4.4.4. 84.8.4.4. 00.00.00.00.00.00.00.00.00.00.00.00.00	4.4.4.4 27.7.5 190 190 190 190 190 190 190 190 190 190	74.43	3.93
Feb.	4.30 3.60 4.76	4.47 4.37 4.24 3.90	3.80 4.03 4.46	4.21 4.42 5.27 5.27	4.50 4.90 4.65	44.40 4.7.44 2.35	4.4.4.4.4.4.4.4.4.87.	3.90
Jan.	4.4.4.4.4.4.4.6.6.6.6.6.6.6.6.6.6.6.6.6	44.44 4.54 4.34 4.07	44.122 4.522 5.522	44.44.3 5.75.5 7.55	4 4 4 9 9 4 4 9 9 9 9 9 9 9 9 9 9 9 9 9	4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	4.43 4.40 4.56 4.89	3.90
Name of Bond	Pitts RV Wayne & Chic 1st M 71 1912. Mortis & Escr. Lis M is 1914. M & St. P. (For Ch dv is M 81 1898. Lehigh Velley RR 1st M for 1898.	Cler (Or it is In at lat M at '5a 1899, Chilefan Valley RR 2nd M reg 7a 1910 Chile & Mor Veer Ry coms at 7a 1910, L'Eli & Mor Veer Ry coms at 7a 1900. Estivationals at M at 7900.	New York & Hadnen RR, cons. M. 79 1900 N. Y. C. & H. R. RR, 1st M. 7. 1903. Chie Plant & Othiney S. R. Cons. M. 78, 1903. Cloridand & Plists cons. sf. M. 78, 1900. Michigan Central RK, cons. M. 78, 1902.	Chiragos Rk I. & Res RR 1 tr. M 968 1917. Chicano & Nov West cons. M 78 1918. Chic St Poul & Minn 18. M 68 1918. E. Penl Minn & Man 2 101 M 68 1919. Nash Chatt & St. L 1st M 78 1913.	St. P. & Stown, City. Ref. is M. of 1919 C. M. & St. P. (So. Min. Dry). Ist M. of 1910. Comedia Southern, Nr. 1st. M. 59, 1908 Citic St. P. Min. & Consilia come. M. os. 1930 St. P. Min. & Man. (Data. Dry). Ist. M. os. 1930	Philadelpin & Ergery M. 8; 1920. C. M. & S. P. (C. &. P. W. Dr.) 1st M. 5; 1921. C. M. & S. P. (W. &. Vin Dr.) 1st M. 5; 1921. C. M. & S. P. (W. &. Vin Dr.) 1st M. 5; 1921. Chie St. Douje & W. Ophems 5; 1951. Chie St. Douje & W. Ophems 5; 1951.	Mer Vork Leak Wever is th & 68; 1921 Hannibal & 82 Joseph cons M 68; 1931 ON V Cons & Hudown River Deb 58; 1994 Theilmore & Ohio 58; 1935 Relimore & Ohio 58; 1935	Chicago & N W Ry Deb 5s 1909. West Shore RR 1st M 4s 2361.
Ref. No.	33 33 37	86 64 14 14	54444	52 52 53 53	52755	88228	45000	26

VIELDS OF RAILROAD BONDS JAN. 1837—JAN. 1888

No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Δ	Dec.
33 33 33 38	Pitts Pt. Wayne & Chie 1-t. M. 7- 1912. Lother & Bessel M. M. et 7- 1914. Lother Walley R.M. 1. M. of 1898. Like Since R. Warkhard bond 7- 1899. Che Col. Chi. & Ind. Ja. M. H. 7- 8- 1899.	3.572	4.46 3.50 4.62	44.54.4 25.55 25.65 20.05 11.05	44.6.44	3.65 4.60 4.60 4.60	4 40 2 4 40 4 0 6 40 1 6 1 6 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	44.6.44 26.23 18.83 8.83	4.38 4.45 4.79 4.86	44.8 3.51 78.89 8.80 8.90	4.40 4.65 3.99 4.93 5.05	3.96 3.96 4.97		44.8.4 22.23 87.88
86 14 14 15 16 16 16 16 16 16 16 16 16 16 16 16 16	Ledigh Valley, RR 2nd M reg '1s 1910. Lichick Nav Week Ry conse '1' 2' 19 195. L She & Meir So conse 1st, at '7's 1940. L She & Meir Co gen M or P 1910. New York to Harden RR conse M os 1900.	44.11 44.53 3.93 3.93	4.52 4.65 4.02	4.23 4.56 4.38 3.77	3.45 3.45 4.59 4.53 4.53	2 4 4 5 5 5 4 5 5 5 5 5 5 5 5 5 5 5 5 5	3.04	84464 8349 8049	4.44.44	4.45 4.59 4.08 4.13	44444	4.54 4.62 4.10 4.05		4.4.4.4.4.50 4.11.4.11.4.01
4446 446 446 446 446 446 446 446 446 44	N V C & H R RR Jst M 7s 1913. Cleich bert X, guinger RK cons M 7s 1993. Cleich bert X, guinger RK cons M 7s 1993. Cleich bert X, guinger R X, and M 7s 1999. Cleich guinger C R Y 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	44444	44444	44444 14664 16664	84444 84444	44.44.4.30 05.55.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	44.44.4 608.44.4	66.00 66.00	4444 2042 453 77	44444 01446 01446 01446 01446 01446 01446 01446 01446 01446 01446 01446 01446 01446	44444 2444 260 24	44.45 4.45 4.69 4.69		33,73
532 532 54	Chicago & Nor West cons M. 7s 1992. Chicago & Nor West cons M. 7s 1992. St. Pain Minn & Man 1 v. M. 6s 1913. St. Pain Minn & Man 2 vid M. 6s 1993. St. P. & Stone City, R. N. st. M. 6s 1993. St. P. & Stone City, R. N. st. M. 6s 1993.	44444	44464 666 966 966 966 966 966 966 966 96	44464 6001298	4.55 5.06 5.06 5.06	59.41 5.61 5.10 5.10	4.46 5.06 5.08 8.58	4.4.4.5.0.4.0.0.4.0.0.0.0.0.0.0.0.0.0.0.	44404 400000 6000000	44.44.61 47.24.64 63.24.63	4.63 4.77 4.91 4.64 4.64	444.64 601.60 601.60		44.56 5.09 5.09 5.09
55 57 59 59	C M & Sr. P (So Min Dry) 1st M 6s 1910. Chin & Min & Omalin With Sh 28 1948. Chin Sr P Min & Omalin cons M 6s 1950. Sr P Min & Min (Dat Dry) 1st M 6s 1910. Philadelpine & Eric gen M 5s 1920.	4.59 4.59 4.73 4.37	4.85 4.85 4.76 4.37	44 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	4.4.4.4 4.60.4.4.4. 4.62.4.8.6.	4.89 4.57 4.71	44444 08.88 25.88 0.00 0.00 0.00 0.00 0.00 0.00 0.00	4 4 4 4 4 4 5 1 2 5 4 5 4 5 4 5 4 5 4 5 4 5 4 5 4 5 4 5	4.91 5.00 4.35	8.4.8.84 7.0.84 7.4.88	5.20 4.39 9.39	5.12 4.71 4.87 4.39		5.20 5.00 5.00 5.45
822 822 84	C. M. R. St. P. (C. R. P. W. Dev.) 1st. M. 5st 1021. M. R. S. P. (Virks. R. Min. Dev.) 1st. M. 5st 1021. Chie St. Louis & N. Orients 5st 1951. Chemylyman Co. gan 1st. M. 47 sst 1921. New York Lack & West 1st. M. co. 1921.	4.57 4.65 4.31 4.23	4.66 6.44 4.44 4.48	4.51 4.32 4.32 4.26 4.50	4.60 4.75 4.31 4.23 4.51	4.63 4.29 4.29 4.20 4.50	4.64 4.30 4.21 4.51	44444	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	44.44.4 4.34.4 61	4.93 4.38 4.31 4.62	4.89 4.24 4.06 4.06		4.34 4.22 4.22 4.61
68 68 68 68	Hamibal & St. Joseph cons M 6s 1911. Y Cent & Hudson River Deb Ss 1994. Baltmare & Ohio Ss 1925. Chick MIW & S Paul Term M Ss 1934. Chicago & N W Ky Deb Ss 1999.	44444 1452 1453 150 150 150 150 150 150 150 150 150 150	4.39 4.46 4.81 4.55	4.45 4.45 4.59 6.59	4.4.4 4.83 4.83 5.53	4.4.48 4.48 4.79 4.53	4.482 4.482 4.832 4.57	4.4.4.4 8.4.4.4 8.6.4.4 17.7	44444	4.81 4.44 4.90 4.90 4.84	4.84 4.41 5.00 4.88	4.81 4.39 5.02 4.79		4.81 4.73 5.06 4.79
71	West Shore RR 1st M 4s 2361 Chicago & N W Ry sf Deb 5s 1933	4.57	3.91	3.93	3.93	3.92	3.93	4.00	4.06	4.10	4.75	4.68	49.49	010

YIELDS OF RAILROAD BONDS JAN. 1888—JAN. 1889

Name of Bond	1										-				
4. 53 4. 4. 53 4.	Ref. No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
0.00	Morris Clev Chic			4.4.4.4 4.32 4.32 4.32 4.32			4.4.4.4 4.30 54.45	4.4.4.4 6.53.33 14.41	4.27 4.35 4.35	4444 666 466 686 75 75 75 75 75 75 75 75 75 75 75 75 75	4.4.4.4 9.33 6.33 6.33	4.34 4.34 4.30 4.31			4.19 4.29 4.24
4.51 4.52 4.52 4.52 4.52 4.52 4.52 4.52 4.52	New Chic		4.44 6.11 6.29	4.03 3.94 4.03 4.29		4.46 4.09 4.08 4.11	4.4.4.4.05 01.4.4.4.05 05.4.4.05	4.4.4.4 2.02 4.26	3.82 3.82 4.26 5.95	3.89 3.79 4.21	3.78 3.94 3.94 4.22				3.93 3.68 3.88 4.14
4.08 4.09 5.00 5.00 5.00 5.00 5.00 5.00 5.00 5	555555 555555			4.44 4.28 4.54 4.54		4.44 4.51 4.63 7.63 7.63	44444 44118 44118	4 4 4 4 4 4 4 5 3 5 5 5 5 5 5 5 5 5 5 5	4.22 4.23 4.23 5.23 5.23	4 4 2 2 2 2 4 4 2 2 3 4 4 2 3 3 4 5 4 5 4 5 4 5 4 5 4 5 4 5 4 5 4 5	444 44.32 45.46	4.4.4.4.22.2.2.2.2.2.2.2.2.2.2.2.2.2.2.			4.01 4.01 4.05 4.15
5.0. 4.79 4.60 4.50 4.80 4.88 4.88 4.88 4.89 <th< td=""><td>Can</td><td></td><td></td><td>4.4.80 5.05 8.58</td><td></td><td></td><td>5.07 5.07 4.61 5.19</td><td>5.04 5.04 5.30 5.30</td><td>4447.4 80.02.24 80.02.44</td><td>55.55 57.10 75.55</td><td>5.00 5.20 5.20 4.66</td><td>5.70 5.36 5.36 4.68</td><td></td><td></td><td>4.92 4.92 5.19 4.45</td></th<>	Can			4.4.80 5.05 8.58			5.07 5.07 4.61 5.19	5.04 5.04 5.30 5.30	4447.4 80.02.24 80.02.44	55.55 57.10 75.55	5.00 5.20 5.20 4.66	5.70 5.36 5.36 4.68			4.92 4.92 5.19 4.45
4.17 4.18 4.18 4.19 4.00 4.02 4.20 4.20 4.20 4.20 4.20 4.20	COPE			4.4.4. 00.4.4.4. 00.7.7.4.		4.83 4.83 4.83 4.95	4444 858: 851: 851: 851: 851: 851: 851: 851:	44.85 44.85 70.8	44.81 10.44 47.94 70.97	4.4.4.4. 8.8.4.6.0 8.34.8.0	4.33 4.76 5.76	5 4 4 4 8 3 5 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0			4.88 4.72 4.30 5.00
4.56 4.56 4.56 4.66 4.66 4.66 4.66 4.66	Chic Penr New Nan V			44.24 4.36 4.36 4.31		4.24 4.14 4.71 4.22	4.24 4.10 4.70 4.70	44.44 20.33 21.33 21.33	4444 2021 4122 4118	4.22 4.4.23 4.71 1.19	44.44 4.28 4.28 4.71 121				4.28 4.08 4.21 4.61
4.38 4.41 4.43 4.37 4.28 4.24 4.24 4.29 4.29 4.31 4.09 4.73 4.73 4.77 4.73 4.71 4.09 4.73 4.73 4.73 4.79	Chic Chic West Chic	more & Oulo \$6 1935 Mine & E. Pull Term M \$5 1914. 850 & N W Ry Deb \$5 1909 850 & N W Ry E Deb \$5 1933	4.60 8.98 3.99 4.61	4.56 4.73 3.98 4.62		44.68 77.73 75.36	4.58 3.93 4.58	4.4.6. 6.9.4.9.4.90.90.90.90.90.90.90.90.90.90.90.90.90.	5.44 10.93 10.13	4.53 3.90 8.90 8.45	5.00 5.00 3.91 4.48				4.59 3.84 4.54 5.54
	Chic St. P.	ago & North Western ext 4s 1926. aul Minn & Man cons M 4½s 1933.	4.63	4.41		4.37	4.28		4.24	4.24	4.29				4.09

YIELDS OF RAILROAD BONDS JAN. 1889—JAN. 1890

. 11	8889981	3.77 3.94 4.01 4.40	4.31 4.50 4.64 4.71	4.84 4.84 4.84 4.69	119 83 32 00	4.11 4.67 4.73	61 23 42 42	888
Jan.	4.02 4.28 4.08				4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.		3.83 4.24 4.24 4.24 4.24	4.08
Dec.	4.04 4.23 4.26 4.19	3.87 3.87 4.91 4.34	86.54.44 98.33 97.77	4.4.4.4. 04.4.4. 08.80	4.68 4.84 3.98	4.44 4.75 4.58 4.82	48.44 4.48 4.23 4.58	4.14 3.99
Nov.	4.05 4.26 4.05 4.05	3.95 3.91 3.97 4.40	44444 33333 77	4.52 4.44 88 88 1.95 1.95 1.95	3.99 3.99	4.05 4.74 4.09 4.64	4.44. 4.16 4.52	4.01 4.13 4.00
Oct.	4444 0.03 70.73	3.98 3.96 3.91 4.31	44.49 4.60 7.60 7.60	444.64 74.44 64.66 46.66 46.66 46.66	4444 3.23 9.24 9.24 9.54 9.54	4 4 4 4 6 5 1 4 4 6 5 1 4 4 6 5 1 4 7 4 4 6 5 1 4 7 4 4 6 1 4 6 1 4 4 6 1 6 1	4.64.44 4.09 4.09 4.09	3.96 4.08 3.99
	4.4.4. 00.4.4.4. 00.5.5.0.0.	4.05.98 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.0	84444 812427 812424	44444 645776	3.4.4.4.8 3.94.76 3.94.4.4	24.64.44 000.00	46.64	3.98
Sept.	1							
Aug.	4.07 4.07 4.07 4.05	4.0.4.4.4.10.10.10.10.10.10.10.10.10.10.10.10.10.	44.44 44.54 68.51	44444	4.19 4.72 4.20 3.96	84.34.3 86.5.6 86.6 86.6 86.6 86.6 86.6 86.6 86	4.64.4. 20.7	3.91
July	3.92 2.14 4.19 4.19	3.71 3.71 4.15 4.08	8.96 4.4.4 4.55 4.60	44444 1757 1757 1758 1758	44.44.6 2002.6	3.97 4.59 4.59 5.65	4.48 4.35 4.45	3.97
June	3.98	3.88 3.60 3.75 3.94	82.44 00.44 7.74 7.58 82.44 85.59	44.44.45.97 12.33 15.93 15.93	4.70 4.70 4.70 4.01	3.98 3.81 4.51 4.67	4.832	3.96 3.96 3.95
May	3.88 4.12 4.26 4.01	3.99 3.54 3.97 3.97	4.02 10.44 10.44 10.50 177.44	4.844 4.844 5.044 4.844 5.044 5.044 5.044	4.4.4.65 4.4.83 4.03	3.99 4.51 4.81	4.43 3.98 4.43	3.98
April	4.00	3.94	44444 100000	45.44 69.83 69.89	4.23 4.23 4.25 10 10 10	4.4.02 4.53 7.97	45.50 45.99 45.99	4.10 4.04 3.97
11	4.03	0.28 5 0.175 0.178 0.178 0.178	24444 200000	25.44 4.89 73 73	44.24.4 2.24.25 4.05.44 0.05.44	44.644 4.09.99 4.09.99	45.79	4.08
Mar.	1							
Feb.	3.98	3.96 4.13 4.02	44444	4.24.44	444444	4.10 4.51 4.52 4.52 4.91	4.8.4.6 9.9.4.6 1.5.4.5 1.5.4.5	4.4.4 0.00
Jan.	4.19 4.29 4.24 4.10	3.93 3.68 4.14 4.01	4.05 4.615 4.66	4.5.4.4. 0.1.4.4.4. 0.1.4.8.5.	4.30 4.28 4.08	4.4.4.4. 101.4.4.4. 2.95	4.6.4.4.4.4.0.00.00.00.00.00.00.00.00.00.00	4.26 4.12 4.05
Name of Bond	Pitts Ft Wayne & Chie Jat M 7s 1912. Lidigis & Bessel st M 8f 7s 1914. Lidigis Valley RR 2nd M reg 7s 1916. Lidigis Valley RR 2nd M reg 7s 1915. LS & Marke Ry cones 3f 7s 1916. LS & Sharke Species 18 M 8f 7s 1906.	Pennaytvania RR Co gen M 6s 1910. Wey York & Harbern RR toons M 7s 1900. N Y C & H R RK 1st M 7s 1914. Melb mulk & groniev Rk cons M 7s 1903. Melbigm Central Rk cons M 7s 1903.	Chicago Rk 1s & Pac RR 1st M 69 1917. Chicago & Now Vest cross M 65 1902. Chic St Paul & Mirnt 1st M 66 1918. "Earl M nr & Man 290 M 68 1908. Nash Chitt & St L 1st M 7s 1913.	St. P. & Sinux, Chy, R.R. 1st. M. 6a 1919. Can M. & S. P. (2 M.M. Day), 1st. M. 6a 1910. Canada Santhern P. J. st. M. 5a 1908. Chick St. P. Min & Comba Goods M. 6a 1920. St. P. Min & Man. Calk Day) 1st. M. 6a 1910.	Philadchini & Eric gen M 5s 1920 M & SP (W & PW DV) 11 M Ss 1921 C M & SP (W) & Min dV) 18 M 5s 1921 The E Louis & N Orleans 5s 1951 Pennsylvania C og ul 18 M 445s 1921.	New York Lack & West 1st M 6s 1921 Marnhald & St Jespin com M 6s 1911 N Y Cent & Hudsin River Deb 5s 1994 Hallmore & Olio Ss 1925. Chio Milw & St Faul Term M 5s 1934.	Chicago & N W Ry Deb 5s 1999. West Shore Rt 1st M 4s 2013. Chicago & N W Ry al Deb 5s 1933. Chicago & North West In 26b 1933. St. Paul Minn & Man con 8M 41/2s 1933.	Cin Ind St L. & Chi gen 1st 4s 1936. Pacific RR of Mo 1st ext M 4s 1938. Illinois Central RR coll 4s 1932.
Ref.		55464	925 925 93 93 93	45055	88228	48828	32128	74 75 76

VIELDS OF RAILROAD BONDS JAN. 1890—JAN. 1891

No. Name of Bond Jan. Feb. Mar. Anel May June July Aug. Sept. Oct. Nov. Dec. Jan. Nov. Dec. Jan. Nov.	11	4885	40508	87.87.0	22022	04845	558528	18688	25.22
Parts F. Wayne & Chicago E. Chi	Jan.	44.28 44.28 47.44 71.74			4 5 5 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5	44444 4444 4424 95444	4.26 4.62 3.95 3.95	4.18 4.46 4.46 4.11 4.11	4.22 4.61 5.08
Name of Bood Jan. Feb. Mar. April May June July Aug. Sept. Oct. 1	Dec.	1							
Parts F. Wayne & Chicago E. Chi	Nov.	4.17			42444 411758 411458	222.25 202.25 202.25 202.25	44×46 2410 000 000 000	44.76 44.49 4.17	4.11 5.18
Marrie & Chic 1st M 7s 1912	Oct.	4444 900 4543 0045 005 005 005 005 005 005 005 005 00	44444 883449 6449	44448 089 088 84	48444 7225 7225 725	44444 88.2.2.28 14.08	84.4.4.8 10.4.4.6.10 10.0.10	4 62 4 46 4 46 4 20	4.06
Marrie & Chic 1st Marrie of Board Jan. Feb. Marr. Araril Mary June July Marrie & Chic 1st Marr. Araril Mary June July Morrie & Enser tet Mar 1911 1912 1914 1915 1914 1915 1914 1915 1914 1915 1914 1915 1916 191	Sept.	4444 062:26 063:444 061:44:51	44444 2446 8448	44444 07.939 01.00	44.70 44.70 44.70 7.70 7.70 7.70	4444 32 132 18 18 19 19	4.4.4.6 80.08 80.08 80.08 80.08	4.01 4.07 4.47 4.15	4.04
Pitte P. Wayne & Chic, 18 M. 7 at 912. 410	Aug.	4.10 4.21 4.39 4.39	44444 23022 123524	4444+ 01000 08000	84444 807.90 817.10	4444 92.126 11.23 12.23	3.88 3.88	4.59 4.40 4.12 4.13	4.03
Pheta F. Wayne & Chic at M. 71 1912. Ann. Ann	July	444.6 62.45 80.88 80.88	44444 01.35 0.25 0.25 0.25	4444 82.77 80.95	4.44 4.91 4.26 57	44.79 11.20 17.20 17.20	4.4.4.6 2.5.6 2.5.6 2.5.6 3.6 3.6 3.6 3.6 3.6 3.6 3.6 3.6 3.6 3	44.49 60.49 10.49 10.49	4.01
Peter R. Wagne & Chic Lis M. 7 is 1912. 4.00	June	44444	44444 74.24 38 38	4.57 4.4.90 4.62 4.63	44444 46.25 46.25 46.25	44444 2003 2013 2013	3.99 4.59 3.83	4.05 4.48 4.07 4.07	3.99 4.50
Peter Pete	-	3.92 3.92	44444 378 378	4444 83.83 90.98	44444 465 465 655 650 650 650 650 650 650 650 650 6	4.8 4.03 4.05 4.79	3.91 4.81 3.84 3.84	4.4.09 4.09 4.03 4.03	4.00
Patrick R. Wayne & Chic 13th M. 71 1912. 4 10 4 00 4 00 Morris & Benes et at M of 73 1914. 4 10 4 00 4 00 Morris & Benes et at M of 73 1914. 4 10 4 00 4 00 Cheldry Willey, KRS con M of 73 1919. 4 10 4 00 4 10 Pennary brain R. R. Co gra M of 1919. 4 10 4 00 4 10 Cheldry R. R. R. R. R. R. R. R. R. M. R. P. 1903. 4 10 4 10 Chicago R. Park R. R. R. R. M. M. P. 1903. 4 10 4 10 Chicago R. R. R. R. R. R. R. M. M. P. 1903. 4 10 4 10 Chicago R. R. R. R. R. R. R. M. M. P. 1903. 4 10 4 10 Chicago R. R. R. R. R. R. R. M. M. P. 1919. 4 10 Chicago R. R. R. R. R. R. R. M. M. R. 1918. 4 10 Chicago R. R. R. R. R. R. R. M. M. R. 1918. 4 10 Chicago R. R. R. R. R. R. R. M. R. R. 1919. 4 10 Chicago R. R. R. R. R. R. R. M. R. R. 1919. 4 10 Chicago R. R. R. R. R. R. R. M. R. 1919. 4 10 Chicago R. R. R. R. R. R. R. M. R. 1919. 4 10 Chicago R. R. R. R. R. R. R. R. M. R. 1919. 4 10 Chicago R. R. R. R. R. R. R. M. R. 1919. 4 10 Chicago R. R. R. R. R. R. M. R. S. I. L. R. M. R. 1919. 4 10 Chicago R. R. R. R. R. R. M. R. S. I. L. R. M. R. 1910. 4 10 Chicago R.	April	4.35 4.35 3.94	44444 726 26 26 4.26 7.30 7.30	4444 68 80 80 80 84 84	44444 80000 2000 2000 2000 2000 2000 200	4.87 4.34 4.11 4.11	44.54 4.82 3.60 3.83	4.4.4.4.4.4.0.0.0.0.0.0.0.0.0.0.0.0.0.0	3.98 4.56
Pitts F. Wayne & Chic 21st M. 7st 1912. 4 0.0		3.90 3.90 3.90	4444 422 222 242 243	44444 107.7.6 10.6 10.6 10.6 10.6 10.6 10.6 10.6 10	44444 679 679 679	4.33 4.33 4.14 4.70	4.82 4.82 3.83 4.83 3.84	4.44 4.45 4.08	3.98 4.50 4.92
Name of Bond Name & Chic Jan 77 21912. Morris & Besser its M. 77 21912. Morris & Besser its M. 77 21913. Morris & Morris & M. 77 21913. Morris &	Feb.	l .	4444 26.13 28.13 4.00	44444 807.80		44444 101.03 100.03	4.15 4.15 3.82 3.82	4.4.4.4.4.4.05.4.05.4.05.4.05.05.04.05.05.04.05.05.04.05.05.05.04.05.05.05.05.05.05.05.05.05.05.05.05.05.	4.00 4.48
Pitts F. Wayne & Chie and N = 100	Jan.	4.02 4.30 4.28 3.77							4.90 4.90
20	Name of Bond	1::::	V Y C & H R RR 1st M 7s 1903. Die Blen & Squiner RR coms M 7s 1903. Michigan Renral RR coms M 7s 1903. Diegge & Nor West coms M 7s 1903.	And See Paul & Minn 1st M 6s 1918. *Prul Minn & Man 2nd M 6s 1909. *And Chart & Se J. Jr M 18 11 11 11 11 11 11 11 11 11 11 11 11	and Suthern P. 1 tal. M. S. 1908. Dic St. P. Min & Oman corn M. e. 1930. The Min & Man (Dic Dry) at M. e. 1930. Jindelphia & Lincern M. S. 1920. M. & St. P. (C. & P. W. Dry) at M. S. 1921.	M. & S. P. (Virg. & Min. Do.) 1st M. 5s 1921. M. 6 El. Louis & N. Orleans 5s 1953. comprivanta C. N. 4 M. 4 S. 1921. ew. York Lank & N. 1est M. 6s 1921. damital & S. G. Joseph cons. M. 6s 1911.	VCRUE & Hudson River Deb 5s 1904. stlimere & Olinis 1925. hie Milre & El Paul Ni Ss 1914. hie Milre & N. Paul Term Ni Ss 1914. forst Shore RR 1st M 45 2504.	Andrew & W. W. ve' in Deb. 5, 1933. Ditcago & North Western vet 4s 1926. I. Paul Minn & Marcenn vet 4s 1956. I. Paul Minn & W. Ching in 1st 4s 1956. In Ind St. D. & Ching in 1st 4s 1956. verifie RN Mo Mo 1st ext. M st 1938.	llinois Central RR coll 4s 1952. ake Erie & Western 1st M 5s 1937. Vabash RR Co 1st M 5s 1939.
	No.				655576 605570				

NO.	
AD B	. 1892
LRO	-JAN.
RAI	1891-
S OF R	JAN.
VIELDS	

Oct. Nov.	6 4.26 4.31 5 4.49 4.46 9 4.60 4.50 3 3.90 3.92	4 4.45 4.37 4 4.75 4.70 7 4.66 4.63 9 4.73 4.60 5 4.57 4.43	3 4.67 4.71 0 5.19 5.19 9 4.62 4.67 0 4.99 4.90	7 4.56 4.52 5.4.81 4.76 4.67 4.27	25 4.87 4.77 6 4.59 4.47 6 4.26 4.46 7 4.55 4.55 1 4.99 4.91	2 4.55 4.44 5 4.73 4.71 7 4.80 4.74 5 3.99 3.98	86 4.83 4.61 3 4.66 4.70 3 4.45 4.57 4 2.22 4.57	2 4.29 4.31 9 4.69 4.70 5 5.00 4.96 2 4.84 4.89
Sept.	5 4.26 2 4.55 0 4.60 6 3.93	11 10 13 14 16 16 16 16 16 16 16 16 16 16 16 16 16	44.83 00.5.20 0.5.20 0.5.20	55.4 7.45.85 7.44.85 4.739	4444 95.50 50.50 10.50	25.44.52 0.44.95 0.3.95	0 4.86 4.38 6.4.43 1.4.43	7 5.05 7 5.02
Aug.	25 4 4 58 6 4 62 8 3 4 70 8 3 9 0	52 55.01 52 55.01 52 55.01 52 55.01	44.844 200.20 200.20	25.70 25.00	44446 20.64.446	44.4.4.4.4.6.4.9.8.18.18.19.9.3	4.56 4.46 4.21	4.31 4.74 5.07 5.17
July	4.53 4.53 4.66 3.98	5.4.35 5.00 4.72 6.56	44.84.8 8.88.1.7.00	42.44 50.54	44.86 13.33 14.53 14.73 14.73	4.97	4 4 4 4 4 4 4 4 5 4 5 4 5 4 5 5 4 5	4.30 4.71 5.14 5.27
June	4.4.4.6.63 7.9.4.6.89 8.9.98	44444 400 1787 1787 1787 1787 1787 1787 1787 17	4475478 07.20 01.00	4.02.44 51.944 51.95	5.03	44.04.8 20.08.8	4.37	4.29 4.72 5.16 4.97
May	4.21 4.30 4.55 5.95 5.95	4 4 4 4 4 4 50 50 50 50 50 50 50 50 50 50 50 50 50	4484W	4.6.4.4.4. 0.88.4.4.4. 0.88.4.4.4.	5.01 4.32 4.31 5.05	3.96 3.96 3.96	4.85 4.53 4.53 4.36	4.29 4.65 5.13 4.87
April	4.20 4.45 4.47 4.00	4.4.4.4 61.61 64.46	120512	4.5.4.4.4. 00.38.4.4.	4444 625 625 600	3.93.7	4.72 4.34 4.51 4.37 4.37	4.29 5.05 4.90
Mar.	81.4 84.4 84.4 84.4 90.4	4.29 4.45 4.40 5.35	4.66 4.86 5.17 5.17 5.10	45.54.4 41.884.4	5.44.45 8.23.45 10.00	4.42 5.01 3.94 3.94	44444 5223.4 53.6 64.6 64.6 64.6 64.6 64.6 64.6 64.6 6	5.08 4.82
Feb.	4.13 4.40 4.40 4.12	4 4 32	5.11 5.02 5.03	4.8.4.4 6.5.4.4 6.5.3.7.60	44444 62229	44446 500 500 500 500 500 500 500 500 500 50	25.4444 27.14.51	5.02 4.80
Jan.	44444 488441 488441	4.11 4.50 4.33 8.28	5.087 5.087 5.087 5.087	4 2 4 4 4 20 2 4 4 4 20 4 8 6	44444 84444 8446 8446	4.1.4.4.6 2.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6.6	4.66 4.18 4.46 4.26 4.21	5.08 4.84 4.84
Name of Bend	Pitte Fr Wayne & Chie 1st M 7s 1912. Charles K Seed 1st M 8f 7s 1914. Challes Nathery RR 2nd M reg 7s 1910. Pennsytvania RR Co gen M 6s 1910.	N. Y. C. & H. R. R. I. M. 7s 1903. Michigan Carral I. R. Cone M. 7s 1903. Michigan Carral I. R. Cone M. 7s 1903. Glieggio R. W. Y. For R. R. 1s 7s 1903. Glieggio & Nort West cone M. 7s 1903.	St Paul & Minn 1st M 6s 1918. M Minn & Mary 2014 6s 1999. Is Clart & St L 1st M 8s 1997. Signe City R U 1st M 7s 1997. E & S P (So Min Dr) 1st M 6s 1999.	Canada Southern Ry 1st M 5s 1998. 11.85 F M 1st W Combin comes M 6s 1990. 12.1 Min & Man Dist Dry 1st M 6s 1910. 13.1 Madelolini K Preperent II 5 1970. 14.8 St P (C. & P W Dry) 1st M 5s 1921.	C M & St. P. (Wis, & Min Dry), 1st M Ss 1921. Register L bank & N. Ordens as 1975. Pumosylvania Co. par 1st M 4 Liga 1931. Registry for R Lorde & West 1st M 5, 6, 1931. Hamiltool & Sc Joseph cons M 6s 1931.	M Y Cent & Hudson River Deb 5s 1904. In Itaniary & Olio 5s 1923. Click Miw R Y Full Term M 5s 194. Click Miw R Y Full Term M 5s 194. West Since R V M X Pob 5s 290. West Since RR 1st M 3s 204.	71 Chicato & N W R.; ef Deb 5a 933. 72 Chicato N Vorfull Yestern tria 1996. 73 St. Pull Mirn & Man core M 41:s 1933. 74 Chi mid N L Col, gen 194 1996. 75 [Vadid R M of Mo 18 et M 48 1938.	Ulinois Central RR cell 4s 1952. Lake Eine W Western 1st M Ss 1937 Wabash RR Co 1st M Ss 1939. Ches & O (East Ext) 1st M 6s 1911.
	Morris Morris Cluic & Penns	N Y C & I Cluic Burl Michigan Chicago R Chicago &	Chic St St Paul Nash Cl St P & S C M & S	C M Piches	C M & Cliic St Cliic St Pennsyl New Yo Hanniba	N V Balti Chic Vest	PGS COice	Ulinois Lake El Wabash Ches &

YIELDS OF RAILROAD BONDS JAN. 1892—JAN. 1893

					1		-	and the owner owner, where	-	-		-	-	-
No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
28884	Pittes Fr. Wayne & Chic Jef. M. 7s 1912. Morris & Besser, 1sef. M. 8f 'ss 1914. Lichtigh Valley. R. R. Jah M. fr. 18f 'ss 1916. Chic & Nort West R. No rons 4f 'ss 1915. Flemsylvania R.R. Co gen M. 6s 1910.	4.25 4.26 3.33 5.33 5.85	44.4.4.5 77.2.3.7 7.8.9 8.8	44446 252649	44446 200 466 466 766 766 766 766 766 766 766 766	44446 5000 5000 5000 5000 5000 5000 5000	21.444.8 81.52.8 85.85.8	44446 FESSE	44446 012228	4444.6 E12.64.8	44.44. 3.35. 3.35. 8.35.	3. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4.	44446 340 90 90 90 90	44.44.5 3.45.30 3.45.88
44 45 52 53	N Y C & H R RR 1st M 7s 1903, 1937 Chic Barl R Ghinev RR coms M 7s 1993. Chicago Rt I s & Pac RR 1st M 6s 1917 St Paul Min & Man 2nd M 6s 1997. Nash Chate & St L 1st M 7s 1913.	4.54 4.54 4.77 4.92	4 4 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5	4.53 4.46 4.68	44444 51.53 1.69	44444 51449 1000	4444	4444 74444 8445	4.44	44.51 4.51 4.68	44444 6554 6659	5.03 5.03 5.03	44448 8125 99	24 4 4 4 4 5 6 6 6 4 6 6 8 8 8 8 8 8 8 8 8 8 8 8 8 8
555 57 58 58 58	St. P. & Sloux City, RR. 1st. M. 6s 1919. M. & S. P. (S. Min Dy.) 1st. M. 6s 1910. Cunda, Sorthern Ry, 1st. M. 5s 1908. Elics P. Min & Omila com, M. 6s 1900. St. P. Minn & Man (Data Dr.) 1st. M. 6s 1910.	44.48.44 2.84.48 3.86.48	44444 0014 0014 0014 0014 0014	26.44.44 26.46.88	44444 2022 2022 2022 2022 2022 2022 202	44444 854489	44.44.4 4.60	4.50 4.46 4.82 4.57	44444 800000000000000000000000000000000	44444 127 127 129 167	44444 8888 8888	4.50 4.87 4.87 4.61	44444 88884	44444 4655 4655 4655 4655 4655 4655 465
\$25 \$25 \$25	Philadelpha & Eric gern M. 5s 1920. W. S. S. P. (C. R. P. W. D. P. 1 1 1 1 M. Ss 1021. C. M. S. S. P. (C. R. P. M. D. P. 18 M. Ss 1021. C. M. S. P. (Vis & Min D. P.) 18 M. Ss 1021. Pennsylvania Co. gat 15t M. 4½8 1921.	4.24 4.62 4.43 4.15	44444	24444 6007184 8007184	4 20 4 50 4 4 50 4 15	44444 874085 874085	4.48 4.48 4.30 4.30	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	44444 813321	4.29 4.62 4.28 4.15	44.44.48.48.13.29	44.44 4.70 11.31 13.13	71.44 07.44 14.33 14.33	44444 133644
28888	New York Lack & West 1st M 6s 1921 Inminal & St Despit non M 6s 1911. N Cern & Hulson New Deb 5s 1994. Ballome & Olos § 193. Chie Alliw & St Paul Term M 5s 1914.	44.41 4.276 4.76 4.74	84444 855 855 855 855 855	44444 5233 4653 4653	44444 6411738	44444 6723 443 613 613 613 613 613 613 613 613 613 61	4.36 4.21 4.45 4.60	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	44444 0222444	24.44.4 52.52.52 5.52.52	44444	44444 686418 6148618	44.32 4.44 4.41 5.65	संबंध स्व हिन्दू हुन्दू हैं इस्टूड्डिस
32228	Chicago & N W Fo Dob 5s 1009. Chicago & N W R 14 236 1009. Chicago & N W R 16 100 5s 1933 Chicago & N Ord Western ext 4s 1956. Chicago & N And Western ext 4s 1956.	4.67 4.71 4.19	4.6.4.4. 6.1.2. 6.1.2.	3.90 3.90 4.78 4.59	46.644 27.74 4.13	3.87 4.69 4.11 5.00 4.50	4.6.4.4. 8.6.6.4.4. 8.6.6.4.4.4.	4.15 4.15 4.15 4.15	46.58.94	4.24.44 2002.44 5003.4	3.93 4.60 4.19 5.33	46.44.4 51.55 51.55	3.92 2.62 4.22 4.22 4.51	4.67 3.94 4.24 4.50
72 22 22 22 22 22 22 22 22 22 22 22 22 2	Cur Ind St. E. Cui gen ist 4s 1936. Pacific RR of Mo is even M. Ms 1938. Illinois Commai NR voil 4s 1932. Illinois Commai NR voil 4s 1932. Wabselt RR Co ist M is 1937.	4.4.4.4.09 4.5.55 4.85	4.24 4.09 4.50 4.80	44.27 44.44 4.51 48.51	4.26 4.14 4.02 4.50	4 5 5 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	4.28 4.11 4.42 4.74	3.04 3.04 3.04 4.46	4.30 3.91 4.47 4.79	4.23 4.14 4.53 4.53	2.4.6.4.7.26.4.5.15.26.28.21.28.21.26.20.21.26.21.26.20.20.20.20.20.20.20.20.20.20.20.20.20.	44.29 3.99 2.52 2.52 2.52	4.31 4.20 4.50 4.87	4.32 4.02 4.00 4.49
821 830	Ches & O (East Ext) 1st M & 1911. Rome Water & Deficient soms M 5s 1922. NY Chic & St Louis 1st M 4s 1937. Ches & Ohio Ry 1st cons 5s 1939.	4.30 4.30 4.80	4.69 4.18 4.84	4.75 4.28 4.86	4.78 4.19 4.19	4.73 4.17 4.17	4.72 4.27 4.08 4.80	4.72 4.28 4.15	4.76 4.25 4.19 4.86	4.68 4.32 4.19 4.89	4.4.4.277.4.277.88	4.73 4.29 4.19 4.89	4.74	4.77 4.28 4.19 4.88
I														

VIELDS OF RAILROAD BONDS JAN. 1893—JAN. 1894

YIELDS OF RAILROAD BONDS JAN. 1894—JAN. 1895

1				-	-			-	-	-	-		-	1
No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
88 94 4 64 4 64 64 64 64 64 64 64 64 64 64 64 64	Morris & Essex 1st M sf 7s 1914 Clabin, Valley KR 27st M roy 7st 79 1910 Pensy Your West Ry cons sf 7s 1915 Pensy Young RK 26 cpm M 6s 1910 Clicago RK 1st & Pac RR 1st M 6s 1917.	4.45 3.63 4.38	4.39 4.39 4.21 4.28	4.32 4.32 3.73 4.25	4.44 4.30 3.63 4.25	4 4 4 4 3 5 4 4 4 3 5 4 4 5 3 5 4 4 6	4.35 3.55 4.35 4.30	3.98 4.43 4.15 3.57	4.34 3.56 4.23 3.56	44.24 20.44.2 21.47.4	3.80 4.28 4.09 3.48	8.4.6.6.4 48.1.8.4.1	24.624 28.46 28.40	3.99
553 553	St. Paul Minn & Man 2nd M 6s 1909. Nasi Chait & & Li 18 M 7s 1913. St. P. & Sioux City RR 1st M 6s 1910. C M & St. P (% Min Dy) 1st M 6s 1910. Ganada Southern Ry 1st M 5s 1908.	4.4.4.4.63 24.884.4.30	4.4.4.4.21 4.21 4.21	4.45 4.38 4.69 4.00	44444 088.39 101.088	4 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	4.4.480 4.4.480 4.681 1.681	4.82 4.82 4.30 4.71	4.34 4.34 1.33 1.33 1.33	4 4 4 4 4 8 8 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5			44444 641789	4.45
55 50 50 50 50 50 50 50 50 50 50 50 50 5	Chfe St. P Min & Omain cons M for 1930. P Min & Min Chat Dr) Est M fos 1930. Pitadehim & Ene ren M 5s 1990. M & St. P (C. & P W Dr) P 18 M Ss 1921. C M & St. P (W St. P M Dr) 18 M Ss 1921.	4.82 4.76 4.52 4.72	4.4.4.4 17.1 1.5.0 5.80	4444 5533 56453	4.65 4.4.4 4.41	4.61 4.07 4.42 4.56	44.4.4 63.4.4.4 63.4.4.4	4.61 4.77 4.77 6.06	44.4 44.14 53.4 54.14 58.3	24.444 25.65 53.45				2.44. 2.94. 4.31. 4.04.
55255	Chie St. Louis & N. Ooleans 5s 1951. Chie St. Louis & N. Ooleans 5s 1951. New York: Lack & Weel, 1st. M. 6s 1921. New York: Lack & Weel, 1st. M. 6s 1911. Baltimore & Ohio 5s 1925.	4.13 4.27 4.81 4.33	4.47 4.22 4.67 4.36	74.44 7.63 7.63 7.63	4.58 88.44 7.58 8.58 7.58	3.28 3.82 4.54 4.54	4.33 4.53	3.90 4.09 4.54 4.54	4.53 4.45 4.51 4.51	4 4 4 4 30 30 30 30				3.90 3.90 3.97 4.14 4.39
21288	Chie Milw & St. Paul Term M 5s 1914. Chicago & N W 7D 6b 5s 1909. West Shorn R 1st M 4s 7861. Chicago & N Wy 1st Dob 5s 1933. Chicago & North Western ext 4s 1926.	3.95 4.64 4.64	4.48 3.90 4.55	4.4.5 3.88 4.4.4 0.4.49	44.844	4 4 8 8 8 4 4 5 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	448.44 83.55 14.48	4 4 4 4 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5	3.87 4.05 4.05	4.33 3.86 3.86 3.90	43.53	3.82 3.82 3.90	4.36 3.83 4.61 3.93	4.45 3.83 4.60 4.09
2422	St. Paul Mir & Man cons M 41/5s 1933 Chi, Dai St. & Chi igen sit se 1996. The Disco Chen To No 18 et av M 18 1938. Thinks Chen TX Ko Oil 4s 1923. Lake En & Western 1st M 5s 1937.	4.52 4.23 4.08	4.59 4.11 4.6.11 4.6.04	4.55 3.99 4.33	4.54 3.93 4.34 3.93	4 4 4 53 3 9 9 4 4 3 4 3 4 5 4 5 4 5 4 5 4 5 4 5 4 5 4	44.52 4.44 3.97 4.35	44.51 3.09 4.38 4.09 5.09	4.50 4.29 4.11 3.97	4.49 4.28 3.95 4.35	4.29 4.44 4.01 7.01	4.49 4.31 4.00 3.97	4.4.4.4.9.9.9.3.9.9.3.3.9.3.3.3.3.3.3.3.	4.43 3.92 4.32 4.32
828828	Abbashen R.R. Co. 1st M. Ss. 1959. Chee & Co. (East Eart) 1st M. 6s. 1911. Rome Water & Ogdens come M. Ss. 1922. Rome Water & Captens come M. Ss. 1922. Chee & Choin 1st M. We 1972. Chee & Choin R. M. We 1979.	4.78 4.24 4.17 4.92	4.87 4.21 4.12 4.83	4.82 4.23 4.09 4.81	44.44 74.44 7.12 40.44	4.78 4.04 4.04	4.84 4.60 4.03 4.03	4.4.4.4.4.08 4.008 4.008	4.4.4.4 88.4.4.4 60.1.0 7.7.4	4.4.4.4.4.4.0074.0074.0074.0074.0074.00	4.81 4.04 3.97 4.65	7.7.4 4.33 3.94 4.02	3.99 4.39 3.94 4.63	4.78 4.47 4.00 3.89 4.69
22	III Central (L N O & T) col 4s 1953.	4.24	4.27	4.17	4.11	4.07	4.12	4.13	4.10	4.08	4.06	4.07	4.08	4.12

VIELDS OF RAILROAD BONDS Jan. 1895—Jan. 1896

200	Š.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	
Chief See Sum. City, RR. 1 is M 69 1990. 4.55 4.50 4.50 4.50 4.50 4.50 4.50 4.50	88444	Essex 1st M st 7s 1914. alley RR 2nd M reg 7s 1910. for West Ry cons f 7s 1915. ania RR Co gen M 6s 1910. Rk Is & Pac RR 1st M 6s 1917.	3.90 3.99 3.44 4.18	4.44 3.48 4.19	3.49 3.49 6.26	3.95 4.13 3.48 4.20	3.98 3.13 3.49 81.3	3.96 3.96 3.45 70.4	3.94 3.92 4.01 4.01	3.39 3.95 3.95	8.6.4.8.8 4.0.9.8.8	3.80 3.38 5.05 4.00	3.75 4.07 4.01 3.34 3.91	3.84 3.94 3.34 3.94	3.90 4.03 4.08 4.08	
See Partic & Omerican Conference Medical Medical Conference Medical Medical Conference Medical	55 55 55 55	St. Paul Minn & Man 2nd M 6s 1909 Mark Clark & & St. J. 18t M 7s 1913 St. P. & Sionx City RR 1st M 6s 1910 Can & & E. P. (So Min Dr.) 1st M 6s 1910 Canda & Southern RV 1st M 5s 1908.	4.45 4.45 4.20 4.02	4.54 4.21 4.50	4.56 4.65 4.62 4.62		4.54 4.29 4.57 4.09	4.41 4.63 4.51 4.51	4.30 4.57 4.10 4.50 4.01	4.44.4 6.44.9 6.44.9 6.48	34.50 3.99 3.98 3.98	4.30 4.50 4.08 3.98	4.4.4.4.7.2.2.2.4.4.4.4.7.2.0.3.4.4.4.4.3.3.3.3.3.3.3.3.3.3.3.3.3.3	44.44 44.15 46.15 61.15	4.54 4.70 4.70 4.20	
Pennsylvania (See Louis & Volentus si 1931) Pennsylvania (See Louis si 194) Pennsylvania (See	57 59 50 60 61	Chie St. P. Min & Omaha cons M 6s 1930. P. Min & Min (Dak Dy), 1st. M 6s 1910. Philadelphia & Erie gen M, 5s 1930. C. M. & St. P. (C. & P. W. Dy), 1st. M 5s 1921. C. M. & Se P. (Wie & W. Dy), 1st. M 5s 1921.		4.4.50 4.39 84.39	4.4.50 2.5.50 4.3.50	4.56 4.31 4.31	4 4 5 5 6 5 6 5 6 5 6 6 6 6 6 6 6 6 6 6	4.52 3.93 4.18 4.47	446.44 46.044 47.066	44.644 46.696 30.096	4.4.5 10.4.4.4 127	4.26 3.93 4.11 4.28	44.844 44.93 4.35 7.05	44.38 44.17 44.17	4.35 4.35 4.31 4.53	
Chienge & N. V. W. P. Deb. St. 1999	88588	Chie St Louis & N Orleans 5s 1951. Chie St Louis & Orleans 5s 1951. New York Lack & West 1st M 6s 1971. The Mannala & St Despit con M 6s 1911. Chie Milw & St Faul Term M 5s 1914.	3.90 3.90 4.44 3.24	46.44 9.89 9.60 9.60 9.60 9.60		3.86 3.86 4.29	3.73 3.73 4.60 3.73 3.73	3.65 3.65 4.58 4.28	3.78 3.78 4.25 4.25	3.59 3.87 4.06 4.16	3.71 3.71 4.24 5.16	3.99 3.99 8.22 8.12	3.78 4.02 4.27	3.79 4.08 4.08 4.08	4.24 4.13 4.24 4.24	
Clin Rock L & Clin term 18, 1995. 2 G. In Table R & Chine L & Chi		k N W Ry Deb 5s 1909 re RR 1st M 4s 2361 R W W Ry ef Deb 5s 1933 k North Western ext 4s 1926 dinn k Man cons M 4½s 1933	4.09 4.09 4.09	48.48 3.99 4.47	3.84 4.58 4.08 4.47	4.51 4.50 4.50 4.50	4.64 4.05 4.05 88.38	4.52 4.52 4.34	4.29 4.29 4.29	48.48.4 74.6.4 20.2 20.2	45.48 3.77 4.29 7.27	4.3.4.5 4.3.4.5 4.2.2.2	3.779 3.95 83.95 83.95	7.7.4.4.4.4.4.8.3.3.3.3.3.3.3.3.3.3.3.3.3.3	4.65 4.56 4.06 4.41	
Clone & Office Exp.) 1st M 6s 1911. N Y Cline & Office Exp. 1st M 6s 1912. N Y Cline & Office Exp. 1st M 1	457 57 87 87 87 87 87 87 87 87 87 87 87 87 87		3.92 2.96 2.96 3.92 87.4	45.39 99.44 99.39 1.81	4.26 9.99 4.26 4.26 1.81	4.33 4.02 4.30 4.30	48.84.4 22.24.4 22.25.7	3.83 3.83 4.26 4.64	4.74 4.22 4.22 4.06	3.77 3.77 4.21 4.66	46.82 20.82 4.17 61.19	4 6 3 3 3 2 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	3.95 4.20 4.20 8.20 8.68	3.92 3.92 4.25 4.86	3.98 3.98 4.31 4.86	
C & O (R & A Dr) 1st cons M 4s 1989. 4.28 4.38 4.39 4.37 4.28 4.16 4 C C & E & E (Ex. Dr) 1st coll 4s 1990. 4.47 4.40 4.41 4.41 4.41 4.42 4.33 4 C Tenn V & G Ry cons 1st M Ss 1956. 4.88 4.84 4.84 4.82 4.73 4.61 4.85			3.89 3.89 4.00 4.69	4.58 3.99 4.78 4.14	4.09 3.92 4.14 4.14	4.15 4.14 4.72 4.12	44.54 4.05 4.05 4.05 8.05	4.48 3.98 3.81 4.45	3.95 3.95 4.45 3.87	3.95 3.95 3.86 3.86	46.64.6 777.44.8	3.92 3.92 3.90 9.49	3.89 3.89 3.89 3.93 8.53	4.8.84.8 4.0.6.9.8 4.0.9.4.9.4.9.9.9.9.9.9.9.9.9.9.9.9.9.9.	4.47 4.01 3.91 4.06	
	885	& O (R & A Dv) 1st cons M 4s 1989 C C & St L (St L Dv) 1st col 4s 1990 Tenn V & G Ry cons 1st M 5s 1956	4.47	4.46		4.47	4.42	4.33	4.11 4.25 4.58	4.15	4.19	4.28	4.35	4.28 4.33 4.68	4.30	

YIELDS OF RAILROAD BONDS JAN. 1896—JAN. 1897

Prof. Mar. April Mar. June July Ang. Sprt.		_	:∥-	1000									-	11-	11-	
R. Zad M. Wey 78 1910. R. Zad M. Wey 1910. R.	No.	Name of Bond	Jan.	Feb.		April	May	June	July	Ang.	Sept.	Oct.	Nov	1	!	E I
Control Cont	MUMO	Essex 1st M alley RR 2nd or West Ry mia RR Co a	3.90 4.03 4.04 4.04 7.32	4.04 9.04 4.33 4.14	1	3.91 4.00 4.05 3.46 4.21	3.90 4.07 4.11 4.18			4.45 4.30 4.56 4.54	4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.					2422
4.68 4.81 4.81 4.82 4.82 4.82 4.82 4.82 4.82 4.82 4.82	MAGOO	e Paul Minn & Man 2nd M 6s 1909. 1 P. & Sjour C. Lis M 7s 1913. 1 P. & Sjour C. Ury RR 1st M 6s 1939. 1 P. Maria Southern Pry 1st M 5s 1906. 1 P. W. Min & Omalia cons M 6s 1930.		4.4.4. 4.17 4.17 4.61		4.39 4.13 4.16 4.61	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4			4.83 4.83 4.95 4.97	44444 4.83.83 4.83.45 4.83.45				£1113	च च च च च
4.59 3.88 3.88 3.88 3.88 3.88 3.88 3.88 3.8	WH000	Min & Man (Dak Dv) 1st M delphia & Erie gen M 5s 1920 & St P (C & P W Dv) 1st M & St P (Wis & Min Dv) 1st St St Louis & N Orleans 5s 1951		4.32 4.24 4.34 2.20	45.44 181.44 15.23 15.23	4.35 3.90 4.19 4.31	4.37 4.33 4.17 4.14			4.4.4.4.4.4.4.4.4.5.4.5.4.5.4.5.4.5.4.5	4.4.4. 70.4.4.38 86.4.4.38				885181	च १० च च च
\$ 5.65	HZ,HOO			3.82 3.98 4.59 4.55		3.86 4.54 4.55 4.59	3.81 4.02 4.17 171 171			4.11 5.05 4.56 4.71	44.04 4.19 4.42 4.68				200 47 47	ಹಿದ್ದಾಗಿ
13.03 13.07 13.07 13.08	20000	Vest Stone RR 1st M 44 2361 Thingoo & NW Rr st Deb 83 933 Thingoo & North Western ext 4s 1926 The Laud Minn & Man room M 4/95 1933 In Ind St L& Chi gen 1st 4s 1936.		3.80 4.48 4.01 4.34		3.82 3.95 1.95 1.95 1.95	3.83 3.92 4.31 5.13			7.77.44 7.77.44 7.77.45 7.77.45 7.77.45 7.77.45	3.91 4.74 4.93				37	345044
4.01 5.08 4.00 4.01 5.09 4.00 5.09 4.00 5.09 5.00 5.00 5.00 5.00 5.00 5.00 5	日ませりり	All CR R O Mo 18: ext M 48 1918 Illinois Central RR cold 18: 1952 Alec Eric & Western Its M 58: 1957 The R M 58: 1957 The & O (East Ext) 18: M 69: 1911		3.96 3.87 4.27 4.52											302228	क्रिक्च
C C & St L (St L Dv) 1st col 45 1990 4.35 4.33 4.33 4.34 4.35 4.37 4.56 4.56 4.57 4.87 5.00 4.87 4.79 4.50 4.67 4.67 4.68 4.66 4.67 4.87 5.00 4.87 4.79 4.50 4.67 4.67 4.88 4.50 4.67 4.87 5.00 4.87 6.79 6.40 4.67 6.40 6.40 6.40 6.40 6.40 6.40 6.40 6.40	MACHO	Rome Water & Ordens cons M. 5s 1922. V. Crice & You found 1st M has 1937. Unc & Unc N. St. Louis 1st M has 1937. Unc & Chor Ny 1st cons 5s 1935. C. & C. & C. & C. M has 1935. C. & C. & C. & A. D. V. St. Tool M has 1935.		3.98 3.86 4.00 4.21		3.99 4.61 4.04 4.24	4.01 4.59 4.20			71.4 4.00 4.99 7.16					15,043.89	30404
	OH.	C C & St L (St L Dv) 1st co Tenn V & G Ry cons 1st M		4.33		4.34									.67	***

VIELDS OF RAILROAD BONDS JAN. 1897—JAN. 1898

Jan.	3.62 3.89 3.12 3.72	3.78 3.78 3.99 3.77	3.93 3.97 3.65 3.54	3.99 3.85 4.02 4.11	3.71 3.92 3.92 3.92	4.17 4.15 3.70 3.71	4.29 3.96 3.83 4.17	3.81
Dec.	3.63 3.63 3.72	3.89 3.77 3.89 3.85	3.97 3.98 3.67 3.55	3.94 3.94 3.65 4.12	3.88 88.88 88.88	4.20 4.66 3.71 3.71	3.95 3.95 4.23 4.55	3.84
Nov.	3.63 3.66 3.12 3.12	3.96 3.99 3.96 3.82	4.03 4.11 4.03 3.71	4.06 4.00 3.67 4.11	3.75 4.22 3.97 3.94	3.822 3.777	4.42 3.98 4.26 4.57	3.87
og:	3.63 3.12 3.12 3.17	44.44 4.02 3.25 88.	4.07 4.17 3.71 3.64	4.17 4.20 3.73 4.20	3.77 3.99 4.00 3.89	3.81 3.81	44.48 3.99 4.25 4.25	3.90
Sept.	3.75 3.08 3.75 3.75	44.84. 3.952 3.86 8.86	4.07 4.20 4.02 3.75	4.17 4.00 4.12 3.73 4.17	3.98 3.98 3.98 3.98	4.21 4.72 3.85 3.75	44.45 3.96 4.38 4.58	3.92
Aug.	3.65	3.85 3.85 3.85 3.85	4.04 4.21 3.76 3.57	4.16 4.00 3.71 4.14	3.79 4.21 3.96 3.89	4.22 4.22 3.83 3.77	3.97 3.93 4.25 4.53	3.91
July	3.60 3.93 3.55 3.18	3.95 3.95 3.85 3.85	3.96 4.21 3.77 3.77	48.49 3.99 4.12 5.06 1.13	3.99 3.99 3.89	4.21 4.78 4.04 3.78 3.78	4.49 3.97 4.27 4.57	3.91
June	3.57 4.18 3.57 3.18	3.94 3.94 3.81 3.88	4.02 4.20 3.92 3.65	4.16 4.00 3.71 4.15	3.83 4.23 4.00 3.95	4.21 4.86 4.13 3.76 3.80	3.95 3.95 4.23 4.61	3.96
May	3.64 4.17 3.67 3.87	3.98 4.32 4.32 3.91	4.07 4.20 3.80 3.73	4.15 4.02 4.21 4.26	3.83 4.24 3.97 3.94	4.26 4.90 4.11 3.83 3.79	3.93 3.93 4.23 4.63	4.00
April	3.72 4.13 3.23 3.84	4.62 3.98 4.38 3.91	4.08 4.21 4.05 3.82 3.75	44.44 44.04 33.73 73.73	3.985 3.98 3.93	4.23 4.89 4.11 3.83 3.83	4.51 4.05 4.25 4.64	3.99
Mar.	3.72 3.85 3.19	4.50 3.98 4.35 3.94	44.44 44.23 3.86 3.76	4.30 4.11 4.42 4.42	3.98	3.87 3.87	4.54 3.93 4.28 4.65	3.99
Feb.	3.72 3.28 3.28 3.94	34.38 3.89 3.89	3.85 3.85 3.83	4 4 4 6 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	3.94 3.94 3.94 3.90	33.86 3.86 3.86	4.4.4.4.4.95 4.36.00	4.07
Jan.	3.96 3.96 3.97 3.97	3.88 88.88	4.32 4.32 3.85 3.91	34.45 4.45 4.43 8.43 8.43	3.98 4.36 4.17 3.96	4.26 4.69 3.92 3.82	4.58 4.05 4.35	4.11
Name of Bond	Morris & Essex 1st M sf 7s 1914. Lehigh Ayalley RR 2nd M reg 7s 1910 Chic & Nor West Ry cons 8f 7s 1915 Pennsylvania RR Cogen M 6s 1910 Chicago Rk 18 & Pac RR 1st M 6s 1917.	Nash Chatt & St. L 1st M 7s 1913. Csr Pet Sigurt RN 1st M 8s 1919. Csr Pet Sigurt RN 1st M 5s 1908. Chick St Paffis & Comba goom M 6s 1930. Philadelphia & Erie gen M 5s 1920.	C M & St. P (C & P W Dv) 1st M 5s 1921. A & St. P (M & M Dv) 1st M 5s 1921. Chic St. Louis & M Dv) 1st M 5s 1921. Chic St. Louis & N Orleans 5s 1951. Bransylvania C og 11st M 4/5s 1921. New York Lack & West 1st M 6s 1921.	Hamibal & St. Joseph coms M 6s 1911. Chicago Min Wey Dale Parl Term Ms 1914. Chicago Ni W ty Dale St 1905. Chicago Ni W ty Dale St 1905. Chicago & Ni W ty St 18 M 4s 230. Chicago & Ni W ty of Dab 5s 1933.	Chicago & North Western ext 4s 1926. Sayan Mine & Ann cons M 45s 1933. Chi Ind St. R. Chii gen 1st 4s 1556. Pacific RR of No 1st ext M 4s 1938. Illinois Central RR coll 4s 1952.	Lake Eric & Western 1st M Ss 1937. Whath RR CO 1st M Ss 1939. Ches & O (Rast Ext) 1st M 6s 1911. Oncur Warer & Ogdeiss cons M Ss 1922. N Y Chic & St Louis 1st M 4s 1937.	Ches & Ohio Ry 1st coms 5s 1939. C RO On O & Th Coll et 1933. C RO C Ma Ly Dy 1st coms M 4s 1939. C C & E L (E L Dy 1st coll et 1939. C C R & E L (E L Dy 1st coll et 1939.	Chic Milw & St Paul gen M 4s 1989
Ref. No.	86644	53 54 57 59 59	82222	200217	25456	77 78 80 81	288888	87

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APPENDIX

VIELDS OF RAILROAD BONDS JAN. 1898—JAN. 1899

	Name of Bond	Jan.		P-1	April	May	June	July	Aug.	00	Oct.	Nov.	. Dec.	
prris & Esse high Valley ic & Nor V nnsylvania icago Rk I	Morrise Breact st. M. af 78 1910 Lohigh Valloy R.R. Zud M. reg. 78 1916 Chie & Nor Weet R.y consaf 78 1915 Petms/Yarnia R.R. Co. gen M. 6a 1910 Chicago Yk. Is & Pec R.R. 181 M. 6a 1917.	3.62	3.05	3.87 3.76 3.10 3.85	3.75 3.75 3.75 8.75	3.87 3.26 3.87	3.85 3.85 3.85 3.83	3.75 3.70 3.80	3.77 3.61 3.08 3.74	3.77 3.65 3.16 3.78	33.92	33.95	33.45 7 3.91 7 3.12 6 3.65	W C CIV
sh Chatt & P & Sioux ic St P Mis lladelphia & M & St P (Naah Chatt & St. List M. 74 1913 Chi Say Mari City INR 1st M 64 1919 Chi Say Mari Est man M. 1919 Chi & Say F. (C. & P. W. Dr.) stst M. Say 1921. Chi & Say F. (C. & P. W. Dr.) stst M. Say 1921.	3.99 3.99 3.93	3.90 3.90 3.77 3.93	4.40 4.00 3.79 4.02	4.61 3.82 4.21	4.04 4.04 3.384 13.84	4.01 3.94 3.80 4.01	3.90 3.90 3.79 3.96	3.83 3.83 3.91	3.89 3.89 3.84 3.91	3.83 3.83 3.83 11.6 3.83	3.822 3.828 3.828	2.24 2.24 2.24 3.73 3.73 7.73	
M & St P (ic St Louis nusylvania w York La	CM & St. P. Wils. & Min. Dv. 184. M. 5s. 1921. CM & St. P. Wils. & Min. Dv. 1951. Pumrsylvane Co. gul. et al. 4/4/6. 1931. Pumrsylvane Co. gul. et al. 4/4/6. 1931. Raminal & St. Joseph cons. M. 6s. 1921. Raminal & St. Joseph cons. M. 6s. 1921.	33.97	3.98 3.70 3.60 4.01	3.82 3.62 3.62 4.05	3.99 3.64 4.12	4.23 3.92 4.65 6.65	3.80 3.62 4.14	4 3 3 6 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	3.99 3.69 3.61 3.95	3.70 3.70 3.64 3.98	45.55 20.55 20.55 20.55	33.92	23.55 23.95 23.95 24.95 25.55 25.55	
ic Milw & icago & N Set Shore R Icago & N Icago & N Icago & N Icago & No	Chie Milw & S. Paul Term M. S. 1914. Chicago & N. W. Po De Sa, 1909. West She N. W. Po To Pe Sa, 1909. Chicago & N. W. Y. of De Ss, 1933. Chicago & North Western set 44 1906.	3.85 4.02 3.67 3.77	3.81 4.05 3.66 3.72	3.85 4.26 3.71 3.70	3.84 3.84 3.84 3.86	4.06 3.78 3.78 3.81	4.01 3.72 3.72 3.79	3.98 4.11 3.69 3.75	3.73 3.73 3.73	3.95 3.68 3.74	3 73 17 17 17 17 17	33.98 3.72 3.72	3.93	
Paul Minn cific RR of nois Centra ke Erie & V bash RR ('8t. Paul Mirne & Man cross M. 4/5s 1933. Pencific RR of Mo 1st ext. M. 4s 1938. Illinois Central RR coll 4s 1952. Take Exter & Western 1st M. 5s 1937. Walnesh RR Co 1st M. 5s 1939.	3.82 3.92 4.17 4.17	3.82 3.98 4.17	3.92 3.96 4.21 4.76	3.89 3.94 4.31	3.98 3.98 4.29 4.64	3.89 3.93 4.23 4.53	3.90 4.20 4.50	3.82 3.82 4.18	3.82 3.82 4.43 84.48	3.79 3.79 44.21	3.91 3.76 4.4.19	23.88 20.03 3.80 3.80 4.13 4.13 88 88 80 80 80 80 80 80 80 80 80 80 80	
es & O (Ea me Water Y Chic & S es & Ohio I	Control Cont	3.70 3.70 3.71 4.29	3.72 3.75 3.96 3.96	3.80 3.88 4.37 4.03	4.31 3.85 3.96 4.43 7.15	3.77 3.85 4.04	3.38 3.70 3.99	3.63 3.78 3.78 3.96	3.76 3.76 3.76 3.97	3.57 3.77 3.99	3.41 3.41 3.98	80.48 77.57 8 3.27.58	3.23.23.23.23.23.23.23.23.23.23.23.23.23	
C & O (R & C C C & St I E Tenn V & C Chic Milw & Lake Sh & M	& O (R. & A Dr.) 1st cons M 4s 1989 C. & Set I. (St. J. Dr.) 1st con 4s 1990. Term V & C. Ny, coms 1st M 5s 1786. Milly & & Fillagen M st 1989. ste E D. & Mich So 1st M 3/5s 1997.	3.83 3.83 3.32	3.84 4.14 3.77 3.31	3.82 3.82 3.82 3.82	3.96 3.90 7.4.8	3.98 4.37 3.94 3.94	3.87 3.87 3.87	3.89 3.81 3.37	3.78 3.78 3.34	3.94 3.82 3.32	88.44.60 83.82 83.82 83.83	3.78	3 20 23 25 25 25 25 25 25 25 25 25 25 25 25 25	

VIELDS OF RAILROAD BONDS JAN. 1899—JAN. 1900

Ref.			1	:	1	-	-	:	-					
è	Name of Bond	Jan.	reb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
86 44 83 84 45 84 45 84 84 84 84 84 84 84 84 84 84 84 84 84 8	Moorie & Essex 1st M of 7s 1914. Chinky Valley RR 2nd M reg 7s 1916 Chinego Rt 1st Per RR 1st M 6s 1917. Nash Chatt & St L 1st M 7s 1913.	3.82 3.50 4.06	3.50	3.50 3.79 3.52 3.62	3.82 3.82 3.50 4.16	3.38 3.77 3.55 4.11	3.70 3.70 3.51 4.08	3.49	3.55 3.36 4.09	3.57 3.34 4.25	3.98 3.38 4.29	3.62 3.62 3.40 4.32	64.8.4 00.7.4 00.4.4 00.7.4 00.4 00.7.4	3.61 3.51 3.52 4.31
54. 57 63 63	St. P & Sioux City, RR 1st M 6a 1919. C. M. & St. P (& R. Ver Worlds own M 64 1900. C. M. & St. P (C. & P. W. DV) 1st M 53 1991. For this K. Loule & N. Orleans 85 1951. Fermsylvania Co. gu 1st M 4248 1971.	3.72 3.65 3.65 3.97	83.56 83.56 83.56	3.399 3.869 3.869 3.869 3.869	3.96 3.96 3.83 4.49	3.59 3.59 3.83 4.6	3.76 3.90 3.79 3.79	3.77 3.93 3.78 3.46	3.80 3.93 3.58 3.80	33.95	3.87 3.98 3.71 3.61	3.92 3.93 3.93 3.64	3.95 83.95 83.95	4.01 4.14 3.67 3.92 3.69
25 73 73 75	New York Inck & West ist M 6s 1921. Chicago & N W Ye st Deb 5s 1933. Things & N W Ye st Deb 5s 1933. Padife RM of Mor one M 4/9s 1933. Padife RM of Mo ist est M st 1938.	3.53 3.87 3.83	3.54 3.92 3.92 3.72	3.53 3.92 3.92 3.69	3.37 3.89 3.71	3.38 3.86 3.61 3.65	3.41 3.50 3.62 3.62	3.86 3.66 3.66 3.66	3.50 3.87 3.68 3.68	3.52	3.558	3.56 3.57 3.79 3.79	3.63 3.78 3.78 3.84	3.56 3.58 3.80 3.80 3.80
88 73 80 81 81 81 81 81 81 81 81 81 81 81 81 81	Illinois Carteral RR coil 4s 1952 Lander Ente W. Western 1 at M so 1957. Wabsail RR Co 13t M So 1937. Watter RR Co 13t M So 1930. Nature Year Co Septiens come M So 1922. N Y Carter & Cours Set M 4s 1937.	3.78 4.31 3.20 3.71	3.77 4.10 3.22 3.71	3.86 4.08 4.31 3.22 3.72	3.78 4.06 3.26 3.68	3.77 4.02 4.21 3.27 3.69	3.76 4.03 3.29 3.68	3.79 3.99 3.28 3.68	3.83 3.31 3.66	8.44.8 3.34.30 3.77.5	3.36 3.36 3.74	3.99 3.48 7.38 7.38	3.28 3.77	3.29 3.29 3.76
888832	(Clea & Ohio Ky 1st cons 8 3999 III Contra (L N O & T) rod se 1953 C & C (K & A Dry) ist cons M se 1989 C (L & SE L (K L Dry) ist cons 1st 1980 D Tenn V & G Ky cons ist M se 1980	3.88 3.88 3.97 4.32	3.78 3.78 4.34	3.86 3.77 3.99 4.29	3.84 3.78 3.97 4.24	3.77 3.77 3.96 4.20	3.76 3.77 3.95 4.22	3.81 3.82 3.94 4.17	3.83 3.83 3.90 4.17	3.80 3.80 3.92 4.23	3.85 3.85 4.27	3.89 3.91 3.94 4.26	44.844 4.00 4.00 4.34	45.21 33.93 4.31 4.31
92 88 83 84 84 84 84 84 84 84 84 84 84 84 84 84	Chic Milw & St. Paul gen M 44 1089 Lesch & Wilch Co let M 345 1997 St. P Milw & Man (Mon EN 181 M 46 1997 Ballmone W Olo RX 181 M 48 1946 Union Pac RX 181 M RM & 18 46 1947.	3.62 3.28 3.77 4.07	3.58 3.25 3.77 4.08 3.83	3.61 3.21 3.71 4.14 3.83	3.56 3.18 3.65 3.78	3.53 3.96 3.96 3.73	3.53 3.14 3.70 3.95 3.73	3.56 3.17 3.73 4.01 3.75	3.55 3.19 3.78 3.78	3.59 3.21 3.86 4.07 3.83	3.62 3.24 3.92 3.88	3.20 3.20 3.82 3.91	3.66 3.18 3.90 3.95 3.95	3.64 3.18 3.84 3.84 3.85
943	Chicago & Nor West gen M 35/5s 1987 Thi Rock is & Ner Ry gen M 44 1988. Atrif Top & Santa Re gen M 48 1993. N Y Cent & Hudson River M 35/5s 1997.	3.42 3.76 3.98 3.13	3.38	3.36	3.29	3.21 3.67 3.94 3.13	3.18 3.67 3.92 3.12	3.20 3.69 3.96 3.15	3.21 3.74 3.97 3.16	3.23 3.77 3.98 3.17	3.25 3.78 4.05 3.18	3.23 3.82 4.06 3.21	3.26 3.85 3.20 3.20	3.28 3.82 4.05 3.20

BONDS	=
RAILROAD	900-IAN, 190
OF	- N
YIELDS	2

	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
P Shice	Chit. & Nor West Ry cons at 7a 1915. Chitego Rk 1s& Pac RK 1st M 6s 1917. Nash Chatt & St. L 1st M 7s 1913. St. Pac Stoux Chyr RK 1st M 6s 1919. Chite St. P Min & Omaha cons M 6s 1930.	3.51 3.62 4.31 4.01 4.14	4.34 3.56 3.93 3.93 3.93	3.43 3.51 4.05 4.05	3.55 3.75 3.79 4.03	3.45 3.86 4.86 80.4	3.46 3.66 3.80 4.10	3.53 3.70 3.35 4.35 4.35	3.50 3.68 4.24 3.85 4.13	3.55 3.69 4.33 4.12	3.57 3.70 4.31 4.09	3.65 4.24 3.76 4.08	3.59 3.64 3.81 4.02	3.55 3.58 4.12 3.81 4.01
C M Chic S Penns New West	C M & St. P (C & P W Dv) 1st M 5s 1921. Consist Louis & N Orleans 5s 1931. Pumsylvania Co gn 1st M 445s 1931. War Net Lack & West 1st M 6s 1921. West Snore RR 1st M 45 3361.	3.67	3.57	3.59 3.59 3.53 3.53	3.58 3.58 3.58 3.58	3.53 3.53 3.53 3.54	3.522	3.90 3.90 3.65 3.65	3.97 3.69 3.69	3.75 3.44 3.60 3.58	3.50 3.50 3.50 3.51	3.69 3.49 3.63 3.53	33.55	3.50 3.53 3.53 3.53
Passen	St. Paul Minn & Man cons M 44/se 1933. Initing Central KR coil 4s; 1092. Itake Brie & Western 18 th 5s 1937. Makshi RR Co. 18 th 8s 1937. Rome Water & Ogdens cons M iss 1922.	3.80 4.06 4.30 3.29	3.73 3.95 3.30 3.30	3.32	3.91 3.92 3.92 3.31	3.952	3.39 3.95 3.39 3.39	3.75 3.91 3.93 3.40 3.40	3.78 3.93 4.19 3.40	3.78 3.94 3.35 3.35	3.93 3.93 3.93 3.35 3.35	3.90 3.90 3.89 3.32	3.857 3.857 3.33.855	3.86 3.86 4.09 3.31
> 20 NO	N V Chic & St. Louis 1st M 4s 1937. II. Commil. (J. NO & T) Fool 4s 1933. C. C. (R. & A. D.) 1st cons 3t M 4s 1983. C. C. & St. L. (St. L. D.) 1st cons 1st 1930.	3.76 3.96 3.93 3.93	3.89 3.96 3.95	3.91 3.91 3.94	3.89 3.89 3.84 3.92	3.70 3.91 3.94	3.71 4.18 3.91 3.96	3.95 3.95 3.95	3.98 3.98 3.98 3.98	3.95 3.95 3.95 3.95	3.93 3.93 3.94 3.91	3.85 3.85 3.85 3.85	33.85	3.85 3.85 3.85 3.85
E Perie	E Tenn V & C Ry cons let M \$a 1956. Chic Milw & S Heul gen M 48 1999 Le Soi & Mich So I et M 5½8 1997 E Min & Minn Ron EN 18 M 4s 1957 Baltinore & Ohio RR 1st M 4s 1958.	3.64 3.84 3.84 4.10	3.02 3.02 4.04 4.04	3.60 3.60 3.19 4.01	3.57 3.85 3.85 3.85	3.158 3.158 4.02	4.27 3.63 3.19 4.03	3.62 3.62 3.19 4.05	3.153 3.153 4.07	3.63 3.63 3.85 4.07	3.65 3.20 3.89 4.03	3.62 3.19 3.86 4.01	3.53 3.53 3.82 3.99	3.52 3.20 3.85 3.96
E 88.4.7	Union Peac RR 1st M RR & 1q de 1947 Chirapo & Nor Weet gam M 3/254 1947 Chir Rock 1s & Peac Ry gam M 4s 1998. And IT Dpp & Sammer Pegam M 4s 1998. N Y Cente & Hudson River M 3/25 1997.	3.28 3.28 4.05 3.20	3.81 3.20 3.78 3.24	3.20	3.80 3.75 3.75 3.99	3.82 3.17 4.00 3.19	3.81 3.75 4.00 3.18	3.78 3.20 4.00 3.20	3.78 3.20 3.75 4.02 3.19	3.20 3.20 3.79 3.20	3.81 3.25 4.01 3.22	3.78	3.74 3.19 3.93 3.19	3.74 3.93 3.93 3.19
3 2 2 2 2 B	Schot Val & New Eng 1st M 4s 1989 Lubilty Valuey (VV) 1st M 45s 1940 Louisville & Nesh unfied 4s 1940. Chi Bene RX (R St. Vo Coora M 4s 1946. Chi Bene & Q (Ill Day) M 33s 1949.	4.05 4.12 4.10 3.96 3.39	4.19 4.09 3.97 3.33	3.33 3.33	3.89 3.89 3.33	3.90 4.14 3.90 4.06 4.06	4.07 4.15 3.91 3.38	4.10 4.11 3.39	4.08 3.91 3.39	4.01 4.07 3.95 3.40	3.93 3.93 3.37	3.34 3.34	3.346 3.346 3.346	3.92 3.99 3.86 3.35
Centra Nor P	Central Pacific 1st ref M 4s 1949. Nor Pac Ry prior lien lg M 4s 1997.	3.90	3.88	3.87	3.86	3.87	3.88	3.86	3.88	3.90	3.91	3.87	3.84	3.84

BONDS	
RAILROAD	TAN 1000
OF.	Tax 1001
VIELDS	-

No.	555.55	82225	77 78 88	85832 8532 8532 8532 8532 8532 8532 8532	888 888 888 889	94 93 94 93	28882	101
Name of Bond	Chick & Now West Rv. coms of 19 1915. Chickop Mr. Is & Per RR 18 18 46 1917. Neal Drink & List M 18 1915. Neal Chick & List M 18 1915. Chick & P. & Shourk Chy RR 18 4f 186 1990. Chick & P. Min & Omata coms M 68 1990.	C M & St. P (C & P W Dv) 1st M 5s 1921. Like St. Loik & N Orleans 2s 1931. Pennsylvania Co. gu 1st M 445s 1921. Wew York Lade & West 1st M 6s 1921. West Silone RR 1st M 4s 2561.	S. Paul Minn & Man cons M 41/4s 1933. Linko Central RR tool led 1922. Liabe Eric & Western 1st M 5s 1937. Whenbain RR C of st M 5s 1939. Rome Wester & Ogdens cons M 5s 1922.	N V Chic & St. Louis 1st M 4s 1937. N V Chic & St. Louis 1st M 4s 1937. (I Contral (L. N O & T) rot 4s 1933. C C R & A Pro 1 st coms 3 M 4s 1939. C C & St. L (8t. L D v) 1 st cont 1599.	E Tenn V & G Ry cons lat M 5s 1056 Chic Miw & S Haul gen M 4s 1989 LARE Din & Mich SO Ist M 545s 1997 P D Miw & Mark (Mon BA) Ist M 4s 1997 Baltimore & Chic RR 1st M 4s 1949	Union Pac RR 1st M RR & ig 4s 1947 Union Pac RR Vers gen M 5/5s 1987. Chi Nools 18 & Pac Ry gen M 4s 1998. Chi Charl Top & Shant F a gen M 4s 1993. N Y Cent & Hudson River M 3-5s 1997.	Scioto Val & New Eng 1st M 4s 1080. Longin Yaller VX V 1st M 145 1940. Lonsville & Nash unfield 4s 1940. Gir New Co com M 4s 1946. Gir Bur & Q (III Div) M 37ss 1949.	Central Pacific 1st ref M 4s 1949. Nor Pac Ry prior lien 1g M 4s 1997
Jan.	3.55 3.58 4.12 4.01	3.53	3.86	3.85 3.85 3.85	3.52 3.52 3.85 3.96	3.74 3.08 3.93 3.19	3.92 3.99 3.35 3.35	3.84
Feb.	3.35 4.17 3.77 3.90	3.58 3.51 3.51	3.86 3.86 4.08 3.29	3.64 3.89 3.84 3.86	4.15 3.51 3.79 3.91	3.74 3.19 3.92 3.19	3.95 3.99 3.85 3.85	3.97
Mar.	3.38 3.61 3.73 3.79	3.53.58	3.69 3.85 4.09 3.27	3.83 3.78 3.83 3.88	4.16 3.52 3.20 3.74 3.89	3.76 3.20 3.70 3.91	3.93 3.95 3.85	3.97
April	3.31 3.65 3.70 3.81	3.55 3.55 3.55 3.55	3.71 3.83 3.84 3.26	3.66 3.77 3.82 3.82	3.21 3.21 3.73	3.79 3.72 3.91 3.19	3.93 3.91 3.85	3.99
May	3.31 3.65 3.64 3.79	3.71 3.59 3.56 3.56	3.75 3.96 4.09 3.35	3.85 3.85 3.85 3.85	3.19 3.84 3.99	3.81 3.22 3.74 3.91	3.92 3.92 3.87 3.41	3.82
June	3.23 3.70 3.70 3.80	3.74 3.59 3.59	3.75 3.94 4.08 3.33	3.85 3.85 3.87 3.87	3.21 3.21 3.75 3.88	3.79 3.20 3.75 3.21	3.95 3.90 3.84 3.41	3.98
July	3.31 3.73 3.70 3.80	3.80 3.65 3.65 3.51	3.78 3.99 4.11 3.31	3.67 3.86 3.84 3.91	3.02 3.02 3.76 3.90	3.3.21	3.93 3.93 3.40	3.95
Aug.	3.34	3.80 3.66 3.66	3.77 3.81 3.99 3.32	3.69 3.85 3.86 3.93	4.19 3.63 3.21 3.75	3.3.75 3.75 3.24 3.24	3.95 3.95 3.91 3.41	3.96
Sept.	3.37 4.28 3.85 3.87	3.82 3.67 3.60	3.76 3.81 3.99 3.25	3.70 3.91 3.91	3.04 3.04 3.74 3.92	3.79 3.25 3.25	4.00 3.92 3.92 3.41	3.98
Oct.	3.40 3.77 3.83 3.83	3.79 3.66 3.58 3.58	8.6.9.8 3.096.8 3.096.8	3.95 3.95 3.95	3.64 3.64 3.22 3.88	3.80 3.79 3.89 3.21	33395	3.95
Nov.	3.35 4.15 3.75 3.75	3.77	3.78 3.94 4.06 3.31	3.62 3.79 3.87 3.88	3.62 3.21 3.78 3.87	3.79 3.78 3.79 3.21	3.94 3.95 3.96 3.91	3.94
Dec.	3.32 3.63 4.15 3.77	3.73	3.79 3.79 4.08 3.31	3.79 3.86 3.86	3.23 3.23 3.73 3.89	3.30	33.90	3.96
Jan.	3.32 3.58 4.10 3.81 3.74	3.67 3.62 3.52 3.55	3.72 3.93 4.09 3.31	3.68	3.70 3.88 3.88	3.79 3.70 3.20 3.21	3.96 3.96 3.89 3.41	3.91

YIELDS OF RAILROAD BONDS JAN. 1902—JAN. 1903

			211.1	111111111	-			
Jan.	3.69 3.94 3.94 3.89	3.70 3.86 3.68 3.68	3.89 3.95 3.95 3.56	3.91 3.91 3.94 3.94	4.15 3.33 3.95 3.95	3.385	3.98 3.98 3.97 3.66	4.01 3.89 4.01
Dec.	3.60 3.68 3.96 3.96 3.93	33.73	3.90 3.90 4.06 3.55	3.95 3.95 3.95 3.95	3.57	3.35	3.98 4.15 4.02 3.99 3.65	3.91 4.04
Nov.	8.55 2.55 2.55 2.55 2.55 3.55 5.55 5.55 5	33.83 33.69 3.58 3.58	3.83 3.97 3.55 3.55	3.76 3.92 3.92 3.94	3.56 3.37 3.37 3.99	3.33 3.35 3.35 3.35 3.35 3.35	3.95 3.95 3.61 3.61	3.91
Oct.	3.54 3.93 3.93 3.87 8.78	3.568 3.564 3.564	3.83 3.87 3.97 3.63	3.93 3.93 3.93	3.55 3.55 3.91 5.01	3.30	3.98 4.10 3.97 3.58	3.90 3.97
Sept.	3.56 3.85 3.85 3.85	3.70 3.76 3.61	3.81 3.84 3.94 3.66	3.92 3.92 3.92	3.74 3.74 3.74 3.89	3.21 3.29 3.24 3.24	3.58 3.58	3.88
Aug.	3.55	3.71 3.80 3.69 3.59 3.52	3.81 3.93 3.93 3.58	3.72 3.84 3.90 3.94	3.52 3.72 3.72 3.90	3.79 3.30 3.90 3.26	3.94 3.94 3.55	3.97
July	3.57 3.48 4.10 3.80 3.78	3.58	3.81 3.79 3.90 3.50	83.89 40.88 40.88 40.88	3.49 3.27 3.71	3.30 3.30 3.61 3.27	3.95 4.00 3.92 3.51	3.95
June	3.77	3.83 3.67 3.56 3.56	3.79 3.74 3.91 3.45	3.75 3.82 3.87 3.87	3.25 3.25 3.70 3.91	3.80 3.30 3.26	3.94 4.01 3.91 3.47	3.93
May	3.36 3.51 3.78 3.78	3.58 3.72 3.47 3.47	3.76 3.73 3.96 3.99	33.372	40.88 54.08 57.08 1.09 1.09	3.79 3.28 3.61 3.25	3.91 3.93 3.87 3.43	3.95
April	3.39 3.47 4.10 3.79 3.74	33.52	3.75 3.77 3.92 3.33	88.88 94.88 88.88	3.24 3.24 3.24 3.88 3.88	33.87	3.92 3.99 3.92 3.87 3.41	3.94
Mar.	3.47 3.79 3.79	3.55 3.48 3.56 3.56	3.77 3.91 3.30 3.30	3.83	3.25 3.25 3.70 3.89	3.77 3.23 3.87 3.87	3.93 3.93 3.85 3.41	3.93 3.93
Feb.	3.33	33.55	3.77 3.77 3.28 3.28	3.70 3.83 3.83 3.90	3.51 3.70 3.70 3.89	3.76 3.27 3.61 3.21	3.95 3.95 3.86 3.41	3.93
Jan.	3.32 3.58 4.10 3.81 3.74	3.67 3.62 3.52 3.57 3.56	3.72 3.93 4.09 3.31	3.68 3.79 3.89	3.22 3.22 3.70 3.88	3.70	3.96 3.96 3.89 3.41	3.94
Name of Bond	Chie & Nor West Ry cons sf 78 1915. Chieven Rk is & Pac R It st M 68 1917 Nash Chatt & St L Its M 78 1913. St P & Sonc City RK 1st M 69 1919. Chie St P Min & Orman cons M 68 1930.	C M & St. P (C & P W Dv) 1st M 5s 1921. Chic St. Louis & N of Nethern 5s 1931. Permeytwalia Co gui 1st M 45s 1931. New York Lack & New 1st M 6s 1921. West Shore RR 1st M 4s 25s1.	Sr. Paul Minn & Man cons M 445s 1933 Minnis Central Rx coil 4s 1932. Likle Ene W Western 18 M 5s 1937. Maksha RX Co est M 5s 1938. Rome Water & Ogdens cons M 5s 1922.	N V Chic & S. Louis 1st M 4s 1937 Ches Wolto RV 1st come 5s 1933 C & O (R & A D V) 1st come 10 18 1953 C & C & & S. L (S. L D V) 1st col 8s 1950	E Tenn V & G Ry cons 1st M 5s 1956. Cale Minw & Ry Paul gen M set 1989. Lake Sha Mitch So 1st M 5/5s 1997. P Min & Min (Mon EN) 1st M set 1997. Bulfmore & Olio RR 1st M set 1987.	Union Pac RR 1st M RR & 1g 4s 1947 Chirago & Nor Warge gran M 53,581 987 Chirago & Pac Pac Pay gran M 54 1998. Attr Pro & Senner Pe gran M 4s 1995. NY Vent & Hudson River M 33,58 1997.	Scioto Val & New Brg 1st M 4s 1989. Leigh Valler (YV) 1st M 45s 1940. Louisville, 8 Nash umfed 4s 1940. Chi Seyen RR & Raw Co Geor M 8s 1946. Chi Bur & Q (Ill Day) M 93; 8 1949.	Central Pacific 1st ref M 4s 1949. Nor Pac Ry prior lien Ig M 4s 1997. Norf & West Ry 1st cons M 4s 1996.
Ref.	55 54 57	062 63 70 70 70 70	77 77 80 80	888888	88 88 90	92222	98889	101

VIELDS OF RAILROAD BONDS JAN. 1903—JAN. 1904

				100110	20112				***
1	1 :	3.73 3.73 3.79 3.84	3.84 3.71 4.04 4.09	4.23 3.78 3.87 4.22 3.91	3.50 3.50 3.50	3.99	4.08 4.04 4.22 4.07	4.06 3.86 4.07 4.18	3.82
1	Jan.	04400			w4400	wwww	चं ल चं चं चं	चं ल चं ल चं	10 4
1	· i	3.72 4.21 3.87 3.81	3.75 4.05 4.13	3.78 3.78 3.93	4.01 4.02 4.23 3.67 3.50	3.95 3.95 3.95 3.95	4.05 4.10 4.22 4.11	3.84 4.11 3.95 4.18	3.87
1	Dec.	10 m m m m	ww4w4	40040	क क क क क	w 41 w w w	क्ल क्ष क	40404	10 di
	-:	3.80 3.80 3.80	3.82 3.76 3.88 4.15	3.75 3.75 3.84 3.91	3.67 3.48 3.48	33.99	172	43.79 3.96 3.96 3.16	337
1	Nov.	44400	30000	40040	44400	w4.ww	3.57 4.10 4.22 4.17	40404	3.87
1		25.8.22	168212	22022	0,033.11	252020	N 10 00 N	- W-1-0	22
	Oct.	3.72 4.09 3.85	3.87 4.08 3.89 4.17	3.71 3.90 3.97 3.97	3.56 3.56	3.98 3.98 3.62 3.97	3.61 4.18 4.15	4.11 4.11 3.97 4.19	3.87
1		1000000	20250	40400	80844	28518	000000	15000	04
1	Sept.	3.75 4.19 3.98 3.98	3.92 3.72 4.07 4.19	3.79 3.79 4.29 4.29	4.10 4.10 3.84 3.61	2.01 4.03 4.07 4.05	4.09 4.16 4.12	4.20 3.93 4.15 4.02 4.21	3.90
İ	-	40000	001153	00000	07400	9940H	00101	00000	30
1	Aug.	3.76 3.94 3.94	3.93 3.72 4.11 3.90 4.16	3.82 3.82 4.28 4.00	3.89	444.84 284.04 10.04	3.69 4.17 4.19	4.16 4.16 4.20	3.90
	-4								- 3
	July	3.90 4.08 4.07 3.91	3.84 3.72 4.10 3.87 4.16	3.80 3.80 3.96 4.23 3.94	4.07 3.99 3.74 3.53	3.99 4.03 3.53 3.94	4.08 3.60 4.14 4.18 4.07	4.14 4.18 4.00 4.17	3.88
1	5								
	June	3.68 4.04 3.86 3.86	3.77 3.69 4.01 3.85 4.16	3.81 3.91 4.20 3.96	3.91 3.98 4.31 3.68 3.46	3.97 3.97 3.85	4.04 4.10 4.16 4.04	4.11 3.81 4.14 3.97 4.10	3.82
	5								
	à	3.72 4.00 4.11 3.83	3.71 3.69 3.98 3.84 4.09	4.18 3.70 3.88 4.15 3.89	3.92 3.95 3.66 3.46	3.98	4.02 4.01 4.15 4.02	4.05 3.75 4.11 3.95 4.05	3.79
ı	May	24400	w w w w 4₁	40040	22422	00000	40444	40404	€ 4
ı	=	3.78 4.03 4.11 3.82 3.97	3.69 3.69 4.01 4.01	3.69 3.69 3.87 4.21 3.93	3.95 3.96 4.24 3.67 3.51	3.95 3.95 3.83	4.01 4.04 4.04 4.05 4.05	3.78 4.11 3.94 4.09	3.84
	April	4400	3000	40040	60,000 € 60,000	w 4. w w w	40444	40404	ω.44
	_	22882	22222	4.23 3.60 3.84 4.18 3.92	\$2052	3.90 3.92 3.52 3.81	3.41 3.41 4.04 4.04 4.07	3.75 4.08 4.08 4.05	3.82
	Mar.	3.76 3.76 3.82	3.67 3.64 3.95 3.91 4.01	40040	3.97 4.20 3.63 3.45	$\omega \omega \omega \omega \omega$	ਚ ਨ ਚ ਚ ਚ	40404	6.4
1		122022	88888	452481	40800	17,025	800084	88882	3.74
-	Feb.	3.965	3.62 3.90 4.00	3.55 3.84 4.08 3.91	3.98 3.59 3.59 3.59	3.95	3.97 3.98 3.98	8.84.84 9.869 9.869	6.4
1	-	82882	220000	9326	337244	30000	880088	28080	3.70
,	Jan.	3.70	3.63 3.89 3.95	3.56 3.83 4.05 3.91	3.94 3.57 3.33	3.3838	80.83 80.83 80.83 80.83 80.83	3.97 3.66 4.01 4.01	6.4
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1							h		gen M 5s 1987 cons M 4½s 1999
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ı			11111	11111	1111	1111	11111		: :
1			11111	11111		11111	1111	1111	: :
1		: 5	1::::	11111	11:11:	st M 4s 1937. s 1948. 4s 1947. ½s 1987.	11:1:	1 1 1 1 1	: :
I		1 1 1 2 2	-: 53 : :	2	6,00	2			: :
J	Name of Bond	55 19.	192	s M 5s 1922. 4s 1937. 4s 1939.	95.5	98.48	56,88	3 M 4s 1946 1758 1949 18 1949 1 4s 1997 M 4s 1996	:66
ı	ı m	25.5×2	35 S	35.05 95.05	48 8 18 19 19	19 18 18	0.723	96.661	19
ł	40	28 1 S	25.4 1.4 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5 1.5	8 193	A 8 8 8	184 48 184 48	\$5.4%2	18 94 85 48 48 48 48 48	272
1	i i	AN BO	1258st	193 184 188 188	3 Kt st	PEREK	Mry 4	M 133	58
1	Z S	ED at B	t 1 st 1 st 1 st 1	8 5 4 5 S	827.8	E E E E	6 t 2 t 2	M 31 M 48 Ig M	M.S.
1		15 Kap No.	M. n.	T.	15 0 DE	RY E	E SE	್ಟಿಕ್ ಕ್ಷನ್ನ	Con
1		4.49.4 g	R R R	ogd Ost	San	or B	E CHAI	Nav Co cons M 4s 195 (III Div) M 3½s 1949. c 1st ref M 4s 1949 nior lien lg M 4s 1997. Ry 1st cons M 4s 1996	F #5
1		500 St. St.	Ves Ves	ZCLES	ರಹ್ಲಿಸಿಕ	Big and	as Selda	ZETEN	Z.S
1		P fin v	York Lack & West 1st M 6s 1921 Shore RR 1st M 4s 2361	2 5 2 3 C	& O (R & A Dv) 1st cons M 4s 1989 C C & St L (St L Dv) 1st col 4s 1990 Tenn V & G Ry cons 1st M 5s 1956 Then N & St Paul gen M 4s 1989 ske Sh & Mich So 1st M 3½s 1997	n & Man (Mon Ex) 1st M 4s 1937 & Ohio RR 1st M 4s 1948 RR 1st M RR & 1g 4s 1947 Nor West gen M 34s 1988 Is & Pac Ry gen M 4s 1988	88888 847 24	\$ C 8 C #	2 or
1		St. Post	# PAGE	P Sic 8	S A S	K Seg 2 E.	le Val	E SER	2 ×
1		SYL	Sis Est	S Ch	SHE	Men Page	St. C. C.	Sal Bar	ral
1		Chic & Nor Weet Ry cons sf 7s 1915 St P & Sioux City RR 1st M 6s 1919 Chic St P Min & Comata cons M 6s 1930. C M & St P (C & P W Dry) 1st M 5s 1921. Pennsylvania Co gu 1st M 4½s 1921	New York Lack & West 1st M 6s 1921. West Shore RR 1st M 4s 2361. St Paul Minn & Man com M 445s 1933 Ullinois Central RR coll 4s 1952. Lake Erie & Western 1st M 5s 1937.	Watash RR Co 1st M 5s 1939. Rome Water & Ogdens cons M 5s 1922. N Y Chic & St Louis 1st M 4s 1937 Chee & Chic Ry 1st coms 5s 1939 III Central (L N O & T) col 4s 1953	C & O (R & St C C & St E Tenn V & Chic Milw 8 Lake Sh & Lake Sh & B	St P Min & Man (Mon Ex) 1s Baltimore & Ohio RR 1st M 4s Union Prec RR 1st N RR & 1g Chicago & Nor West gen M 34, Chi Rock 1s & Pac Ry gen M 4	Atch Top & Santa Fe gen M 4s 1995 N Y Cent & Hudson River M 3½s 1997. Scioto Val & Wew Eng 1st M 4s 1989 Lehigh Valley (N Y) 1st M 4½s 1940 Louisville & Nash unified 4s 1940	Oregon RR & Nav Co cons M 4s 1946 Chi Bur & Q (Ill Div) M 3½s 1949 Christian Ra 1949 Orar lac Ry prior lien lg M 4s 1997 Norf & Weet Ry 1st cons M 4s 1996	Central RR of N J gen M 5s 1987 Hocking Valley 1st cons M 4½s 19
	-						48.80 € €		
	Ref.	57 57 63 63	64 73 76 77	82 83 83	88 87 88	\$2228	988 888 888	102 109	104

YIELDS OF RAILROAD BONDS IAM, 1904—IAM, 1905

Jan.	3.86 3.91 3.64 3.62 3.63	3.69 3.81 3.98 4.05	3.64 3.82 3.79 3.92	3.555	3.75	3.98	3.3.3.9 8.38.93 8.88.83	4,15
Dec.	3.90 3.70 3.75	3.70 3.87 3.84 4.01	3.71 3.81 3.96	3.50 3.50 3.83	3.88 3.77 3.55 3.91	3.89 3.89 3.89	3.71 3.99 3.99 3.68	4.12
Nov.	3.98 3.98 3.73 3.78	33.71 4.00 4.00	3.70 3.70 3.87 3.97	3.98 3.65 3.80 3.87	3.86 3.79 3.56 3.91	3.52 3.93 4.02 3.95	3.74 3.98 3.99 3.70	4.14
Oct.	33.99	3.71 3.89 3.80 4.12	3.69 3.76 3.98 3.94	3.97 3.56 3.52 3.87	33.88	3.53 3.96 3.97 3.91	3.80 3.99 3.99 3.71	4.18
Sept.	3.97 3.97 3.80 3.66	3.72 3.93 4.12 4.12	3.98 3.98 3.95	3.96 3.51 3.51 3.87	3.92	3.51	3.80 3.90 3.72	4.18
Aug. S	3.97 3.97 3.85 3.65	3.72 3.97 3.82 3.96 4.12	3.94 3.87 3.94 3.94	3.50 3.50 3.50 3.84	3.91 3.56 3.84 3.92	3.98	3.79	4.16
July	3.77 3.77 3.77 3.70	3.72 4.01 4.00 4.10	3.76 3.83 3.96 3.96	3.97 3.51 3.86 3.86	33.78	3.52	3.73	4.17
June Ji	3.83 3.83 3.83 3.83 3.83	3.74 4.03 4.07 4.14	3.83 3.84 3.86 3.96	3.54	38.50.53	3.53	3.82	4.20
	4.08 3.91 3.79 3.79	3.74 3.87 3.87 4.19 4.19	3.87 3.82 4.18 4.01 3.89	3.98 3.70 3.55 3.55	33.98 33.98 33.90 33.90 33.90	3.58 4.01 4.04 3.97 3.97	3.86 3.88 3.88 3.88 3.84 3.84	4.25 4
il May						3.59 4.4.05 4.08 4.00 3.4.4.4.		
. April	22 4.12 5 3.88 9 3.92 9 3.79	33.75 10.45.09 14.05 19.05	3 3.77 3 4.20 4 3.92 8 3.99	33.71 33.71 33.71 4.00	3.98 3.3.59 6.3.3.59 6.4.01		2 3.91 3 3.90 6 4.11 7 3.88	2 4.27
Mar.	2 4.15 0 3.85 6 3.89 7 3.79	9 3.73 9 3.91 1 4.09 3 4.24	3.87 2.4.23 2.3.94 3.98	22.4.00 3.73.73 4.00 4.00	2 4.01 9 3.89 0 3.62 8 4.06	3.62 7 4.07 2 4.23 1 4.11 8 4.05	3 3.92 3 3.93 3 3.93 3 3.87	9 4.32
Feb.	4.31 3.80 3.81 3.81	3.70 3.89 4.23	3.92 3.92 3.97	3.52 3.52 3.99	4.8.8.4 0.9.89	3.61 4.07 4.22 4.11 4.08	3.89 3.93 3.83 3.83	4.29
Jan.	4.22 4.10 3.79 3.84 3.84	3.71 3.88 4.09 4.23	3.78 3.91 3.99	3.50 3.50 3.50 9.90	83.59 83.59 83.91	3.58 4.04 4.07 4.06	3.86 4.07 3.92 4.18 3.82	4.32
Name of Bond	(s. P. & Sigury City R.R. i sts. M. 6s. 919) Citic St. P. Min & Omnia cons M. 6s. 1930. Ch. R. & St. P. (C. & P. W. 197) 1st M. 5s 1921. Pennsylvamia C. on 1st M. 44; 87. 1921.	West Shore RR 1st M 4s 2361. St Faul Minn & Mann cons M 4/4s 1933 Illinois Central RR coil sc 1922 Labe Enc & Western 1st M 5s 1937 Walbash RR Co 1st M 5s 1939	Rome Water & Ogdens cons M 5s 1922 Y w. Pink. & St. Journis 1st M 1949 Chee & Ohlo R y 1st cons 3s 1936 C & O (R & A D y) 1st cons M 4s 1935 C & O (R & A D y) 1st cons M 4s 1939	C C C & St L (St L Dv) 1st col 4s 1990. Them Y & Q F ye cons 1st A 5s 1956. Chic Mirw & St Faul gem M 4s 1996. Chic Mirw & St Faul gem M 4s 1999. St P Mir & Man (Mon Ex) 1st M 4s 1997.	Baltimore & Ohio RR 1st M 4s 1948 Chinon Per RR 1st M RR & 18 st 1947 Chinospo & Nort West gen M 53-58 1907 This Dec I be F R y gen M 4s 1998. Atch Top & Santa Pe gen M 4s 1995.	N Y Cent & Hudson River M 3½4 1997. Lehigo Yali & Wew Eng 18t M 458 1990. Lehigo Yali Po Y J 18t M 458 1990. Conswille & Nava Diago 1900. Oregon R.R. & Nav Co cons M 48 1966.	Chi Bur & Q (III Div) M 35/s 1949. The start of M sk 1949. Nor Pac No prior len! fo M sk 1997. Nor R West Nor ste com sk 44 1996. Central RN of N J ger M K 5 1997.	Hocking Valley 1st cons M 4½s 1999
No.	54 57 63 64	7723	8837	88888	82222	98288	\$2225 \$2255	105

YIELDS OF RAILROAD BONDS JAN. 1905—JAN. 1906

Chic St P. N. & St. N. & Chic	Name of Bond	Jan.	Feb.	Mar.										
c St P. C St St C St St C St St C St St St Shor St Shor St Shor St Shor St St Shor St St St St St St St St St St St St St				÷	Tide of	May	June	July	Aug.	9	- 1	۹ ۱	- 1	Jan.
Paul M nois Ce ke Eric Ibash R me Wa Y Chic	Chie St P Min & Onabla cons M 6s 1930. C M & St P (C & P W D v) 1st M 5s 1921. Bernsylvania Co gu 1 st M vi 45s 1921. New York Lack & West 1st M 6s 1921. West Shore RR 1st M 4s 2361.	3.91 3.62 3.63 3.63	3.68	3.80 3.67 3.68 3.70	3.83 3.68 3.71 3.67	3.81 3.72 3.74 3.69	3.73	3.50	3.74 3.72 3.68 3.68	3.75	3.74 3.81 3.65 3.65	3.73 3.89 3.71 3.71	3.77 3.90 3.72 3.72	3.79 3.71 3.71
Y Chic	St. Paul Minn & Man cons M 445s 1933. Lake Eric & Western 1st M 5s 1937. Lake Eric & Western 1st M 5s 1937. Makhai R R Co 1st M 5s 1939. Rome Water & Ogdens cons M 5s 1922.	3.81 3.82 4.05 3.64	3.89 3.78 4.05 3.63	3.89 3.76 4.01 3.65	3.90 4.02 4.10 3.65	3.91 4.02 3.67	3.82 3.71 4.01 3.68	3.83 9.69 3.69 3.68	3.80 3.71 3.60 3.60	3.76 3.72 3.69 3.69	3.73 3.74 4.01 4.08 3.77	3.76 3.76 3.99 3.75	3.81 3.74 4.00 4.18 3.79	3.77 3.72 4.00 4.17 3.80
2 % 2 % 2 % 2 %	N Y Chic & St Louis 1st M 4s 1937. III Central II, N & Y 100 4s 1935. C C O (R & A D) 1 st cons 4s 1950. C C C & St L (St L Dy) 1 st cons 1 st 1950.	3.82 4.02 3.79 3.92	3.78 3.90 3.90	3.79 3.91 3.96	3.83 3.94 3.96	3.79 3.93 3.93 3.93	3.77 3.92 3.92 3.95	3.77 3.78 3.94 3.94	3.78 3.77 3.96 3.96	8.9.77. 8.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.	3.77 3.91 3.92	3.78 3.93 3.93 3.95	3.80 3.79 3.89 3.98	3.78 4.02 3.92 3.93
Tenn V nic Milw kee Sh 8 P Min	E Tenn V & G Ry cons 1st M 5s 1956. Lake Mink S Pull gen M se 1990. Lake Sit & Mich So 1st M 33s 1997. Ey Wite Wan (Mon Es) 1st M se 1937. Baltimore & Oilo RR 1st M se 1948.	3.3.49 3.82 3.82 3.82 3.82	3.54 3.81 3.83 3.83	3.54 3.54 3.84 3.84	3.56 3.56 3.58 3.88	3.55 3.83 3.83 8.83	3.84 3.84 3.82 3.82	3.50 3.50 3.81 7.00	3.60 3.48 3.48 3.81	3.63 3.83 3.83	3.85 3.85 3.85	3.83 3.83 3.83 3.89	3.64 3.85 3.90 3.90	3.62 3.81 3.81 3.85
nion Par nicago & ni Rock ch Top Y Cent	Union Pac RR 1st M RR & lg 4s 1947 Chicago & No West gen M 45 1987 Chi Rock 18 & Pac Ro gen M 45 1988 Chi Act Top & Santar F gen M 45 1995 N Y Cent & Hudson River M 33/ss 1997.	3.76 3.75 3.89	3.74 3.50 3.77 3.89	3.54	3,72 3,53 3,90 3,52	3.78 3.79 3.91 3.53	3.77 3.79 3.89 5.53	3.74 3.74 3.87 3.87 4.54	3.73 3.79 3.89 3.54	3.53	3.82	3.54 3.54 3.57	33.75	3.73 3.51 3.90 3.56
ioto Va. chigh Va outsville regon R. ni Bur &	Scioto Val & New Eng 1st M 4s 1989 Leight Valler (VN 7) x In M 54s 1940 Louisville & Nasiu unified 4s 1940 Louisville & Nasiu unified 4s 1940 Chi Bur & Q (Ill Day) M 35;s 1945 Chi Bur & Q (Ill Day) M 35;s 1945	3.98 3.85 3.87 3.69	3.93	3.96 3.95 3.91 3.08	3.96 3.99 3.92 3.92	3.99	3.98 3.95 8.95 8.90 8.90	3.88	3.95 3.98 3.79 3.71	3.94 3.92 3.90 3.71	3.93	3.98 3.98 3.74 3.76	3.98 3.98 3.76	3.99
ntral P or Pac I orf & W ntral R	Central Pacific 1st ref M 4s 1949. Nor Reve Ry princip len B, M 4s 1997. Nord Revet Ry 1st cone M 4s 1996. The Carrier R R of M 2 gen M 5s 1997. Hocking Valley 1st cone M 45s 1999.	3.93 3.98 3.98 3.66 4.11	3.82 3.82 4.06	33.99 4.07 4.07	3.98 3.95 3.95 4.10	3.99 3.94 3.08 4.09	3.82 3.95 4.10	33.99 4.3.92 4.00	3.80 4.03 8.09 8.09 8.09	3.82 3.70 4.04	3.97 3.83 3.72 4.06	3.86 3.74 4.09	3.85 3.96 4.17	3.99 3.81 3.76 4.15
N & W Ry Div 1s Ore Sh Line RR c Southern Pac 1st A T & S Fe Ry ac Northern Pac Ry	N & W Ry Div 1st 1 & gen M 4s 1944. Southern Fac 1st 1 & gen M 4s 1946. Southern Fac 1st 1 of M 4s 1953. T & S P & P W and M 4s 1945. Northern Fac My Gent Inn 3s 2047.	4.13 4.13 4.24 3.95	4.08 4.13 4.17 3.93	44.06 9.14.16 3.95	4.08 4.16 3.23 3.96	4.06 4.21 4.21 3.95	4.04 4.23 3.96	4.04 4.12 4.19 3.93	4.14 4.17 4.23 3.91	4.12 4.13 4.18 3.92	3.90 3.90	44.44.80 11.25.24	4.07 4.23 3.94	4.05 4.11 4.19 3.92

VIELDS OF RAILROAD BONDS Jan. 1906—Jan. 1907

•	,			21.		7121			
	Jan.	3.94	3.91 4.24 3.90 4.19	3.92 4.04 3.75	3.74 3.97 3.92 3.61	3.98 3.75 4.06 4.09	3.99 3.99 3.95	4.33 4.33 4.33	4.27 4.37 4.13 4.16
	Dec.	4.04 3.90 3.90 4.04 5.90 5.90	3.88 4.19 3.91 11.11	3.92 3.99 4.22 3.77	3.3.3.4.3 9.0.98 9.0.98	4.4.3.39 4.08 9.08	3.89 3.89 3.89 8.90 8.90 8.90	4.08 4.27 4.24 4.30	4.25 4.35 4.07
	Nov.	4448 002 103 103 103 103 103 103 103 103 103 103	8 4 4 8 4 5 8 6 4 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	3.88 44.04 3.74 3.74	3.99 3.99 3.99 5.91	3.98 4.108 4.08	3.90 3.88 3.90 3.90	3.01 4.27 4.26 4.26	4.26 4.33 4.01 4.15
	Oct.	45.45.8 93.83.83	8 4 4 8 4 4 8 6 4 2 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5	3.90 3.97 4.11 3.71	3.93 3.93 3.93 3.93	3.96 3.78 4.11	8.48.43. 90.89.89.90.90.90.90.90.90.90.90.90.90.90.90.90	3.92 4.26 4.26	4.26 4.36 4.02 4.12
	Sept.	444.8 90.98 18.8 18.8 18.8	54.4.6.4 7.86 1.86 1.56	3.91 4.00 4.22 3.70	3.94	3.99 4.09 4.09	44.06 2.94.01 2.94.08	3.96 4.26 4.26	4.37
	Aug.	23.44.4	344.3 43.35 15.25	3.86 3.98 4.08 3.71	33339	3.96 3.75 4.06 4.06	3.988.888888888888888888888888888888888	4.03 4.27 4.22 4.19	4.24 4.37 3.98 4.04
	July	2.6.4.6. 7.0.4.6.0.4.	3.78 4.13 4.08 4.08	3.68 3.68 3.68	3.59 3.59 3.59	4.8.8.4. 2.6.4. 0.01.	3.98 3.91 3.87	4.18 4.18	4.35 3.96 4.07
	June	3.99.99.99.99.99	3.78 4.10 4.25 4.08	3.69 3.69 3.69 3.69	33.88	3.95 4.00 4.00	3.88 3.88 3.86 3.86	4.02 3.90 4.15 4.15	4.35 3.98 4.06
	May	33.80	13.79	3.79	33.93	3.98 4.01 4.04	3.90 3.90 3.90 3.90	4.00 3.91 4.25 4.17	4.36 4.03
è	April	3.92	3.77 4.18 4.25 4.25 4.12 4.12	3.83 4.03 3.74 3.74	3.54 3.85 3.85 3.85	3.95 3.96 4.02	3.86 3.86 3.88 3.88	3.99 3.89 4.17 4.22	4.27 4.34 3.97 4.05
Jones I	Mar.	3.90	77.55 77.55 77.85 1.10	3.84 3.98 4.02 3.73	3.54 3.95 3.89 3.89	3.95 3.92 4.01 4.00	3.85 3.84 4.03 3.87	3.99 3.82 4.18 4.09	4.26 4.26 4.04
1	Feb.	33.78	3.73 3.98 3.78 3.78 0.02	3.79 3.67 3.67	3.50	3.91 3.92 3.96 3.99	3.82 3.79 3.85 3.85	3.99 3.78 4.16 4.07	4.17 4.22 3.95 3.99
Jan.	Jan.	3.70	3.72 4.00 4.17 3.78 4.02	3.92	3.73	3.90 3.90 3.99 3.99	3.80 3.75 3.99 3.81	3.95 3.76 4.15 4.05	4.19 4.23 3.92 3.97
	Name of Bond	Chic Set P Min & Comaha cong M os 1930 Chic Set P (C. & P W Dry 1 st M M S 1921. Fernissy vania C o gu 1 st M 4/5s 1921. Weef Shore R R 1 st M 4/5s 1921.	Illinois Central RR coil 48 1932. Table Dis W Western 18 M 53 1937. Wheel Root 1st AM 58 1939. N Y Chick St Louis 1st M 48 1937. Gries & Olio My 1st cons 58 1939.	III (Central (L. N. O. &. T.) col 44 1953 (C. C. R. &. A. D. Y. Ist const. M. 48 1989 (C. C. R. &. C. L. G. L. D. J.) Het col 48 1989. (C. C. R. W. &. C. R. C.	St. P. Mich So 1st M 33s, 1997. St. P. Mich So 1st M 33s, 1997. St. P. Mich St. Mich St. Miss Miss 1997. Birthmon Ro. R. R. Miss 1995. Union Pac R. M. R. R. R. st. 995. Chicago & Now West gen M 35s, 1995.	Chi Rock is & Per Ry gen M 48 1988. Arch Trop & Sama Fr gen M 41 1995. N V Cent & Huston River M 33,54 1997. Edot O'di & New Fin a fet M 45 1990. Edot Willey (N Y) 1st M 4358 1940.	Louisville & Nash unfiled 4s 1940. Chi Was R. & Ko Coon M. W st 9166. Chi liu K. Q. (III Dr.) M. 3/28 199. Cernal backfic kir m M. si 1997.	Are Week Fyst cong M 4s 1996. Contral REG NY Fee M 8s 1987. Hocking Valley 16 to con M 4/4s 1994. N & W NY DY 18 to K for M 4s 1944. Ore Sh Line RK cons 18 x 35 1946.	Southern Pac 4st ref M st 4s 1955 AT R & S Fie Ry and M at stamped 1995 Northern Pac Ry gen lion 3: 2407 All Coast Line 1st cons M 4s 1952
	. e.	13225	81 82 83	8883	83000	98 93 94 95	88888	00243	12088

YIELDS OF RAILROAD BONDS	JAN. 1907—JAN. 1908

H			AN. 1701	oner were	oner.		ı					I			
400	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	
23882	Chie S. P. Min & Omaha cons M 6s 1930. C. M. & S. P. (C. R. P. V. D.) 1 ket N 5s 1921. Pennsylvania Co gal 1st M. 4 4/5s 1921. Weg Shore NR 1 st M 48 2 G/1. S. Paul Minn & Man cons M 4 ½s 1933.	44.8.84 20.94.8.8 40.88.80	4.4.4. 2.8.00 2.8.8.00	4.15 3.93 5.07 5.05	4.18 4.10 4.11 3.91 4.07	4.17 3.91 4.13 4.13	4.15 3.90 4.15	4.14 4.12 3.94 4.17	4.44.4 22.22.4 22.22.4	4.44 4.18 4.26	4.4.4.4 2.5.4.4.4.4 3.3.5.4.4.4.4	4.81 4.50 4.50	24.44.4 08.51.4 21.13	4.37 4.10 3.99 4.23	
22332	Illinois Central RR coll 4s 1952	3.91 4.24 4.29 3.90 4.19	3.95 4.23 3.91 4.21	8 4 4 8 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	3.96 4.28 3.97 4.30	4.34 4.34 4.39 4.39	4.38 3.99 4.43	4.4.4.4.4.4.6.0.4.5.0.4.5.0.4.5.0.1.0.4.5.0.1.0.1.0.1.0.1.0.1.0.1.0.1.0.1.0.1.0	4.4.4.4 80.4.4.65 4.00.4	4.13 4.13 4.13 64.13	4.38 4.38 4.17 4.17	24444 089 088 088	4.4.4.4.4.4.4.63	4.49 4.49 4.23 4.49	
826833	III Central (D. N.O. &. T), col. 4s. 1953. C. &. O. (R. &. D. D.) 1st const. 4s. 1990. C. C. &. S. E. (St. D. D.) 1st const. 4s. 1990. Term V. &. (R. cross 1 st. N. 5s. 1956. Chie Mirw. &. P. Patul gen. M. 4s. 1990.	3.92 4.06 3.75 3.75	4.00 4.14 4.22 3.81	3.4.4.2 3.26 3.99	4.02 4.16 4.21 3.92	4.07 4.07 4.27 3.92	4.10 4.32 4.33 3.94	4.09 4.29 4.40 3.94	4.13 4.20 3.98	4.17 4.26 4.54 4.00	4.33 4.77 4.01	4.44 4.45 4.88 4.88	4.87 4.83 4.84 4.04	4.27 4.64 4.64 3.96	
222838	Lake Sh, & Mich So, 1st M 3/5s 1997. 12 Min & Min (fon Ex) 1st M 4s 1937. 13 Halmore & Olio RR, 1st M 4s 1948. Chino Po, RR, 1st M RR, 1st 1947. Chicago & Nor West gen M 3/5s 1997.	3.74 4.05 3.97 3.61	3.76 3.99 3.97	3.79 3.79 3.71 3.71	3.76 4.10 3.99 3.77	3.79 4.13 4.05 3.75	3.83 4.03 3.80	3.81 4.13 5.03 5.73	3.80 4.14 4.19 3.77	3.74 4.25 4.21 3.81	3.87 8.30 8.27 8.87	4.47 4.48 4.29 3.91	3.95 4.41 4.00 4.00	3.88 4.26 3.99 3.99	
955 55	Chi Rook Ia & Pac Ry gen M 4s 1988. 1441 Top & Smarth F fegn M 4s 1959. N Y Cent & Hudson River M 53/ss 1997. 1640 Chi M 18 1899. Lehigh Valler (N V) 1st M 44/ss 1990.	3.98 4.06 4.06	4.01 3.78 4.08 4.11	44.84.4 00.44.0 11.09.0 12.09	3.82 3.82 4.15 4.19	4.06 3.4.11 4.19 9.19	3.89 3.89 4.20	4.08 3.90 4.39 4.21	4.19 4.39 4.19	44.22 61.44 61.22 72.41	44.45 4.45 4.22	4.50 4.37 4.47 4.44	4.31 3.99 4.61 4.53	4.11 3.94 4.39 4.39	
86888	Louisville & Nash unified 4s 1940. Chi Bur & Q (III Day M 33;81949. Chi Bur & Q (III Day M 33;81949. Nor Pac Ry prior len th sis 4 1997.	8.48.48 90.99 80.00 80.00	4.01 3.93 3.98 3.98	4 4 4 4 4 11 4 4 4 4 10 0 0 5 10 0 3	4444 01.44 02.20 80.88	4.04 4.02 4.02 4.00	44.13 44.23 4.139 4.03	4.16 4.21 4.06 4.31 4.01	4.20 4.15 4.15	44.29 44.33 44.13	44444 924244 1884 1888	4.50 4.43 4.61 4.22	4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	4.15 4.13 4.10 4.00	
98898	Norf & West Ry 1st cons M 4s 1996 Chernal RR of M 2gm M 5st 1987. Hocking Valley 1st cons M 24ss 1990 W. W. Ky Dy P. est 1 k gm M 4s 1944. Ore Sh Line RR cons 1st M 5s 1946.	3.96 4.33 4.23 2.33	4.14 4.32 4.23 4.33	4,16 4,34 4,31 4,41	4.4.4 4.4.4 4.4.4	4.18 4.03 4.53 4.53	4.28 4.95 4.45 4.45	4.04 4.04 4.68 4.50	4.31 4.42 4.80 4.59	4.35 4.20 4.92 4.92 4.64	4.4.40 4.63 4.65	4.57 4.79 5.22 4.92	4.4.7.4. 2.0.4.7.4. 7.7.7.4.	4.15 4.15 4.78 4.78	
11088	Southern Pac 1st ref M sf 4s 1955. A T & S F Fe R Aud M 4s stamped 1995. Northern Pac Ry gen lien 3s 2047. Acl Coast Line 1st cons M 4s 1952.	4.27 4.13 4.16	4.28 4.44 4.18 4.18	4.44 4.29 4.28	4.48 4.28 4.32	4.47 4.52 4.21 4.26	4.63 4.30 4.28	4.41 4.68 4.29 4.35	4.56 4.74 4.41 4.53	4.64 4.72 4.46 4.65	5.03 4.74 4.74	4.98 4.06 4.96	4.83 4.49 4.85	4.52 4.73 4.34 4.68	
11													-	-	

VIELDS OF RAILROAD BONDS Jan. 1908—Jan. 1909

-	Jan.	3.90 4.00 3.87 3.87	3 3 3 3 9 4 4 3 9 9 4 4 3 9 9 4 4 9 9 4 4 9 9 9 4 4 9 9 9 9	3.37 3.88 3.88	33.99 3.99 3.74 74	3.97 3.97 3.75 4.11 4.08	84.84.96 3.91.96 3.91.90	4.05 4.23 4.32 4.14	4.30
	-	3.98 3.99 3.91 3.91	23.99 23.96 13.96 13.96	4444.05	33.70	48.84.4 108.99 1.08.44.99	3.98 4.06 3.90 3.91	4.388 4.388 4.35	4.34
	Dec.								
	Nov.	3.99 4.01 3.93 3.99	3.99 4.28 3.96 4.16	4.04 4.19 3.89	3.73 3.91 3.68	44.6.44 08.19 08.19	3.91 3.91 3.90 9.16	4.27 4.38 4.22	4.4
	Oct.	4.09 4.02 3.93 4.01	4.31 4.31 4.52 4.21	4444.6 0.42.4.6 2.02.2 2.02.2	3.93	4.10 4.01 4.15	44.10 11.45 11.46 14.05	3.99 3.99 4.33 2.42 262	4.28
	Sept.	4.02 4.03 3.92 4.02	3.93 4.33 4.53 4.23 5.23	3.93 3.93 3.93	3.78 4.15 3.91 3.80	4.19 3.84 4.14 4.15	3.93 3.93 3.93 3.93	44.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4	4.28
	Aug.	4.14 4.05 3.92 4.03	86.4444 98.53 98.53 10.44	4.00 4.35 3.95 3.95	3.80 4.18 3.91 3.91	4.23 3.86 4.18 4.21	4444. 00.4 00.6 00.6 00.6 00.6 00.6	4.37 4.37 4.30	4.35
	July	4.09 3.92 4.09	4.04 4.51 4.71 4.05	3.99 3.90 3.90	3.80 4.18 3.94 3.84	4.20 4.33 11.30 4.28	44.16 4.21 3.95	4.97 4.93 4.59	4.63
	June	4.15 3.93 4.15 4.15	4.09 4.78 4.08 4.32	3.98 3.98	3.84 3.99 3.85	4.30 4.30	4.18 4.23 4.23 4.21 3.99	4.44 4.07 4.66 7.37	4.65
	May J	4.21 4.17 4.00 4.13	64.44 6.00 6.33 6.33	4.02 4.23 4.68 3.96	3.84 4.15 4.02 3.82	4.14 3.96 4.35 4.31	4.24 4.26 4.26 3.99	4.44 4.70 4.38	4.51
1303	April	4.28 4.20 4.18 4.18	44444 113 14.08 14.08	4444.6 4.29 4.39 4.39	24.44.0 2.05.0 3.85	4.20 4.52 4.52	44.27 4.32 4.26 4.03	4.28 4.08 4.75 4.37	19.4
Not L	Mar.	4.4.3 4.22 20.44 20.25 12.4	84.444 84.84 84.80 85.	3.92 9.29 3.92 9.29	3.86	4.30 4.34 3.98	4.38 4.38 4.27 4.05	44444 86444 874	4.64
AN. L'OO	Feb.	4.32 4.13 3.98 4.21	44.4.61 13.84.84.84	3.92 3.92 3.92	3.89 4.14 3.89	4.35 3.97 3.85 3.85 3.85	4.4.4.4 4.21 4.02	4.4.4. 9.4.4.4. 4.4.4.4.4.4.4.4.4.4.4.4.	55.44
	Jan. I	4.37 4.10 4.23 4.23	44444	3.96 3.96	3.88 3.99 3.99	44.84. 111.46.44. 39.43.	4.15 4.15 4.00 4.00	4.28 4.47 4.78 4.56	4.52
	Name of Bond	Chie St P Min & Omaha cons M 6s 1930. C M & St P (C & W DY) 114 M Ss 1921. West Shore RR 1st M 45s 1921. West Shore RR 1st M 4s 25d.	Illinois Central RR coll 4s 1952. Lake Brie Western ist M 3s 1937. NY Toll Re St. St. St. St. St. St. St. St. St. St.	III Central (L N O & T) col 4s 1953 C & O (R & A D V) 1st cons M 4s 1959. C C & St. (St. L D L) 1st col 4s 1990. E Tenn V & G N cons 1st M 8s 1950.	Lake Sit, & Mich So, 1st M 3/s, 1997. P. Min & Man (Mon EN) 1st M 4s 1937. Bairbrave & Olio RR 1st M 4s 1948. Chicago & Nor West gen M 4s 1948. Chicago & Nor West gen M 35s 1967.	Chi Rock Is & Pac Ry gen M 4s 1988. Acht Top & Sante Fegen M 4s 1995. N'Y Cent & Hudson River M 354s 1995. Schoo Val & New Eng 1st M 4s 1999. Chigh Valloy (N'Y) 1st M 435s 1990.	Louisville & Nast unified 4s 1940. Chighn RR Nave Coons M 4s 1946. Chigh Bur & O(III Dry) M 3/3s 1949. Central Pacific Ist ref M 4s 1949.	Norf & West Ry 1st cons M 4s 1996 The constraint RN of Y grem Ms sin 1987 Hocking Y alley 1st cons M 4jes 1999 W W RY DIY st 1 k grem Ms 4s 1944 OP SI LIME RR cons 1st M 5s 1946.	Southern Pac 1st ref M sf 4s 1955 A T & SF R ya di M 4s stamped 1995.
	Ref.	23252	828377 CNMEH	24288 HOORO	229888	24882 04887	<u> 20002</u>	2005 2005 2005 2005 2005 2005 2005 2005	108 So 109 A

VIELDS OF RAILROAD BONDS

Name of Board Jan. Freb. Mar. April May June July Aug. Sept. Oct. Nav. Dec. Like Sp. Micks P. Mir. & Combine com M. 455 1930 3.85 3.89 3.94 3.90					OAD D	OND	יעוווווו)		noi
Name of Board	Jan.	4.04 4.01 4.26 4.26	3.99 4.17 4.09 4.26	3.93 3.93 3.93 3.93	3.98 3.98 3.84 2.22	4.4.4.4. 11.4.4.4. 11.0.03	3.94 4.39 4.39	4.28 4.24 4.11 4.11	4.00 4.51 3.78 4.44 4.29	4.04 4.03 4.10
Care S. P. Mir & Combin crops M 6s 1930. 359 358 359	Dec.	4.07 4.07 3.90 4.28	3.98 4.00 4.04 4.26	3.93 3.93 3.93 3.90 3.90	3.93 4.04 3.84 4.21	4.4.4.4.4.4.1.3 4.03	3.96 4.36 4.36	4.29 4.24 4.11 4.11	3.98 4.52 4.42 4.31	44.04
Check Store RR 18th & Combine com M 46 1930. 357 3 57 3 57 3 57 3 57 3 57 3 57 3 5	Nov.	43.33.4 3.90 2.90 8.28	3.98 4.24 3.97 4.06	3.83 3.83 3.83 3.83	3.91 4.02 4.03 88 22 22	4.4.02 4.03 4.03 1.03	6.46.44 96.44 96.36	4.25 4.25 4.17 4.25	3.78 4.43 3.18 4.43	4444
Chick S. P. Mir & Combin crops M of 1930 3 kg		3.90 3.90 4.25	3.99 3.98 4.02 4.22	3.90 3.82 4.01 3.86	3.89 3.99 3.85 4.15	4.06 4.06 4.06 1.15	3.93 4.31 4.31 4.31	4.25	84.844 80.45 30.45 80.45	4 4 .03
Chick St. Pulit & Combin com M of 1930. 359 358	Sept.	3.99 3.99 4.23	3.96 4.13 4.00 4.01	3.83 3.83 3.88 3.88	3.90 3.99 3.83 4.15	4.05 3.99 4.13	3.92 3.89 4.37	4.25 4.25 4.25 4.05	3.93 4.45 3.81 4.34	4444
Chick St. Philip & Combin corn of 6 1900. Jan. Feb. Mair. April. May. June. July Mess Stone RR 1st Ms. 2004. 25 13 20 3 20 3 20 3 20 3 20 3 20 3 20 3 2	Aug.	3.98 3.98 3.88 4.23	3.95 4.14 3.96 4.02 4.17	3.84 3.91 3.97	3.86 4.02 3.97 3.83 4.15	3.99 3.98 4.08 4.14	3.88 4.25 4.37	4.25 4.25 4.27 4.06	3.90 4.42 4.32 4.23	4 4 4 4 24 24 2
Chief. S.P. Mill. & Commission of 1930. 1879 1878 1879 1878 1879		3.90	3.94 3.94 4.03 1.16	3.75 3.75 3.75 3.75	3.82 3.94 3.79 4.13	3.97 3.97 3.94 4.13	3.87 4.37 4.37	4.23 4.23 4.06 4.19	3.88 3.78 4.24 4.24	96.44
Chick S. P. Mir & Comain cord M 6s 1930. 3 page 3 p	June	3.94 3.93 4.25 4.25	3.93 3.98 4.01 4.15	4.37 3.83 3.98 3.83	3.85 3.95 3.77 4.14	3.90 3.90 3.90 5.1.4	3.91 4.26 4.36	4.15 4.26 4.05 4.05	3.87 4.41 3.76 4.33 4.20	94.4.4
Chick P. Mir & Comain or M & Gand Chick S. P. Mir & Comain or M & 6130 Chick S. D. Mir & Comain or M & 6130 Ill. And M. R. Comain or M & 6130 S. S. S. S. S. S. S. S. S. S. S. S. S. S	-	3.88	3.91 4.11 4.00 4.16	33.94	3.95 3.95 4.12	43.95 43.95 13.92 13.92	24.25 44.25 35.25 35.25	24.4.4.4.4.4.4.4.28 24.24.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4	3.86 3.75 4.31 18	3.98
Chief S. P. Mirk & Combin com M for 1930. Jan. Pech Mark Chief S. Der K. R. H. M.		3.89	3.91 1.00 1.00 1.00 1.00	33.95 3.95 3.95 3.95	3.78 3.96 3.76 4.08	3.92 4.3.92 4.12 1.12	3.90 4.35 4.35 4.35 4.35	4.13 4.27 4.04 4.13	3.87 3.76 4.30 4.18	3.97
Chic St. P. Mir & Combine or M. 6 1930. Chic St. P. Mir & Combine or M. 6 1930. Chic St. P. Mir & Combine or M. 6 1930. St. Chic St. Chic M. 6 1930. N. V. Chic & St. Loit 1 18 1939. N. V. Chic & St. Loit 1 18 1939. N. V. Chic & St. Loit 1 19 1930. St. Chic & St. Loit 1 19 1930. N. V. Chic & St. Loit 1 19 1930. N. V. Chic & St. Loit 1 19 1930. St. Chic M. St. Loit 1 1930. St. Chic M. St. Loit 1 1930. St. C		3.90 3.90 4.26	3.87 4.10 4.00 4.17	3.87 3.98 3.98 3.85	3.78 3.98 3.96 4.14	4.3.4. 2.92 1.92 1.12	3.80 4.45 4.15 3.77	4444	3.88 3.78 4.31 4.18	3.97
Chie St P Min & Comba on M Gen 1900 West Shore RR Bt M Ad 2301 West Shore RR Bt M Ad 2301 When A Chair R B M Ad 2301 When Shore RR B M Ad 2301 When A Chair R M M A 2301 When A Chair R M M A 2301 When A Chair R M M A 2302 When A Chair R M M M A 1903 When A Chair R M M M A 1903 When A Chair R M M M M M 1903 When A Chair R M M M M M M M M M M M M M M M M M M	-	3.85 3.85 4.20	3.93 3.97 3.98 4.18	3.87 3.94 3.83	3.76 3.95 3.76 4.08	4.8.4.00 0.8.8.8.00	3.87 4.04 4.16 4.33	4.24 4.22 4.04 4.15	3.89 4.41 4.31 4.19	3.95
Click P. Min & Combin com of 60 1900. Week Shore RR 1st M 42 200 M. Weeks R 1st M 42 200 M. Weeks R 1st M 42 1903. One U. R. S. Louis 1st M 44 1903. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd II. N Or EV Droit of 1909. R. Cornerd R. R. Man M. 45 1909. Chi Reach Es Per R. Wee M. 45 1909. Chi Reach Es Per R. Wee M. 45 1909. Chi Reach R. P. Wee M. 45 1909. Chi Reach R. P. Wee M. 45 1909. Chi Bur R. Q. (III Dr.) M. 3194 1909. Chi Bur R. Q. (III Dr.) M. 3194 1909. Chi Bur R. Q. (III Dr.) M. 3194 1909. Chi Bur R. Q. (III Dr.) M. 3194 1909. Nor P. R. Yorde In at P. M. 44 1904. Nor P. R. Yorde In at P. M. 44 1904. Nor P. R. Sy Profe In in It will 48 1907. Nor P. R. Sy Profe In in It will 48 1904. Nor P. R. Sy Profe In in It was 1904. Southern Per 1st real M 48 1904. Southern Per 1st real M 48 1904. Real Helden Co 1st & ert M 48 1904. Real Real Real Real Real Real Real Real	Jan.	3.90 3.87 3.99 4.24	3.94 4.00 1.00 1.15	3.88 3.97 3.97	33.74	3.96 3.96 3.91 3.91	3.90 3.88 4.23 5.32	4.74 4.23 4.30 4.08	3.92 3.78 4.37	92.3
	Name of Bond	Dic St P Min & Omala cons M 6s 1930. St Shore RN 18 M 4s 230. St Paul Minn & Man cons M 45s 1933. Walter St Paul Minn & Man cons M 45s 1933. Walter R Co 1st M 5s 1939.	N Y Chie & St. Louis 1st M 4s 1937. Ref. & Ohio Wr. 1st coms 51 1938. III. Central Li N O & T. 7 col 4s 1935. C & St. L (St. L Dv.) 1st con 4s 1990.	E Tenn V & G Ry cons 1st M is 1956 The Milw : St Pain gen M is 1999 Late Sh & Mich St 1st M 3/54 1997 Late Sh & Mich St 1st M 3/54 1997 Thin The M Sh Is M Sh 1988 Thin Pe R K 1st M RR & lig 18 1947	hiteggo & Nor West gen M 34/s 1987. Inche E & Ver Fy gen M 44 1988. Actri Top & Santa Fe gen M 48 1995. Y Cent & Halland River M 24/s 1997. Scioto Val & New Eng 1st M 48 1999.	chigh Valley (N Y) 1st M 445,8 1940. When while R Nish unified & 1040. Negon R R Nish C Grow M 48 1946. The Z Q (III DIV) M 519.049. Christ Petilic Ist ref M 48 1949.		Dre Sh Line RR cons 1st M Sa 1946. Son them Par I ser ref M is 4 s 1955. And them Par Re St soil M 48 stammed 1995. And them Par Re St soil M 48 stammed 1995. All Coast Line Isc cons M 48 1992.	Del & Hudson Co. 1st & ref M. 4s. 1943. Thermal of Georgia cons. M. 5s. 1945. Cenneyi venila R.R. cous M. 4s. 1946. Cenneyi venila R.R. cous M. 4s. 1946. A.R. N. (Alf. Knox & Clin Dey) 4s. 1955.	Illinois Central RR ref M 4s 1955. Chic Burl & Quincy gen M 4s 1958. Chic Burl & Quincy gen M 5s 1994. The Par RR 1st linn & ref M 4s 2008.
	No.				98488					118

YIELDS OF RAILROAD BONDS JAN. 1910—JAN. 1911

TELDS OF RAILROAD BONDS JAN, 1911—JAN, 1912

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4.15 4.03 4.62	44.30 44.30 44.13 4.33	3.96 3.93 3.96	4.05 4.05 4.03 4.18	4.05 4.15 4.17 4.01	4.06 4.40 4.36 4.35	4.25 4.35 4.21 4.07	4.45 4.44 19	4.15
4.6.4.4 80.9.4 60.05	4.4.4.90 4.21 4.30	4.4.4. 4.04. 3.95	4.17 4.17 4.19 4.19	4.05 4.25 4.13 4.04	4.4.4.4 4.33 7.33 7.33			44.17
4.08 4.03 4.04	4.01 4.28 4.24 4.24 4.35	44.43 3.91 3.94 3.94	4.06 4.03 3.98 4.17	4.25 4.25 4.12 4.02	4.06 4.39 6.36	4.26 4.33 4.22 4.07	46.44.4 17.33	94.4.
4.12 4.12 4.03 4.57	4.02 4.30 4.22 4.45	4.49 3.96 4.07 3.96 3.95	4.44.11 4.044 4.17	44444 024444 024444	4.33 4.33	4.44 4.37 4.26 4.08	3.85 3.85 4.44 17	4.4.4.
44.12 40.44.04 7.05	4.03 4.27 4.23 4.36	3.95 3.95 3.95	44444 11.444 17.02 17.02	4 4 4 9 4 4 36 4 15 0 5	44.44 4.44 4.45 4.45 4.45	4.38 4.33 4.23 4.10		44.72
46.44 20.09 40.44 4.48	4 4 . 06 4 . 27 4 . 21 36	3.94 3.94	44444 00.4001 00.4001	4.14 4.14 4.16 4.06	4444 90,44,49 34,45	4.27 4.27 4.23 4.10		4.4.4. 0.4.4. 0.4.1.4.
4.6.4.4.4 0.00.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	4.03 4.27 4.20 4.30	44.84.8 49.00 94.09	4.04.04 4.05 1.18	44.44.4 4.25 4.13 9.16	4 4 4 4 4 9 6 9 6 9 6 9 6 9 6 9 6 9 9 9 9	44.44 4.24 4.24 0.86		4.01
4.08 9.09 84.08 84.08	4.02 4.23 4.20 4.35	3.93 3.93 3.93	44444	44.08 4.14 4.15 4.04	4.37 4.37 4.31	44.44 4.24 4.25 4.07		71.4
4.08 4.08 4.46	4.24 4.29 4.20 4.30	3.94 3.93 3.94 3.94	4.04 4.11 4.04 3.97 4.16	4.14 4.13 4.14 0.4	4.4.03 4.35 3.35 4.30	4.23 4.25 4.23 4.06	4.33	4.4.4 00.4 00.0
4.08 4.08 4.48	4.02 4.27 4.20 4.35	3.93 3.93 3.93	4.44.13 4.04 1.94 1.04	4.14 4.19 4.10 6.02	4.4.4.4. 7.4.4.4. 29.2.4.29	4.4.4.4.4.4.4.2.2.4.2.6.08	4.53 4.35 4.35	4.14
4.13 4.13 4.11 4.43	4.01 4.24 4.11 4.11 4.30	3.94 3.94 3.97	4.04 3.99 4.16 4.15	4.25 4.25 4.25 4.20 4.03	4.44.04 30.44.30 30.49.30	4.39 4.39 4.32 4.33	3.82 3.82 4.44 4.36 17	4.14
4.13 4.12 4.12 4.41 1.41	4.44 4.21 4.17 8.17	3.93 4.04 3.93 7.07	3.98 4.12 4.12	4444 00.4444 00.4444	4 4 4 4 4 4 4 6 3 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	4444 25 27 27 27 27	4.35 4.41 4.14	4.12
46.44 41.04 41.10 44.10	4.01 4.20 4.17 4.17	3.92 3.92 3.98	4.44 3.93 4.09 4.09	4.4.4.4.4.08 4.11.13 1.02	4.4.4.4.4.4.4.39	4.26 4.27 4.27 4.01	3.82 3.82 4.40 4.41	4.63
Dic St. P. Min & Cmala cons M 6s 1930. St. Shor RN 1st M 4s 230. Ye had Min & Man on M 45/4s 1933. Which Chert RN Coll 4s 1952. Washan RN Co 1st M 5s 1939.	V V Chic & St. Louis 1st M 4s 1937. I Central (L N O & Pt) 700 4s 1935. CR R & A Day 1st coms N 4s 1935. CC & St. Cft L Day 1st cons N 4s 1990.	7. Tenn V & G By cons 1st M 5s 1956 McMilw & K Pall gen M st 1989 alre Sh & Mich So 1st M 33s 1997 Thing the R 198 M 8 1945 Thing Pac RR 1st M RR & 19 st 1947	hicago & Nor West gen M 34/8 1987. Rock I & Per Ky gen M 48 1988. Kth Top & Suhar Fe gen M 48 1995. Y C en & Birladon Kiven M 54/8 1997. enigh Valley (N Y) 1st M 44/8 1990.	ouisville & Nash unified 4s 1940. Tregon RR & Nay Co coms M 4s 1946. The Bur & Q (III DV) M 34g 1949. Nor Pac Xp prior lien Ig M 4s 1997.	oorf & West Ry 1st cons M 4s 1996. Goodling Nation 1 gem Ms 3s 1937. Goodling Valley 1st cons M 42/5s 1999 W Ry Dyu Pat It & gen M 4s 1944. 7e Sfi Line RR cons 1st M 3s 1946.	outhern Pac 1st ref M st 4s 1955 T. & She Ng and M, 4s stampoid 1995 forthern Pac Ry gen lien 3s 1947 Lokal Link 1st cons M, 4s 1952 Pet Midson Co 1st & ref M 4s 1943	Central of Georgia coms M 5s 1945. Emmsylvatia R 5008 M 4s 1954. Grasse Chyr Jes M 3s 1950 M (Alt Rotos & Cin Diby 18s 1955. Illinois Central RR tef M 4s 1955.	Chic Burl & Quincy gen M 4s 1958. Southern Ry 1st cons M 5s 1994. Un Pac RR 1st lien & ref M 4s 2008.
73 73 73 73 73 73 73 73 73 73 73 73 73 7	22222	98889 9989 9989	93 93 95 11	255598 255598	55555	111098	113 115 116 117	1119
	Chic St P Min & Omaha cone M 6s 1990 4 14 4 19 4 13 4 13 4 12 4 10 4 09 4 07 4 12 4 21 4 17 4 18 4 18 4 18 4 18 4 18 4 19 4 07 4 10 4 19 4 19 4 19 4 19 4 19 4 19 4 19	West Store R7 extra decreased Mes 1990. 4418 413 413 419 419 410 410 410 410 410 410 410 410 410 410	West Shorn R. ter M. 4. 2004. Sp. 3 975 3	West Stars R7 184 M 42 200 M 68 1930 H 44 184 184 184 184 184 184 184 184 184	Week Shorn RR1 ext M 42 CM 6 1990 6 194 1 1 4 1	Week Short RR 1 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 2 et M 42 2014. Week Short RR 3 et M 42 2014.	Week Shore RR 1 et M 44 2004 Mes 1990 4 19 4 19 4 19 4 19 4 19 4 19 4 19	Cucke St. Put. 1 at 8 counts count M 4 194 194 194 194 194 194 194 194 194 1

YIELDS OF RAILROAD BONDS JAN. 1912—JAN. 1913

Name of Board Dan Name of Board Dan Peb. Mar. Peb.	Ref.						-	-	-				;	1	1
Week Shore RR 14 44 250, 199 1	ů	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Now.	Dec.	Jan.
Cree & Oth Pay Car Con & 1939. III. Cerral LN O & S. 70 of 1939. III. Cerral LN O & S. 70 of 1939. III. Cerral LN O & S. 70 of 1939. III. Cerral LN O & S. 70 of 1939. Inc. S. 80 of 1939. Inc.	222	West Slore RR 1st M 4s 23d1. St. Paul Minn & Man cons M 454s 1933. Illinois Central RR coll 4s 1952. Walasis RR Co 1st M 5s 1939. N Y Chie & St Louis 1st M 4s 1937.				3.98 4.14 4.04 4.52	3.99 4.02 4.54 4.01	84444 87758	4.4.4.4 4.55 4.02	44.44 23.44 10.66	4.4.4.4. 2.2.4.4.4. 2.4.4.4.4.4.4.4.4.1.4.1.4.1.4.1.4.1.4.1.	4444 2224 4605 411	4444 000 000 000 000 000 000 000 000 00	44.4.4.4.2.2.2.4.4.0.2.2.2.4.4.4.0.2.2.2.2	44.06 4.24 4.04 4.06 4.06
Linke Sin & May So is M JA54 1997 Lillian Proc Rit in M Ric Rig 44 1997 Lillian Proc Rit in M Ric Rig 44 1997 Lillian Proc Rit in M Ric Rig 44 1997 Acti Town War grant M 45 1998 Acti Town Ric Riv M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1999 Lillian Ric Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 45 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Ric Rinke Rinke M 1996 Lillian Rinke Rinke Rinke M 1996 Lillian Rinke Rinke Rinke M 1996 Lillian Rinke Rinke Rinke M 1996 Lillian Rinke	888 878 878					4.4.4.4 12.4.4.4.4 14.4.4.9	4.31 4.45 4.45 4.07	44444 71444 4444 7044	44444 8444 11.88	44444 62244 151 151 151	4.4.4.4.4.4.4.4.4.4.4.4.4.4.3.3.4.4.4.4	4.42 4.42 4.44 4.48 1.10	4.38 4.45 4.45 4.10	4.39 4.21 4.31 8.51 8.03	4.39 4.23 4.41 4.50
Arch Top & Sunt Fage M 44 1995. N Y Crit R Hutlann Brow M 3/45 1995. Louishig Valley (N) 18 M 4/45 1990. Louishig Nahu Mirkel 40190. Chain Brow R & Nahu Mirkel 40190. Chain Brow R & Nahu Mirkel 40190. Chain Brow R & Nahu Mirkel 40190. Chain Pacific R (M) 1990. Chain Pacific R (M) 1990. Chain Pacific R (M) 1990. Chain Mirkel M 1990. Chain Mirkel M 1990. Chain M 1990.	88228					3.90 3.91 11.14 81.11	3.93 2.93 3.93 7.12	3.98 3.98 4.13	84.24 86.14 86.13 86.13	4.4.4.4 2023 81.23	44.44 4.20 4.21 4.24 4.24	3.97 4.16 4.01 4.23	0.44.44 1.15 1.19 2.19 3.19	4.02 4.05 4.22 4.31	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
Central Re Q (III D) M 3/3 1949. 411 411 411 410 410 71 411 411 411 411 411 411 411 411 411	48 288					4.4.4.4 25.05 25.05	4.05 4.18 4.05 5.25	4.04 4.03 4.27 7.27	44.44 60.44 60.44 60.44 60.44	44.44.4 4.133 4.133	4.4.4.4. 2.2.4.4.	44.44 00.44.44 00.44.14 00.44.14	4.12 4.25 4.16 4.38	4.4.4.4. 82.1.4. 84.1.4.	4.11 4.24 4.38 4.38
Harching Valley I are one M 445 999. R. & W. P. D. VIR R. Earn M 41 994. Conf. In the R. F.	95255	Chi Bur & Q (III Div) M 33/ Central Pacific 1st ref M 4s Nor Pac Ry prior lien Ig M Norf & West Ry 1st cons M Central RR of N J gen M 5s				44.23 40.44 70.44	4.13 4.04 4.04 80.4	4.18 4.20 4.05 4.12	4.4.4. 4.03 4.03	4444 282 281 281 281 281 281	44444 401111	4.32 4.26 4.13 4.13	44.4.4. 72.4.4. 21.4.	4.30 4.10 4.15	4.30 4.09 4.09 81.18
Morthern De Ry per mit no 3 5042, 4 33 All Chair Lin 1st Gross M 48 1952, 4 34 All Chair Lin 1st Gross M 48 1954, 4 4 4 1 4 5	585586					4.4.4.4 4.25 4.05 4.05	4.4.4.4. 64.2.4. 25.4.4.4.	4.4.4.4.4.4.4.4.4.5.4.3.0.0.0.0	44444 64444 7444 7444 7444 7444	4.4.4.4 64.4.4.4 1.3.2.2.4.4	4.4.4.4.4.533 5333 5333	4.4.4.4.4.5.4.5.4.5.4.5.4.5.4.5.4.5.4.5	4.48 4.49 4.49 4.332 55	44444 84446 84448	4.44.45 25.45 27.35
Kanesa City Sa. Fee H. M. 8, 1990. L. & N. (Kill Kook & Cit. Day), 48, 1955. L. & N. (Kill Kook & Cit. Day), 48, 1955. Lillineis Central R. Fee H. M. 4, 1955. Southern R. J. ist come M. 55, 1994. A. (Cit. Park & Chita Come, 1994. A. (Chita Chita	13221	Northern Pac Ry gen lien 3s 2047. Atl Coast Line 1st cons M 4s 1952. Del & Hudson Co 1st & ret M 4s 1943 Central of Georgia cons M 5s 1945 Pennsylvania RR cons M 4s 1948.	4.35 4.21 3.82 2.82		.4	4.33 4.25 4.07 3.83	4.4.4.5 25.4.4.6 2.8.2 2.8.2	4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	44.49 4.29 3.46 3.81	4.4.4 4.06 4.46 3.85	4.38 4.127 4.127 3.85	4.37 4.09 4.52 3.92	4.40 4.12 4.50 3.87	4.44 4.25 4.12 3.90	4.44 4.26 4.52 3.90
Un Pac RR ist lien & ref M 4s 2008 4.11 4.10 4.11 Atl Coast Line (L & N coll) 4s 1952 4.25 4.25 4.25 4.25	115 118 119	Kansas City So Ry 1st M 3s 1950. L. & N (Atl Knox & Cin Div) 4s 1955. Illinois Central RR ref M 4s 1955. Chic Butl & Quincy gen M 4s 1958. Southern Ry 1st cons M 5g 1994.	44.44 4.19 4.15 63.15			4.48 4.22 4.19 4.64	4.4.4.4.4.4.2.2.2.2.4.65.9.4.65	4.52 4.39 4.20 4.65	4.4.4 4.23 4.23 65	4.52 4.40 4.29 4.68	4.4.4.4.4.4.2.4.4.7.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1	4.57 4.31 4.24 4.70	4.56 4.24 4.24 4.71	4.55 4.43 4.26 4.27	4.60 4.24 4.22 4.22 4.68
Nor Ry 1st & ref M 4½s 1961.	120 121 122 123	Un Pac RR 1st lien & ref M 4s 2008 Atl Cosst Line (L 8 N call) 4s 1952. Nor & West (P C & C) Joint 4s 1941 Grt Nor Ry 1st & ref M 4½s 1961	4.25	4.25	4.4.4	44.44	4.15	4.14	4.13 4.52 4.23	4.15 4.26 4.26 4.23	4.32	4.37	4.17	4.18 4.44 4.25 4.25	4.20 4.45 4.52

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Control Cont	Control Cont
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#1184	#17845 14846 81214 20181 41288 41854 #17841 74488 41214 20181 41286 88884 #17841 74484 41214 74144 41286 88884 #17851 74846 88888 88888 #17851 74846 88888 88888 #17851 74846 88888 88888
44444 44444 44444 44467 1088246 801151 186652 481689	44444 44444 44444 44444 44444 444444 1288248 851254 15455 41568 41688
44. 44.4.4. 4.4.4.8.8.8.8.8.8.9.9.9.9.9.9.9.9.9.9.9.	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
ON N. W. Ry. Day 181 f. Rem. M. 41 944. On Cores. Day 181 f. Rem. M. 41 944. ON Cores. Day 182 f. R. 41 41. ON Cortes and M. 48 stamped 1995.	N & W By Dry 1st I k kem M 4s 1944. Southern Per (Strict M st 1956. Southern Per (Strict M st 1956. Northern Per Rygen British 1952. Northern Per Rygen British 1952. Del & Huddon Co let Re Ry 1943. Del & Huddon Co let Re Ry 1943. Del & Huddon Co let Re Ry 1943. Pennsylvanie RR Gons M 4s 1984. Rygens (Pry 18 M 3s 1986. L. & N (Atl Know & Cin Dry) 4s 1955. Chic Burl & Christy gen M 4s 1958. Chic Burl & Ching South N 1994. Chic Burl & Ching South N 1994. Chic Burl & Ching K M 4s 1958.
	M.I. Coust. Line 1st cone M. 45 1922. Control of Coeper, cone M. 45 1923. Control of Coeper, cone M. 51 1948. Roman City, S. W. 14 M. 31 1950. L. R. M. CANCE, R. C. M. 21 1948. L. R. M. CANCE, R. C. C. M. 21 1955. L. R. M. CANCE, R. C. M. 21 1955. Chic Butt & Quincy gen M. 43 1955. Chic Butt & Quincy gen M. 43 1956. Chic Butt & Quincy gen M. 45 1956. Santhum R. L. S. 45 cross M. 53 1994. Un Pre-R. R. 15 is live K or M. 45 7006.
	Atl Knox & Cin Div) 4: 1955. 4-13 14. 14. 1955. 4-23 17. Quiny, gen M 18: 1958. 4-23 17. Het comb M 18: 1994. 4-26 18. R. 18: 18: 19: 14. 4-26 18. R. 18: 18: 18: 18: 14: 14: 14: 14: 14: 14: 14: 14: 14: 14

YIELDS OF RAILROAD BONDS JAN. 1914—JAN. 1915

Name of Road Name	100				111 1 111	1222				
Name of Bond	Jan.	4.4.4.4 17.11.4 1.50 1.50	4.80 4.22 4.22 4.56	4.23 4.43 4.28 4.39						4.24
Name of Road Name of Bond Name of Bond Name of Road Name	Dec.	4.4.5 8.4.5 8.4.5 8.4.5 8.4.5	4 4 4 4 4 4 4 4 4 4 4 4 4 4 8 8 3 8 9 8 9 8 9 8 9 8 9 9 9 9 9 9 9 9	44.44.44.45.39	44.57 4.57 4.64 8.3	4.53 4.44 4.79 83	4.4.4.8.87.4.8.7.9.7.4.9.7.3.9.7.4.9.8.8.9.7.4.9.9.7.4.9.9.9.7.4.9.9.9.9.9.9.9.9	4.12 4.12 4.12 4.74	4.79 4.56 4.52 4.85	4.81
Name of Bond	Nov.									
Name of Board Name of Boar	Oct.									-
Market Store RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264.	Sept.									-
Market Store RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264. Market STore RZ 14tt M 42 264.	Aug.					A. J. Combined S. Affred			-	
Name of Bond	-	4.49 4.40 4.40 5.50	4.4.4.4 61.15 64.15 64.15	4.13 4.75 4.38 4.34	44444 43223 4434 4436 4436 4436	44.21 4.21 4.51 5.51	44.58 4.51 4.51 8.39	44.23 44.79 4.79	4.4.4.4 28.39 25.35 30	4.21
Market Shore R2 114 May 25021. Market Shore R2 114 May 25021. Ma	June	4.4.4.4 4.35 4.52 52 52	4.4.4.4.4.58 4.0.4.4.35	44444 2525 25404	4444 4428 4429 33	4.23 4.23 4.49 4.58	4.44 4.58 4.58 3.43 4.58	4.16 3.96 4.81 4.51	4.40 4.76 4.23 4.23	4.74
Name of Bond Jan Feb Mat April Man Feb Mat April Multi-structure Man -	44444 257.44 25.35 45.35	4.24 4.24 4.34 4.34	44.44 77.27 44.18 45.27	4.44 4.33 129 35 35	4.23 4.23 4.53 4.60	4.53 4.40 4.47 4.30	4.20 3.90 4.77 4.51	4.40 4.75 4.26 4.53	4.82	
Name of Bond Jan Peb Mar.	-	4.44.4 4.33 4.53 53	4.57 4.24 4.10 4.32	44444 717 717 718 718 718 718	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4 4 2 2 2 3 4 4 5 5 1 5 2 3 4 5 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1	44444 54545 1366	4.26 4.77 3.93 4.79 4.52	4.35 4.75 4.27 4.50	4.78
Week Store RR 14 M & 1905. 1906.	-	4.4.4.4 26.4.4.4 58.30	4444 855 851 841 841 841 841 841 841 841 841 841 84	4.4.4.4.26 4.20 4.20 2.30	44444 455444	4.24 4.25 4.26 4.50 4.50	44444 4646 464 35	4.26 4.75 4.75 4.78	4.4.4.4 4.27 8.33 8.34	4.24
Name of Bond		4.44 4.45 4.45 4.45 4.45	4.49 4.18 4.17 4.27	44444 2034 2034 45.20	44444	4.43 4.43 4.54 4.54	4.53 4.45 4.45 4.34 4.34	4.74 4.75 4.76 4.54	4.44.44.34.27.44.34.34	4.08
	Jan.	4.44 4.34 4.34 61	4.52 4.66 4.09 4.40	44.44 24.24 24.24 44.24	44444 488444	4.22 4.32 4.55 4.63	44444 84.56 84.39	4.4.4.4 4.81 10.4.4.85 10.04	4.44 38 4.34 4.49 4.49	4.23
	Name of Bond	Vest Slove RR 1st M 4s 2361. Blains Central Rx 6014s 1952. Vabes Rx Co 1st M 5s 1959. Vaples Rx Co 1st M 5s 1939. The Rx Co 1st M 5s 1937. The Rx Co 1st Co 1s	II Central (L. N. O. & T) tool 4s 1953. From V. & C. Py corns 1st M. 8s 1956. Lic Milw. & Et. Paul gen. M. 4s 1989. Est R. M. Mich. So. 1st M. 3s 1997. Anthmore & Ohio R.R. 1st M. 4s 1948.	inion Pac RR 1st M RR & lg 4s 1947. Nation & Now Week gen M 3,545 1957. Ni Rock is & Pac Ry gen M 45 1988. Nation & Swall as pec M 45 1988. Y Cent & Hudson River M 3,558 1907.	chigh Valley (N Y) 1st M 44/s 1940. Weight Valley (N Y) 1st M 44/s 1940. Pregen RR & Nav Co cons M 4 \$1946. The R Q (II) Dry M 5/s 1949. Entral Pacific 1st ref M 4 1949.	tor Pac Ry prior iten ig M 4s 1997. Ry Ry Res Ry Ry 18 cross M 4s 1996. central Ry G N J gen M 5s 1937. Ry Ry Ry S Ry Ry Ry Ry Ry Ry Ry Ry Ry Ry Ry Ry Ry	re Sh Line RR cons 1st M 5s 1946. Onthern Pack 1st HM sif sh 1953. T RE SP Ry and JM sis stamped 1955. If Construent Pack Ryes line is 3 1947. If Coast Line 1st cons M si 1952.	lod & Hudson Co 1st & ref M 4s 1943. Referential of Georgian come M 5s 1945. emms/raim & R. Cors M 4s 1945. Referential CH Cors Fix M 3s 19450. Referential CH Cors Fix M 3s 1950.	linois Central RR ref M 4s 1955 In Berl X Olinico gen M 4s 1958 outhern RV six coms M 5s 1994. The RR RI st line X Fer M 4s 7006. Il Coast Line (L & N coll) 4s 1952.	Norf & West (P C & C) Joint 4s 1941. Card Nor ky 1st & Per off M 44/8 1961. Cardada So 1st & Per cons 5s 1962
	Ref.									122 123 123 123 123

ELDS OF RAILROAD BOND: JAN. 1915—JAN. 1916

1	Jan.	4.34 4.43 4.59	4.80 4.70 4.13 4.46	4.14 4.25 4.24 4.24	4 4 4 53 4 4 55 4 55 4 31	4.28 4.24 4.61 6.61	4.52 4.58 4.35 4.35	4.94 4.02 4.62 4.57	4.36 4.85 4.43 4.08	4.26
	Dec.	4.36 4.63 4.45 4.60	4.81 4.73 4.15 4.51	4.15 4.26 4.27 4.27	4.37 4.48 4.30 4.36	4.29 4.84 4.62 4.63	4.53 4.44 4.24 4.24	4.4.4.4.4.4.4.7.7.7.7.7.4.5.4.5.4.5.4.5.	44.44 4.77 4.69	4.28
	Nov.	4.38 4.74 4.50 4.62	4.83 4.12 4.15 4.55	4.31 4.76 4.26 4.30	4.44 4.32 4.61 33	4.34 4.34 4.59 4.59	44.44 4.39 4.39 5.33	4.4.4.94 4.65 4.55	44.44.44.44.66.66.66.66.66.66.66.66.66.6	4.26
	Oct.	4.44 4.94 4.63 4.73	44.49 4.4.60 7.72	4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	4.54 4.64 4.79 4.79	5.03 4.72 4.89	4444 87.78 4.60 35	5.10 4.92 4.88 4.88	44.88 4.88 4.88	4.37
	Sept.	5.04 5.04 4.94 4.84	5.4.4.4.89 83.4.83 83.83	4.4.8.4.4.4.4.4.55	4.66 4.75 4.90 4.48	4.4.5.4.4 86.93 86.93	4.4.4.4 88.23 48.82 1.51	5.20 5.02 4.92 4.95	5.15 5.15 4.71 4.91	4.52
	Aug.	5.13 5.13 4.95 4.82 4.83	5.18 4.89 4.30 4.84	4.39 5.02 4.41 4.56	4.59 4.94 5.50 4.50	4.58 5.02 4.90 4.81	4.88 4.4.89 7.73 5.73	5.09 4.99 4.80 8.80	5.07 5.07 5.15 88	4.46
	July	5.08 4.95 4.73 4.80	5.18 4.85 4.29 4.85	44444 242445 442444	44.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4	4.4.4.4.7.7.8.7.4.7.8.7.4.7.8.7.4.7.8.7.4.7.7.8.7.4.7.7.8.7.7.7.4.7.7.7.7	4.4.4.4. 8.59 8.59 8.59 8.59	5.04 4.98 4.85 4.75	5.04 5.04 5.06 5.06 5.85	4.4
	June	4.45 4.94 4.58 4.58	4.99 4.49 4.27 7.27	4.4.4.4.4.4.4.2.4.4.2.4.4.2.4.4.2.4.2.4	44.44 60.44.4 77.44	4.42 4.38 4.79 4.71	4.83 4.75 4.52 4.43	5.04 4.13 4.72 4.73	5.03 5.03 4.54 4.91	4.28
	May	44.44 4.83 4.70	5.01 4.43 4.24 5.65	4.4.4 4.837 4.4.4 4.4.1	74.4.4. 24.4.4. 33.	4.4.4.4. 4.8.3.4.7.7.	4.4.4.4.4.4.4.4.35	4.94 4.93 4.77 4.70	5.01 4.41 4.83 4.75	4.28
0761	April	4.34 4.96 4.50 4.75	4.96 4.76 4.28 6.60	44.44 4.38 4.26 4.39	4.41 4.56 4.67 4.67	4.33 4.74 4.77	24.4.4.4 51.7.04.6	4.92 4.43 4.72 4.70	5.03 4.42 4.84 4.84 7.77	4.32
	Mar.	4.40 4.87 5.11 4.53	5.01 4.44 4.27 69.46	4.30 4.39 4.35 4.35	4.53 4.46 4.76 4.76 4.76	4.36 4.34 4.77 4.77	4.86 6.7.4 7.51 7.51 8.35	4.4.4.4. 11.1.4.4.4.6.6.6.7.3	5.06 5.06 4.49 4.83	4.42
AN. 1915-JAN.	Feb.	4.41 5.03 4.46	4.30 4.24 4.24 6.55	4.44 4.32 4.32 4.41	4.48 4.54 4.75 4.45	4.4.4.4 4.8.33 4.6.7.7	4.78 4.77 4.45 4.28	4.91 4.90 4.74	5.03 4.46 4.79 4.73	4.28
JAZ	Jan.	4.41 5.11 4.50 4.76	4.80 4.80 4.22 4.56	4.39 4.39	4.44 4.45 55 4.43 8.43	4.4.4.4 7.7.4.4 7.7.6 7.7.6	44444 200 200 200 200 200 200 200 200 20	44.4.4.4.4.4.4.4.7.7.7.7.7.7.7.7.7.7.7.	4.5.4.4 20.8.4.4 7.6.70	4.24
	Name of Bond	West Shore RR 1st M 4s 2361. Thinnis Central Rx coll 4s 1952. Walsah RX Co 1st M 5s 1939. V Dick St Louis 1st M 4s 1937. Che & Chio Ry 1st cons 5s 1939.	III Central (f. N O & T) col 4s 1953. Frenn V & G y cons 1st M 5s 1956. Chic Milw & SP Paul gen M 4s 1090. Belthare R & Micho S 1st M 3s 1997. Beltharore & Oilo RR 1st M 4s 1948.	Union Pec RR 1st M RR & 1g 4s 1947. Chi Rook 1s & Pac Ry gren M 4s 1988. Chi Rook 1s & Pac Ry gren M 4s 1988. The Top & Santar Fe Egn M 4s 1995. N Y Cent & Hudson Krev M 3/4s 1997.	Louisville & Nisah unified 4s 1940. Chi Bur & Q. (III Day) May 5s 1945. Chi Bur & Q. (III Day) Mays 1949. Chern Pacific 1st For May 1949. Nor Pac Ry prior lien [& M 4s 1997.	Norf & West Ry 1st cons M 4s 1996 Central RN of N gem Ms 31987. Hocking Valley 1st cons M 44s 1999 We W Py Dry te 1 & gem Ms 4s 1944. Ore Sh Line RR cons 1st M 5s 1946.	Southern Pac 1st ref M sf 4s 1955, Ta & S Fe Ry ad M 4s stamped 1995. Northern Pac Sy gen lien 3s JA47. Ho Cast Line is from M 4s 1952. Del & Hidson Co 1st & ref M 4s 1953.	Central of Georgia cons M 5s 1945. Remselvata R Koors M 4s 1948. Ranse City So Ky 1et M 5s 1950. R N (Alt Knox & Cin D'n) 4s 1955. Illinois Central RR ref M 4s 1955.	Chic Burl & Quincy gen M 4s 1958. Southern PV 1950 com M 5s 1994. Un Pac RK 1st lien & Tef M 4s 2006. Nord Case Line (Le N coul) as 1952. Nord & West (P C & C) Joint 4s 1941.	Grt Nor Ry 1st & ref M 41/4 s 1961.
	Ref.	882328	888 888 988 988 988	22222	20001 10001	103 105 106 106 106	111098	115	122021	123

VIELDS OF RAILROAD BONDS JAN. 1916—JAN. 1917

00				111 1 131	1222				
Jan.	4.55 4.49 4.67	4.56 4.02 4.40 4.04	4.14 4.19 4.20 4.20	44444 112118	44444 4456 3330 3330	4.43 4.26 4.05 4.84	3.99 4.77 4.34 4.34	4.89 4.50 4.18	4.00
Dec.	44.44 60 60 75 75 75	44.59 44.07 4.08	44444 82.24 12.12 13.13	4.44 2.78 4.27 4.27	44444 25224 44552	4.52 4.52 4.10 8.88	4 4 4 4 4 4 5 5 3 3 5 5 4 5 5 6 5 7 6 6 5 8 7 7 8 8 5 8 7 8 8 7 8 8 9 8 7 8 9 8 9 8 9 8 9 8 9 8 9 8 9 8 9 8 9	4.4.4.4.4.55.23.23.23.23.23.23.23.23.23.23.23.23.23.	4.04
Nov.	4.55 4.55 4.70 7.71	4.4.4.4.4.4.4.4.4.05	4.27 4.24 4.14 4.31	4.30 4.28 4.28	4 4 4 4 4 27 2 2 2 4 5 5 5 7 2 2 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	4.4.56 4.35 4.85 4.85	4.03 4.44 4.44 4.32	4.91 4.74 4.25	4.83
Oct.	4.4.4.36 4.54.56 4.54.80	6.44.44 6.44.44 6.50 8.13	4 4 73 4 20 4 32 4 32 4 32	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4.44.44 6.60 4.60 4.60	4 4 4 4 4 4 5 4 4 4 4 4 6 6 6 8 6 8 6 8 6 8 6 8 6 8 6	4.87 4.65 4.49 4.34	4.91 4.79 4.72 4.24	4.78
Sept.	4.44 4.73 4.59 8.85	4444 45212 1231	44444	44444 44688	44.44 4.94 4.59 4.55	7.444 7.444	4.4.4.4.4.7.6.36.36.36.36.36.36.36.36.36.36.36.36.3	4.95 4.96 4.75 4.28	4.06
Aug.	4.48 4.75 4.59 86	44.44 64.44 74.58 85.44 19.88	44.44 42.33 42.33 42.33	4.4.50 4.4.73 4.4.41	4.27 4.57 4.57 5.57	4.80 4.43 4.12 4.98	5.02 5.02 4.77 4.34	4.95 4.95 4.26 4.26	4.88
July ,	4.4.4. 4.6.4. 4.61.73	4.44 4.44 4.15 4.15	4.35 4.35 4.35 4.38	4.46 4.41 4.38 4.33	4.26 4.93 4.62 4.55	4.75 4.43 4.07	4.03 4.94 4.77 4.62	4.36 4.26 4.26	4.86
June .	64.4.4.4.6.6.8.	4.67 4.40 4.18 4.18 4.16	4.35 4.34 4.37 4.36	4.35 4.35 4.37 4.31	4.22 4.70 4.62 4.55	4.47 4.47 4.95 4.95	4.38 4.38 4.38	4.93 4.84 4.73 4.27	4.84
May	4.40 4.72 4.56 4.81	4.69 4.35 4.51 4.51	4.44.4. 2.30 3.30 3.30	4.48 4.35 4.36 4.30	44.44 4.65 4.65 4.54	4.70 4.45 4.19 5.95	4.03 4.77 4.60 4.37	4.93 4.45 4.71 4.28	4.81
April	4.37 4.72 4.39 4.81	4.36 4.36 4.16 4.19	4.38 4.28 4.28 4.40	4.33 4.33 4.35 31	4444 744 622 458 55	4.4.4.4.4.4.15 96.4.4.4.96	4.85 4.71 4.36	4.43 4.80 4.70	4.79
Mar.	4.4.4.4.4.60 80.4.60 18.55	4.36 4.14 4.50 4.15	4.44 4.25 4.25 4.35	4.33 4.33 4.33 2.29	4.73 4.57 4.57 4.53	4.42 4.42 4.18 4.95	4.82 4.82 4.56 36 4.36	4.87 4.43 4.69 4.27	4.78
Feb.	4.4.4.4 7.7.4 7.7.4	44.4.32 44.47 44.47	4.23 4.23 4.30	44444 4855 485 200 200	4 4 4 4 4 4 4 5 2 3 4 5 2 8 5 8 5 2 5 8 5 2 5 8 5 2 5 8 5 5 8 5 5 6 6 6 6 6 6 6 6 6 6 6 6 6	4.54 4.40 4.19	4.05 4.60 4.58 4.32	4.87 4.77 4.26	24.76
Jan.	44444 4851 88	44.44	4 4 7 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4 4 4 4 4 4 5 2 7 3 8 2 3 3 1 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	4.24 4.82 4.61 52	4.58 4.19 4.19 4.94	4.02 4.62 4.57 4.36	4.44 4.43 4.26	4.05
Name of Bond	West Shore RR 1st M 4s 2361. Illinois Corral RR 6s 1041s; 1952. Chies & Ohn Ry 1st M 5s 1939. Illicantal (L N O & T) ond 4s 1953.	In Tenn V & G Ry cons 1st M 5s 1956. Chic Minw Ss Praid gen M st 1980. Late Silw Kitch So 1st M 73/2s 1987. Baltimone & Ohio RM Ist M st 9 1948. Union Pea RK 1st M st 6 1947.	Chicago & Nor West gen M 31/5s 1987. Chie Rock 1 & Par Key gen M 4 st 1988 Arch Too & Saina Fe gen M 4s 1995. N Y Cent & Bulson Kiver M 43 35s 1997.	Oregon RR & Nav Co cons M 4s 1946. Cit Plan & Q (III DV) M 545.8 1949. Central Pacific 1st ref M 4s 1949. Nor Tac VP prior thei 1 M 4s 1997. Nor E West Ry 1st cons M 4s 1996.	Central RR of N J gen M Sa 1987 Hocking Valley 18 croum M 448,9 1990 N & W PA DIV 181 R gen M 48 1944 Southern Pac 18t crow 18 M 89 1946 Southern Pac 18t crof M 4 18753.	A T & S Fe Ry adj M 4s stamped 1995 Norther Pac Ry gen lien 5s 2047 Alt Coast Line 1st cons M 4s 1992 Del & Ritioson Co 1st & rel M s 1945. Central of Georgia cons M 5s 1945.	Pennsylvania RR cons M 4s 1948. Kansa City So Ry et Rt M 5s 1950. Thins N Lit Know & Cit Dily 4s 1955. Illinois Cenral RR Fer M 4s 1955. Cith Ebut & Quincy gen M 4s 1958.	Southern Ry 1st cons M 5s 1994. The R R R 1st lien 8 ref M 4s 2008. At I Coast Line (L 8 vic M 18 1952. At Ord Weet (C 8 C) Joint 4s 1941. Get Nor Ry 1st & ref M 4/8s 1991.	Canada So 1st & ref cons 5s 1962. Morris & Esex 1st ref M 345g 2000. Annastyania RR cons M 415g 1960.
No.	88282	928838	28488	25558	\$5000 8000 8000 8000 8000 8000 8000 8000	22222	1115	22222	25 1

VIELDS OF RAILROAD BONDS JAN. 1917—JAN. 1918

Jan.	5.10 5.46 5.18 5.18	5.31 4.74 4.76 4.94 5.36	4.78 4.86 5.00 5.32 5.22	5.31 4.81 4.78 5.90	5.95 5.27 5.37 5.37 4.99	5.02 5.02 5.78 5.86 5.86	5.37 5.25 5.03 5.46 5.18	6.02 5.17 5.83 4.81	4.61
Dec.	5.06 5.67 5.28 5.28 5.78	5.47 4.87 5.97 5.41	5.11 5.13 5.13	5.43 4.89 5.92 5.98	5.27 5.30 5.44 5.19	5.17 4.92 5.84 5.79	5.05 5.25 5.05 5.47 5.17	5.90 5.18 5.70 4.51	4.64
Nov.	5.37 5.06 5.72	5.40 4.71 5.40 5.40	4.85 4.90 5.02 5.38 5.00	5.33 4.68 5.80 5.80	5.33 5.16 5.47 5.08	54.54.5 57.887 7.00 7.00	5.41 5.25 4.97 5.39 5.09	5.65 5.13 4.55 4.55	4.63
Oct.	4.96 5.39 5.00 5.00	5.08 4.70 4.60 5.19	4 + + 4 4 4 9 9 2 2 9 2 2 9 2 5 7 7 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	5.27 4.63 4.69 5.57	5.55 5.00 5.00 4.95 4.97	5.11 5.50 4.47 5.60	5.22 5.22 4.84 5.38 4.94	5.39 5.10 5.13 4.54	4.49
Sept.	5.62 5.02 5.59 5.59	5.21 4.64 5.09 5.09	4.4.4.4 96.96 96.90 96.90	5.23 4.77 5.49 5.49	5.37 4.94 5.04 4.95	5.20 5.20 5.70 5.70	5.10 5.04 5.22 5.22 4.84	5.38 5.15 5.07 4.44	4.48
Aug.	4.88 4.98 4.94 5.37	5.08 4.50 4.57 5.00	4.59 4.78 4.74	5.08 4.68 4.58 5.50	5.13 4.81 4.92 4.84	5.21 5.21 5.60 5.60	5.08 4.89 5.13 4.70	5.29 5.00 5.01 4.39	4,43
July	4.85 5.21 5.00 4.90 5.11	84.4.4. 84.15.1.90	4.4.4.4. 84.0.4. 72.	5.06 4.63 4.56 5.57	4.4.4.4.4.95 4.90 4.90 8.31	5.45 5.45 5.63	5.04 4.84 5.12 4.68	5.40 4.93 5.06 4.39	4.44
June	5.03 4.96 5.06 5.06	4444.0 444.0	4.44 4.44 4.64 4.64 4.64	44.44 60 4.57 84.53 7.53 84.53	82.4.4.4. 82.93.4.8.4.8.98	4.7.4.5.3.19 2.65.19 3.65.00	4.44 5.77 4.62 4.62	5.15 4.96 5.01 5.01	4.44
May	4, 4, 4, 4, 94 4, 94 5, 06	2.4444 14.444 19.4449	44444 44575	5.37 5.37	44444 67.75 7.76 7.76	5.23 2.23 2.23	5.04 4.79 5.11 4.50	5.11 4.94 5.00 4.18	4.33
April	4.4.4.4 20.08 1.09 1.09	44.63 44.24 47.74	4 4 4 4 4 6 6 4 6 6 7 6 6 6 6	2.4.4.4.6 2.4.6.01.0	4.4.4.4.6.0 4.85.4.66.0	5.04 5.07 5.08 5.08	44.44 46.73 46.73 46.45 46.43	5.04 4.84 4.97 4.10	4.27
Mar.	4.4.4.4 6.50 6.7.	4 4 4 4 4 4 5 8 8 4 4 5 8 8 4 4 5 8	4.21 4.21 4.37 4.37	4.36 4.23 4.96	4.454	4.45 5.00 4.02 4.91	44.48 4.48 4.95	4.94 4.73 4.82 4.82	4.25
Feb.	4.40 4.56 4.48 4.74	44.14.4 44.12.23 44.12.23	4 4 4 4 4 5 3 5 5 5 5 5 5 5 5 5 5 5 5 5	4.4.25 4.22 4.22 4.95	44.44 4.45 4.53 8.53 8.53	4.38 4.93 3.98 4.86	4.4.4.4.4.28 4.933	4.04 4.04 4.04	4.21
Jan.	4.30 4.52 4.49 4.67	4.02 4.04 4.14 4.15	4.19 4.20 4.36 4.18	4.44 4.171 4.84	4.46 6.33 6.4.50 6.4.4	4.05 4.05 3.99 4.77	4.23 4.23 4.28	4.50 4.76 4.00	4.15
Name of Bond	West Shore RR 1st M 4s 2361 Walso Central Rx coll-4s 1932 Walsols KR Co 1st M 5s 1939. Walso Will N 5s 10 5s 1939. III Central (I, N 0 & T) col 4s 1933.	E Tenn V & G Ry cons 1st M 5s 1956. Les Sha Mich So Ist M 554 1997. Union Pac RX 1st M RK N 1st 4s 1947. Childratic & Row 1st ext may 154 1997. Childratic & Row 1st ext m M 4s 1988.	Atch Top & Santa Fe gen M 4s 1995 Louisville & Neath unlited 4s 1940 Louisville & Neath unlited 4s 1940 Chi Bark W. Coonsh M 4s 1946 Chi Bur & Q (Ill Day) M 34s 1946	Central Pacific 1st ref M 4s 1949. The Pack Princh leful M 4s 1996. Norf & West Ry 1st coms M 4s 1995. Norf West Ry 1st coms M 4s 1995. Hockman Riv of M 2 gam M 3s 1995. Hockman Valley 1st coms M 445s 1999.	N & W By Div 1st l & gen M 4s 1944. Southern Pac 1st red M 4s 1946. Southern Pac 1st red M 4s 1945. T & S Pe W red M 4s stronged 1995. Northern Pac By gen lien 3s Old*.	Atl Coast Line 1st rous M 4s 1952. Atl Widson Orlst & ref M 4s 1943. Central of Georgia coas M 5s 1945. Farmstyvinal R Kross M 4s 1948. Kansso (19 So Ry 1st M 3s 1950.	L & N (Atl Knox & Cin Div) As 1955. Line Gentral Ref of 44 st 1955. Chic burl & Quincy gen M 48 1958. Chich burl & Coming gen M 48 1958. Un Pac Rk 18t len & ref M 48 2008.	Atl Coast Line (L & N coll) 44 1952. Get Nor Ny 18 K ref M 44/8 1961. Get Nor Ny 18 K ref M 44/8 1962. Moratis So I sker from 85 1962. Moratis & Desex 18t ref M 34/8 2000.	Pennsylvania RR cons M 4½s 1960
Ref.	882323	888 93 93 93	48886	101 102 103 105	100 100 110 110 110 110	1112	116 113 119 120	121 123 123 124 125	126

YIELDS OF RAILROAD BONDS Jan. 1916--Jan. 1917

100									
Jan.	4.30 4.52 4.49 4.67	4.25 4.02 4.04 4.04	4.14 4.55 4.19 4.08	4.36 4.18 4.21 4.17	44.44 4.33 8.33	4.60 4.26 4.05 4.84	3.99 4.77 4.34 4.23	4.89 4.28 4.50 4.18	4.76
Dec.	44444 886 866 87	.4.4.4.4 07.50 08.4.0 0.4.0 08.4.0	4444 25,23 21,24 21,25	4.40 4.28 4.27 4.27	4444	4.69 4.35 4.10 4.88	4.02 4.45 4.45 4.33	4444 202 86.738 203 203 203	4.04
Nov.	4.50 4.50 4.71	4.61 4.43 4.46 4.96 4.96	4.27 4.24 4.14 4.34	4.43 4.28 4.28	44444 CXXX4 CIV4XX	4.66 4.35 4.85	44.03 4.44 4.32	4.91 4.74 4.06 4.25	4.83
Oct.	44.44.4 26.56.4 80.80	4.63 4.16 4.16 4.16	4.31 4.27 4.30 4.32	4.48 4.59 4.33 4.23	4.44.4 2.2.2.34 3.4.64	4.44 4.39 4.89 89	4.49 4.49 4.49 4.49	4.91 4.79 4.72 4.24	4.05
Sept.	4.4.4.4.4.59 6.59 8.85 8.85	4.4.4.4.4.5.1.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2	4.38 4.27 4.44	4.44.4 1.38 2.38	4.27 4.94 4.62 4.55	44444 86.58 86.98 80.98	4.08 4.76 4.62 4.36	4.95 4.43 4.75 4.28	4.87
Aug.	4.4.4.4.4.8.50 8.50 8.80 8.80	44.44. 44.47. 44.58. 19.88.	4.34 4.33 4.28 4.28	4.44 4.42 4.44 4.41 33	4444 27.72 4.57.72 55.55	4.80 4.43 4.12 4.98	4.07 4.07 4.63 4.34	4.95 4.95 4.80 4.26	4.08
July	44444	44444 84444 8458 8458	4.44.4 7.76 4.32 4.33 8.33	4.46 4.41 4.38 4.38	4.4.4.4.69 4.62 4.62 5.55	4.75 4.57 4.07 4.98	4.03 4.77 4.62 4.40	4.94 4.84 4.79 4.79	4.04
June	44444 64008	44.40 1.44.40 1.54.40	4.34 4.74 4.27 4.31	4.46 4.35 4.37	4.22 4.86 4.62 4.62	4.47 4.47 4.15 95	4.86 4.86 4.67 8.38	44.44 74.44 73.73	4.84
May	44444 62228	4.69 4.35 71.4 4.51	4.36 4.73 4.28 4.30	4.44 4.44 4.35 4.36 4.31	4444 465 465 463	44.44 04.44 04.44 05.19 05.19	4.44 7.77 4.37	4.93 4.45 4.71 4.28	4.02
April	4.4.4.4.4.57.7.2.4.81.81	4.67 4.36 4.16 4.51	4.38 4.28 4.28 4.40	4.49 4.62 4.33 4.35	4444 44.58 44.58 58 58	4.66 4.15 4.96	4.03 4.71 4.58	4.94 4.43 4.70 4.27	4.79
Mar.	4.4.4.4.4.68 81.60 81.81	4.68 4.14 4.14 5.14 4.15 1.50	44.44 4.25 35 35 35	4.49 4.33 4.31 4.29	4.73 4.50 4.57 4.53	4.56 4.42 4.18 4.95	4.44 4.82 4.56 4.36	4.43 4.43 4.79 4.27	4.78
Feb.	44.34 4.53 4.77	4.69 4.13 4.47	4.4.4 4.23 4.24 4.24	4444 4.28 4.29 5.29	44.44 4.59 4.58 5.52	4.57 4.40 4.19	4.05 4.75 4.58 4.32	4.87 4.41 4.77 4.26	4.30
Jan.	4.44.4 65.71 8.59	44.44	4444 424 335 833 833	4.4.4.4 2.55 2.85 2.85	4.24 4.82 4.61 4.62	4.58 4.35 4.19 4.94	4.02 4.77 4.62 4.37	4.85 4.43 4.08 4.26	4.4.4
Name of Bond	0 West Shore RB 1st M 4s 2361. 6 Illinoide Central Rb Coul 4s 1952. 2 Chees & Ohio Kp Co 1st M 5s 1939. 2 Chees & Ohio Kp Tac come 5s 1939. 3 Ill Central (LN O & T) Col 4s 1933.	IB Term V & G Ry come last M 5s 1956. Chic Multw & St Paul gen M st 1989. Labe Sh & Mich So last M 37se 1997. Baltimene & Olio RM Est M st 1948. Union pec RK 1st M R Re 1948.	Chicago & Nor West gen M 314gs 1987. Chic Rock 1s & Pes Ky gren M 4s 1988 Arch Too & Santa Pe gen M 4s 1995. N Y Cent & Hudsen Kiver M 4s 3199. Louisville & Nash unified 4s 1940.	Oregon RR & Nav Co coms M 4s 1946 Curl Bur & Q. (Ill Day) M 3938 1949. Central Pacific Ist ref M 4s 1949. The Re Ry princil fine Ig M 4s 1997. Norf & Week Ry 1st coms M 4s 1996.	Central RR of N J gen M 5s 1987 N ecking Valley 1st crous M 4459 1999 N & W Po Div 1st 18 gen M 4s 1944 Southern Pac 1st ref M 6s 1944 Southern Pac 1st ref M 6s 1875.	A. T. & S. Fe. Ry adj. M. 4s stamped 1995 Norther Pac. Ry gen lien is 2047 Aril Coast Line 1st cons M. 8s 1952 Del & Hutdon Co. 1st. & ref. M. 4s 1943. Central of Georgia cons. M. 5s 1945.	Permsylvania RR coms M 4s 1948. Kan (SH Trans Chr. 181 M 3s 1950. L & N Chr. Know & Chr. Div) 4s 1955. Chr. Ban (R Krof M 4s 1955. Chr. Barl & Quincy gen M 4s 1955.	Southern Ry 1st cons M 5s 1994. In the RR 1st line W ref M 3s 2008. In Cosat Line (L & World) 4s 1952. On the West West (C & C) Joint 4s 1941. Gr Nor Ry 1st & Ere IM 43s 1961.	Canada So 1st & ref cons Ss 1962. Morris & Essex 1st ref M 3½s 2000. Pennsylvania RR cons M 4½s 1969.
5.0	82222	228848	88832	88588	22828	22228	42378	22222	24 25 3

YIELDS OF RAILROAD BONDS JAN. 1917—JAN. 1918

Prop. Mar. April May June July Arts. Sprt. Oct. Nov. Dec. Arts.		_		-	-	-				ľ						
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,	Name of Bond		Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	
4.15 4.15 4.15 4.15 4.15 4.15 4.15 4.15	00 West Shore RR 1st M 4s 2361 10 Illinois Central Rx 6x coll 4s 1952 12 Ches & Chio Ay Rx Col 1st 1935 12 Ches & Chio Ay Rx form 8s 1939 13 Ches & Chio Ay for 17 yool 4s 1933.	1:::::	4.30 4.52 4.49 4.49		1	1							400000			
The control of the	86 E Tenn V & G Ry cons 1st M 5s 1956. 88 Lake Sh & Michol S1 st M 35s 1997. 91 Union Pac RR 1st M Rk & ij ss 1947. 92 Childago & Now West gen M 35s 1997. 93 Chil Rock Is & Pac Ry gen M 4s 1988.	1111	4.02 4.04 4.14 4.55													
4	44 (Atch Top & Santa Pe gen M 4s 1995 50 N V Cen & Huddon River M 3/3s 1997 50 O O O Chi Bur & Co Con M 4s 1946 60 O Chi Bur & Q (III Diy) M 3/4s 1946															
4	01 Central Pacific 1st ref M 4s 1949. 02 Nor Per Ry princip left 1st 1949. 03 Nort West Ry 1st const M 4s 1996. 04 Central R Ref O'l grem M 5s 1997. 05 Getting R Pet O'l grem M 5s 1997.					44440	4.4.40 5.40 5.37									
4.6 4.6 4.8 4.8 4.8 4.8 4.8 4.8 4.8 4.8 4.8 4.8	06 N & W Ry Div 1st l & gen M 4s 1944. 07 Gree Sh Line R Ry Cross 1st M 8s 1946. 08 Southern Pac 1st ref M st 1955. 09 A T & S Fe & Ry and M st stronged 1995															
4.39 4.48 4.73 4.70 4.77 4.78 5.48 5.40 5.40 5.45 5.45 5.45 5.45 5.45 5.45	MAI Coast Line 1st cons M 4s 1952. Del & Hillson Co 1st & red. M 4s 1943. Central of Georgia cons M 5s 1945. Bensayvania RX cons M 4s 1945. Is Kansas City So Ry 1st M 5s 1950.															
4.08 4.09 5.00 5.11 5.40 5.40 5.00 5.18 5.50 5.60 5.00 5.00 5.00 5.00 5.00 5.00	116 L. & N. (Art Knox & Cin Div) 4s 1955. 117 Hinne Central Kr of 14 st 1955. 118 Chich Bird & Quincy en N. 4s 1958. 119 Shuthern Ry 18 com M. 5s 1954. 120 Un Rec RM, 18t Inn & ref M. 4s 2008.		44444 8234 8283												5.37 5.03 5.46 5.18	
4.21 4.25 4.27 4.33 4.44 4.44 4.43 4.48 4.49 4.63 4.64	21 Atl Coast Line (L. & N coll) 4s 1952. 22 North West (C. & C. J. John 1st 1941. 23 Ger Nor Ry 1st & ref M. 474.s 1961. 24 Chanda So 1st & ref ons 1st 1962. 24 Chanda So 1st & ref ons 1st 1962. 25 Mornis & Desex 1st ref M. 3742 2000.		4.68 4.50 4.76				5.11 4.94 5.00 5.00 4.18									
	26 Pennsylvania RR cons M 4½s 1960				- 10	- 1				- 1			- 1		- 1	

VIELDS OF RAILROAD BONDS JAN. 1918—JAN. 1919

		7	N. 1918	AN. 1918—JAN. 1919	6161										
Ref.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	11 .
8828	West Shore RR 1st M 4g.2341 Illinois Central RR coll 4g 1992 Walanah RR Co 1st M 59 1999. Ill Central (L N O & T) col 4s 1939.	5.00 5.46 5.18 5.69	5.17	5.13 5.26 5.26 5.37	5.64 5.64 5.65 5.65	5.15 5.49 5.27 5.27	5.33	5.43	5.71	5.38	5.26 5.33 5.33 5.53	5.18 5.18 5.28 5.30 5.30	5.288	1	5.20 5.20 5.54 5.54
93 93 93 93	Term V& Corons let M is 1956. Lake Sh W. Mich S. 181 M 13/58 1997. Union Phe R. H. M. M. M. M. 1959. 1997. Chingo & N. Wor Weet gen M. Sy 5/59 1987. Chi Nock la & Poc Ry gen M is 1988.	5.31 4.74 4.76 5.36	5.18 4.84 4.84 5.23	5.15 4.82 5.00 5.37	5.34 5.07 5.07	5.34 4.84 4.77 5.00 5.35	5.52	5.49 5.08 5.08	5.25 5.25 5.35	5.23 5.23 5.23 5.23	5.51 4.94 5.15 5.40	5.34 4.83 4.93 7.93	5.444.65		5.30 5.00 5.22
488886	Ach To R. Senne Fe gen f. 4s 1995. N. Y. Cort & Hudoon Ever M 354s 1997. Louisville & Nash unfled 4s 1940. Origins RIC & Nash volve 4s 1940. Origins & Q. (III Dry) M 354s 1940.	4.78 4.86 5.00 5.32 5.22	4.4.4.5 5.20 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1	5.19 5.19 5.19	5.23 5.23 5.23 5.22	5.39 5.13	5.11 5.24 5.24	5.36 5.36 5.36	5.02 5.25 5.33	5.35	44000 84000 8600 8600 8600 8600 8600 860	4.68 4.68 5.95 4.95	4.92 4.92 4.97		5.76 5.04 5.04 5.09
1001001	Central Pacific 1st ref M 4s 1949. Where R vs profile ling M 4s 1995. Nord West Ny 1st cons M 4s 1996. Nord West Ny 1st cons M 4s 1996. Houstmal RN et M 7 gam M 5s 1989. Housting V alley 1st cons M 4s/5s 1999.	5.31 4.81 5.90	24.4.4.5 25.85 26.	5.30 5.83 5.82 5.90	5.94 5.94 5.95	5.25 5.99 5.96 5.96	5.33 5.90 5.90	5.4.4.5 00.4.4.5 00.5.00 0.00	5.00 5.00 6.00 6.00	5.02 5.02 4.92 5.98	24.4.4.5 86.23 86.23 86.23	24.96 4.65 4.65 5.37	25.44.45 26.63 26.63 26.63 26.63		5.22 4.76 5.82 5.57
20000	W. & W. Ry. Dr. 1st I & gen M. 4s 1994. One Sh. Line Ry. consist M. As 1946. Southern Pac I start M. 181 4s 1955. I S. S. Per Ry off M. 4s sempod 1995. Northern Pac Ry. gen lien 3s 7047.	55.27 7.27 7.37 6.99	5.24 5.24 5.21 5.21	5.37	5.5.33	5.23	5.60 5.27 5.33 5.41	5.29 5.29 5.40 5.03	5.32 5.32 5.34 5.37	5.39 5.39 5.66 5.25 5.25	5.28 5.38 5.34 5.09	5.00 2.00 4.00 88.40 88 80 80 80 80 80 80 80 80 80 80 80 80	5.05 4.94 4.93 4.93		5.29 5.11 5.04 4.97
1112	All Coast Line Ist cons M 4s 1952. Control of the Rev Hold of	5.02 5.02 5.78 5.86	5.722 5.722 5.74 5.67	5.05 5.13 5.81 5.81 5.81	5.08 5.30 5.90 8.90 8.90	5.10 5.23 5.81 5.62	5.27 5.95 4.95 5.56	5.39 6.06 4.98 5.80	5.32 5.46 5.01 5.70	5.31 5.05 5.05 5.84	5.14	4.81 5.45 5.45 5.45 5.45 6.49 6.49	2.45 2.45 4.70 4.70 5.42		5.07 5.07 5.40 5.54
116 117 119 120	KW (AM KYON & CLO DAY) 4s 1955. Illinois Cental RR ref M 4s 1955. Clic But & Chorce on M 48 455. Southern Ry timeor with M 48 456. Un Pac RX 1st Intel & ref M 4s 5008.	5,37 5,25 5,03 5,46 5,18	5.04 5.04 5.95 5.01	5.45 5.03 5.03	5.26 5.26 5.43 5.08	5.42 5.04 5.04 5.05	5.23 5.30 5.15 5.16	5.38	5.38 5.19 5.09 5.09	5.54 5.27 5.27 5.70	5.53 5.07 5.46 4.99	5.10 5.4.93 5.173 5.174	5.06 3.4.92 5.22 4.94 4.75		5.37 5.04 5.24 4.91
223221	Mort Caset Line (A. & Noull) se 1952. Norf & West (P. C. & C.) burt se 1941. GET Norr Ry 1st & ref (M. 44/s 1961. Canada & P. 1st se ref rom 8 se 1106. Morris & Esser I st ref M. 3/s/s 2000.	6.02 5.17 4.98 5.83 4.81	5.89 5.09 4.89 5.56	55.99 5.55 6.56 9.56	5.96 5.41 5.62 4.67	5.85 5.45 4.84 5.53	6.04 5.56 4.98 4.66	6.03 6.83 8.83 8.83	5.73 5.73 5.86 4.68	5.87 5.87 5.89 5.89	5.92 4.98 4.65	5.29 5.24 5.176 5.13	5.33 5.27 5.27 5.27 5.27 5.27 5.27		5.40 5.11 5.26 4.56
126	Pennsylvania RR cons M 4½s 1960	4.61	4.62	4.67	4.67	4.67	4.73	4.77	4.79	4.85	4.80	4.60	4.66		4.74
1										The second second		1			11

VIELDS OF RAILROAD BONDS JAN. 1919—JAN. 1920

						-							
Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	oct.	Nov.	Dec.	Jan.
RR 1st M 4s 2361. al RR coll 4s 1952. Co 1st M 5s 1939. Ry 1st cons 5s 1939. N O & T) col 4s 1953.	5.20 5.20 5.60 5.54	5.05 5.23 5.15 5.15	5.25 5.53 5.39 5.18 5.18	5.32 5.56 5.49 5.12 5.78	5.14 5.48 5.36 5.16 5.60	5.04 5.33 5.14 5.14	5.45	55.827	55.52	5.29 5.63 5.33 5.87	5.54 5.87 5.80 5.50 6.10	5.30 5.90 5.91 6.15	5.51 5.86 5.86 6.15
E Tenn V & G Ry cons 1st M 5s 1956 Lake Sh & Mich So 1st M 345s 1997 Union Pac RR 1st M RR & 1g 4s 1947 Chicago & Nor West gen M 3/5s 1987 Chi Rock 1s & Pac Ry gen M 4s 1988	5.30 4.84 5.00 5.22	5.28 4.85 5.04 5.22	5.34 4.92 5.14 5.14	5.25 4.89 5.04 5.29	5.24 4.88 5.02 5.31	5.30 4.77 5.03 5.03	5.24 5.00 5.00 5.07	5.32 5.33 5.33	5.04 5.10 5.10 5.19 5.30	5.47 4.91 5.11 5.40	5.58 5.01 5.20 5.20 5.55	55.110 55.25 57.25	5.04 5.14 5.14 5.47
p & Santa Fe gen M 4s 1995 1t & Hudson River M 3½s 1997 1c & Nash unified 4s 1940 RR & Nay Co cons M 4s 1946 & Q (III Div) M 3½s 1949	4.76 5.04 5.09 5.09	4.90 5.15 5.01 5.12	4.86 5.22 5.22 5.25 5.25	4.94 5.21 5.21 5.21	5.11 5.10 5.06	4.93 5.15 5.31 5.10	5.01 5.19 5.19 5.18	5.04 5.04 5.65 5.65	55.73	5.03 5.26 5.42 5.14 5.14	5.18 5.12 5.36 5.37	850.23 22.23 22.23 22.23	5.22
Pacific 1st ref M 4s 1949 prior lien Ig M 4s 1997 Vest Ry 1st cons M 4s 1996. RR of N J gen M 5s 1987 Valley 1st cons M 4½s 1999	5.22 4.76 4.79 5.57	5.29 4.78 4.76 5.70	5.42 4.84 4.78 4.78 5.74	5.41 4.85 4.85 5.79	5.34 4.87 5.89 5.89	5.37 4.93 4.97 5.76	5.55 5.04 4.98 5.82	5.82 5.19 5.04 6.05	5.71 5.24 5.13 6.31	5.58 5.12 5.04 6.16	5.77 5.27 5.11 4.95 6.39	5.66 5.18 6.95 44	5.73 5.22 4.99 6.37
W Ry Div 1st 1 & gen M 4s 1944 Sh Line RR cons 1st M 5s 1946 Ther Pec 1st ref M 4s 1955 & S Fe Ry adj M 4s stamped 1995 thern Pac Ry gen lien 3s 2047	5.29 5.04 5.11 5.18 4.97	5.36 5.09 5.31 5.31 5.06	5.22 5.22 5.17 5.33	5.48 5.20 5.24 5.33 5.17	5.42 5.20 5.30 5.36	5.38 5.13 5.32 5.08	5.41 5.36 5.26 5.44 5.16	5.34	55.55 5.65 5.65 5.63 5.63 5.63	5.27 5.27 5.26 5.26	5.52	55.55	5.53
11 Atl Coast Line 1st cons M 4s 1952. 12 Del & Hudson Co 1st & ref M 4s 1943. 13 Central of Georgia cons M 5s 1945. 14 Pennsylvania RR cons M 4s 1948. 15 Kansas City So Ry 1st M 3s 1950.	5.07 5.40 5.40 5.54 5.54	5.05 5.13 5.58 5.38	5.08 5.09 5.69 5.72	5.20 5.16 5.72 4.86 5.77	5.532	5.16 5.18 5.64 5.64 5.73	5.25 5.16 5.75 5.75	5.47 5.35 5.00 5.00 6.37	5.42 5.53 6.04 6.42	5.28 5.29 4.90 5.95	5.42 5.39 5.91 5.04 6.14	5.45 5.61 5.03 6.33	5.45 5.67 5.03 6.10
L. & N. (Atl Knox & Cin Div) 4s 1955 Illinois Central RR ref. M. 4s 1955 Chic Burl & Quincy gen M. 4s 1958 Southern Ry 1st cons M. 5s 1994 Un Pac RR 1st lien & ref M. 4s 2008	5.37 5.04 5.24 5.24	5.05 5.04 5.28 4.89	5.39 5.13 5.33 4.92	5.32 5.29 5.15 5.37 5.01	5.35 5.08 5.33 4.98	5.40 5.07 5.07 5.31 4.98	5.27 5.27 5.08 5.11	55.33	5.24 5.24 5.05 5.19	5.44 5.14 5.05 5.08	22,23,38	55.55.55	55.248
Atl Coast Line (L & N coll) 4s 1952 Norf & West (P C & C) Joint 4s 1941 Grt Nor Ry 1st & ref M 44/8s 1961 Canada So 1st & ref cons 5s 1962 Morris & Essex 1st ref M 3½s 2000	5.40 5.11 4.97 5.26 4.56	5.51 5.05 5.34 4.64	5.71 5.16 5.04 5.37 4.72	5.73 5.07 5.07 4.81	5.59 5.21 5.03 5.41	5.53 5.01 5.36 4.84	5.08 5.07 5.07 5.35 83	6.01 5.28 5.18 5.73 4.93	5.32 5.32 5.17 5.61	5.75 5.28 5.02 5.62 4.86	2.5.5.4 88.88 9.90	5.11 5.71 5.95 4.96	5.67 5.67 5.83 4.98
4½s 1960	4.74	4.74	4.76	4.85	4.83	4.76	4.76	4.76	4.90	4.95	4.97	5.00	4.99

SLDS OF RAILROAD BONDS JAN. 1920—JAN. 1921

No.	70 78 83 83	9375 9375 9375 9375 9375 9375 9375 9375	48886	102222	100000	111111	1110	122222 122322 122322	1 26 1
Name of Bond	West Shore RR 1st M 4s 2361. While Central RR ventlet 192. While RR Co 1st M 5s 1939. Chee & Ohio ky 1st come 5s 1939. III Central (LN O & T) col 4s 1953.	E Tenn V & C Ry cons 1st M 5s 1956 Lake Sh & Mich So 181 M 35,58 1997. Chirap Ros Rist M R R Vily 4s 1947. Chirapo & Nor West gen M 3,58 1957. Chi Rock 13 & Pro Fy gen M 4s 1958.	44 Ach Top & Santa Fe gen M 44 1995 20 IN V. Cant & Bridgen Riven J. 73,54 1997. 20 Outwille & Nish Infiled 49 1940 20 On Bridgen RR & Nish Unifed 49 1946 20 On Bur & Q (III Div) M 3958 1946.	Control Pacific 1st ref M 4s 1949. The Ry proper liter Is M 4s 1996. Nort & West Ry 1st cors M 4s 1996. Nort Rather Ry 1st cors M 4s 1996. Hocking Yalley 1st cors M 45s 1997.	W & W Pr. Dr. 1st I & gen M 4s 1944. Ore Sh Lue Kroon 1st M 5s 1946. Suttlern Pec 1st ref M 1st 1955. It S F E Re Vaid M 4s stronged 1995. Northern Pec Ry gen lien 3s 7947.	Art Coast Inne strons M 4s 1952 Del Ke Histon Co str & Rrd M 4s 1945. Centra Hor Corni a coast N 5s 1945. Pennsy van R K coast M 4s 1948. Kansas City So Ny 1st M 3s 1950.	W. (Att. Trans, & Cin. Dry.), and all lines Central RR evi M. (§1955. Citic Burk Quincy gen M. (§1956. Citic Burk Quincy gen M. (§1956. University N. (§1967.), and (§1967	Cook Line (R. N. Cool)) 4s 1952. Norf & West (P. C. & O.) John 4s 1941. Grt Nor Ny 1st & ref M. 4/4s 190. Mannis & Dissex 1st ref M. 3/4s 2000. Mannis & Essex 1st ref M. 3/4s 2000.	Pennsylvania RR cons M 41%s 1960.
Jan.	5.51 5.86 5.51 6.15	5.07 5.34 5.34 5.47	55.22	5.73 5.22 5.17 6.37	5.53 5.69 5.53	5.45 5.67 6.03 6.10	5.81 5.28 5.24 5.34	6.10 5.67 5.14 5.83 4.98	00
Feb.	5.54 6.18 6.05 5.88 5.88	5.94 5.30 5.30 5.59	5.25 5.25 5.66 5.77 5.48	5.46 5.46 5.05 6.50	5.87 5.57 5.81 5.71	5.68 5.75 6.19 5.21 6.26	6.23 6.04 5.40 5.47	6.29 5.26 6.16 5.02	200
Mar.	5.58 6.14 6.06 5.87 6.35	5.25 5.25 5.25 5.25 5.26	5.53	5.98 5.37 5.05 6.46	5.67 5.67 5.67	5.67 5.67 5.26 6.38	5.45 5.93 5.57	6.35 5.85 5.27 6.22 5.11	0
April	6.43 6.10 6.10	5.36 5.38 5.39 5.99	5.55 5.21 5.21 8.33	5.62 5.62 5.62 5.16 6.90	5.91 5.88 5.01 5.84	5.79 5.81 6.70 5.21 6.67	6.27 6.12 5.60 6.18 5.80	6.75 6.09 5.66 6.11 5.32	20. 2
May	5.98 6.38 6.38 6.96	5.43 5.67 5.89 6.05	5.62 5.60 6.23 6.57	5.31 5.72 5.72 7.25	6.29 6.42 6.28 5.86	5.95 6.38 7.05 5.48 6.80	6.52 6.44 6.05 6.34 5.79	7.02 6.34 6.10 6.54 5.35	5 48
June	5.95 6.58 6.27 6.99	5.24 5.35 5.76 5.89	5.57 6.06 6.28 5.88	5.36 5.71 5.52 7.26	6.28 6.40 6.10 6.19 5.79	5.97 6.94 5.07 6.75	6.67 6.18 5.87 6.29 5.76	6.96 6.06 5.82 6.54 5.57	2 45
July	5.83 6.63 6.08 6.71	6.38 5.47 5.64 5.03	5.57 5.98 5.93 5.93	6.33 5.55 5.40 7.04	6.21 5.94 6.16 5.86	6.05 6.74 5.71 6.70	6.81 5.68 6.30 5.74	7.01 6.27 5.78 6.56 5.32	2
Aug.	5.62 6.28 6.53 6.05 6.05	6.30 5.40 5.40 5.80	5.35 5.82 6.09 5.77	5.25 5.32 6.63	6.41 6.11 6.02 5.06	5.84 5.73 5.57 6.64	6.37 5.46 6.09 5.44	6.21 5.62 6.36 5.20	10
Sept.	5.41 6.09 6.17 5.81 6.20	6.04 5.22 5.37 5.28 5.59	5.78	5.33 5.15 6.31 15	6.15 5.94 5.72 5.44	5.67 6.41 6.44 6.44	5.90 5.69 5.92 5.31	6.20 5.91 5.55 5.96 5.11	
g.	5.87 5.99 5.99 5.90	5.75 5.32 5.15 5.44	5.21 5.09 5.61 5.39	5.24 5.09 5.09	5.52 5.52 5.52 5.53	5.23 6.23 41.30 6.41	5.68 5.46 5.15 5.23	6.03 5.63 5.21 5.69 4.97	2
Nov.	5.56 5.93 6.18 5.61 6.21	5.238	55.25	5.97 5.30 5.30 5.93	5.88 5.65 5.67 5.43	5.05 5.05 6.05 6.05	5.87 5.27 5.71 5.36	5.94 5.98 5.35 5.76 5.03	
Dec.	5.84 6.13 6.46 5.90 6.40	5.97 5.20 5.42 5.84	5.40 5.30 5.85 5.88	6.04 5.48 5.40 5.19 6.38	5.87 5.78 5.78 5.58	5.965 6.335 6.629	6.06 5.76 5.59 6.05 5.40	6.30 6.03 5.57 6.04 5.23	
Jan.	5.59 5.93 6.16 5.70 6.09	5.87 5.08 5.25 5.27 5.63	5.20 5.15 5.71 5.32	5.91 5.15 5.15 6.23	5.52	5.40 5.05 5.16 6.41	5.90 5.25 5.73 5.12	5.81 5.88 5.88 5.07	,

VIELDS OF RAILROAD BOND JAN. 1921—JAN. 1922

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No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
82828	West Shore RR 1st M 4s 2361 Innio Central Rx coul-4s 1952 Watsels Rx Os 1st M 5s 1939 Central (L N Ox T) col 4s 1933. Ill Central (L N Ox T) col 4s 1933.	5.59 6.16 6.09	6.00 4.00 10 10 10 10 10 10	5.63 6.24 6.10 6.10	5.71 6.05 6.35 5.68 6.18	5.63 6.32 6.19	5.76 6.32 5.94 6.40	5.63 6.14 6.41 5.94 6.19	5.31 5.84 5.93 5.93	5.47 5.78 6.10 5.66 5.86	5.47 5.73 6.10 5.64 5.85	5.08 5.71 5.50 5.50	5.31 5.31 5.30 5.44	5.12 5.40 5.04 5.37
888 888 83 83	E Tem V & G Ry cons 1st M 5s 1956. Les Sh & Mich So 1st M 354 1997. Union Pac RR 1st M RR & 1st 4s 1947. Chicknew & Norwest gen M 354 1997. Chi Rock 1s & Pac Ry gen M 4s 1983.	5.87 5.25 5.25 5.27	5.76 5.31 5.31 5.31	5.81 5.18 5.40 5.37 5.90	5.76 5.42 5.39 5.78	5.79 5.19 5.51 5.75	5.53 5.60 5.80	5.35 5.35 5.46 5.71	5.32 5.33 5.34 5.64	5.73	5.75 5.27 5.27 5.27 5.44	5.59 4.98 5.15 4.55	5.45 4.67 4.91 5.07	5.43 4.51 4.65 4.97
\$2886 <mark>5</mark>	Arch Top & Santa Fe gen M 4s 1995 V. Cent & Hudson River M 345s 1997. Louisville & Nash unified 4s 1940. Louisville & Nash unified 4s 1940. Chi Bur & Q (III Div) M 345s 1949. Chi Bur & Q (III Div) M 345s 1949.	5.20 5.15 5.48 5.71	5.533	5.21 5.21 5.55 5.43	5.25 5.21 5.62 5.47	55.53	5.51 5.78 5.78	5.22 5.36 5.82 5.33	5.19 5.47 5.67 5.36	5.26 5.25 5.32 5.33 5.33	5.13 5.40 5.24 5.24	5.19 5.32 5.08	4.44.4 7.13.4 8.98.4	4.60 4.64 4.89 5.06 4.87
102201	Central Pacific Jar ref M 4s 1949. Word Re Rey principle in B M 4s 1996. Norf & West Rv Jas coms M 4s 1996. Nortent R Rv OH 2 gen Ma 1987. Hocking Valley 1st coms M 45/8 1999.	5.23 5.15 6.23	5.30 5.30 5.00 6.00	5.36 5.27 5.19 6.12	5.22 5.22 5.22 6.24	6.5.30	6.17 5.39 5.35 6.59	6.04 5.27 5.27 6.38	5.94 5.26 5.19 5.23 6.16	5.78	5.72 5.24 5.14 5.17 6.07	5.40 4.97 5.80	5.25 4.4.81 5.84 5.50	5.13 4.62 4.75 5.46
108 108 1108	N & W Ry Div 1st l & gen M 4s 1944. Southern Pac 1st l & gen M 5s 1946. Southern Pac 1st rel M 1st 18 1955. T & S Fe W gel M 4s stamped 1995. Northern Pac Ry gen lien 3s 2047.	5.89 5.52 5.63 7.47	5.71 5.72 5.73	5.90 5.57 5.81 5.57	5.74 5.77 5.77 5.52	5.97 5.79 5.79 5.46	5.00 5.76 5.84 5.61	55.55 45.55 45.55	5.78 5.51 5.31	5.76 5.50 5.53 5.23	5.51	5.26	5.36 5.09 5.11 5.00	5.15 5.13 5.04 4.92
1111111 111111111111111111111111111111	Atl Coast Line let coms M 4s 1952 Re R Huskon Coast & R re M 4s 9943. Central of Georgia coast N 4s 45. Fernsylvania R R coas M 4s 1948 Kansas (Cty So Ry 1st M 3s 1950	5.40 6.06 5.16 6.41	5.48 6.17 6.43	5.55 5.69 5.41 6.47	6.32	5.66 5.86 6.28 6.34	5.78 6.03 6.54 6.43	5.54 6.43 6.28	5.66 5.30 5.32 6.27	5.34 5.08 6.08 5.37 6.12	5.40 6.10 6.03	55.55.55 5.110 7.110	5.82 5.82 5.49 5.49	5.65 5.65 5.54 5.54
116 118 119 120	L. & N. (Atl Knox & Cin Div) 4s 1955. Lines Central Kre M. Ast 1955. Chic Barl & Quincy gen M. 4s 1958. Chich Barl & Quincy gen M. 4s 1958. Unitern Ry it storin M. St. 1954. Un Pac R.K. 1st lien & ref. M. 4s 2008.	5.90 5.26 5.73 5.12	5.05 5.17 5.82 5.18	5.30	5.24 5.37 5.37 5.37	5.94 5.71 5.33 5.33	5.84 5.88 5.18 5.43	5.93 5.05 5.29 5.29	5.85 5.31 5.93 5.17	5.84 5.26 5.26 5.37 5.13	55.30	5.56 4.58 4.98 4.94	5.24 5.07 4.85 4.82	5.18 4.70 5.63 4.70
121 123 124 125	Atl Coast Line (L & N coll) +9 1952. Ger Nor W, 1st C & Co. J Joint +3 1941. Ger Nor W, 1st & ref M +4/s 1961. Mornal & S. Jet K er for sis 3 1902. Mornis & Bisser 1st ref M 3yls 2000.	6.10 5.38 5.88 5.88	5.91	5.97 5.97 5.97 5.97 5.17	5.36 5.99 5.98 5.16	6.31 6.10 5.54 6.00 5.18	6.45 6.42 5.67 5.22 5.22	6.21 6.14 5.94 5.24	6.02 5.26 5.14 5.14	5.91 5.38 5.38 5.38	5.90 5.38 5.77 5.13	5.67 5.23 5.23 5.46 4.75	5.54 2.454 4.57	5.52 5.30 4.89 4.48
126	Pennsylvania RR cons M 4½s 1960	5.06	5.16	5.27	5.35	5.37	5.47	5.38	5.27	5.30	5.29	4.97	4.88	4.83
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BONDS	53
LROAD	-IAN 19
OF RAII	TAN. 1922-
TELDS	-

Ref.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.
833370	West Shore PR 1st M 4s 2361 Websah RK coll+st 1952. Websah RK Co 1st M 5s 1939. Ill Central (L N 0 & T) col 4s 1933.	55.54 5.04 5.37	5.04 5.23 5.31 5.40	5.33	5.14 5.00 5.15	5.05 5.22 4.91 5.20	5.03 5.22 4.88 5.28	5.04 5.04 5.08 5.14	4.74 4.90 5.03 4.73 5.05	4.87 4.95 5.07	8.44 8.19 11.63 11.53 11.53	5.00 5.26 5.26 5.26 5.26	5.24 5.24 5.24 5.23	5.01 5.115 4.90 5.21
8357888	E Tenn V & G Ry cons 1st M 5s 1956. Bell & Sin M (first Sin R M 5s 1997) Union Pec RR 1st M RR 20 1st 4s 1947. Chi Rector & Novesteen M 5s 1898. Chi Rock 1s & Pec Ry gen M 5s 1988.	5.44.4 5.75 5.75 7.97	5.33 4.59 4.76	5.24 4.57 4.77 4.80	5.18 4.44 773 4.89	5.15 44.44 4.72 86.44 86.44	5.12 4.48 4.47 4.70	24.4.4.4.4.5.1.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2	5.05 4.4.51 4.51 8.78	5.03 4.48 4.37 4.75	5.07 4.52 4.61 8.61	25.24 25.52 26.54 26.54 26.54	5.16 4.65 4.72 4.92	5.09 4.56 5.03 5.03
28888	Arch Top & Santa Fe gen M 4s 1995. V Cent & Thalson River M 3/54 1997. Louisville & Nash unified 4s 1940. Chi W Con Con M 4s 1946. Chi Day M Co Cora M 4s 1946. Chi Day M (O Chora M 3) 39 1949.	4.4.4.6. 5.06.4.87	4.57 4.84 5.07 4.87	4 4 4 5 8 6 6 6 9 8 8 6 9 8	4.58 4.73 4.89 4.62	4.57 4.87 4.87 7.04	4.44 4.74 4.83 4.67	4.54 4.56 4.50 5.50	44.37 44.55 44.55	4.4.4.4.4.4.5.5.25.42.48.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4	4.4.4.4 7.75 4.8.4.7 7.73	4.53 4.91 4.91	4.44.44 00.7.44 7.70	4.4.4.4.4.4.7.3.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2
55555	Central Pacific 1st ref M 4s 1949. Mor Pac Ry moli fail Ig M 4s 1997. Nor R West Ry 1st com M 4s 1995. The Carrier I Ry 1 grem M st 1987. Hocking Valley Ist com M 45g 1999.	5.4.4.5 5.4.62 5.4.62	5.17 4.63 5.42 5.42	5.44.45 5.36 3.36	4.94 4.68 7.26 3.26	5.26 5.26 5.26	4.4.4.5 26.63 26.63 26.63	4444.7 445.3 445.8 52.3	544.52 4.33 5.112	4.47 4.32 4.32 5.07	8.4.4.61 5.4.4.61	4.56 4.56 5.33	5.30 5.30	4.38 4.63 5.30
20800	W. W. W. D. V. Ist I & gen M. 4s 1944. Ore Shi Lee RR corns 1st M. 8s 1946. Sunitorn Fee I ster of M. 6s 18 1955. It S. Fe V. Fee I ster of M. 4s stemped 1955. Northern Fee Use on J. 6s stemped 1957.	5.15 5.13 5.04 5.04 9.94	5.19 5.16 4.99 5.00	24.44.4 20.00 20.0	5.07 4.96 4.71 4.86	5.4.4.4 08.8.8 88.8.8 8.8.5 8.5	4.94 4.82 4.73 2.92	4.4.4.4 80.4.4.4 80.82 80.82	4.5.4.4 44.7.4 47.73	07.4 06.4 07.4 07.4 07.4	4.84.4 4.674.8 85.89	5.01 2.44.45 2.952 2.953	4.97 4.79 4.88 4.88	5.06 4.73 6.92 92 92
#####	Arl Coast Line ist cons M 4s 1952. Dol & Etingon Cost & Per Af As 1943. Central of Copya cons N 5s 1943. Central of Copya cons N 5s 1943. Entersystem R K cons M 4s 1948. Enters City So PK 1st M 5s 1950.	44.84.8 8.86.90 8.84.8 8.54.8	5.53 5.53 5.53	5.06 5.33 5.43 5.43	5.26 5.36 5.33	5.12 5.12 5.12 5.17	4.68 5.20 5.20 5.08	7.74 4.50 4.50 4.50 8.93	4.54 5.07 4.47 4.92	4.54 4.60 4.96 4.52	4.67 5.13 5.08	4.83 4.91 5.23 4.62 5.10	5.15 5.15 5.15	5.25 5.25 5.20 5.20
1119	N. (Auk Tome & Cin Dry 4, 4955. Illinos Central RR for M. 481955. Citic Burk & Quince sen M. 48195. Un Fee ZR Ast Income M. 58194. Un Fee ZR Ast Income M. 58194.	5.44 5.70 5.63 7.63	41.45 41.93 41.75 45.75 45.75	4.98 4.76 5.41 4.67	4.75 4.75 5.26 4.58	4.86 4.78 4.66 5.23 4.67	4.4.4.9 5.28 5.28	4.79 4.47 5.18 4.53	4.77 4.56 5.07 4.49	4.4.82 5.06 5.06	5.44.83 5.10 5.10 6.65	4.93 4.86 4.76 5.21 4.71	4.89 4.80 5.17 4.67	4.82 4.68 5.17
122222	And Coast Line (L. & N. coll) 4s 1952. Nort & West (P. C. & C. J. Joint 1st 1941. Grt Nor Ns 1 & Ford M. 47,51 961. Grt Nort S. & Ford Ont 1962. Montis & Beset ist ref M. 37,52 2000.	5.52 4.89 5.33 5.33	5.48 5.27 4.89 4.52	5.32 5.25 4.50 4.55	5.22 5.15 5.15 5.12 4.50	5.19 5.07 5.14 5.14 4.36	5.24 5.04 5.12 4.44	5.10 5.04 4.69 5.05	5.00 5.02 4.72 4.34	5.07 4.90 4.90 4.35	5.18 4.99 5.05 4.45	5.30 4.82 5.07 4.62	5.22 5.09 5.08 5.08 5.08	5.20 5.01 5.03 4.52
126	Pennsylvania RR cons M 4½s 1960	4.83	4.76	4.77	4.74	4.67	4.65	4.54	4.54	4.48	4.47	4.59	4.66	4.63

YIELDS OF RAILROAD BONDS JAN. 1923—JAN. 1924

No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.		Dec.
8228	West Shore RR 1st M 4s 2361. Withous Cernel RK coll-4s, 1952. Wabash RR Co 1st M 5s 1939. Check Chin Ry st cons 5s 1939. III Central (J. N O & T) col 4s 1953.	5.01 5.01 5.15 4.90 5.21	5.02 5.02 5.15 5.28 5.28	5.06 5.13 5.37 5.06 5.40	5.24 5.24 5.41 5.40	5.06 5.06 5.38 5.34	5.03 5.18 5.43 5.36	5.04 5.12 5.47 5.33	5.02 5.12 5.47 4.97 5.32	5.10 5.02 5.50 4.97 5.31	5.07 5.20 5.40 5.04	1500#5	000000	5.06 5.03 5.03 5.00 4.98 5.37 5.37 5.37
937788	E Tenn V & G Ry cons 1st M 5s 1956. Les fix Michols 1st M 35s 1997 Union Pac RR 1st M RR & 1st 4s 1997 Chichego & Now West gen M 35s 1987 Chi Rock Is & Pac Ry gen M 4s 1988.	5.09 4.56 4.74 5.03	5.13 4.68 4.83 5.00	5.21 4.81 5.186	5.14 4.69 4.73 4.97 5.16	5.15 4.65 4.83 5.15	5.15 4.64 4.62 4.86 5.15	5.12 4.67 5.12 5.12	5.11 5.44 5.95 5.14	5.14 4.73 4.59 5.21 5.21	5.09 5.06 5.06 5.06 4.05 5.06		00000	5.09 4.67 4.67 4.65 5.03 5.10 5.10
28888	Arch Top & Santa Fe gen M 4s 1995. V Cent & Haldson River M 3/5s 1997. Lodisville & Nash unified 4s 1940. Chiesen RR. & Nav C cons M 4s 1946. Chi Bur & Q (III Div) M 3/5s 1949.	4.62 4.83 4.93 4.73	4.44.4 4.75.4 4.70 6.70	5.00 5.00 5.01 5.01	4.4.828 5.928 5.08 6.98	44444 847.44 848.00 848.00	4.59 4.90 4.95 8.86	4.4.4.4.9.70 7.9.4.4.9.70	4.47 5.00 4.84	4.4.8.8.4 00.00 00.00	4.44.4 98.49.8 86.89		20000	4.58 4.62 4.92 4.90 4.97 4.98 4.89 4.91
20000	Central Pacific 1st ref M 4s 1949. The Rep Nath Colle list M 4s 1997. Norf & Week Ry 1st cons M 4s 1996. Norf Week Ry 1st cons M 4s 1996. Hochrint RR of M 7 gem M 8s 1997. Hochring Yalley 1st cons M 445s 1999.	4.72 4.38 4.63 5.30	44.44.44.44.44.44.44.44.44.44.44.44.44.	4.91 4.59 4.74 5.51	5.27 4.88 4.61 5.50	5.01 4.81 5.47 7.47	5.05 4.85 4.62 5.42	5.44.98 5.74.77 5.54.54	4.88 4.42 4.74 5.39	44.44.86 44.44.71	4.44.8 5.44.8 5.82.8 44.8		80.486	4.87 4.95 4.92 4.96 4.48 4.58 4.84 4.81 5.39 5.37
26869	N & W Ry Div 1st 1& gen M 4s 1944. Southern Fee Sh Lie Kross 1st M 5s 1946. Southern Fee 1st ref M fi 4s 1953. T & S Fe Wed M 4s stronged 1995. Northern Fee Ry gen lien 3s 1947.	5.06 4.73 4.92 4.92	5.05 4.86 4.98 8.99 8.99 8.99	5.25 4.98 5.10 8.82	5.23 4.95 5.15 5.07	5.09 4.91 5.02 5.01	5.08 4.88 5.03 5.04	5.07 4.88 5.03	5.05 5.05	5.05 5.05 5.08	5.01 5,09 5,09 5,14		001-04	4.97 4.94 4.90 4.88 4.78 4.85 5.01 5.02 5.14 5.25
111111	At I Coast Line 1st cons M 4s 1952. Les & Rudson Co 1st & Per M 4s 1943. Central of Georgia cons M 5s 1945. Central of Georgia cons M 5s 1945. Kanssyvania R K cons M 4s 1948. Kansse City So Ry 1st M 3s 1930.	4.78 5.25 4.70 5.20	5.21 5.21 5.25 5.24	5.16 5.16 5.33	5.21 5.21 5.42 5.42	5.32 5.32 5.35 5.36	5.36 5.36 5.36 5.43	5.23 5.35 5.45 6.49	4.5.2.2 2.2.2.2 2.2.2.2	5.27 5.39 5.09	5.33 5.33 5.10		0 m m m 0	5.85 5.34 5.37 5.00 5.00 5.00 5.01
1119	L. & N (Ad Knox & Cin Div) 4s 1955. Linels Cernel Kr of M 4s 1955. Chie Burl & Quincy Rev M 4s 1955. Chie Burl & Quincy Rom M 4s 1956. Uniter RV 1st sow M 5s 1959. Un Pec RK 1st fen & ref M 4s 2008.	4.82 4.82 5.17	4.483 5.23 4.73	5.03 5.03 5.35 4.90	5.23 5.29 88.38	5.05 4.93 5.30 7.79	5.02 4.87 5.24 5.24	5.20 4.88 5.24 5.24	5.07 4.886 5.29 87.78	5.16 4.98 5.31 4.90	5.09 5.04 5.31 4.94		-000000	5.10 4.93 4.93 4.93 5.24 5.23 4.84 4.87
122222	Atl Coast Line (L & N coll) 4s 1952. Ger Nor Ry 1st & C & O. Joint 1st 1941. Ger Nor Ry 1st & Per of M 4/4s 1961. Morata & S. 1st & Per from 5s 1962. Morata & Essex 1st ref M 3/5s 2000.	5.20 5.01 4.74 5.03 4.52	5.25 5.10 5.06 5.06 4.54	5.39 5.24 5.20 5.20 4.60	5.49 5.20 5.23 5.23 6.66	5.37 5.18 4.82 5.19	5.41 4.83 5.18 5.18	5.29 4.87 5.13 4.67	5.29 4.97 5.08 4.71	5.27 5.22 5.01 5.17 4.73	\$5.23 \$5.23 \$1.44 \$7.75		2000	5.23 5.08 5.08 5.09 5.09 5.09 5.09 5.06 4.63
126	Pennsylvania RR cons M 4½s 1960	4.63	4.66	4.78	4.84	4.76	4.75	4.78	4.78	4.68	4. 8.4	4.81		1 4.81

VIELDS OF RAILROAD BONDS JAN. 1924—JAN. 1925

Jo d	The second secon		1		1	-	-	-	-	-					
No.	Name of Bond	Jan.	Feb.	Mar.	April	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	_
88888	West Shore RR 1st M 48 2361. Illinois Central RR cold 41 952. Wadash RK Cold M 61 933. Chre & Chin Ky ex coms 54 1930. Ill Central U. N O & D. 10 48 1953.	5.01 4.99 5.30	5.05 5.05 4.99 5.31	5.06 5.20 5.20 5.28 5.28	5.12 5.12 5.12 5.22	44.24.8 76.93 80.88	4.87 5.04 5.04 5.01	44.88 4.79 6.79 99.49	4.78 4.94 4.94 5.05	44.84 4.94 5.06	8.4448 8.65 8.65 8.65 8.65 8.65	4.4.4.8 2.9.9.9 4.0.0	4.88 4.98 4.95 5.10	4.86 4.93 4.93 5.08	
88 93 93	E Tenn V & G Ry cons 1st M 5s 1956 Lake Sh & Mich 50 1st M 3458 1997. Union The RK 1st M RR & 1st 4s 1947. Chingo & Now West groun M 345 1957. Chingook 1st & Pac Ry gen M 4s 1958.	8 4 4 6 8 9 8 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	5.44.6 0.74.6 0.	5.03 5.03 5.03	5.03 5.03 5.03	24.4.4. 25.25. 89.98	5.03 4.45 4.91 4.91	44444 7444 787	4.4.4.98 6.7.4.4.55 7.8.7.0	4 4 4 4 4 8 8 5 5 5 5 5 5 5 5 5 5 5 5 5	44444 77578	4.44.48 4.55.5 6.73	44444 85 10 10 10 10 10 10 10 10 10 10 10 10 10	4.50 4.83 4.83	
28886 5	Atch Top & Santa Fo gen M 4s 1995. Y Cark & Hudson River M 13,5s 1999 Louisville & Nash unified 4s 1940. Chingwon R R N NY Co cross M 4s 1946. Chi Bur & Q (III Div) M 335s 1949.	4.4.4.4 82.98 87.87	5.05 5.05 7.05 7.05 7.05	4.44 5.72 5.72 6.90	4.4.4.4.883.883.883.883.883.883.883.883.	44444 7.82483	4.4.4.4.4.50 4.90 5.7.4	44444	44444 65.65 64.74 67.83	444.61	44444	44444 84064 81085	200 6 6 7 5 200 6 6 7 5	4.52 4.63 4.69 4.73 5.74	
101 103 104 105	Central Pacific 1st red M 4s 1949. Nor Pac Ry wrote lies Ig M 4s 1997. Nord R West Ry 1st cons M 4s 1997. Central RR of N I gen M 5s 1987. Pocking Valloy 1st cons M 44;8 1999.	4 4 4 4 9 8 5 2 5 2 5 2 5 9 9 9 9 9 9 9 9 9 9 9 9 9	5.44 5.32 5.32	5.05 5.05 5.75 5.32 5.33	4.98 4.59 4.75 5.25	4444 81.72 81.73	24.83 4.83 5.11 5.11	5.4444 5.67.45 5.05 7.05 7.05 7.05 7.05 7.05	5.48 5.08	4.87 4.48 4.73 5.08	44448 5.7444 100	24.4.4.4.4.4.6.7.4.4.6.0.8.	5.64.4.88 5.64.4.60	54.44 5.52 5.02 5.02	
108 109 109 110	N & W Ry Div 1st I & gen M 4s 1944. The St Line Ry tons 1st M 5s 1946. Southern Pac 1st ref M 1st 1s 1955. The S Fe Ry oil M 4s strong 1995. Northern Bec Ry gen lien 3s 7047.	4444.82 823.82 17.022	5.02 4.83 5.00 5.20	5.03 4.87 4.91 5.28	4.83 4.83 4.85 5.27	4.4.4.8 87.92 20.20	4.4.88 24.4.4.69 5.02 5.02	24.44.4 26.25.2	44444 80088	4.4.4.4. 07.4.4.4. 86.93.88.	44444	44444 86.39 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.0	4++85 5.00.8	4.567 4.364 4.364 5.364	
111111	Atl Coast Line 1st cons M 4s 1952. Market B Hudson 2 tt & ref M 4s 1943. Central of Georgia costs N 5s 1945. Central of Georgia costs M 5s 1945. Kanssybenha RM costs M 4s 1958. Kansas City So RV 1st M 5s 1950.	5.32 5.32 5.32 5.19	5.17 5.28 4.83 5.27	5.12 5.33 5.23 5.23 5.23	5.10 5.24 5.24 5.23	5.03	4.4.4.5 02.3.9 04.9.0.0	5.02 5.02 5.02 5.02	5.02 5.02 5.03 5.08	4.92 5.05 5.05 5.08	4.90 4.90 5.04 5.04	4.61 4.95 5.93 5.01	4.4.5.4.8 5.0.4.8 5.0.4.8 8.0.4.8	4.66 5.01 5.01 5.07	
1116 1119 1119	L & N (Atl Knoz & Cin Div) 4g 1955. Chinois Central R or M 4g 1955. Chino Ban & Quinoy gen M 4g 1956. Suddhen Ry 1 tero m M 5g 1994. Un Pao RK 1st lien & ref M 4g 2006.	4.87 4.78 5.19 5.19	4.91 4.91 5.17 4.80	5.01 4.96 5.15 4.84	4.88 5.10 5.10	4.78 5.78 5.03	5.00 5.00 4.65	4.4.4.4 00.93 00.93	4.4.4.4 52.00 6.00 6.00 6.00 6.00 6.00 6.00 6.00	4.66 4.05 4.03 4.03	4.60 4.97 4.97 6.65	4.4.4.4. 6.00.4.4. 8.00.4.4.	44.44.45.05.05.05.05.05.05.05.05.05.05.05.05.05	07.44 07.44 77.44 77.74	
121 122 123 124 125	Arl Coast Line (T. & N. coll) 4s 1952. Cert Nor Ny 18; Ever M. 44/s 1901. Cert Nor Ny 18; Ever M. 44/s 1901. Monris & Essex 1 set ref ons 8 - 1902. Monris et resex 1 set ref M. 3½s 2000.	5.15 5.02 4.63	5.18 5.16 4.98 5.07	5.03 5.04 5.04 5.05 4.59	5.12 4.98 5.04 5.04	5.07 4.93 5.02 4.59	5.04 4.90 4.95 5.4	4.95 4.95 4.95	4.4.4.4.4.4.7.20 4.5.24.4.50	4.93 4.78 4.93 4.51	4.92 4.94 4.91 4.91	4.88 4.70 4.91 4.55	4.80 4.75 4.91 4.54	4.88 4.44 11.71 7.57 7.57	
126	Pennsylvania RR cons M 4½s 1960	4.79	4.80	4.77	4.73	4.69	4.58	4 54	4.56	4.59	4.57	4.54	4.58	4.55	
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VIELDS OF RAILROAD BONDS JAN. 1925—JAN. 1926

West Shore RR List M 42 2501. West Shore RR List M 42 2501.	Ref.	Name of Bond	Tan.	Feb.	Feb. Mar. Apr.	Apr.	May	June	July	Ang.	Sept.	Oct.	Nov.	Dec.	Jan.	11 .
Chicago, R. Nor. West, gran. M. Jiffe 1987. Chicago, R. Nor. West, gran. M. Jiffe 1987. Chicago, R. Nor. West, gran. M. Jiffe 1987. Chicago, R. Nor. West, gran. M. Jiffe 1987. Chicago, R. Nor. Card. B. Hulldown, R. Liver, M. Jiffe 1987. Chicago, R. R. M. Hulldown, R. Liver, M. Jiffe 1987. Chicago, R. R. M. Hulldown, R. Liver, M. Jiffe 1987. Chicago, R. R. M. Hulldown, R. Liver, M. Jiffe 1987. Chicago, R. West, Program, M. Jiffe 1987. Chicago, R. West, Program, M. Jiffe 1987. Chicago, R. W. R. West, Program, M. Jiffe 1987. Chicago, R. West, Program, M. Jiffe 1987. Chicago, R. W. R. West, Program, M. Jiffe 1987. Chicago, R. W. R. West, Program, M. Jiffe 1987. Chicago, R. W. R. West, Program, M. Jiffe 1987. Chicago, R. W. R. West, Program, M. Jiffe 1987. Chicago, R. W. R. West, Program, M. Jiffe 1988. Chicago, R. W. West, Program, M. Jiffe 1988. Chicago, R. West, Program, M. Jiffe 1988. Chicago, R. W. West, Program, M. Jiffe 1988. Chicago, R. W. West, Program, M. Jiffe 1988. Chicago,	52888	RR 1st M 4s 2361 ral RR coil 4s 1952 L N O & T) col 4s 1953 Mich So 1st M 358 1997 RR 1st M RR & le 4s 1947	5.08 5.08 4.50 4.60	5.04 5.04 4.50	58.44 5.04 5.04 5.04	5.01 5.01 5.47 5.47	4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	4.78 4.99 4.43	1	5.09 5.09 4.45 4.45	4.84 5.03 4.46 4.57	1	4.84 5.02 4.48 4.48	4.4.8.22 25.20 8.52 8.53	4.4.4.4 7.4.4.4 7.4.4.4 0.50	42570
Can Bre & Quillo Hard M 4344 1990 Can Bre & Parish & Art 1905 Norfe Week Ry six corn M 44 1996 Norfe Week Ry six corn M 44 1996 Norfe Week Ry six corn M 44 1996 San Six corn Ry Can D 1994 San	98 8 8 8 8 8	Nor West gen M 3½s 1987 & Pac Ry gen M 4s 1988. Santa Pe gen M 4s 1995. Hutson River M 3½s 1997. & Nav Co cons M 4s 1946.	4.83 4.84 4.63 4.63	4.83 4.51 4.63	4.4.4.78 4.58 4.58 4.58 4.58	4.4.4.4.4.4.5.4.5.4.5.4.8.3	4.44.4			4.83 4.51 4.51 4.54	4.73 4.51 4.54 4.54 1.81	44444	4.53 4.53 4.76	4444 64.44 74.75 84.74	4.70 4.44 4.56	-6488
N. W. W. P. P. D. T. S. F. D. S.	85884	Chi Bur & Q (III Div) M 33/s 1949. Nor Pac Ry prior lien lg M 48 1997. Nor Week Ry prior lien lg M 48 1997. Central RGR Week RW 38 19087.		4 4 4 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5	4.58 4.45 4.45	4.4.4.4 6.59 6.54.5	44444 447.44 45.55			4.4.4.4. 62.53. 62.53.	4.65 4.86 4.47 4.56	***	44444 1257 1257 126 127 127 127 127 127 127 127 127 127 127	44.4.4. 60.4.4.4. 58.58	नं सं स सं सं	55 55 55
Alt Count, Lies Pr. gen I He as 1987 Alt Count, Lies Pr. gen I He as 1987 Alt Count, Lies Pr. gen I He as 1987 Alt Count, Lies Pr. gen I He as 1987 Le M. Kilkowa & C. m. Division and As 1988 Le M. Locat Line gen miffed 454 1964 Le M. Locat Line gen miffed 454 1964 Le M. Louis Sowketern is M. As 1998 Le M. Kilkowa & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le M. Commanda & C. m. Division and As 1998 Le	55555	Hocking Valley 1st cons M 41/5 1999. W W Jy Div 1st 1 & gen M 4 1944. Ore Gil Line RR cons 1st M 3s 1946. Sublemer Re List For M 4 4 1945. A T & S Fe Ry adj M 4 8 stamped 1995.		5.00 4.88 4.66 4.66 4.84		4.4.99 4.60 4.56 4.81	4.75 27.44 27.52 4.75			5.04 4.81 4.75 85.75	5.02 4.75 4.73 4.73		24.444 27.75 77.77	4.4.4.4.4.67.2 7.67.2 7.67.2	4.74 4.74 4.56 4.71	04021
Chick Burl R Quincy gen, M 44 958. Chick Burl R Quincy gen, M 44 958. Chick Burl R Quincy gen, M 44 958. Chick Burl R Quincy gen, M 44 958. Chick Burl R Quincy gen, M 44 950. Chick Burl R Grand Sci 1907. Chick	111411		4.4.4.4. 20.7.4. 07.7.4	44444		5.00 4.43 4.55 4.55 5.56	44.44.457.45.45.45.15.4			5.05 4.59 4.65 4.77			44.44 65.44 70 70	25.55.30 25.55.30 25.55.30	44444 45864 49884	22222
Chaudidan North R. 28 yes 46.06 65.4 1046. Chaudidan North R. 28 yes 46.06 65.4 1046. Chaudidan North R. 28 yes 46.06 65.4 1046. Chaudidan North R. 28 yes 46.06 65.4 1046. At Coast Line gen unified 45.4 1066. At Coast Line gen gen gen gen gen gen gen gen gen g	118 123 124	Chic Burl & Quincy gen M 4s 1958. Waldburn Ky 1 across M 5s 1904. Un Pac RK 1st lien & ref M 4s 2008. En No RY 1st & ref M 4s 2001. Cunda So 1st & ref on S 1962.	4.97 4.97 4.95	4.62 4.93 4.71 4.93		4.4.4.4.4.58 4.7.38 4.7.38	4.85 4.55 4.71 4.81			4.64 4.74 4.74 4.88	4.62 4.84 4.67 4.74 4.86		4.82 4.70 4.75 4.84	4 4 4 4 4 4 4 5 8 5 2 5 2 5 3 5 5 5 5 5 5 5 5 5 5 5 5 5 5	15.4 1.60 1.71 1.72	18815
Penngydwnia RR gren M 5a 1968. 480 480 480 480 480 480 480 480 480 480	126 127 128 129 130	1 1 1 1 1	5.20 5.20 5.43 5.01 4.84	40004		44.55 25.15 24.55 88.			40044	5.44 5.46 4.96	4.58 5.10 5.42 4.90		5.13 4.88 4.88	5.1.5. 4.8.3.1.3.2.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8	4 + 52 4 + 73 4 - 73	0.80.85
Cleve Cin. Chi & & L. L. Ky gen. M. 4s 1993. 4.89 4.90 4.87 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.77 4.80 4.70 4.70 4.70 4.70 4.70 4.70 4.70 4.7	131 132 134 134	Pemrsylvania RR, gen M, 58 1968. Chr On Ry, gen Gerier C, 58 1973. St. Louis SW western 1st M, 48 1990. Ches & Olio Ry, gen M, 458 1992. Ches & Olio Ry, gen M, 458 1992.	5.02 5.02 5.02 5.10	48.44.88 26.93 40.54	4.83 5.36 5.01 5.01 5.06	5.41 5.41 5.93 5.05	88.4.4 88.4.4 97.49		するすすす	5.35 5.02 4.86 4.95	5.31 5.31 5.89 5.91 5.92		4.8.24 4.8.85 4.8.85 5.00 5.00 5.00 5.00 5.00 5.00 5.00	25.19 27.19 17.19 17.19	C. 1.2	೭=೪೮೩
Canadian + ac 1c) + // acb moca.	136 137 139 140		4.85 4.98 5.03 5.03	8.44.8 0.00 0.00 0.00	1	5.02 5.02	4.80 4.88 4.95 8.95	i	1	(1	1	11	4.70 4.92 4.92	4.4.4.4	4.74	#8####################################

YIELDS OF RAILROAD BONDS JAN. 1926—JAN. 1927

LUC	,			111.1.1.1				
Jan.	4.61 4.35 4.35	44.57 44.37 587 587	4.39 4.39 4.38	4.43 4.50 4.55	44444 355 355 355 355	4.38 4.38 4.38 4.38	5.04 4.89 4.49 4.55	4444
Dec.	44444 6077646 377646	4.4.4.4. 6.4.4.4.4. 6.4.4.4.1.	44444	444.59 45.58 59 59	4444 66666	44.44 44.71 44.71	5.06 4.45 4.53 6.53	4 4 4 4 4 50 55 50 55 50 55
Nov.	4-4-4-4-4-4-58 88.88-4-4-4-4-4-8-8-8-4-4-4-4-4-4-4-4-4-	44444	44444 44444 774 4433	4444 44.48 586.44 586	4444 445 38 38	4.65 4.43 4.72 4.44 4.44	5.05 4.44 5.05 5.05 6.54 4.54	85 4 4 4 4 6 6 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
Oct.	44444 86244 44444	44444 64437 6443 6443	4444	44444	4444	44444 477744	5.07 5.05 4.63 4.70	4.67 4.67 4.70 4.62
Sept. 0	44444 87844 87844	44.44.68 44.36 44.36 63.45	46.49	4444 4.53 4.53 63 63	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	444.67 44.52 4.76 4.76	25.44.4 26.63 26.63	4.93 4.71 6.71
-	44444	44.66 44.48 44.48	44.52	44.67 4.54 4.54 4.60 4.64 4.64	44.44	4.4.4.4.4.52.4.4.4.52.4.4.4.52.4.4.4.52.4.4.4.4	5.09 5.13 5.13 4.64 4.70	4.97 4.65 4.71 4.65
Aug.	1			44444	44444 44444			
July	4.4.5 4.4.38 4.4.45	4.4.4.4.4.4.4.4.4.6.5.4.4.4.4.4.4.4.4.4.	44444	च च च च च	4 4 4 4 4	4.44 4.45 4.45 4.45 4.45 4.45 4.45	55.06 8 5.06 2.06 4.46 6.71	8 4.97 2 4.66 7 4.73 9 4.63
June	4.36 4.30 4.39	4.4.4.4. 22.4.4.9.	4.4.4. 4.53. 4.453.	4.44.47.4.51.4.52.4.54.62.54.54.54.54.54.54.54.54.54.54.54.54.54.	4.4.4.4.4.4.4.5.15.15.15.15.15.15.15.15.15.15.15.15.1	44444 4444 4644 4644 4644 4644 4644 46	5.05 4.98 4.62 6.62	4.63 4.63 4.67 4.67
May	4.35 4.35	4.65 4.43 4.43 4.43	4.4.4.4.4.4.4.35	44444 45474 459	4.4.4 4.40 4.41 4.41 4.41	4444 84444 8744 84444	5.05 5.01 4.63 4.58	4.62 4.70 4.70
Apr.	4.4.4.4.4.4.4.38 4.4.38	44.44 69.44 63.44 63.44	44444 6664 6644 6644 6644 6644 6644 66	4.76 4.48 4.66 4.71	4.4.4.4 4.4.4.4 7.4.4.4	4.44 4.49 4.78 4.43 84.43	5.08 5.13 4.62 4.62	4.96 4.69 4.76 4.65
Mar.	4.4.4.4. 25.7.4.4.4.4.4.4.4.4.4.4.4.5.5.4.4.4.4.4.	4.44 4.44 4.49 7.76	4.74 4.74 4.57 4.57	44.57 44.57 47.73	4.50 4.50 4.50 4.50	4.76 4.55 4.47 4.47	5.10 5.20 4.79 4.72	5.01 4.75 4.84 4.72
Feb.	44.44.44	44444 68444 8844 8844 8844 8844 8844 88	44444 555 853 853 853 853 853	4.55 4.75 4.75 4.75	44444 45544 515644	44.44.4 44.54 44.81	5.09 4.75 7.75	5.07 4.76 4.71 4.81
Jan. F	44.44 4.76 4.76 50 7.44 7.50	4.44 4.70 4.56 6.99	4.4.5 4.43 55 55 55	4.90 4.50 4.71 4.83	4.44 4.56 4.49 51	4.78 4.60 4.79 4.52	55.25 5.25 4.79	44.78 47.88 7.78
Name of Bond	West Slore RR 1st M 4s 2361 Illinois Certal RR coll \$4 1052 Ill Certal IV 0 & T) vol \$4 1053 Ill Certal IV 0 & T) vol \$4 1053 Ill Certal IV 50 st M 3 455 9077 Friend Pac RR 1st M Re & 1945 1097	Chicago & Nor West gen M 31/s 1987. Chi Rock Is & Per by gen M 4 st 1983. Attor Top & Sana Fe gen M 4 st 1993. NY YORNE WITH St 1995. Ourgon RR & Nay Co cons M 4s 1946.	CM Bur & Q (III Div) M 345s 1949. Central Pacific 1st first 1st 1949. Nor Pac Ry mor lien Ig M 4s 1997. Nor R West Py 1st cons M 4s 1966. Central Re Of N J gen M 5s 1987.	Hocking Valley 1st cons M 4)±s 1999 Ove Sin Line RR cons 1st M 5s 1946 Southern Pet 1st ref M si 4s 1955 A T & F De Ry and M 4st stamped 1995 Northern Pac Ry gen lien 3s 2047.	Atl Coast Line ist cons M 4s 1952. Pennsylvania RR cons M 4s 1948. Thinks Worth Knox & Cin Divy 4s 1948. Thinks Central RF ter M 4s 1955. Gilts Gentral RF ter M 4s 1958.	Southern Ry 1st, cons M Ss 1994. Of Pto RXR st little Ryref M 48 2008. Canda So 1st Ryref M 454 1961. Canda So 1st Ryref Cons Ss 1902. Pennsylvania RR cons M 4/5s 1960.	Canadian Nor Ry 25 yr sf deb 6/5s 1946. Grt Nor Ry gen Serbes B 5/5s 1902. Atl Coast Line gen unfled 4/5s 1904. Pennsylvania RR gen M 4/5s 1905.	Grt Nor Ry gen Series C 5s 1973. St Louis SWestern 1st M 4s 1979. Mor Kinssas - Poras Ry 1st M 4s 1990. Chee & Colin Ry gen M 445s 1970. Cleve Cho In Ry Ry L Ry gen M 484 1993.
No.	25 28 28 28 21	22222	01000 1000 1000 1000 1000 1000 1000 10	1008 1008 1108 1108	1114	119 120 123 124 126	128 128 130 131	132 133 134 135 136

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-	c. Jan.	4.31 4.35 4.43 4.43 4.06 4.08 4.10 4.11	4.17 4.16 4.26 4.26 4.07 4.08 4.12 4.15	4.30 4.30 4.13 4.13 4.07 4.10 4.15 4.14 4.19 4.22	4.13 4.15 4.31 4.31 4.09 4.12 4.08 4.04	4.11 4.11 4.11 4.13 4.38 4.38 4.10 4.12	4.43 4.14 4.14 4.73 4.60 4.55 4.36 4.36 4.34	4.26 4.26 4.30 4.28 4.58 4.61 4.37 4.40 4.34 4.35	36 4.36 111 4.12 143 4.42 33 4.33	.45 4.39 .46 4.48 .54 4.52
	Nov. Dec.	4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	44.09	44444	44.44.44	44444	444444	44444	444.44	44.51
	Oct. N	44.4.4.4.4.4.56 11.20 12.12	24.4.4.4.4.4.1.23 8.1.4.4.4.1.2	4444 4444 22122 22282	4.44 4.30 4.12 4.17 17	4444 104 104 104 104 104 104 104 104 104	4 4 4 4 4 4 5 1 4 4 4 5 1 4 4 4 5 1 4 4 4 4	4.31 4.45 4.45 4.45 4.45	4.4.2 4.2.2 4.2.2 4.40	44.58
	Sept.	4.45 4.62 4.15 4.15	4.28 4.43 4.15 4.21	44.45 4.16 4.24 4.35	4444 14.45 17.15 1.15	4.23 4.122 4.139 1.19	4.56 4.96 4.96 4.47	4.37 4.56 4.51 4.51	4.46 4.26 4.26 4.61	4.4.4.4.6.0 07.4.4.6.0 07.4.4.6.0 07.4.4.6.0
	Aug.	4.47 4.71 4.20 4.19	4.31 4.41 4.25 4.33	4.44 4.25 4.25 4.26 4.34	4.4.4.4.4.25 4.19	4.26 4.23 4.23 4.57	44.58 44.97 44.97	4.44 4.69 4.69 4.55 5.55	4.51 4.64 4.64 4.64	4.65 6.74 6.76
-	July	4 58 4 75 4 75 4 75 7 75 7 75	4.38 4.17 4.28 4.34	4.50 4.24 4.27 7.24 7.27	4.44 4.47 4.17 4.19	44444 25222 26224 26224 2624 2644 2644 2	4.4.4.4.4.96.60 4.8.83.4.61.61	44.44 4.52 4.57 4.59	4444	4.4.4.4. 8.8.4.4.4.55
	June	4.57 4.24 4.24 4.24	4.31 5.4.49 5.4.19 7.4.28	44.24	4.4.49 2.4.49 4.22.49 81.49	4.25 4.24 8.24 4.24 6.26	4.4.4.4. 4.7.4.4.63	44.44 45.74 45.58 55.88	24.30 4.30 4.56 8.4.30	4.82
	May	4.53 6 4.54 1 4.71 2 4.26 4.20	4.30 7 4.45 7 4.16 1 4.21 9 4.31	8 4.22 8 4.22 8 4.227 8 4.227 8 4.357	4 4.21 9 4.52 3 4.22 6 4.22 6 4.22	4 4.24 3 4.21 2 4.25 2 4.21 4.20	22 24 25 24 24 25 26 26 26 27 26 26 26 26 26 26 26 26 26 26 26 26 26	24.43 3 4.46 6 4.60 6 4.60	7 0 0 0 4.24 3 4.26 4.26 4.44 4.45	4.4.4.68 4.7.4.4.68
200	Apr	8 4.49 8 4.71 8 4.22 8 4.22	2 4 4 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	44444 44444 424444 4263	0 0 4 4 7 7 4 4 4 7 7 4 4 4 7 7 7 7 7 7	22.44. 22.44. 24.44. 27.44. 27.44. 27.44. 27.44. 27.44. 27.44.	7.88.21 8.82.45 7.44.45 8.55 8.55 8.55 8.55 8.55 8.55 8.5	6 4.30 5 4.29 0 4.63 7 4.45	4444
John L	. Mar.	55 4.55 55 4.52 77 4.74 37 4.30	28 4.43 28 4.23 40 4.32 39 4.32	39 4.56 39 4.32 30 4.33 30 4.33 30 4.33	39 4.31 53 4.44 55 4.30 55 4.30	35 4.30 36 4.30 36 4.28 31 4.24 4.27	55 35 35 37 37 4.4.32 50 4.4.98 50 4.62 50 4.62 50 50 50 50 50 50 50 50 50 50 50 50 50	22 4.4.4.7 22 4.4.4.4.4.4.4.6.28	52 47 40 40 40 59 40 40 59 40 59 40 59 40 59 40 59 59 59 59 50 50 50 50 50 50 50 50 50 50 50 50 50	76 4.73 87 4.82 87 4.84 89 4.54
1221	Feb.	++++	51 4.49 27 4.28 37 4.40 39 4.39	57 4.59 39 4.39 30 4.31 38 4.36 58 4.60	350 4.49 350 4.49 350 4.49 350 4.35	35 4.35 35 4.39 35 4.36 36 4.63 4.63	68 38 38 04 69 61 61 61 64 60 61 61 64 60 61	55 4.52 53 4.51 61 4.64 54 4.62	50 4.62 50 4.47 12 4.40 68 4.69 59 4.58	71 4.76 86 4.86 87 4.87 57 4.59
140	Jan.	4.61 4.77 4.35 4.34	4.51 4.27 4.37 4.37	44444 75.30 75.83 75.83	4444 4444 32250 3533	4.4.4.4.4 8.8.8.8.8		44 4 4 4 4 4 4 4 4 6 1 1 4 6 1 1 4 6 1 1 4 6 1 1 4 6 1 1 4 6 1 1 4 6 1 1 4 6 1 1 4 6 1 1 4 6 1 1 4 6 1 1 1 1		4.71 4.87 4.57
	Name of Bond	West Shore RR 1st M 4s 2361 Ill floins Central RR coll 4s 1953 Ill Central (L. N O & T) col 4s 1953 Central (L. N O & T) col 4s 1953 Union Pac RR 1st M RR & El 8s 1947	Chicaro & Nor West gen M 3½s 1987. Atch Took 18 & Por Ry gen M 48 1988. Atch Too & Santa Fe gen M 48 1995. Ve Cent & Hadson River M 3½s 1997. Chi Bur & Q (III Div) M 3½s 1999.	Central Pacific 1st ret M 4s 1949. Norf Rec Ky profilen Ig M 4s 1997. Norf & West Ry 1st cons M 4s 1996. The Comman Rich of J gen M 5s 1987. Hocking Nafley 1st cons M 445s 1999.	Southern Pac 1st ref M st 4s 1955 W. S. Fe Rey (api M 4s stramped 1995 Northern Pac Ry gen lien 3s 2047 M. Coest Lune is cross M 4s 1952. Pennsylvania RR cons M 4s 1948.	L. & N. (Atl Knox & Cin Div) 4s 1955. Linios Certin RR teef M st 1955. Chic Burl & Quincy gen M 4s 1958. Chic Burl & Quincy gen M 4s 1958. Un Pate RK 1st iron & M 5s 1994. Un Pate RK 1st iron & Keef M 4s 2008.	Canada So 1st & ref cons 5s 1962. Canadian Nor Ka cons M. 45s 1960. Canadian Nor Ky 25 yr ef deb 6/5s 1946. I Nor Ky gan Series B. 55s 1954. At I Coast Line gen unified 4/5s 1964.	90 Pennsylvania RR gen M 4)/ss 1065. Pennsylvania RR gen M 85 1068. 21 Grt Nor Ry gen Serlec C 8 19/3. 22 Louis Swetern 1st M = 11990. 24 MocKansse-Texas Ry 1st M 4s 1990.	Ches & Ohio Ry gen M 44/sé 1992. Cleye Cin Clin & St. L. gen M 48 1993. Y Central RR cousel M 48 1998. Y Central RR cousel M 48 1998. Lehigh V RR (Fel) gen cons M 48 3003.	O Canadian Pac Ry 4% deb stock. H Southern Ry dev & gen M 4s 1956. Z Chie & West Ind RR cons M 4s 1952. Si Pitt Cin Chi & Sc L gen M 5s 1975.
	Ref.	70 88 91 91	28888	25225	8000111	1118	124 127 128 129	133213	135 136 139	44 14 14 14 14 14 14 14 14 14 14 14 14 1

ELDS OF RAILROAD BONDS JAN, 1928—JAN, 1929

Jan.	4.80 4.39 4.44 4.58	44.33	44.49 4.552 4.63 4.53	4444 555 545 55 55 55	4.47 4.65 4.46 5.17 4.83	44.64 46.53 46.58 46.58	4.77 4.58 4.47 4.52 4.59	4.61 4.80 4.85 4.58	4.73
Dec.	44444	34.64.5 34.64.5 36.4.3	44444 45524 86224	44444	44.46 4.71 4.82 8.82	4.59	44.44 4.44 5.42 4.52	4.57 4.76 4.88 4.57	4.66
Nov.	44444 86.34 44.38	4 52 4 52 4 52 4 50 4 30	4.4.4 4.41 4.51 4.53	44444 44444 4364	44.44	4.54 4.53 4.53 4.60	4.45 4.45 4.45	4.53 4.45 4.49	4.55 4.60 4.65
Oct.	24.4.4.4. 24.6.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4	44.34	4.44	44444 44444 644444	4.4.4.5.3.7.2.4.85	4.56 4.54 4.74 4.74	4.56 4.40 4.41 4.41	44.54 46.54 60 60	4.56
Sept.	44444 252524	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	55. 54. 54. 55. 55. 55. 55.	44.44 45.50 44.44 50	4.41 4.69 5.03 4.92	44.44.45 62.44.49 18.89	44.4.4.4 04.38 06.88	4.54 4.72 4.82 4.63	4.67
Aug.	4.4.4.4.4.4.51 4.51 1.51	4 4 4 4 4 4 51 3 4 4 4 5 1 3 4 4 4 5 1 3 4 4 4 5 1 3 4 4 4 5 1 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	5.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4	4.52 4.57 4.57 4.57	4.4.4.5 5.00.5 4.55 4.55	44.4.4. 63.4.4.4. 64.7.4.	44.44 44.44 63.44	4.58 4.58 4.70 7.70	4.64
July	4444 222 24.23 15.45 15.	4444	44444 55 15 15 15 15 15 15 15 15 15 15 15 15	45444	44444 553 493 793	44444 7469779	4.4.4.4.4.4.36.33 6.33 6.53	4.52 4.58 4.97 4.67	4.63
June	4.4.4 4.27 4.38	4444	4.4.4.45 4.4.47 4.40	4.35 4.27 4.23 4.48	4.57 4.93 4.93 8.93	4.54 4.57 4.74 6.60	4 4 4 4 4 82.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5	4.4.4.4.4.65.3.4.4.85.4.4.85.4.4.85.4.4.85.4.85.4.8	4.53
May	4 4 4 4 4 4 55 6 5 4 4 4 5 5 5 6 6 6 6 6	4444 415 424 815 817	4.24 4.33 4.35 4.35	4 23 4 24 4 25 4 36	4.74 4.74 4.74	4444 464 464 464 464 464 464 464 464 46	4.4.4 4.20 4.21 4.55	4444 44.65 44.65	4.40
Apr.	44444 000 100 100 100 100 100 100 100 10	44444 61864	44444	4.4.4 20 4.20 5.33	44444 54226 5426 5426 5426 5426 5426 542	44444 8664 4864 8486 8486 8486 8486 848	44444 6.30 1.30 1.30	4.39 4.53 4.53	4.45
Mar.	44444 £4586	44444 11.6 6.13 6.13	4444 2224 2225 2525 253	44444 21.8 17.8 17.8	4.4.4.4.4.4.65.16.05.10.00.00.00.00.00.00.00.00.00.00.00.00.	4444	44.34 4.15 4.15 4.10	4.44 4.45 4.53	4.34
Feb.	4.46 4.10 4.11 1.13	4.09	44444	4.17 4.13 4.36	44.44 11.45 14.64 14.64	4444	44444 66464	4.37	4.34
Jan	4.4.4.4.4.4.1.1.26.1.1.26.1.1.26.1.1.26.1.1.26.1.1.26.1.1.26.	4.06 4.13 10.13	44.44	4.4.4.4.4.4.12.23.23.23.23.23.23.23.23.23.23.23.23.23	4.1.12 4.1.13 4.73 4.73	4.4. 4.28 4.40 4.40	4.136	4.33	4.35
Name of Bond	West Shore RR 1st M 4s 2361 INCENTALION OF ST ON 4s 1953 Linch Share M And So 1st M 31s,8 1993 Union Pec RR 1st M RR R 1st 4s 1947 CHIROWS 1st M SH R M R 1st 91 1998	Atch Top & Santa Fe gen M 4s 1995 V Cent & Hudson River M 3/s 1997. Central Pacific 1st ref M 4s 1949. The Reg R prick (incl. Id. 4s 1995. Norf & West Ry 1st cons M 4s 1996.	Central RR of N J gen M 5s 1987 Contral RR of N J gen M 5s 1987 Southern Part 1st on M 4 4s 1955 Southern Part 1st of M 4s 1955 T & S Fe W avid M 4s semped 1995 Northern Park Ry gen lien 3s 2447	All Coast Line 1st cons M 4s 1652. Indexybrain R Known M 4s 1048. Illinois Central R R eff M 4s 1953. Ellinois Cherring Ren M 4s 1958. Southern Ry 1st cons M 5s 1994.	Un Pac RR 1st lien & ref M 4s 2008 Lundri So 1st Ver Gonss 3 1962 Pennsylvania RR cons M 4.5s 1960 Andrein Nor Nor So yr af dol 65 s 1946 Grt Nor Ry gen Beries B 51;s 1952.	Atl Coast Line gen unflied 4½s 1964. Mansylvain R. gen M. 4½s 1965. Pennsylvain R. gen M. 5 s 1965. Pennsylvain R. gen M. 5 s 1965. St. Lonis So Western 1st M. 4s 1999.	Mo-Kansas-Texas Ry, 1st M. 4s 1990. Ches Wollo Ry gen M. 4.5s 1992. Oleve Chi Chi & St. L gen M. 4s 1993. NY Certral RR, consess M. 4s 1998.	Lebigh V RR (Pu) gen coms M 4s 2003 Canadian Pac Ny, Gub suocis Controllem Ry dev N gen M 1st 1936 Chic West Ind RK coms M 4s 1932 Phits Cin Chi N St L gen M 5s 1975.	Great Wor Ry gen M 4½s 1976. Chi Mil & St Paul Ry gen M 4s 1989 Ere RR cons prior lien 4s 1996.
Ref.	0288 198 198	285 <u>5</u> 28	\$200 100 100 100 100 100 100 100 100 100	111411111111111111111111111111111111111	124 124 124 124 128	129 130 131 132 133	134 135 136 137 138	83448	445 145 145

YIELDS OF RAILROAD BONDS JAN. 1929—JAN. 1930

4 + 57 4 + 37 4 + 55	4.50	4.58 4.63 4.45 4.45	4.53 4.59 4.51 4.61	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4.65 4.458 4.77 4.67	44444 65 65 65 65	4.54 4.71 4.95	4.68
44.45 44.45 44.45 56.45	4.47	******** *********	44444 60 64 60 64 60 64 60 64 60 64 60 64 60 64 60 60 60 60 60 60 60 60 60 60 60 60 60	44464 477 813 808	44444 67 67 75 75 75 75	4 4 4 6 4 4 4 5 5 9 4 4 4 5 1 9 4 9 4 9 4 9 9 4 9 9 9 9 9 9 9 9 9 9	4.53 4.67 4.67 4.67	4.73
23.4.4.4 4.53.4.55 61.53	44444 24884 450 450 450	4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	4.4.4.4.4.4.4.5.4.6.5.4.6.5.4.6.5.4.6.4.4.4.5.5.5.5	4.47 4.86 5.26 5.00	44.64 4.73 4.76	4.74 4.66 4.67 4.45 4.73	4.71 4.84 5.02 4.82	4.85
00.14.4 78.44.4 6.64.45.5 40.4	4.39 4.76 4.69 4.46	25.77.7.4 8.80 8.00 8.00 8.00 8.00 8.00 8.00 8.	2.35.25 2.35.25	54.45 5.19 5.19	4 4 4 80 4 70 8 8 77 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	4.4.4.4 00.00 87.18	4.68 5.05 4.73	4.75
250.55 20.55	\$128128 \$128128	28.17.8 1.83.08	44444 1888 179 179 179	4.65 4.90 5.27 5.05		444.44 27.70 89.51 89.89	5.00 5.00 5.10	5.00
	132.23							4.99
								4.92
	42224		28228		1.924.80			4.84
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			44444	44400	-14-44-44-44		ままろろき	4.83 4.
							4444	4.4.4 £.7.7
West Storre RR 1st M 4s 2361 Il Central (L. N. O. & T.) roul 1s 1953 alec Sh. & Mich'so 1st M 1545 1997 Lili Rock Is & Pec Ry gent M 4s 1988	Atch Ton & Santa Fe gen M 4s 1995. V. Cark M Hudson River at N 35s 1997. Central Parific 1st tel M 4s 1996. The Rky princip (len EM 4s 1997) Von & Wyer Ry 1st coms M 4s 1996.	Zentral RR of N J gen M 5s 1987 Cheffing Yalley et cons. M 145s 1990 Southern Pac 1st et 1875 Southern Pac 1st et 1875 Te S Fe Ry and M st stringed 1995 Vorthern Pac Ry gen lien 3s 7047.	At Coast Line 1st cons M 4s 1952. Stansylvania No cons M 4s 1958. Illinois Central RR ref M 4s 1958. Illinois Central RR ref M 4s 1958. Southern Ry 1st cons M 5s 1994.	In Pac RR 1st lien & ref M 4s 2008. Manda So 1st & ref cons si 1902. Pensayivania RR cons M 434s 1900. Mandan Nor Ry 55 yr 54 follo 615s 1946. Frt Nor Ry gen Series B 534s 1952.	At I Coast Line gen unffied 4½s 1964. Wannsylvain R gen M 1½s 1965. Pemsylvain R R gen M 15 1963. Pemsylvain R R gen M 15 1963. From R yee Series C 5 3 1973. From S yee Gen 1 8 1 4 8 1989.	Mo-Kansas-Tewas Ry 1st M 4s 1990. We will More and M-4s 1992. They Cim (Th R. St. Lent M as 1993. They Cherlul Ry Compol M as 1993. You charlul Ry Compol M as 1998. For & Peer Ry 1st M 3s 2000.	celigit V RR (Pa) gen cons M 4s 2003. andmin Pac Ne 47 of the sprocek. Southern Ne dev R gen M 4s 1956. Pac R See M 4s 1956. Pac See See See See See See See See See Se	Great Nor Ry gen M 4½s 1976. Chi Mil & St Paul Ry gen M 4s 1989 Erie RR cons prior lien 4s 1996.
20 88 91 93	95 101 103 103	105 108 109 110	1114	124 124 126 127 127	129 130 131 132 133	134 135 136 137 137	139 140 141 143	145 145 146
	West Store RR List Ma 4250. 11. Central (L.N. Ok. Tr), 2014 s 1953. 12. Mod Store R. R. Mark Store R. Mark Store R. Mod	Hill Central (LN O & L') cold s 1933	Comman (LN O & Cr.) of a 1935. 4.03 4.	Control Register Mark State St	High State Registry	Michael Roop Ref. 12, 10, 10, 20, 20, 20, 20, 20, 20, 20, 20, 20, 2	Microstrian Registry Market 2006 4.00	High State Registry

ELDS OF RAILROAD BONDS Jan. 1930—Jan. 1931

Name of Bond	Lon	Foh	Mar	Anr	Mar	Inno	Tuly	Aug.	Sept.	Ö	Nov.	Dec.	Jan.
	4.84	4.59	4 4 507.7	4.51		4.49	4 4	44	. ('	1	. 1	
Lake Sh & Mich So 1st M 3½s 1997. Union Pac RR 1st M RR & It get 1947 Chi Rook Is & Pac Ry gen M 4s 1988.	444	4 4 4 4 56 56	444	444	8.7.7. 8.7.7.	444 8.33 154	4.25	8 4 4 4 8 1 3 3 1 9 1 9 1 9 1 9 1 9 1 9 1 9 1 9 1	4.4.4 2.1.5	444	3112	614	+.13 +.17 +.28
Atch Top & Santa Fo gen M 44 1995 N Y Cent & Hudson River M 13,43 1997 Courtal Pacific 1st ref M 45 1997 Nor Favo prior fine H M 45 1997 Nor West Ky 1st cons M 45 1996	4 4 4 4 4 25 50 36 98	4.44.47 4.63 4.53	4.4.39 4.52 4.53 4.33	44444	4 4 4 4 4 4 4 4 4 4 5 5 4 4 5 3 3 3 8 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	44444 60446 1100	4.31 4.31 4.21	44.44 22.24 4.24 5.24 5.33	44444 12224	44444 133 121 121	4.44.44 27.24 21.24	44444	4 4 2 2 8 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
Central R.R. of N J gen M 5s 1087. Hocking Yulley 1s 2008 M 44,5s 1999. Southern Peu, 1st reft N at 4s 1955. A T. E. S. F. E. R. ya di M 4s stamped 1995. Northern Peu ER yagu lien 8s 2047.	4 4 4 4 4 6724 6724 6724 6724 6724 6724 6724 672	44444 552 50 50 50 50 50 50 50 50 50 50 50 50 50	44444 64.39 64.39	44444 40848	44444	44444 40447	44444 4888 8128	44444 85258	44444 2422 2422 2522 2522 2522 2522 252	44444 2727 38	44444 04584 04884	44444 254 254 255 255 255 255	4.32 4.23 4.19
Atl Coast Line 1st cons M 4s 1952. Bensyvania R Koron M 4s 1948. Illinois Cortral RR vef M 4s 1958. Southern RN vef M 4s 1958. Southern RV 1st cons M 5s 1994.	4.53 4.59 4.57 4.57	4 4 4 4 4 4 4 4 4 4 4 4 8 6 2 5 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	44444 84444 83448	4.58 4.41 4.53 4.56	4 4 4 4 4 2 3 8 8 4 5 4 5 4 4 4	44444 65443 655	4.4.4.4 4.30 4.30 4.30	44444 1234 124 124	44.44.4 42.15	44444	44444 222 221 200 100 100 100 100 100 100 100	44.59 44.90 4.68	44444 2513 2413 443 443 443
Un Pac RR 1st lien & ref M 4s 2008. Canda So 1st & ref Cons 5s 1907. Pennsylvania RR cons M 41/5s 1960. Gr. NOR yen Seres B 5/5s 1902. Att Coust Line gen unified 4/5s 1904.	4 4 4 4 4 8 4 4 4 4 8 4 4 8 8 8 8 8 8 8	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4.40 4.43 4.81 4.57	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	44444 4725 50	44444	4.65 8.33 8.50 4.68	4.4.4.4 5.3.3.4 4.7.4 8.30 9.50 9.50 9.50 9.50 9.50 9.50 9.50 9.5	4.4.4.4 4.50 4.66	4.17 4.20 4.71 4.71	4.56 4.56 4.56 4.54	4.31 5.01 4.70	4.19 4.60 4.13 4.78
Pennsylvania RR gen M 41/4s 1965 Pennsylvania RR gen M 51 9086 Ger Nor Ry gen Series C 81 973 St_Loris Soffestern 1st M 1st 91090	4.4.4.4.67 77.4.4.4.67	4 4 4 4 4 87 88 87 89 80 69	4.52 4.72 4.59 4.62	4 4 4 4 4 62 22 25	4.51 4.65 4.65 4.66	4 4 4 50 67 67 67 67 67 67 67	4.4.4.4.4.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5	4.4.45 4.45 4.45 4.48	44444 886 844 844 844 844 844 844 844 84	4.48 4.48 4.46 4.46	44444 445 4484 515	4444 4.92 4.64 5.64	4.48 4.74 4.71 4.71 84
Ches & Ohio Ry gen M 41/s 1992. Cleve Chi Chi & Stoze In M 44 1993. Tex & Pere K 194 M 5 2000. Tex & Pere K 194 M 5 2000. Lehigh V RK (Fs) gen com M 4s 2003.	4.59 4.50 4.54 4.54	4 4 61 4 5 50 4 63 6 59	44444 64443 64464	4.44 4.44 4.57 5.52	44.44.4 85.30 08.53	4.4.4.4 4.538 4.538 4.538	44.46 4.33 4.43 4.43	4.44 4.25 4.46 4.37	4.3 4.18 4.45 4.33	4.31 4.17 4.36 4.36	4.4.4.4 200.00 200.00 200.00 200.00	44444 42,339 41,73	44.21 44.21 44.48 58
Canadan Pac Ry 4% deb stock. Southern Ry dev R gen M 44 1056. Olic Wast Int RR 008 M 48 1055. Great Nor KR gen M 435 1975. Great Nor KR gen M 435 1976.	4.4.4.4 1.7.1 1.08 1.08	5.01 5.01 4.74 7.14 7.14	4.64 4.59 4.79 4.58	4.4.4.4 8.56 8.56 8.56	4.63 4.79 4.54 4.61	44.4.4.4.52 4.52.4.4.63	4.50 4.72 4.52 4.50	4.45 4.570 4.557 5.53	4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	4.44 4.44 4.46 4.46 4.54	5.05 4.74 4.56 4.56	5.16 5.08 4.71	4.54 4.77 4.77 4.50
& St Paul Ry gen M 4s 1989. cons prior lien 4s 1996.	4.66	4.79	4.69	4.74	4.72	4.70	4.75	4.71	4.65	4.71	4.79	5.01	4.79

VIELDS OF RAILROAD BONDS JAN. 1931—JAN. 1932

	Name of Bond	Jan.	Feb.	Mar.	Apr.	May	June	July	Aug.	Sept	Oct.	Nov.	Dec.	Jan.
93164	West Shore RR 1st M 48 2361 Union Pac RR 1st M RR & 1 (25) 1997 Union Pac RR 1st M RR & 1 (5) 1997 Alch Rock 1 & 8 CP (8) 1998 Alch Top & Santa Re gn M 48 1998	4.13 4.17 4.17 4.07	44444 4400 4400 5000 5000	4 4 4 4 4	4.08 4.45 4.45	4.11 3.92 4.40 4.00	4.35 3.93 4.58 4.01	4.36 3.89 4.50 4.50	3.94 3.94 4.60	4.4.30 4.86 4.15	4.50 5.20 4.36	5.08 4.73 5.33 4.43	5.76 5.02 6.12 4.73	5.63 4.91 5.52 4.65
20000	N Y Cent. & Hudson River M 3/4s 1997. Terrar Bache is a pri M 14 1994. Nor Pac Ry prior Hen Ig. M 44 1997. Nord & Week Ry 151 const M 48 1996. Central RK of N J gen M 58 1997.	4.28 4.28 4.25 4.09	44.30 44.30 44.10 4.35	4.26 4.27 4.09 4.35	4.33 4.05 4.35	4.17 4.29 4.01 4.32	4.21 4.26 4.35	4.27 4.27 4.30	4.31 4.20 4.42 4.01	44444 2445 2446 2446 2446 2446 2446 2446	5.07 4.32 4.32	5.45 4.92 4.37	5.01 6.08 5.25 4.57	5.95 5.11 5.11 5.34
288821	Hocking Valley 1st cons M 41/s 1999. A T & SFe Ry add M 4st 1955. A T & SFe Ry add M 4st stamped 1995. A Towntier Pack Ry gen lien is 2047. At I Cost Line 1st cons M 4s 1992.	4.23 4.19 4.37 4.26	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4.25 4.25 4.21 4.24 4.24	4.33 4.27 4.51 4.51	4.18 4.18 4.15 4.53	4.34 4.17 4.17 4.44 4.28	4.34 4.25 4.25 4.20	4.43 4.43 4.62 4.05 5.02	4.4.60 4.4.4.2 4.86 4.33	5.114 5.114 5.115 5.117 5.12	5.05 5.13 5.14 5.14	55.35 57.22 5.74 5.85	5.44 5.39 5.38 5.88
4118 250 270 270 270	Pennsylvania RR cons M 4s 1948. Chik bart X Quincy gen M 1s 1958. Southern Ry 1st cons M 5s 1954. The Re RR 1st lene & tr M 4s 7008. Canada So 1st & tet cons 5s 1962.	4.13 4.14 4.19 4.19	4.55 4.55 4.55 4.55	44444 520 520 520 520	4.07 4.16 4.23 4.58	4.06 4.06 4.13 4.13	4.03 4.03 4.54 4.58	4.05 4.05 4.13 4.58	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4.33 4.33 4.37	4.58 5.34 4.70 5.37	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	5.08 6.76 5.33 6.79	4.85 4.96 6.07 5.24 6.38
330,528	Pennsylvania RR cons M 44/s 1960 Chi Nor My gue Series B 53/s 1952. Atl Coast Line gen united 4/s 1964. Internylvania M gen M 14/s 1964. Pennsylvania LN gen M 18/s 1966.	4.4.4.4 84.48 84.48	4.80 4.83 4.37 4.45	4.46 4.46 4.46	4.52 4.52 4.52 4.51	44.44 11.7.4.4 06.4	4.13 4.47 4.52	4.44 4.45 4.52	48.4.4.4 48.4.4.4 46.56.4	4.33 6.10 4.59 4.72 5.05	4.56 6.49 5.21 5.10	5.38 5.23 5.23	8.17 5.97 5.95 5.95	5.02 7.55 6.07 5.60 5.61
3334333	Grt Nor Ry gen Series C 5s 1973. Lou 's Sowlearen' ret M, 4s 1980. Mo-Kansan-Peas Ry 1st M, 4s 1980. Mes Ry Dia Ry gen M, 45, 8 1992. Cleve Gin Chi R' 5s, L' gen M, 4s 1993.	44444 41222	44.44 258 258	4.4.68 4.4.4.4.4.4.23	4.90 4.90 4.25 4.31	4.25 4.25 4.25	5.36 315 315 315 315 315	5.28 4.55 4.55 4.33	4 + 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	5.85 5.44 4.91 4.41	6.78 6.77 5.41 5.00	6.26 6.82 5.31 5.16	5.58 5.58 5.59	6.83 6.60 5.24 5.59
450 450 450 450 450 450 450	N Y Central RR consol M 4+ 1998 Cark Pach Ry 18 M 55 2000 Cabligh V RR (P3) gen const M 45 2000 Cabligh V RR (P3) gen const M 45 2000 Chi & West Ind RR (P3) 8 1952 Chi & West Ind RR (P3) 8 1952	44444 7483	4.45 45.45 47.45	4.48 4.63 4.63 4.68	4.51 4.51 4.51 4.54 4.69	4.54 4.70 4.53 4.73	4.61 4.61 4.62 4.76	44444 60 60 70 70 70	4.85 4.94 5.00	5.45 5.70 5.45	5.16 6.29 6.34 5.96	5.08 5.30 5.30 6.30	5.90 7.88 6.52	5.87 7.72 6.52 6.55
45443	Pitts Cin Chi & St L gen M 5s 1975 Great Nor Ity gen M 43/48 1970. Cin Mil & St Paul Ry gen M 4s 1989. Erie RR cons prior lien 4s 1996.	4.50 4.79 4.66	4.56 4.68 4.70	4.51 4.71 4.58	4.55 4.69 5.05 4.61	4.52 4.63 4.93 4.60	4.66	4.54	5.09 4.97 4.58	5.78 5.34 4.90	5.09 6.37 6.07 5.54	5.19 6.15 6.46 5.71	5.65 7.40 7.42 6.73	5.54 6.63 5.89
1	The second secon		-				1	1	1				-	-

YIELDS OF RAILROAD BONDS Jan. 1932—Jan. 1933

			APPE	NDIA			
Jan.	5.52 4.50 5.62 5.62	44.54.5 4.04.98 5.98	44.59 44.59	6.23 5.55 6.96	5.11 5.44 5.24 5.24 5.24	5.38 5.38 5.58 5.45	5.42
Dec.	25.84 4.33 6.08	55.46 5.08 6.28	4.74 80 80 80 80 80	6.50 5.95 6.68	5.48 5.45 5.84 5.90	6.18 5.90 6.00 5.58	5.40
Nov.	5.59 44.71 5.89 5.84 5.84	55.41 55.02 5.02 5.03	4.82 4.82	5.97 5.87 5.81 6.07	5.40 5.37 5.37 5.30	5.83 5.83 5.80 5.80 5.80	5.40
Oct.	5.44.33	44.24.8 64.24.4 64.44.4	44444 8869 69.529 69.69	5.80 5.71 6.12	52.28	5.76 5.76 5.64 5.64	5.36
Sept. 0	5.35	5.48 5.37 5.48 5.48	4.84 4.95 4.66 4.61 6.61	5.82 5.65 5.51 6.10	55.33	55.33	5.57
Aug. Sc	5.38 4.74 4.50 5.72 5.72	55.63 5.17 5.17 5.17 5.17	4.90	6.28 4.78 5.98 5.79 5.79	5.564	55.55.73	5.98
-	5.80 4.96 4.79 5.01 7.06 5	5.15 6.34 6.34 5.77 5.88 5.88	5.22 5.28 5.06 4.4 5.14 4.4 5.14	7.01 5.06 6.75 6.75 5.06 7.08	5.80 5.30 6.25 6.35 5.94 8.94	6.82 6.15 6.09 6.32 8.32	5.35 4
e July	55.84 5.00 5.00 5.00 5.00 5.00 5.00 5.00	4.84 6.38 6.01 7.73 6.05	255577 412585 455574	7.81 7.81 7.86 7.88 7.88	6.53 5.86 6.26 6.59 6.01	7.65 8.29 7.76 6.33	5.40 5
June	1						
May	23.82 1.4.94 8.4.98 8.36 8.36	8 4.76 8 6.47 8 6.54 8 7.66	8 5.61 5 5.74 0 5.15 0 5.40	5 6.69 6 4.97 3 7.76 5 7.82	6.54 7 5.73 9 5.78 0 6.18 6.07	7.51 0 6.99 0 6.59 5 6.45	5.39
Apr.	4.81 4.77 4.98 6.66	8 5.28 6 2.88 6 2.82 8 5.428	3 5.18 5.10 5.10 5.30	6.45 6.45 6.33 6.95	5.38 5.27 5.27 5.39 6.38	5 6.61 6.30 7 6.14 6.14	5.60
Mar. A	5.44 4.56 4.84 5.72	5.44 5.01 5.01	5.13 5.013 4.93	5.93 5.93 5.83 6.41	5.55 5.46 7.70	6.15 6.03 5.89 5.97	5.03
Feb.	5.52 4.89 4.70 6.00	5.16 5.22 5.73 5.75	5.23 4.92 5.11 5.01	6.28 5.00 5.72 6.34	5.87 5.87 5.54 5.54 6.60	6.67 5.62 5.98 6.07	5.14
Jan.	5.63 4.86 4.94 5.95	5.11 5.34 5.34 5.59	5.38 4.95 5.24	6.38 5.02 5.60 5.61 6.60	5.24 5.03 5.87 5.87	5.89 5.83 5.83 6.29	5.23
Name of Bond	West Shore RR 1st M 4s 2361 Atch Sh & Micho Su B M 35s 1997 Atch Fop & Santa Fe gan M 4s 1995 Central Pacific star of M 3/3s 1997 Central Pacific star ref M 4s 1949	Nor Pac Ry prior lieu ig M 4s 1997. Central RR of N 13 cross M 4s 1996. Central RR of N 1 groun M 5s 1987. Georgical Pages 1998. Section 1997. Southern Pac 18st ref M si 4s 1955.	A T & S Fe Ry adj M 4s stamped 1995 Worthern Pac Ky gen lien S 2047 Pennsylvanin R K cons M 4s 1948. The buil & Durney gen M 4s 1958. Un Pac RR 1st lien & ref M 4s 3008.	Canada So 1st & ref cons Ss 1962. Pennsylvanin RK cons M 44,58 1960. Pennsylvanin RK gen M 44,58 1966. Pennsylvanin RK gen M 58 1966. St Lonis SWyestern 1st M 48 1998.	Mo-Kansus-Texas Ry 1st M 4s 1990 Ches & Ohlo Ry gm M 4y-5a Cheve Cin Chi & St. Lgm M 4s 1993. Y Central Ry Concol M 4s 1993. Tex & Pac Ry 1st M 3s 2000.	Canadian Pac Ry 4% deb stock. Brit Sin Chi Si Li gen M Ss 1975. Brit R R cons prior lier 4s 1996. Chansivanian R Re sm M 4/48 1981. Chincapo & Brit et Ss 1992.	C & O (Rich & All Div) 1st 4s 1989 C C C & St L (St L Div) 1st 4s 1990
See.	988 95	22228	201180	331326	38 33	82448	50

VIELDS OF RAILROAD BONDS Jan. 1933—Jan. 1934

	162	LILLOZ	נטם טני	ND III	פעעש		
à	5.37 4.23 5.80 5.80	5.08 5.08 5.99	5.35	5.03 5.03 5.90 5.90	55.12 5.24 5.87	5.20 4.90 4.96	5.18
Jan,	24442	44040	चुं संसंस्थ	40004	400000	N44N4	Š.
· i	5.67 4.40 4.56 6.72	5.02 4.15 5.40 6.99	5.22 5.22 5.22 5.87	5.38 5.22 5.42 5.42	5.72	45.38 45.38 45.38 45.38	5.82
Dec.	24440	24240	40440	40000	40000	20004	'n
5	5.48 4.31 7.26	5.10 4.24 5.37 4.75	5.03 5.64 4.91 6.20	33555	8210821	4.07.80	8
Nov.	N4441	W4W4L	2440	5.60 5.60 7.50 5.63	5.88 5.76 5.77 6.98	5.55 5.47 85.78 4.40	5.80
	80747	28788	22024	8000 HT	41-440	44400	ci
ő	4.93 4.27 4.34 6.27	4.86 4.08 5.12 6.48	5.22 4.59 4.44 5.74	5.20 5.20 5.13 6.64 5.11	55.34 6.334 6.38	5.34 5.14 5.36 4.27	5.42
-:	33333	523333	200000	20420	0.45.85	20118	17
Sept.	4.89 4.19 4.33 6.13	4.85 4.13 5.03 4.63 6.42	5.29 4.54 4.53 5.65	5.22 5.14 6.31 5.32	5.04 5.27 5.27 5.28 6.71	5.18 5.21 5.30 4.02	5.27
	N & L & Z	24277	10 4 to 4 to	25002	55546	50000	_
Aug.	4.75 4.18 4.17 5.41	4.63 4.04 4.95 4.52 5.62	4.55 4.43 4.34 5.39	5.02 5.80 5.80 5.80	4.37 4.87 4.95 5.04 6.06	5.07 4.93 5.06 4.06	5.31
	00 to to 00	000000	- wowo w				**
July	4.88 4.27 4.23 5.28	4.62 4.13 5.05 4.55 5.50	4.61 5.05 4.45 4.50 5.38	4.30 4.94 5.08 6.15 4.65	5.06 6.04 6.04	5.20 4.81 5.14	5.44
June	5.11 4.53 4.31 4.60 5.73	4.78 4.06 5.23 4.69 6.03	4.98 4.78 4.58 5.90	5.28 5.38 6.48 4.70	5.30 5.31 5.20 5.99	5.52 4.86 5.23 5.50 4.33	5.41
May	5.42 4.53 4.50 4.80 6.45	5.13 4.23 5.65 4.88 6.58	5.31 4.88 4.85 6.36	5.64 5.64 7.06 5.28	5.39 5.39 5.48 6.40	6.05 5.17 5.60 5.64 4.57	5.50
Z							
ř.	5.73 4.76 4.68 4.98 7.46	5.25 4.45 6.04 5.17	5.09 5.32 5.32 6.54 6.54	6.20 6.20 7.72 5.69	5.00 5.88 6.70 5.61	6.86 5.81 6.09 5.72 4.78	6.07
Apr.							
Mar.	5.45 4.61 4.73 6.92	4.39 5.72 5.14 7.14	5.48 4.74 4.79 6.35	4.58 5.86 6.04 7.38 5.27	5.41 6.45 5.51 7.62	6.29 5.72 5.94 5.67	5.82
M	24440	44000	40440	40000	40001-	00004	
Feb.	5.30 4.47 4.36 4.59 6.29	4.81 4.18 5.45 6.33	5.27 4.67 4.57 6.10	5.54 5.54 5.98 5.00	4.54 5.35 6.16 7.27	5.96 5.49 5.53 5.47 4.36	5.50
표	24440	44040	40440	40000	40000	N 10 10 10 4	
<u>.</u>	5.52 4.50 5.62 5.62	5.98 5.98	5.11 4.59 4.44 6.23	4.29 5.51 5.56 6.66 5.11	5.44 6.24 5.24 6.15	5.80 5.58 5.50 5.45 4.31	5.42
Jan.	N444N	44040	40440	40000			'n
			11111	11111	11111	11111	St L (St L Div) 1st 4s 1990
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ě	. s 1 s	9 9	88: 1	4½s 1960 1½s 1965 5s 1968 4s 1989 M 4s 1990	:8%:::	75 : 1 : 8	66
m	:27%	252 152 152 152 153	25.25	56.88	8.29	2 8 3	5
0	22425	24-74	H 2 2 4 5	8 8 6 1 8	14.80.0	85 8 38 48	4
Name of Bond	\$ 23 1.8	7 × × 4	S.K. S.	4½s 1966 4½s 1965. 5s 1968 I 4s 1989 M 4s 199	20 S	M. 42.	13
ž	\$4 5 X	Sing Sing	ref lie	STREE	del del	5.4 × 5.0	3
	Mare and	E O E O	Z 28% 8	cons M 4½s 1960 gen M 4½s 1965 gen M 5s 1968 rn 1st M 4s 1989 s Ry 1st M 4s 1990	4 7 S 7 %	Dis a lieu	A
	t Sa St	# # 7 # B	re e com	SHEER	5 S S 5 4	# 5 % # F	T,
	13 data 8	EXZ TE	Se E E Ra	RRRRR	స్థానికి	E PER	Ó
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	ac & Se	55.52.2	84.82°	Son	P C L	0.8 8 %	Š
	18 G 25 2 1	Tagara Lagara	Sario	4444 g	A S S S S S S S S S S S S S S S S S S S	2248	8
	tra Const	4.5 H. S. S.	Pa Pa	E E E E	ad K	ZG B P	၁၁
	West Shore RR 1st M 4s 2361. Lake Sh & Mich So 1st M 31/s 1997. Attof Top & Santa Fe gen M 4s 1995. N Y Cent & Hudson River M 31/s 1999 Central Pacific 1st ref M 4s 1949.	Nor Pac Ry prior lien ig M 4s 1997 Norf & West Ry 1st cons M 4s 1996. Central RR of M J gen M 5s 1987 Hocking Valley 1st cons M 43/s 1999. Southern Pac 1st ref M si 4s 1955	A T & S Fe Ry adj M 4s stamped 1995 Northern Pac Ry gen lien 3s 2047 Chic Burl & Quincy gen M 4s 1958 Un Pac Rt 1st lien & ref M 4s 2008 Canada So 1st & ref cons 5s 1962	Pennsylvania RR cons M 4½ Pennsylvania RR gen M 4½ Pennsylvania RK gen M 58; R. Louis SoWestern 1st M 44 Mo-Kansas-Texas Ry 1st M	Ches & Oho Ry gen M 4½s 1992. New Cin Chi & St. Lgen M 4s 1993. N Y Central RR consol M 4s 1993. Exer Re Re R M S 2000. Candidat Re Ry 4% deb stock.	Pitts Cin Chi & St. L. gen M 5s 1975. Erie RR cons prior lien 4s 1996. Pennsylvania RR gen M 4½s 1981. C. & O (Rich & All Div) 1-t 4s 1989.	ပိ
÷	08480	80523	20128	33333	332	24489	20

VIELDS OF RAILROAD BONDS Jan. 1934—Jan. 1935

		AI	1 131(1)1	.21		
Jan.	3.57 3.67 3.65 3.85	3.55 3.93 3.93 3.90	3.77 3.77 4.38 3.56	3.81 4.04 4.06	4.25 4.64 4.30 4.05 4.17	4.37 3.78 4.35
Dec.	3.74 3.74 3.72	3.62 4.00 4.74 3.93	3.61 3.61 3.86 3.69	44.23 4.23 4.24 7.71	4.46 4.46 4.14 4.29	4.46 3.80 4.41
Nov.	3.87 3.82 3.82 4.04	3.68 4.08 4.02	3.71 3.71 3.77 77	44.33 3.99 4.34 4.81	44.44 4.30 4.30 8.39	3.85
Oct.	4.88 3.78 3.88 3.91 4.12	3.79 4.15 5.05 4.14	3.80 3.80 3.84 3.84	44.4 44.56 44.47 47.88	4.50 4.25 4.46	4.50 3.92 4.66
Sept.	5.09 3.85 3.96 4.01	3.83 4.20 5.37 4.30	3.95 3.95 3.98	4.51 4.09 4.96 4.96	4.66 4.38 4.55	3.96 4.55
Aug.	3.95 3.95 4.20	3.76 4.71 5.14 4.18	3.78 3.97 3.89 3.89	44.44 4.05 4.38 7.79	5.03 5.03 4.43 4.54	4.56 3.90 4.46
July	4.75 3.73 3.82 3.81 4.06	3.73 6.44 6.09 7.09 8.49 9.09	3.92 3.92 3.83 3.83	4.37 4.48 4.03 4.21 4.61	4 4 4 4 4 5 2 4 4 4 2 0 0 2 3 9 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	3.87 4.29
June	4.72 3.64 3.88 3.73 4.06	3.75 4.14 4.14 4.12	3.79 3.98 3.86 3.86	4.34 4.23 4.23 4.62	44.59 4.54 4.54 4.38	3.86 4.33
May	3.81 3.95 3.95 4.10	3.78 4.22 4.22 4.25	4.43 3.84 4.03 3.95	6.44.44 6.41.42 6.31.43 6.31.43	4.4.4.4.4.65 88.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.	3.92 4.37
Apr.	4.76 3.91 3.95 4.13	3.85 4.44 4.28 22.44 22.44	4.3 3.90 6.7.4 6.03 8.03	4.46 4.06 4.17 4.28 4.57	4.72 4.99 4.41 4.41 84.48	4.68 3.97 4.52
Mar.	4.80 4.01 4.20	3.91 4.29 4.29 4.26	4.4.4.4.4.4.4.4.9.5.00.4.00.4.00.4.00.4.	4.56 4.46 4.46 4.59	5.11 4.79 4.54 4.54	4.84 3.98 4.56
Feb	4.4.4.4.09 4.1.4.4.35	3.93 4.82 5.05 4.33	4.55 4.14 4.19 4.97	4.69 4.79 4.24 4.54 4.69	5.25 5.25 4.91 4.65	4.93 4.05 4.86
Jan.	5.37 4.23 4.34 4.67	5.08 5.08 5.99 4.63	4.81 4.35 5.31 4.22	5.03 5.02 4.41 5.05 5.12	5.24 5.20 4.90 4.99	5.26 4.06 5.18
Name of Bond	West Store RR 1st M 4s 2361 Lide Sile West Stories of 1st M 35,52 1997 A 10 To & Stories Stories of 1st M 35,52 1997 N Y Card & Dividen Kiver M 34 1997 No Pack Ry priori lite Ing M 4s 1997.	Norf & West Ry 1st cons M 4s 1996 Gentral RR of M 1ge M As 1977 Hocking Valley 1st cons M 445s 1979 Souther Pac 1st cons M 445s 1955. AT Res Per Ry adj M 4s stamped 1995.	Northern Rec Ry gen lien 3a 2047 Chic Ban K Quincy gen M 4a 30 1058. Canada So 1at Ker for M 4a 2003. Canada So 1at Ker for no 5a 1700 Pennsylvania RR core M 4/54 1960.	Pennsylvania R.R. gen M 4½4, 1965. Ches & Olio R.y gen M 4½4, 1986. Ches & Olio R.y gen M 4½4, 1992. Ches C n Chi R. St. L gen M 48, 1993. N Y Central RR consol M 48, 1996.	Tex & Pac. For 1st M 53 2000. Canadian Pac R 454 Adv 5400. Pitts Cin Cin & Cit Form M 78 1975. Eire M X rons prior leim 48 1090. Fermsylvania R R gen M 45,8 198.	Chicago & Brie 1st 5s 1982 C & O (Rich & All Div) 1st 4s 1989. C C C & St L (St L Div) 1st 4s 1990.
Ref.	58482	52555	222080 222080 262080	130 135 137 137	138 140 143 145 146 147	148

YIELDS OF RAILROAD BONDS fan. 1936

. 1	33.54	3.36 3.78 3.78 3.74	3.96 3.44 3.66 3.36	3.92 4.05 4.34	4.18 4.50 3.96 3.95	4.20
Jan.						
Dec.	33.61 3.65 3.65 3.65 3.65 3.65	3.42 5.06 3.84 4.10 3.82	3.50 3.73 3.73 3.40	6.4.8.4.4. 6.1.4.4.	4.24 4.00 4.00	4.23 4.36
Nov.	3.04 3.73 3.73 3.91	3.89 3.89 3.85 3.85	3.60 3.79 4.41 3.43	4.05 3.70 4.33 4.84	4.32 4.31 4.14 4.05	4.27 4.48
Oct.	3.55 3.55 3.74 3.92	3.88 3.88 3.88	3.80 3.80 3.45 3.49	4.09 4.29 3.71 4.23	4.34 4.34 4.12 4.08	4.28 3.58 4.51
Sept.	4.96 3.53 3.63 3.91	3.42 3.86 3.88 3.88	3.50 3.50 3.50 3.50	44.09 3.81 4.18 7.73	44.44 4.04 4.08 9.09	4.25 3.56 4.34
Aug. S	3.51 3.72 3.90	3 23 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	33.75	44.23 3.79 41.77	44.32 44.04 4.04 4.01	4.28
July	3.58 3.58 3.63 3.79	3.40 3.88 3.80 3.79	3.72 3.72 3.41 3.41	44.01	3.9522622	4.21
	33.67	3.40 3.81 3.81 3.83 3.83	45.52 4.35 4.35 4.35 3.35 3.35	44.05 44.23 44.23 44.23	44.26 44.28 3.99 3.99	4.27 3.55 4.26 4
June						
May	3.50 3.50 3.74 3.74	3.87 3.87 3.87 3.87	3.52 3.74 3.443 3.50	44.5.44 27.7.2.49 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.0	44.44 4.23 4.03 4.06	3.49
Apr.	3.52	3.46 4.86 3.85 3.85 3.86	3.745	44.34 3.74 5.23	4.34 4.31 4.06 4.11	4.32 4.37
Mar.	3.52 3.63 3.71 3.71	3.47 3.88 3.88 3.80	3.44 3.72 3.44 3.47	4.12 3.73 5.17	4.24 4.74 3.99 4.10	3.53
Feb.	4.72 3.50 3.62 3.59	3.48 4.60 3.86 3.82	3.46	3.73 3.73 4.00 4.01	4.17 4.23 4.01 4.10	4.24 3.55 4.26
Jan.	3.57 3.67 3.65 3.86	3.55 4.60 3.93 3.90	3.51 3.77 3.77 3.56	4.11 4.32 3.81 4.04 4.66	4.25 4.64 4.05 4.05	3.78
Name of Bond	West Shore RR 1st M 4s 250. At the She M 1st M 4 25 30. At th Top R Sanda Pegren M 4s 1995. At the Cone R Hallon M 4s 1995. Nor Pac Ry prior Hen Is M 4s 1997. Nor Pac Ry prior Hen Is M 4s 1997.	Norf & West Ry 1st cons M 4s 1996 Central Rx of N 2gen M 3s 1987. Hocking Valley 1st cons M 4ys 199 Centrer Pace 1st C M 4s 1995. A T & S Fe Ry od M 4s stamped 1995.	Northern Pac Ry gen lien 3s 2047 Chick Barl X Duror gen M. se 1958. Un Pac RK 1st lien & ret M. st 2008. Manda So 1st K ret fonts 5t 1950. Pennsylvania RK cons M. syżs 1960.	Pennsylvania RR gen M 4½s 1966. The marsylvania RR gen M 81 1968. Ches & Ollo Ry gen M 4½s 1992. Plee Che Chi Se L pen M 88 1993. N Y Central RR consol M 88 1998.	Thex & Pac Ry 1st M Ss 2000. The dandish Pac Voy & deb stoock. Pitts Cin Chi & Ye for M Ss 1975. Pitts Cin Chi & Ye for M Ss 1975. Pitts Cin Chi & Ye for M Ss 1975. Pitts Rx lons patrol lief at 1978. Pennsylvatia RX gen M 4/45 1978.	Chicago & Erie 1st, 5s 1982. C & O (Rich & All Div) 1st 4s 1989. C C C & St L (St L Div) 1st 4s 1990.
Ref. No.	58485 28487	S4888	82228 82228	37 CON	145 145 147 147	148

TABLE 4

American Railroad Bond Yields, January Index Numbers

- 1. An unadjusted chain index number based on simple geometric averages of the yields each January.
- 2. An unadjusted chain index number based on simple arithmetic averages of the yields each January.

In both the index numbers (geometric and arithmetic), the chaining is backwards and forwards from January 1925. In each case the index number for January 1925 is the average (geometric or arithmetic) of the yields in January 1925 of the bonds used from January 1924 to January 1925.

Date	(1) Geometric Index	(2) Arithmetic Index
January 1857 (1858) (1859) (1860) (1861) (1862) (1863) (1864) (1865) (1866) (1866) (1867) (1868) (1868) (1868) (1870) (1871) (1872) (1873) (1874) (1874) (1876) (1877) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1878) (1888) (1888) (1888) (1888) (1888) (1888) (1888) (1888)	1ndex 9.517 10.204 8.671 8.788 8.662 8.412 6.136 6.658 6.867 8.108 7.786 7.892 7.992 8.215 7.849 7.213 6.764 6.506 6.157 5.797 5.169 5.213 5.182 5.123	1ndex % 9,644 10,376 8,776 8,920 8,781 8,513 6,189 6,702 6,908 8,143 7,850 8,038 8,263 7,850 7,562 7,685 7,685 7,685 7,255 6,607 6,543 6,188 5,824 5,194 5,242 5,205 5,149
" 1885 " 1886 " 1887 " 1887 " 1888 " 1889	5.049 4.620 4.548 4.621 4.473 4.451	5.076 4.643 4.564 4.643 4.499 4.472

TABLE 4—(Concluded)

Date	(1) Geometric Index	(2) Arithmetic Index
January 1891 " 1892 " 1893 " 1894 " 1895 " 1896 " 1897 " 1898 " 1899 " 1900 " 1901 " 1902 " 1903 " 1905 " 1906 " 1907 " 1911 " 1912 " 1913 " 1914 " 1915 " 1916 " 1917 " 1918 " 1917 " 1918 " 1919 " 1922 " 1923 " 1924 " 1925 " 1926 " 1927 " 1928 " 1929	% 4.600 4.557 4.610 4.557 4.510 4.525 4.28S 4.28S 4.200 3.841 3.906 3.795 3.905 4.023 3.874 3.905 4.023 3.874 3.906 4.108 4.107 4.179 4.169 4.442 4.586 4.468 4.468 4.468 4.953 4.945 4.774 4.643 4.451 4.184 4.500	4. 622 4. 677 4. 631 4. 547 4. 310 4. 331 4. 222 3. 859 3. 824 3. 810 3. 818 4. 035 3. 885 4. 018 4. 035 4. 116 4. 174 4. 187 4. 276 4. 456 4. 476 5. 216 5. 077 5. 584 5. 011 4. 857 4. 949 4. 645 4. 187 4. 454 4. 187
" 1930 " 1931 " 1932 " 1933 " 1934 " 1935 " 1936	4.503 4.315 5.591 5.222 4.944 4.171 4.008	4.504 4.322 5.637 5.290 4.997 4.209 4.047

TABLE 5

American Railroad Bond Yields, Six Index Numbers of Best 5 and Worst 5 Bonds

In this table are six index numbers for the yields of American railroad bonds annually (each January). These six index numbers fall into two groups of three each; one group based on operations performed on the 'best five bonds' each year and the other group based on operations performed on the 'worst five bonds' each year.

The index number in column 1 was constructed in the following manner: Out of the total number of bonds whose yields were used in our monthly index numbers from January 1857 to January 1858 there were selected the five bonds having the lowest yields in January 1857. The average of the yields of this particular group of five bonds was then calculated for January 1857 and the average of the yields of the same five bonds calculated for January 1858. The percentage change in this average from January 1857 to January 1858 was then taken as the percentage change in the index number of column 1 from January 1857 to January 1858. For the next year the five bonds having the lowest yields in January 1858 were chosen and the same procedure repeated. Such annual percentage changes were then 'chained' to make the index in column 1.

Column 2 was constructed as follows: Out of the total number of bonds whose yields were used in our monthly index numbers for the period January 1857 to January 1858 there were selected the five bonds having the lowest yields in January 1858. The average of the yields of this particular group of five bonds was then calculated for January 1857 and the average of the yields of the same group calculated for January 1858. The percentage change in this average was then taken as the percentage change in the index number of column 2 from January 1857 to January 1858. Succeeding years were calculated in the same manner. Annual percentage changes were then 'chained' to make the index in column 2.

Column 3 was constructed by selecting from the total number of bonds used in the monthly index numbers from January 1857 to January 1858 the five bonds having the lowest yields in January 1857 and also the five bonds having the lowest yields in January 1858 without any consideration as to whether these two groups (of five bonds each) were or were not composed of the same five bonds. The percentage that the average yield of the January 1858 group of five bonds was of the average yield of the January 1857 group of five bonds was then taken as the percentage that the January 1858 index figure in column 3 was of the January 1857 index figure in the same column. Percentages were chained together as in columns 1 and 2.

The construction of columns 4, 5 and 6 can be easily understood from the preceding explanation, remembering simply that in each case the bonds chosen were those having the *highest* yields instead of the *lowest* yields. Each of the six index numbers was 'chained' backward from January 1936. The three index numbers based on the yields of the 'best five bonds' show, therefore, the same yield in January 1936 as the average of the yields of the best five bonds in January 1936. Similarly, the three index numbers based on the yields of the 'worst five bonds' show in January 1936 the same yield as the average of the yields of the worst five bonds in that month.

All averaging was geometric.

Six index numbers, three based on the 5 bonds each year having the lowest yields and three based on the 5 bonds each year having the highest yields.

		1	Best 5 Bond	S	7	Vorst 5 Bon	ds
		(1) Earlier January	(2) Later January	(3) Either January	(4) Earlier January	(5) Later January	(6) Either January
Jan.	1857	4.35	13.65	7.63	20.33	6.02	11.15
Jan.	1858	4.59	14.00	7.98	22.36	6.64	12.28
,,	1859	4.15	12.31	7.14	17.90	5.52	9.99
,,	1860	4.16	11.98	6.94	18.55	5.82	10.38
**	1861	4.12	11.78	6.86	17.87	5.72	10.11
"	1862	4.11	11.70	6.82	17.19	5.59	9.78
,,	1863	3.11	8.78	5.12	12.19	4.00	7.00
,,	1864	3.50	9.79	5.73	12.72	4.21	7.36
"	1865	3.58	9.82	5.76	12.62	4.38	7.43
37	1866	4.51	11.64	7.13	14.07	5.15	8.53
,,	1867	4.36	11.03	6.83	13.49	5.04	8.29
"	1868	4.42	11.10	6.92	13.53	5.05	8.31
"	1869	4.48	11.09	6.95	13.85	5.27	8.59
"	1870	4.57	11.18	7.05	14.05	5.41	8.80
"	1871	4.51	10.66	6.90	13.10	5.21	8.35
,,	1872	4.43	10.07	6.66	12.29	5.10	8.02
,,	1873	4.52	10.26	6.79	12.46	5.17	8.13
,,	1874	4.50	10.11	6.71	12.55	5.21	8.19
"	1875	4.26	9.16	6.22	12.13	5.03	7.91
"	1876	3.97	8.46	5.78	11.32	4.70	7.39
"	1877	3.94	7.90	5.52	10.92	4.53	7.13
"	1878	3.98	7.90	5.55	10.65	4.47	6.98
"	1879	3.82	7.51	5.30	9.89	4.19	6.50
"	1880	3.62	7:11	5.02	9.22	3.97	6.12
"	1881	3.23	6.30	4.48	8.23	3.59	5.49
"	1882	3.26	6.22	4.45	8.41	3.69	5.62
"	1883	3.34	6.24	4.53	8.06	3.59	5.40
"	1884	3.28	6.06	4.41	7.99	3.57	5.36
"	1885	3.24	5.80	4.29	7.85	3.53	5.28
23	1886	3.01	5.31	3.94	7.03	3.24	4.78
22	1887	2.99	5.27	3.92	6.82	3.17	4.65
"	1888	3.06	5.40	4.01	6.96	3.27	4.78

TABLE 5—(Concluded)

]	Best 5 Bond	s	V	Vorst 5 Bon	ls
	(1) Earlier January	(2) Later January	(3) Either January	(4) Earlier January	(5) Later January	(6) Either January
Jan. 1889	2.92	5.06	3.82	6.96	3.28	4.79
" 1890	3.00	5.05	3.87	6.68	3.14	4.59
" 1891	3.16	5.25	4.05	6.91	3.31	4.80
" 1892	3.13	5.13	3.98	6.64	3.20	4.62
" 1893	3.10	5.08	3.94	6.63	3.21	4.62
1094	3.11	5.04	3.94	6.66	3.24	4.65
" 1895	2.96	4.75	3.74	6.27	3.12	4.41
1000	2.94	4.70	3.71 3.64	6.26	3.19 3.11	4.44 4.31
1001	2.90	4.60	3.46	5.77	2.97	4.31
1000	2.79	4.32	3.40	5.51	2.84	3.93
1099	2.72	4.06 4.05	3.29	5.53	2.84	3.99
1900	2.74	4.05	3.28	5.31	2.80	3.83
1901	2.74	3.98	3.28	5.26	2.79	3.81
" 1902 " 1903	2.74	4.15	3.47	5.35	2.84	3.89
" 1903	3.07	4.35	3.64	5.51	2.95	4.00
" 1905	3.02	4.23	3.57	5.20	2.82	3.81
" 1906	3.09	4.26	3.61	5.21	2.86	3.84
" 1907	3.23	4.45	3.77	5.36	2.96	3.97
" 1908	3.40	4.69	3.97	5.69	3.32	4.35
" 1909	3.27	4.50	3.82	5.14	3.02	3.95
" 1910	3.35	4.58	3.91	5.16	3.06	3.98
" 1911	3.40	4.65	3.97	5.18	3.14	4.01
" 1912	3.42	4.66	3.99	5.18	3.15	4.03
" 1913	3.49	4.75	4.07	5.27	3.22	4.10
" 1914	3.62	4.86	4.20	5.48	3.40	4.27
1919	3.69	4.93	4.27	5.67	3.52	4.42
1910	3.62	4.80	4.18	5.49	3.48	4.30
1917	3.55	4.70	4.09	5.45	3.48	4.29
" 1918 " 1919	4.24 4.31	5.43 5.40	4.80 4.81	6.52 5.96	4.38 4.11	5.26 4.88
" 1920	4.63	5.69	5.10	6.67	4.60	5.47
" 1921	4.75	5.72	5.19	6.70	4.66	5.51
" 1922	4.32	5.10	4.66	5.90	4.25	4.95
" 1923	4.27	5.00	4.59	5.54	4.04	4.65
" 1924	4.35	5.09	4.68	5.56	4.07	4.68
" 1925	4.31	4.98	4.62	5.30	3.90	4.47
" 1926	4.25	4.85	4.53	5.11	3.79	4.34
" 1927	4.12	4.69	4.39	4.87	3.60	4.13
" 1928	3.91	4.42	4.15	4.55	3.37	3.85
" 1929	4.22	4.72	4.46	4.86	3.60	4.12
" 1930	4.22	4.68	4.45	4.90	3.66	4.16
1901	3.98	4.39	4.18	4.82	3.69	4.16
1934	4.62	5.08	4.85	6.90	5 57	6.17
1900	4.14	4.38	4.25	6.41	5.63	6.01
1934	4.07	4.26	4.15	5.78	5.44	5.56
1900	3.56	3.59	3.57	4.72	4.61	4.65
" 1936	3.42	3.42	3.42	4.51	4.51	4.51

TABLE 6

Index Numbers of the Yields of American Railroad Bonds
Based on Sigma Equations

(Quarterly January 1857—January 1879; Monthly January 1879—January 1936)

- Col. 1. The Sigma index number whose yield in January 1925 was 4.50 per cent (4.4998%).
- Col. 2. A cumulation of the logarithms of the slopes of the lines fitted by Sigma ratios $\frac{\sigma_y}{\sigma_x}$.
- Col. 3. Logarithms of the Sigma index number whose yield in January 1925 was 5.00 per cent (5.0009%).
- Col. 4. Logarithms of the Sigma index number whose yield in January 1925 was 4.50 per cent (4.4998%).
- Col. 5. A cyclical curve (see Appendix D) fitted to the logarithms of the 4.50 Sigma index (Col. 4).

The figures in column 3 are not introduced in this table because they have any great significance of their own. They are introduced primarily because, if they are used with the figures in column 4, any sigma index whatever may be quickly obtained. The relation between the figures in column 3 and those in column 4 is such that any other sigma index falls, at each date, the same proportion of the distance between the figures of column 3 and those of column 4. For example, if for each month we take a figure which is half way between the figure in column 3 and the figure in column 4, we obtain a new sigma index.

TABLE 6

Date	Sigma "4,50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 Log. "4.50"	5 Cyclical curve to Log. "4.50"
1857 J A J O	6.745 6.745 6.868 7.972	Ī .99551 .03825 .09254	1 .24366 1 .23938 1 .28966 1 .41591	.82900 .82899 .83683 .90159	
1858 J A J O	7.006 6.591 6.385 6.310	.07342 .01258 .02982 1.96854	1.33762 1.24678 1.25134 1.18749	.84545 .81894 .80514 .80001	
1859 J A J O	6.258 6.183 6.409 6.278	Ī.95204 Ī.96828 Ī.98462 Ī.98401	1.16947 1.17843 1.20891 1.19931	.79644 .79119 .80682 .79779	
1860 J A J O	6.139 6.137 5.923 5.898	$\begin{array}{c} .03437 \\ \overline{1} .97054 \\ \overline{1} .94691 \\ \overline{1} .97022 \end{array}$	1.23898 1.17722 1.14115 1.15972	.78809 .78795 .77250 .77074	
1861 J A J O	6.135 6.104 6.148 6.346	.00118 Ī.98600 .00429 Ī.99099	1 .20556 1 .18896 1 .20947 1 .21056	.78784 .78560 .78875 .80252	
1862 J A J O	6.099 5.962 5.627 5.089	1.94065 1.89995 1.85798 1.86484	1.14865 1.10627 1.05067 1.01177	.78528 .77539 .75027 .70660	
1863 J A J O	4.609 4.772 4.825 4.942	1.85633 1.82670 1.83981 1.75906	.96286 .95819 .97159 .93309	.66361 .67867 .68352 .69390	
1864 J A J O	5.222 4.774 4.065 4.947	$\begin{array}{c} \overline{1}.74356 \\ \overline{1}.76412 \\ \overline{1}.92929 \\ \overline{1}.82602 \end{array}$.94862 .92086 .96304 .97341	.71781 .67885 .60905 .69433	
1865 J A J O	5.402 5.985 6.045 6.344	1.73380 1.70119 1.72200 1.63154	.95827 .98642 1.00103 .98072	.73259 .77706 .78139 .80238	

TABLE 6 (Continued)

Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 Log. "4.50"	5 Cyclical curve to Log. "4.50"
1866 J A J O	6.649 6.548 6.370 6.164	Ī.57803 Ī.65817 Ī.61284 Ī.65649	.98041 1.00575 .97498 .97876	.82274 .81613 .80416 .78987	
1867 J A J O	6.342 6.344 6.204 6.283	1.60403 1.64366 1.66270 1.65879	.96962 .98577 .98429 .98809	.80222 .80238 .79268 .79819	
1868 J A J O	6,359 6,243 6,245 6,281	1.61149 1.64012 1.59944 1.65740	.97366 .97731 .96117 .98735	.80336 .79541 .79553 .79806	
1869 J A J O	6.382 6.542 6.460 6.556	$\begin{array}{c} \overline{1}.67317 \\ \underline{1}.62815 \\ \underline{1}.65201 \\ \overline{1}.67570 \end{array}$	1.00127 .99264 .99720 1.01410	.80499 .81569 .81025 .81667	
1870 J A J O	6.519 6.395 6.377 6.374	1.69528 1.62365 1.55900 1.62055	1.02068 .98097 .95549 .97831	.81415 .80584 .80458 .80443	
1871 J A J O	6.383 6.439 6.398 6.280	Ī.60991 Ī.52420 Ī.50781 Ī.62558	.97470 .94808 .94017 .97384	.80502 .80879 .80604 .79793	-
1872 J A J O	6.159 6.295 6.028 6.214	1.58512 1.51999 1.61239 1.60527	.94976 .93694 .95090 .96122	.78950 .79899 .78025 .79335	-
1873 J A J O	6.249 6.222 6.152 6.391	1.57862 1.60949 1.59581 1.70236	.95367 .96338 .95330 1.01553	.79579 .79387 .78904 .80560	
1874 J A J O	6.180 5.984 5.845 5.716	1.62845 1.67444 1.74453 1.76504	.96808 .97388 .99809 .99963	.79100 .77703 .76676 .75710	

TABLE 6 (Continued)

Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 Log. "4.50"	5 Cyclical curve to Log. "4.50"
1875 J A J O	5.627 5.414 5.414 5.363	1.73536 1.77829 1.75095 1.76477	.97679 .98355 .96831 .97179	.75029 .73351 .73353 .72942	
1876 J A J O	5.247 5.252 5.094 5.254	Ī.74612 Ī.70881 Ī.75308 Ī.69445	.95209 .93339 .94302 .92666	.71991 .72032 .70708 .72051	
1877 J A J O	5.050 5.349 5.153 5.204	$\begin{array}{c} \overline{1}.77163 \\ \overline{1}.67745 \\ \overline{1}.69357 \\ \overline{1}.70061 \end{array}$.94950 .92654 .91785 .92534	.70327 .72831 .71212 .71626	
1878 J A J O	5.107 5.174 5.037 5.025	$ \begin{array}{r} \overline{1}.71931 \\ \overline{1}.67905 \\ \overline{1}.69691 \\ \overline{1}.70359 \end{array} $.92653 .91273 .90955 .91161	.70824 .71377 .70224 .70108	
1879 J F M A M J A S O N D	4.933 4.883 4.947 4.947 4.805 4.731 4.670 4.670 4.791 4.757 4.717 4.710	1.66360 1.60920 1.61950 1.61940 1.63732 1.65443 1.66544 1.65790 1.63375 1.63375 1.66571 1.643739	.88507 .85810 .86785 .86774 .86242 .86293 .86200 .85947 .86217 .86495 .80658	.69307 .68870 .69438 .69431 .68169 .67493 .66929 .66997 .68043 .67727	.6958 .6925 .6893 .6861 .6832 .6807 .6785 .6767 .6753 .6741
J F M A M J J A S O N D	4.673 4.635 4.632 4.657 4.652 4.551 4.419 4.391 4.387 4.349 4.255 4.183	I. 64438 I. 63266 I. 63263 I. 61728 I. 61728 I. 65277 I. 68509 I. 67441 I. 66940 I. 65940 I. 65940 I. 65941	.85331 .84489 .84361 .84157 .84019 .84542 .84701 .83945 .83305 .82856 .81749 .81153	.66962 .66609 .66481 .66809 .66761 .65815 .64526 .64261 .64219 .63841 .62291	.6717 .6702 .6682 .6658 .6628 .6594 .6555 .6513 .6468 .6421 .6373 .6327 .6283

TABLE 6 (Continued)

	1	2 7	3	4	5
Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	Log. "5.00"	Log. "4.50"	Cyclical curve to Log. "4.50"
1881 J F M A M J J A S O N D	4.160 4.258 4.276 4.224 4.067 4.019 3.988 4.019 4.138 4.170 4.109 4.119	Ī.64866 Ī.61812 Ī.63296 Ī.653292 Ī.67334 Ī.66942 Ī.68851 Ī.68898 Ī.66867 Ī.668826 Ī.69474	.80465 .80214 .80994 .81314 .80789 .79866 .80319 .80671 .80844 .81435 .81693 .82102	.61914 .62923 .63101 .62567 .60926 .60407 .60078 .60408 .61679 .62009 .61371 .61474	.6242 .6208 .6179 .6156 .6140 .6129 .6122 .6119 .6117 .6118
1882 J F M A M J J A S O N D	4.107 4.098 4.147 4.130 4.114 4.148 4.096 4.132 4.184 4.157 4.206 4.265	Ī.69759 Ī.71308 Ī.69910 Ī.68515 Ī.68564 Ī.68163 Ī.67788 Ī.667788 Ī.66712 Ī.665174 Ī.61689	.82116 .82777 .82606 .81770 .81395 .81004 .81250 .81462 .81175 .81238 .81069 .80236	.61352 .61259 .61770 .61592 .61426 .61782 .61240 .61620 .62164 .61881 .62385 .62993	.6132 .6139 .6146 .6155 .6163 .6170 .6178 .6198 .6211 .6227 .6246
1883 J F M A M J J A S O N D	4.233 4.219 4.261 4.283 4.278 4.278 4.285 4.334 4.364 4.329 4.322 4.263	Ī.61496 Ī.63868 Ī.62286 Ī.59982 Ī.59961 Ī.58999 Ī.58078 Ī.56289 Ī.57913 Ī.56372 Ī.58614	.79824 .80655 .80434 .79744 .79690 .79616 .79412 .79559 .79220 .79444 .78824 .79033	.62658 .62525 .62952 .63166 .63120 .63126 .63205 .63692 .63993 .63637 .63568 .62969	.6266 .6287 .6306 .6321 .6337 .6336 .6331 .6322 .6312 .6301 .6290
1884 J F M A J J A S O N D	4 .154 4 .184 4 .184 4 .173 4 .217 4 .250 4 .242 4 .237 4 .234 4 .209 4 .200 4 .196	Ī.63299 Ī.58949 Ī.56771 Ī.55843 Ī.57972 Ī.62031 Ī.63026 Ī.59541 Ī.60159 Ī.61289 Ī.61894 Ī.60126	.79741 .78348 .77554 .77108 .78327 .80214 .80545 .79114 .79316 .79501 .79674 .78915	.61847 .62159 .62157 .62037 .62498 .62835 .62764 .62670 .62417 .62350 .62282	.6282 .6275 .6271 .6267 .6265 .6261 .6255 .6245 .6231 .6210 .6182 .6148

TABLE 6 (Continued)

	1	2	3	4	5
Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	Log. "5.00"	Log. "4.50"	Cyclical curve to Log. "4.50"
1885 J F M A M J A S O N D	4.059 4.007 3.957 3.938 3.889 3.847 3.826 3.817 3.807 3.798 3.800 3.776	Ī.65353 Ī.66278 Ī.67408 Ī.69234 Ī.68920 Ī.68513 Ī.68497 Ī.68329 Ī.66792 Ī.65193 Ī.65363	.79603 .79442 .79232 .79199 .79494 .78880 .78445 .78338 .78150 .77351 .76664 .76465	.60842 .60277 .59733 .59529 .58980 .58513 .58268 .58169 .58058 .57958 .57973	.6108 .6064 .6018 .5972 .5928 .5888 .5852 .5821 .5795 .5773 .5755
1886 J F M A M J A S O N D	3.757 3.706 3.706 3.727 3.719 3.717 3.658 3.657 3.745 3.745 3.763 3.789	T.62669 T.61610 T.60719 T.59990 T.60328 T.58310 T.60452 T.61315 T.59044 T.58972 T.57745 T.57629	.75112 .74106 .73756 .73718 .73749 .72974 .73087 .73405 .73568 .73568 .73568 .73560	.57475 .56894 .56894 .57136 .57038 .57022 .56328 .56310 .57344 .57367 .57550 .57856	.5726 .5715 .5707 .5700 .5696 .5694 .5694 .5696 .5701 .5708 .5718
1887 F M A M J J A S O N D	3.746 3.746 3.762 3.794 3.787 3.787 3.782 3.805 3.902 3.920 3.868 3.801	Ī.59105 Ī.59722 Ī.59703 Ī.59738 Ī.57507 Ī.57204 Ī.60871 Ī.60193 Ī.58631 Ī.59226 Ī.60262 Ī.60262	.73605 .73832 .74018 .73725 .73492 .73496 .74459 .74700 .75195 .75617 .75431	.57358 .57353 .57546 .57909 .57832 .57945 .57537 .58041 .59124 .59325 .58746 .57994	.5743 .5757 .5778 .5788 .5802 .5815 .5826 .5834 .5838 .5839 .5836 .5836
1888 J F M A M J A S O N D	3.795 3.758 3.781 3.782 3.752 3.683 3.617 3.616 3.595 3.578 3.578 3.572	T. 60210 1. 61030 1. 60789 1. 60789 1. 61754 1. 64733 1. 66105 1. 65876 1. 65878 1. 70148 1. 69716 1. 68385	.74581 .74483 .74649 .74713 .74690 .75111 .74923 .74809 .75871 .76324 .76034	.57915 .57500 .57760 .57767 .57422 .56616 .55835 .55821 .55567 .55373 .55290 .55459	.5815 .5797 .5774 .5746 .5715 .5679 .5641 .5601 .5561 .5523 .5487

TABLE 6 (Continued)

	(Continued)					
Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 Log. "4.50"	Cyclical curve to Log. "4.50"	
1889 J F M A M J J A S O N D	3.513 3.458 3.402 3.455 3.428 3.424 3.483 3.522 3.547 3.570 3.568 3.595	Ī. 70187 Ī. 70963 Ī. 74482 Ī. 71246 Ī. 70490 Ī. 68524 Ī. 66071 Ī. 64154 Ī. 62818 Ī. 63863 Ī. 66887 Ī. 64986	.75537 .75234 .76317 .75331 .74616 .73630 .73273 .72933 .72980 .73399 .74236 .74173	.54567 .53856 .53168 .53843 .53500 .53448 .54199 .54683 .54983 .55270 .55243	.5431 .5412 .5400 .5395 .5398 .5406 .5420 .5438 .5459 .5483 .5507 .5532	
1890 J F M A J J S O N D	3.617 3.600 3.613 3.628 3.617 3.654 3.673 3.688 3.699 3.739 3.743 3.781	1.62620 1.63784 1.63784 1.63993 1.63135 1.62312 1.61835 1.62853 1.62853 1.62414 1.64964 1.65331	.73458 .73721 .73973 .73973 .73973 .73921 .73776 .73803 .74391 .74770 .74803 .75911 .76513	.55841 .55626 .55791 .55966 .55830 .66284 .66502 .56880 .56813 .57270 .57317	.5555 .5577 .5596 .5612 .5626 .5638 .5651 .5664 .5679 .5696 .5715	
1891 F M A M J A S O N D	3.742 3.763 3.763 3.819 3.874 3.874 3.891 3.872 3.884 3.872 3.884 3.872	1.62430 1.61382 1.63806 1.62305 1.62902 1.62666 1.62258 1.61183 1.57977 1.56983 1.55010	.74848 .74598 .75650 .75472 .75920 .76432 .76290 .76091 .75828 .74763 .74261 .73461	.57309 .57477 .57546 .57955 .58189 .58798 .58821 .59007 .58786 .58933 .58789 .58677	.5759 .5782 .5804 .5824 .5841 .5855 .5868 .5867 .5861 .5861	
1892 J F M A M J J A S O N D	3.776 3.761 3.775 3.764 3.758 3.728 3.713 3.715 3.737 3.739 3.765 3.768	Ī.57998 1.57254 1.56709 1.56308 1.55281 1.56369 1.56626 1.56968 1.58000 1.57707 1.56447 1.57303	.73536 .73102 .73063 .72797 .72364 .72403 .72319 .72461 .73087 .73015 .72862 .73198	.57698 .57534 .57589 .57565 .57488 .57149 .56975 .56995 .57250 .57284 .57581	.5818 .5799 .5779 .5760 .5744 .5729 .5718 .5710 .5707 .5708 .5713	

TABLE 6 (Continued)

-	Tribbb o (Continued)						
Date	1 Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 Log. "4.50"	Cyclical curve to Log. "4.50"		
1893 J F M A M J J A S O N D	3.749 3.740 3.743 3.749 3.785 3.830 3.865 3.857 3.865 3.826 3.798	Ī.57182 Ī.55794 Ī.558159 Ī.60543 Ī.66581 Ī.66581 Ī.693460 Ī.63559 Ī.60024 Ī.57113 Ī.55056	.72931 .72338 .73083 .73185 .74181 .75207 .77621 .79330 .76625 .75307 .73785 .72757	.57390 .57285 .57318 .57289 .57389 .57813 .58325 .58710 .58625 .58714 .58268 .57957	.5734 .5749 .5766 .5782 .5797 .5809 .5818 .5821 .5819 .5819 .5797		
1894 J F M A M J A S O N D	3.730 3.706 3.698 3.627 3.612 3.621 3.616 3.591 3.571 3.554 3.512 3.507	Ī.59308 Ī.57958 Ī.56142 Ī.58179 Ī.59561 Ī.59290 Ī.60546 Ī.60820 Ī.60479 Ī.59405 Ī.60443 Ī.60775	.73487 .72709 .71970 .71861 .72188 .72192 .72614 .72415 .72048 .71431 .71376	.57165 .56887 .56796 .55959 .55771 .55878 .55821 .55516 .55281 .55074 .54559 .54494	.5750 .5719 .5684 .5649 .5615 .5584 .5559 .5538 .5522 .5510 .55492		
1895 J F M A M J A S O N D	3.520 3.553 3.561 3.566 3.512 3.476 3.477 3.411 3.427 3.450 3.470 3.430	Ī.60316 Ī.60430 Ī.60715 Ī.60715 Ī.60744 Ī.61337 Ī.58287 Ī.58287 Ī.59314 Ī.58402 Ī.58037 Ī.64060	.71359 .71808 .72018 .72018 .72092 .71651 .70724 .70066 .69854 .69810 .69763 .69885 .71738	.54654 .55059 .55159 .55222 .54549 .54113 .54124 .53290 .53486 .53778 .54035 .53530	.5483 .5472 .5461 .5448 .5421 .5408 .5395 .5385 .5378 .5378		
1896 J F M A J J A S O N D	3.478 3.458 3.489 3.501 3.487 3.451 3.484 3.585 3.578 3.543 3.512 3.487	I. 64093 I. 62969 I. 61288 I. 60270 I. 60036 I. 61812 I. 64607 I. 68164 I. 65041 I. 65041 I. 65041 I. 65037	.72354 .71641 .71352 .71108 .70847 .71081 .72650 .75462 .73986 .73567 .71790 .71041	.54132 .53885 .54270 .54422 .54250 .53791 .54211 .55449 .55372 .54942 .54555 .54251	.5386 .5399 .5416 .5450 .5450 .5464 .5471 .5472 .5465 .5451 .5430 .5402		

TABLE 6 (Continued)

	TABLE 6 (Continued)						
Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 Log. "4.50"	Cyclical curve to Log. "4.50"		
1897 J F M A M J A S O N D	3.429 3.392 3.367 3.343 3.380 3.289 3.264 3.298 3.265 3.285 3.285 3.293 3.249	Ī.61534 Ī.62527 Ī.62493 Ī.63263 Ī.63302 Ī.64127 Ī.63763 Ī.62598 Ī.65877 Ī.64162 Ī.62560 Ī.62660	.70704 .70620 .70292 .70292 .70296 .70132 .69937 .69459 .70161 .69908 .69348 .68809	.53525 .53043 .52729 .52418 .52239 .51701 .51375 .51834 .51392 .51657 .51758	.5378 .5341 .5303 .5264 .5229 .5189 .5165 .5149 .5142 .5146 .5152 .5164		
1898 J F M A M J A S O N D	3 .253 3 .260 3 .314 3 .378 3 .402 3 .353 3 .265 3 .285 3 .310 3 .285 3 .319	I.61051 1.60802 I.62285 I.63236 I.59100 I.58966 I.62409 I.58359 I.58201 I.58201 I.58560 I.60005	.68222 .68214 .69513 .70724 .69412 .68737 .68918 .67904 .67952 .67574 .67406 .67073	.51232 .51322 .52034 .52858 .53169 .52544 .51389 .51661 .51983 .51664 .50990 .50488	.5179 .5195 .5208 .5217 .5220 .5217 .5205 .5186 .5160 .5129 .5094 .5059		
1899 J F M A M J A S O N D	3.150 3.158 3.150 3.113 3.095 3.095 3.110 3.128 3.148 3.176 3.196 3.177	T. 60510 1. 60261 T. 60273 T. 61296 T. 600553 T. 59959 T. 60014 T. 60008 T. 60804 T. 608657 T. 64488	.66613 .66621 .66785 .66402 .65866 .65634 .65864 .66112 .66666 .67086 .67294	.49834 .49938 .49826 .49316 .49070 .49067 .49275 .49526 .49803 .50193 .50195	.5026 .4996 .4973 .4957 .4948 .4945 .4947 .4953 .4961 .4971 .4980 .4990		
1900 J F M A M J J A S O N D	3.174 3.156 3.143 3.141 3.148 3.154 3.154 3.172 3.179 3.200 3.189 3.170	T. 62550 1. 61825 1. 62001 1. 60938 1. 602285 1. 62615 1. 61708 1. 61082 1. 60683 1. 59044 1. 58193 1. 57612	.67748 .67215 .67099 .66655 .67291 .67503 .67283 .67146 .67077 .66746 .66283 .65797	.50162 .49920 .49734 .49709 .49812 .49890 .50034 .50145 .50231 .50524 .50375 .50101	.4997 .5004 .5008 .5010 .5010 .5008 .5006 .5004 .5003 .5003 .5004 .5007		

TABLE 6 (Continued)

	1	2	3	4	5 Cyclical
Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	Log. "5.00"	Log. "4.50"	curve to Log. "4.50"
1901 J F M A M J J A S O N D	3.166 3.143 3.149 3.158 3.179 3.200 3.202 3.196 3.206 3.190 3.189	T.56987 T.57452 T.56808 T.56639 T.56645 T.55744 T.55236 T.56066 T.56906 T.56763 T.55763	.65526 .65383 .65232 .65254 .65577 .65269 .65375 .65683 .65900 .65644 .65206	.50054 .49745 .49824 .49941 .50226 .50234 .50515 .50536 .50457 .50602 .50381 .50369	.5011 .5015 .5018 .5021 .5023 .5024 .5025 .5025 .5026 .5027 .5029
1902 J F M A M J J A S O N D	3.185 3.168 3.179 3.179 3.208 3.243 3.270 3.292 3.306 3.327 3.344 3.347	I.54536 I.55282 I.54216 I.53686 I.52136 I.50027 I.48748 I.47834 I.47601 I.48492 I.47480 I.49045	.64936 .64959 .64742 .64565 .64455 .64274 .64254 .64274 .6497 .64923 .64557 .65553	.50314 .50082 .50227 .50226 .50619 .51093 .51455 .51742 .51932 .52201 .52467	.5037 .5043 .5052 .5063 .5077 .5095 .5116 .5141 .5169 .5200 .5234 .5268
1903 J F M A M J J A S O N D	3.363 3.388 3.434 3.487 3.455 3.463 3.551 3.622 3.595 3.531 3.493 3.508	I.46779 I.45454 I.44582 I.42346 I.43963 I.45831 I.41181 I.37617 I.40814 I.43449 I.44386 I.43446	.64896 .64863 .65272 .65284 .65303 .65917 .65779 .65803 .66228 .66112 .65892 .65835	.52665 .53000 .53578 .54240 .53840 .53950 .55027 .55899 .55567 .54792 .54317 .54507	.5303 .5335 .5366 .5394 .5419 .5441 .5459 .5474 .5486 .5494 .5499
1904 J F M A M J A S O N D	3.510 3.519 3.560 3.551 3.557 3.533 3.503 3.482 3.483 3.491 3.491 3.476	T. 42173 T. 42087 T. 38975 T. 37483 T. 35281 T. 35401 T. 36201 T. 36442 T. 34741 T. 33523 T. 34079	.65527 .65622 .65358 .64899 .64494 .64231 .63778 .63767 .63841 .63555 .63310	.54527 .54643 .55139 .55037 .55108 .54819 .54438 .54181 .54201 .54286 .54297 .54107	.5498 .5492 .5485 .5476 .5468 .5459 .5450 .5441 .5431 .5422 .5411 .5402

TABLE 6 (Continued)

	1 1	2	3	4	5
Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	Log. "5.00"	Log. "4.50"	Cyclical curve to Log. "4.50"
1905 J F M A M J J A S O N D	3.438 3.443 3.452 3.455 3.461 3.455 3.445 3.451 3.457 3.466 3.491 3.491	Ī.35499 Ī.33941 Ī.34158 Ī.34481 Ī.35166 Ī.34474 Ī.34124 Ī.33465 Ī.32579 Ī.32500	.63067 .62790 .62960 .63064 .63133 .63136 .62934 .62938 .62873 .02797 .63055 .63294	.53634 .53690 .53814 .53853 .53919 .53770 .53722 .53779 .53879 .54292 .54286	.5393 .5385 .5378 .5374 .5374 .5374 .5374 .5378 .5384 .5393 .5404 .5417
1906 J F M A M J A S O N D	3, 485 3, 516 3, 558 3, 553 3, 576 3, 569 3, 583 3, 623 3, 663 3, 651 3, 637 3, 655	1.32985 1.31489 1.30139 1.32718 1.31744 1.31375 1.31247 1.28769 1.27180 1.27450 1.27450 1.27896	.63118 .63207 .63361 .63911 .63994 .63831 .63978 .63988 .64173 .64073 .64083	.54210 .54606 .55124 .55064 .55343 .55254 .55420 .55910 .50385 .56237 .56071 .56291	.5446 .5464 .5483 .5503 .5523 .5543 .5561 .5578 .5694 .5602 .5637
1907 J F M A M J J A S O N D	3.651 3.679 3.741 3.716 3.712 3.726 3.726 3.755 3.761 3.823 3.823 3.828	Ī.29639 Ī.28744 Ī.28814 Ī.31615 Ī.34247 Ī.37452 Ī.37989 Ī.39052 Ī.42887 Ī.43157 Ī.48795 Ī.46519	.64482 .64647 .655390 .65639 .66124 .66992 .67026 .67700 .68659 .69487 .71858 .70459	.56240 .56573 .57803 .57014 .56960 .57125 .57037 .57463 .57529 .58235 .59047 .58302	.5652 .5669 .5686 .5703 .5718 .5734 .5747 .5747 .5765 .5770 .5769
1908 J F M A M J J A S O N D	3.739 3.680 3.718 3.709 3.726 3.713 3.692 3.715 3.698 3.698 3.678 3.672	Ī.42687 Ī.46653 Ī.45852 Ī.44271 Ī.39654 Ī.40395 Ī.40397 Ī.34457 Ī.32798 Ī.32033 Ī.30297 Ī.28964	.68413 .68772 .69005 .68473 .67509 .67533 .67272 .66196 .65669 .65480 .64924 .64606	.57283 .56577 .57033 .56929 .57129 .56974 .56735 .56987 .56805 .56771 .56556 .56491	.5758 .5749 .5737 .5723 .5709 .5695 .5683 .5672 .5664 .5658 .5655

TABLE 6 (Continued)

	o (continued)					
	1 1	2_	3	4	5	
Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	Log. "5.00"	Log. "4.50"	Cyclical curve to Log. "4.50"	
1909						
J	3.672	<u>1</u> .26265	.64119	.56493	.5654	
F	3.672	1.23288	.63611	.56490	.5656	
M	3.681	1.23431	.63739	.56595	. 5659	
M	3.668 3.678	1.25493 1.23567	.63927 .63730	.56436 .56563	.5663	
Ĵ	3.702	1.22535	.63837	.56839	.5669	
Ĵ	3.695	$\bar{1}.22764$.63794	.56759	.5686	
A M J J A S O N D	3.722	1.20460	.63754	.57082	.5698	
S	3.754 3.736	I.18528	.63834	.57452	.5711	
N	3.738	1.22791 1.24172	.64280 .64524	.57240	.5724	
ä	3.753	1.22653	.64461	.57257 .57443	.5738	
	0.100	1.22000	.01101	.07440	.5752	
1910	9 701	7 01770	04404			
J F	3.761 3.773	$\frac{1}{1}.21753$ $\frac{1}{1}.20742$.64401 .64387	.57528 .57672	.5765	
M	3.801	1.19514	.64516	.57989	.5776 .5786	
A	3.812	1.19514 1.23232	.65217	.58106	.5794	
\mathbf{M}	3.797	1.26822	.65664	.57940	.5800	
J	3.809 3.827	1.27206	.65871	.58078	.5806	
A	3.827	$\frac{1}{1}.27304$ $\frac{1}{1}.26511$.66097 .65960	.58287 .58291	.5811	
ŝ	3.818	1.22396	.65153	.58177	. 5816 . 5820	
0	3.796	$\bar{1}.22178$.64874	.57933	.5824	
A M J A S O N D	3.819	<u>1</u> .22534	.65201	. 58203	.5829	
	3.818	1.22516	.65172	.58177	.5833	
1911		_				
J F	3.824	1.20565	.64938	.58250	.5838	
M	3.844 3.857	1.18183 1.18248	.64807	.58476	.5842	
	3.843	T 19405	.64959 .64978	.58619 .58467	.5846 .5850	
M	3.841	1.19405 1.18137	.64772	.58448	.5852	
ĵ	3.851	1.17787	.64838	.58565	.5854	
- 1	3.858 3.868	1.17496	.64872	.58641	. 5854	
s l	3.862	1.17817 1.20659	.65030 .65380	.58752	.5854	
A M J A S O N D	3.849	1.21454	.65352	.58677 .58525	.5853 .5852	
N	3.833	1.21059	.65111	.58347	.5851	
	3.839	1.21066	.65182	.58417	.5851	
1912		_				
J F	3.838	1.20217	.65044	.58410	.5851	
M	3.841 3.857	1.18775	.64862	.58444	.5852	
	3.857	$\frac{1}{1}.18733$ $\frac{1}{1}.19718$.65034 .65192	.58623	.5855	
M	3.850	1.21290	.65354	.58633 .58553	.5858 .5863	
A M J A S O N	3.865	1.21078	.65488	.58720	.5870	
J	3.875	1.20957	.65577	.58828	.5878	
A S	3.908 3.918	$ar{1}.19431 \\ ar{1}.20733$.65719	.59204	.5889	
ŏΙ	3.917	1.20733 1.20587	.66025	.59312	.5902	
N	3.916	1.20704 1.20654	.65987	.59278	.5917 .5934	
	3.929					

TABLE 6 (Continued)

	TIDDD & (Continued)						
Date	1 Sigma "4.50" in Jan, 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 Log. "4.50"	5 Cyclical curve to Log. "4.50"		
1913 J F M A M J A S O N D	3.914 3.921 3.975 4.041 4.083 4.077 4.092 4.063 4.027 4.064 4.130 4.149	Ī.20959 Ī.21995 Ī.23115 Ī.20603 Ī.21215 Ī.26758 Ī.23889 Ī.23889 Ī.23816 Ī.21986 Ī.21017	.66010 .66252 .67026 .67348 .67349 .68746 .68608 .68103 .67702 .68037 .68496 .68548	.59261 .59340 .59934 .60655 .61103 .61033 .61186 .60883 .60496 .60895 .61585 .61790	.5973 .5995 .6017 .6039 .6060 .6078 .6092 .6107 .6107 .6107 .6103		
1914 J F M A M J A S O N D	4.075 4.035 4.043 4.027 4.013 4.013 4.061	$\begin{array}{c} \overline{1}.20759\\ \overline{1}.18055\\ \overline{1}.19548\\ \overline{1}.21383\\ \overline{1}.23229\\ \overline{1}.21810\\ \overline{1}.21308\\ \end{array}$.67732 .66897 .67200 .67318 .67458 .67238 .67665	.61014 .60584 .60666 .60502 .60347 .60355 .60862	.6091 .6086 .6083 .6082 .6085 .6090 .60111 .6126		
	* * 4.212	Ī.26312	.70080	.62446	.6143 .6161 .6180		
1915 J F M A M J A S O N D 1916	4 .155 4 .152 4 .168 4 .134 4 .148 4 .178 4 .232 4 .250 4 .249 4 .179 4 .091 4 .069	1.26387 1.26270 1.27835 1.27126 1.26853 1.27041 1.28088 1.29273 1.30734 1.28736 1.24865 1.25808	.69509 .69456 .69894 .69420 .69506 .69569 .70603 .71017 .71279 .70180 .68562 .68494	.61861 .61829 .61987 .61641 .61775 .62105 .62649 .62843 .62826 .62107 .61177	.6198 .6213 .6224 .6229 .6229 .6223 .6214 .6202 .6189 .6177 .6164 .6152		
J F M A M J A S O N D	4.048 4.050 4.063 4.071 4.071 4.076 4.077 4.039 4.011 3.997	I.26399 I.24936 I.25195 I.26014 I.26515 I.27807 I.29502 I.30182 I.29103 I.27487 I.26793 I.28618	.68374 .68151 .68322 .68556 .68707 .68868 .69134 .69169 .68478 .68051	.60724 .60754 .60881 .60973 .61036 .60966 .60918 .61028 .60634 .60332 .60172	.6140 .6127 .6112 .6097 .6082 .6067 .6053 .6042 .6034 .6031 .6033 .6041		

*Stock Exchange closed.

TABLE 6 (Continued)

			(Continued)		
Date	1 Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	Log. "4.50"	Cyclical curve to Log. "4.50"
1917 J F M A M J J A S O N D	3.939 4.008 4.039 4.103 4.227 4.264 4.316 4.351 4.416 4.474 4.582 4.624	Ī.28312 Ī.28093 Ī.29113 Ī.32028 Ī.31435 Ī.31386 Ī.31092 Ī.33063 Ī.32072 Ī.33741 Ī.36621	.67536 .68248 .68770 .70023 .71188 .71738 .72089 .72387 .73417 .73788 .75172 .76177	.59542 .60294 .60627 .61315 .62598 .62985 .63509 .63865 .64498 .65071 .66113	.6057 .6081 .6114 .6156 .6205 .6261 .6322 .6385 .6448 .6509 .6566 .6615
1918 J F M A J J A S O N D	4.577 4.596 4.669 4.718 4.676 4.745 4.730 4.779 4.811 4.733 4.484 4.555	Ī.37692 Ī.32606 Ī.31930 Ī.32530 Ī.30730 Ī.30730 Ī.34939 Ī.31316 Ī.32888 Ī.29706 Ī.26379 Ī.26379	.75981 .75069 .75604 .76187 .75440 .75825 .76798 .76492 .77102 .75770 .72819 .72659	.66059 .66244 .66915 .67377 .66988 .67617 .67486 .67925 .68219 .67515 .65172	.6656 .6688 .6711 .6724 .6730 .6731 .6727 .6720 .6714 .6707 .6702 .6699
1919 F M A M J A S O N D	4.656 4.683 4.688 4.750 4.740 4.754 4.835 4.865 4.785 4.874 4.894	Ī.20078 Ī.22016 Ī.25401 Ī.25401 Ī.21804 Ī.20293 Ī.23438 Ī.33104 Ī.33530 Ī.29828 Ī.32605 Ī.35332	.73414 .73968 .74852 .75149 .74459 .74352 .75126 .77363 .77724 .76265 .77618 .78370	.66800 .67053 .67097 .67672 .67577 .67706 .67980 .68436 .68709 .67986 .68793 .68973	.6698 .6699 .6703 .6711 .6724 .6743 .6768 .6800 .6836 .6877 .6918
1920 F M A J J A S O N D	4.900 5.025 5.030 5.149 5.308 5.315 5.257 5.116 5.049 4.939 4.939 5.130	Ī.33551 Ī.36562 Ī.36159 Ī.40705 Ī.43869 Ī.41046 Ī.42581 Ī.41463 Ī.34026 Ū.30480 Ī.30480 Ī.33348 Ī.34100	.78042 .79780 .79741 .81804 .83933 .83265 .83178 .81713 .79442 .77763 .78619 .80139	.69023 .70113 .70164 .71170 .72495 .72547 .70891 .70324 .69360 .69846 .71005	.6997 .7030 .7058 .7079 .7092 .7097 .7098 .7095 .7088 .7081 .7075 .7071

TABLE 6 (Continued)

TABLE 0 (Continued)							
Date	1 Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 Log. "4.50"	Cyclical curve to Log. "4.50"		
1921 J F M A M J A S O N D	4.959 4.998 5.058 5.087 5.138 5.213 5.028 4.998 4.992 4.749 4.588	Ī.33680 Ī.32362 Ī.32046 Ī.32023 Ī.20515 Ī.33226 Ī.32334 Ī.30269 Ī.26502 Ī.24958 Ī.27731 Ī.29542	.78590 .78657 .79114 .79400 .79299 .80660 .79418 .78506 .77543 .77233 .75545 .74380	.69544 .69881 .70402 .70653 .71080 .71709 .70648 .70144 .69875 .69833 .67658 .66156	.7067 .7066 .7066 .7063 .7055 .7041 .7016 .6979 .6931 .6870 .6800		
1922 J F M A J J A S O N D	4.477 4.497 4.523 4.439 4.429 4.407 4.286 4.281 4.282 4.407 4.478	Ī.31413 Ī.29874 Ī.23441 Ī.22991 Ī.21253 Ī.22966 Ī.26457 Ī.22471 Ī.20623 Ī.18853 Ī.19842 Ī.18827	.73684 .73577 .72685 .71806 .71426 .71475 .70870 .70135 .69858 .70836 .71692 .71456	.65098 .65290 .65538 .64734 .64631 .64406 .63210 .63147 .63161 .64406 .65114	.6646 .6571 .6505 .6451 .6411 .6387 .6378 .6382 .6396 .6417 .6444		
1923 J F M A M J A S O N D	4.457 4.492 4.611 4.629 4.547 4.562 4.556 4.526 4.526 4.587 4.614 4.593 4.615	$\begin{array}{c} \bar{1}.19983\\ \bar{1}.19415\\ \bar{1}.19856\\ \bar{1}.20403\\ \bar{1}.21140\\ \bar{1}.21089\\ \bar{1}.22301\\ \bar{1}.22426\\ \bar{1}.20043\\ \bar{1}.18964\\ \bar{1}.17569\\ \bar{1}.16127\\ \end{array}$.71498 .71750 .72956 .73217 .72544 .72685 .72816 .72556 .72762 .72855 .72448 .72461	.64899 .65237 .66376 .66553 .65767 .65915 .65855 .65575 .66154 .66409 .66205	.6502 .6529 .6556 .6579 .6598 .6615 .6627 .6635 .6638 .6637		
1924 J F M A M J J A S O N	4.587 4.621 4.634 4.590 4.560 4.483 4.422 4.486 4.469 4.441 4.460 4.507	$\begin{array}{c} \overline{1}.14648\\ \overline{1}.12292\\ \overline{1}.10766\\ \overline{1}.11913\\ \overline{1}.09339\\ \overline{1}.10494\\ \overline{1}.10952\\ \overline{1}.07062\\ \overline{1}.08697\\ \overline{1}.09117\\ \overline{1}.06929\\ \overline{1}.04649\\ \end{array}$.71985 .71995 .71941 .71662 .71062 .70461 .69919 .70088 .70109 .69889 .69817 .70025	.66148 .66467 .66604 .66182 .65897 .65157 .64559 .65187 .65020 .64750 .64931	.6619 .6609 .6599 .6588 .6576 .6562 .6547 .6531 .6514 .6499 .6486 .6477		

TABLE 6 (Continued)

		IMBLE	(Continued)		
	1	2	3	4	5
Date	Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	Log. "5.00"	Log. "4.50"	Cyclical curve to Log. "4.50"
1925 J F M A M J J A S O N D	4.500 4.495 4.437 4.396 4.338 4.379 4.436 4.499 4.465 4.510 4.493 4.457	1.04167 1.02640 1.07922 1.10644 1.11191 1.05035 1.03552 1.02654 2.98531 2.98297 2.98238	.69904 .69697 .69707 .69626 .69122 .69001 .69373 .69437 .69413 .69440 .69258 .68909	.65320 .65271 .64708 .64303 .63733 .64135 .64695 .65316 .64985 .65413 .65253 .64909	.6471 .6470 .6472 .6475 .6479 .6481 .6482 .6481 .6477 .6471 .6465 .6457
1926 J F M · A J J A S O N	4.409 4.372 4.376 4.323 4.306 4.387 4.342 4.346 4.343 4.349 4.307 4.283	2.99371 2.99718 2.99935 2.99353 2.99204 2.91439 2.94484 2.95548 2.95548 2.93573 2.93573 2.93573 2.95229	.68541 .68204 .68268 .67678 .67225 .67136 .67438 .67600 .67543 .67427 .67045	.64435 .64066 .64109 .63575 .63408 .63716 .63770 .63813 .63783 .63835 .63418	.6449 .6439 .6429 .6417 .6404 .6391 .6377 .6364 .6350 .6336 .6322 .6305
1927 J F M A M J A S O N D	4.243 4.244 4.184 4.114 4.100 4.132 4.134 4.113 4.076 4.043 4.005 3.996	2.96750 2.96464 2.99441 1.01769 1.02674 1.02772 1.00086 1.00448 2.98701 2.997114 2.95107	.66637 .66615 .66267 .65767 .65705 .66040 .66076 .65591 .65231 .64713 .64157 .63887	.62772 .62776 .62155 .61428 .61275 .61620 .61636 .61417 .61023 .60670 .60260	.6285 .6262 .6236 .6206 .6175 .6143 .6114 .6089 .6069 .6057 .6055
J928 J F M A M J J A S O N D	4.010 4.039 4.068 4.086 4.100 4.178 4.259 4.329 4.263 4.276 4.260 4.312	2.93225 2.91727 2.87495 2.87368 2.92420 2.94415 2.91910 2.89723 2.92070 2.88321 2.86441 2.88210	.63881 .64077 .64062 .64244 .64767 .65762 .66388 .66931 .66439 .66288 .65860 .66640	.60318 .60634 .60939 .61130 .61269 .62100 .62930 .63644 .62969 .63105 .62936 .63465	.6065 .6082 .6104 .6131 .6161 .6193 .6226 .6260 .6294 .6326 .6357 .6385

TABLE 6 (Continued)

Date	Sigma "4.50" in	Cum. Log. of sigma	3 Log. "5,00"	4 Log. "4.50"	5 Cyclical curve to
	Jan. 1925	slopes		2.0g. 4.00	Log. "4.50"
1929	4.343	2.88250	. 66959	09701	0.444
J F	4.382	2.80200	.67432	.63781	.6411
M	4.407	2.93376	.67986	.64410	.6451
A	4.406	2.89393 2.93376 2.90420 2.90522	.67741	.64401	.6466
M	4.423	2.90522	.67920	.64572	.6477
Ĵ	4.464 4.490	2.91976	.68432	.64969	.6485
J _A	4.451	2.90909	.68604 .68609	.65225 .64852	.6489
S	4.521	2.90522 2.91976 2.90909 2.95525 2.89924	.68823	.65520	.6482
J A S O N	4.492	2.85834 2.93611 2.87776	.68245	.65239	.6470
N	4.387	$\frac{2}{2}$. 93611	.67818	.64223	.6452
D	4.349	2.87776	.66979	.63836	.6428
1930	4.333	2.90365	.67018	.63682	.6399
J F	4.317	0.01051	.67227	.63519	.6367
M	4.244	2.94058	.66415	.62783	.6334
A	4.304	2.86676	.66452	.63388	.6300
M	4.268 4.234	2.94954 2.94058 2.86676 2.89753 2.91729 2.93964 2.96978	.66313 .66121	.63023	.6268
J J A S O N	4.182	2.91729	.65766	.62679 .62142	.6237
Å	4.113	2.96978	.65305	.61420	.6178
S	4.062	2.94580 1.01166	.64545	.60869	.6146
0	4.034	1.01166 1.06928	.64845	.60567	.6112
D	4.066 4.116	1.12325	.65801 .66984	.60916 .61452	.6077
1931					
J F	4.012	<u>1</u> .03688	.64875	.60341	.6008
M	4.018 4.033	$\frac{1}{1}.03138$ $\frac{1}{1}.00677$.64878 .64791	.60401 .60561	.5981
A	4.007	1.08989	.65402	.60279	.5960
A M	3.918	$\bar{1}.14865$.65174	.59309	.5971
J A S O	3.927	$\frac{1}{1}.16878$ $\frac{1}{1}.17315$.65557	.59414	. 5999
Į.	3.920	1.17315	.65532	.59327	.6042
S	3.950 3.980	1.24538	.66985 .69572	.59657	.6100
ŏ	4.174	1.36195 1.43658	.73444	.62063	.6246
N	4.321	1.40774	.74214	.63564	.6325
D	4.496	1.53738	.79637	.65283	. 6403
1932	4.537	Ĩ.45138	.77456	.65680	.6472
J F	4.609	<u>1</u> .41490	.77190	.66364	.6527
M	4.509	Ī.41929	.76346	.65409	. 6564
A	4.604	1.51631	.79988	.66314	.6580
M	4.526 4.556	1.66061 1.68234	.84634	.65570 .65858	.6546
J A S O	4.522	1.59600	.81960	.65532	.6502
A	4.340	$\bar{1}.47676$.76238	.63753	.6444
S	4.274	<u>1</u> .44163	.74593	.63079	.6379
0	4.268	1.45832	.74980	.63015	.6311
N D	4.280 4.119	1,49997 1,60227	.76313	.63143	.6245

TABLE 6 (Concluded)

		INDEE 0	(Concruded)		
Date	1 Sigma "4.50" in Jan. 1925	Cum. Log. of sigma slopes	3 Log. "5.00"	4 x Log. "4.50"	5 Cyclical curve to Log. "4.50"
1933 J F M A M J J A S O N D	3.933 3.912 4.051 4.220 4.113 3.996 3.944 3.890 3.870 3.878 3.956 3.939	1.59726 1.63219 1.65622 1.65371 1.58383 1.53102 1.48171 1.49248 1.58324 1.59322 1.66751 1.63457	.75948 .77097 .79632 .81293 .77392 .74302 .72218 .71933 .74724 .74997 .78879 .77292	.59471 .59241 .60760 .62529 .61417 .60156 .59591 .58988 .58771 .58861 .59734	.6132 .6090 .6056 .6032 .6013 .5999 .5986 .5971 .5954 .5932 .5907
1934 J F M A J J A S O N D	3, 884 3, 845 3, 782 3, 726 3, 671 3, 582 3, 579 3, 613 3, 659 3, 603 3, 522 3, 459	1.52847 1.41357 1.40198 1.39331 1.40439 1.43042 1.41824 1.45778 1.46245 1.46245 1.46837 1.46112	.72833 .69154 .68158 .67304 .66924 .66502 .66165 .67606 .68719 .67606 .66781	.58933 .58486 .57770 .57122 .56478 .55411 .55381 .55794 .56342 .56666 .54678 .53887	.5848 .5817 .5783 . 57 47
1935 J F M A I J S O N D	3.374 3.283 3.229 3.224 3.269 3.251 3.236 3.291 3.303 3.311 3.270 3.250	1.46468 1.49297 1.56042 1.57781 1.52906 1.52391 1.51338 1.50275 1.51264 1.52135 1.53964 1.52014	.64812 .64430 .65871 .66417 .65365 .64960 .64429 .64832 .65289 .65673 .65714 .64828	.52810 .51621 .50909 .50845 .51446 .51204 .51003 .51730 .51886 .51998 .51451 .51191	
1936 J M A M J J A S O N D	3.210 3.177 3.113 3.100 3.066 3.052 3.075 3.101 3.073 3.064 3.034 2.989	1.48775	.63302	.50645	
1937 J	3.011				

TABLES 7 AND 8

CERTAIN MATHEMATICAL FUNCTIONS AND EQUATIONS DERIVED FROM THE LOGARITHMS OF THE YIELDS OF THE RAILROAD BONDS USED IN INDEXES

The information in each horizontal line of these tables refers to a definite group of bonds, each bond in the group having either actual or interpolated quotations on both the dates given in the first two columns. The bonds from which the tables are constructed are, year by year, the same bonds which were used in constructing the bond index numbers. The groups in two horizontal lines may or may not be the same. The names of the bonds used in any particular period may be found by referring to Table 3.

The x's of the table refer in all cases to the logarithms of the yields in the earlier date (first column of table). The y's refer to the logarithms of the yields in the later date (second column of table). All functions and equations are in terms of logarithms; for example, the x's and y's of the equations are in all cases logarithms of yields. Thus the first equation in the last column of Table 7 might read "The logarithm of the yield in the later January equals 1.18693 times the logarithm of the yield in the earlier January, minus .13852."

The origin for all equations is zero. At the origin actual yields in both the earlier and the later dates are therefore unity, as $\log r = 0$.

The Least Squares Straight Line Equations of Table 7 need no particular description. In the eighth column the earlier January (x) has been considered the independent variable, in the ninth column the later January (y) has been considered the independent variable. In statistical nomenclature, they are the two regression equations.

In the equations which we have termed Sigma Equations neither variable is considered independent. They are equations of theoretical linear relationship between x and y, fitted by the method of least squares, the assumption having been made that the tendency to deviation from theory in the x and y elements of each observation is in proportion to the respective x and y standard deviations. For a fuller discussion of the significance of these Sigma Equations see Ch. IV.

Table 7 contains a column entitled 'Root-Mean-Square-Displacement'. These figures give a measure of scatter of the observations about the Sigma line $(y = \frac{\alpha}{2x}x)$. This measure of scatter, unlike the coefficient of correlation (r), is not necessarily affected by the mere inclusion or exclusion of bonds of lower and lower grade—in other words by the mere range of the observations.

DEVIATIONS ROOT-M SQUA F VIELDS DISPLA	STANDARD DEVIATIONS OF LOGS OF VIELDS		ARITHMETIC OF LOGS O	Dates of Identical Groups of Bonds ²		
MEN MEN			OF LOGS O			
σ_{y} $\sqrt{\sigma_{x}\sigma_{y}}$	σx	M_y	Mr	y (later date)	x (earlier date)	
.06620 .0163	.05577	.93300	.90277	Jan. 1858	Jan. 1857	
.04906 .0263 .05930 .0138	.06473	.86427 .87007	.93493	Jan. 1859 Jan. 1860	Jan. 1858 Jan. 1859	
.05494 .0088	.05930	.86380	.87007	lan, 1861	Ian. 1860	
.04704 .000	.05407	.85327	.86600	Jan. 1862	Jan. 1860 Jan. 1861	
.04106 .0234 .03567 .0096	.04985	.73518 .78100	.87218 .74552	Jan. 1863	Jan. 1862	
.03458 0150	.03537	.79309	.77968	Jan. 1864 Jan. 1865	Jan. 1862 Jan. 1863 Jan. 1864	
.02559 .0198	.03662	.86447	.79232	lan, 1866	Jan. 1865	
.02867 .0116	.02700	.85168 .85430	.86932 .85230	Jan. 1867 Jan. 1868	Jan. 1866	
, 03361 .010	.02916	.86325	.85390		Jan. 1867 Jan. 1868	
.03075 .0106	.02922	.87048	.85852	Jan. 1870	Jan. 1869	
.02231 .013 .02108 .014	.02716	.85400 .83576	.87376 .85400	Jan. 18/1	Ian. 1870	
.02108 .0143 .02418 .005	.02454	.84596	.84043	Jan. 1872 Jan. 1873	Jan. 1871 Jan. 1872	
.02641 .004	.02355	.84790	.84652	Jan. 1874	Ian. 1873	
.03266 .0086	.02553	.82033 .79195	.84576 .82057	Jan. 1875	Jan. 1874	
.03418 .0094	.03334	.77967	. 79195	Jan. 1876 Jan. 1877	Jan. 1875 Jan. 1876	
.03212 .0098	.03623	.77755	.78145	Jan. 1878	Jan. 1877	
.02829 .0065	.03216	.75659 .73126	.78045 .75752	Jan. 1879	Jan. 1878	
.02352 .005	.03275	.69312	.74288	Jan. 1880 Jan. 1881	Jan. 1879 Jan. 1880	
.03929 .010	.03510	.70058	.69692	Jan. 1882	Tan. 1881	
.03256 .0076	.03939	.70121 .69652	.70379	Jan. 1883	Jan. 1882	
.03363 .0066	.03227	69019	.70145	Jan. 1884 Jan. 1885	Jan. 1883 Jan. 1884	
,03272 .006.	.03480	65241	.69103	Jan. 1886	Jan. 1885	
.03023 .0076	.03281	.64489	.65216	Jan. 1887	Jan. 1886	
.03108 .008	.03030	.65249	.64508 .65414	Jan. 1888 Jan. 1889	Jan. 1887 Jan. 1888	
.02960 .0089	.03523	.63639	.63850	Jan. 1890	Jan. 1889	
.02956 .006	.02969	.65421	.63989	Jan. 1891	Jan. 1890	
.02671 .0075 .02679 .005	.02958	.65095	.65500	Jan. 1892 Jan. 1893	Jan. 1891	
.02861 .007.	.02724	.64789	.64649	Ĭan. 1894	Jan 1892 Jan 1893	
.02979 .007	.02910	.62450	.64783	Jan. 1895		
.03356 .0076	.03076	.62853 .61635	.62650 .62735	Jan. 1896 Jan. 1897	Jan. 1895 Jan. 1896	
.03104 .007	.03139	.59144	.61525	Jan. 1898		
.03312 .009	.03353	.57486 .58059	.58980	lan. 1899	Jan. 1898	
.03501 .007	.03341	.58059	.57368 .58276	Jan. 1900 Jan. 1901	Jan. 1899 Jan. 1900	
.03133 .004	.03133	.57059	.57192	Jan. 1902 Jan. 1903	Tan. 1901	
.02466 .005.	.02948	.58361	.57124	Jan. 1903	Jan. 1902	
.02191 .005 .01872 .004	.02437 .02183	.59630 .58067	.58338	Jan. 1904 Jan. 1905	Jan. 1903 Jan. 1904	
.01996 006	.02115	.58775	.58465	lan. 1906	Jan. 1905	
.01853 .004	.02001	.60551	.58872	Jan. 1907	Tan. 1906	
.02502 .007- .01714 .006	.01853	.63105	.60551 .63105	Jan. 1908 Jan. 1909	Jan. 1907 Jan. 1908	
.01864 .004	.02068	.61327	.60709	Jan. 1910	Jan. 1909	
.01838 .003.	.01889	.61975	.61355	Jan. 1911	Jan. 1910	
.01824 .004 .01893 .003	.01838 .01861	.62105 .63086	.61975 .62170	Jan. 1912 Jan. 1913	Jan. 1911 Jan. 1912	
.01895 .005	.01904	.64793	.63056	Jan. 1914	Jan. 1913	
.02208 .004	.01940	.66251	.64870	Jan. 1915	Ian. 1914	
.02297 .005.	.02296	.65037	.66172 .64988	Jan. 1916 Jan. 1917	Jan. 1915 Jan. 1916	
.02433 .004	.02484	.71617	.64020	Tan. 1918	Jan. 1917	
.02055 .007	.03083	.70505	.71617	Jan. 1919	Jan. 1918	
.02802 .006 .02811 .006	.02055 .02802	.74076 .74612	.70505 .74076	Jan. 1920 Jan. 1921	Jan. 1919 Jan. 1920	
.02668 .008	.02811	.69907	.74612	Jan. 1922	Jan. 1921	
.02050 .006	.02668	.68595	.69907		Jan. 1922	
.01813 .005	.02050 .01813	.69417 .67888	.68595 .69417	Jan. 1924 Jan. 1925	Jan. 1923 Jan. 1924	
.01660 .003	.01854	.67258	.68471	Jan. 1926	Ian. 1925	
.01670 .003	.01774	.65511	.67344	Jan. 1927	Tan. 1926	
.01613 .003	.01749 .01638	.66302	.65687	Jan. 1928 Jan. 1929	Jan. 1927 Jan. 1928	
.01460 .005 .01533 .004	.01460	.66328	.66302	Jan. 1930	Jan. 1929	
.01272 .004	.00936	.62939	.65593	Jan. 1931	Jan. 1930	
.05491 .013	.02114	.75290 .70841	.64041 .73806	Jan. 1932 Jan. 1933	Jan. 1931 Jan. 1932	
.05875 .017 .04807 .014	.05698	.68790	.71155	lan, 1934	lan. 1933	
.03934 .012 .04149 .010	.04557	.60821	.68211 .60821	Jan. 1935 Jan. 1936	Jan. 1934 Jan. 1935	

Note 1. These are the yields in Table 3.

Note 2. The variables are the logarithms of bond yields. The first two columns give, of course, only the dates to which yields relate.

Note 3. For a description of the nature of these equations see Ch. IV.

EQUATIONS OF LEAST SQUARES STRAIGHT LINES FITTED TO LOGARITHMS
OF YIELDS
OF YIELDS
LINES FITTED TO LOGARITHMS

of)	LINES FITTED TO LOGARITHMS OF VIELDS			
When x is the independent variable	When y is the independent variable	$y = a + \frac{\sigma_y}{\sigma_x} x$		
1 10129v 06130	70170 1 17777			
y = 1.10138x06129 y = .59365x + .30925	x = .78178y + .17337 x = 1.03341y + .04178 x = .77373y + .19107	y=1.18693x13852		
	v = 77373v ± 10107	y = .75793x + .15566 y = 1,20872x17459		
y = .0440x + .07691 y = .83750x + .12800 y = .60311x + .20916 y = .72839x + .23797 y = .79911x + .17004	x = 1 05376y - 04017	v = 02642v 4 05775		
v = .83750x + .12800	x = 1.05376y04017 x = 1.10666y07828	y = .86993x + .09991 y = .82353x + .01691 y = .77130x20598 y = .97779x + .03073		
y = .60311x + .20916	x = .88927y + .21841 x = 1.22440y21074 x = .83582y + .11680	v = 82353x + 01691		
y = .72839x + .23797	x = 1.22440y21074	v = .77130x20598		
y = .79911x + .17004	x = .83582y + .11680	v = .97779x + .03073		
y = .40729x + .54177 y = .87710x + .08920	x = .83450y + .07092 x = .77811y + .20662 x = .90231y + .08146 x = .77535y + .18458 x = .83126y + .13493			
y = .87710x + .08920	x = .77811y + .20662	y = 1.06171x07129 y = 1.01732x01276 y = 1.15259x12095		
	x = .90231y + .08146	y = 1.01732x01276		
y = 1, 93383x - 01629 y = 1,03003x - 01629 y = 92035x + 0.8035 y = 58128x + .34611 y = .52305x + .38908 y = 93582x + .05947 y = 1,08146x06758 y = 1,15797x15903 y = .94505x + .01647 v = 896411 x - 0.7055	x = .77535y + .18458	y = 1,15259x12095		
y = .92035x + .08035	x = .83126y + .13493			
y = .58128x + .34611	X ≈ .80123y+.13821	y = .82155x + .13616 y = .94451x + .02915		
y = .52305x + .38908	x = .58631y + .36398	y = .94451x + .02915		
y = .93582x +.05947	x = .96427y + .02470	y = .98514x + .01802		
y=1.08146x06758	x = .85969y + .11759	y = 1.12159x10155		
y=1.15/9/x15903		y = 1.27914x26152		
y = .94505X + .01047 y = .89541x + .07055	x = .89936y + .10832	y = 1.02509x04921 y = 1.06050x06019		
y = .89541x + .07055 y = .81405x + .14141 y = .83941x + .10147 y = .90281x + .04736	x = .79616y + .17121	y ≈ 1.00050x00019		
v = 83941x + 10147	x = 1.03583y02396 x = 1.08492y04039	y = .88651X +.08479		
v = .90281x + .04736	X=1.06492y = .04039	y = .87900x +.07011		
y = .90201A T .04730	x = .90030y T.0302+ y = 04236y ± 09071	y = 1,00030x - 0,0019 y = .88651x + .08479 y = .87960x + .07011 y = .95671x + .00653 y = 1,00991x05712		
y = .96113x02088 y = 1.03073x01775	x = .98636y + .03624 x = .94236y + .08971 x = .82278y + .12050	y=1.00991x05712 y=1.11926x07945		
y = .78936x + .14567	v = 1 15494v = 10500	y = 1.11920x07943 y = .82675x + .11935		
	v = 02788v ± 05516	1 -1 04220r - 03466		
y = .97754x + .00936	v = 88032v ± 08267	y = 1.04239x03466 y = 1.04843x04001		
y = .97754x + .00936 y = .90693x + .02570 y = .96693x + .02570 y = .86773x + .07899 y = .94724x + .04145 y = 1.19214x13980 y = .76707x + .14087 y = .94347x + .05046 y = .8387x + .03646 y = .97394x + .01825 y = .97394x + .01825 y = .97394x + .01825 y = .97394x + .01825	x = .02276y + .12050 x = 1.15484y10599 x = .92788y + .05516 x = .88932y + .08267 x = 1.02621y + .02152	y = .94009x + .00278 y = .92120x + .04412		
v = 86773x + 07899	x = 1.02254y00727 x = .90026y + .05767 x = .75296y + .17222	v = 02120v = 04412		
v = 94724x + 04145	x = 90026y + 05767	y = 1,02576x04912 y = 1,02576x04921 y = 1,25828x18306 y = .84011x + .09998 y = .99561x + .01713 y = .90297x + .05050 y = .98132x + .00770		
y = 1.19214x13980	y = .75296y + .17222	v = 1 25828v - 18306		
v = 77607x + 14087	x = 1,09958y06126	V = 840117 ± 00008		
v = .94347x + .05049		v = .99561x + .01713		
y = .83892x + .10146	x = 1.02889v01476	v = .90297x + .05950		
y = .93837x + .03566	x = .97443v + .02099	v = .98132x + .00770		
y = .97394x + .01825	x = .88309y + .07435			
y = .96167x + .00150	x = ,95181y + ,01721 x = 1,0288y - ,01476 x = ,97443y + ,02099 x = ,8830y + ,07435 x = ,91807y + ,07435 x = ,91807y + ,07435 x = ,9228y + ,07095 x = ,9323y + ,0035 x = ,9323y + ,0035 x = ,9428y + ,0433 x = ,10627y - ,0433 x = ,10627y - ,0433 x = ,10627y - ,00470 x = 1,0167y - ,00470 x = 1,0167y - ,00470	y = 1.02347x03853 y = 1.09084x05488 y = .94279x + .02489		
y = 1.03861x02216 y = .89557x + .05452 y = .93117x + .01854	x = .87283y + .07790	y = 1.09084x05488		
y = .89557x + .05452	x = 1.00755y + .00635	y = .94279x + .02489		
y = .93117x + .01854	x = .95216y + .05211	y = .98892x01699		
y = .91150x + .03726	x = .93452y + .05258	y = .98892x01699 y = .98761x00763		
y = .99399x + .01036	x = .90485y + .04833	y = 1.04810x02068		
y = .99399x + .01036 y = .86661x + .06690 y = .90267x + .05433	x = 1.11962y05757	y = 1.04810x02068 y = .87978x + .05922 y = .94511x + .03006 y = .83643x + .10581		
y = .90267x + .05433	x = 1.01057y00470	y = .94511x + .03006		
y = .80243x + .12523	x = 1.14697y09814	y = .83643x + .10581		
y = .80243x + .12523 y = .84878x + .10114 y = .80833x + .09812	x=1.04937y04236 x=1.09918y04129	y = .89936x + .07163 y = .85755x + .06874 y = .94368x + .03603 y = .92586x + .06044		
y = .80833x + .09812	x = 1.09918y04129 x = .96914y + .01504	y = .85/35x + .068/4		
y = .86305x + .08317 y = .88302x + .08566	X = .909149 +.01304	y = .94368X +.03003		
y = .88302x + .08566	x = 1.03009y03501 x = 1.65234y + .19385	y = .92380x +.00044		
y=1.189/2406933	x=1.33354y17550	y=1.3304/x=.1800/		
y = .02002x \(\pi\).20977	x=1.05856y04209	y = .00510x +.17245		
v = 04246v ± 04150	v = 00548v = 00340	y = .901311 T.00005		
v = 04508x ± 03534	v = 06034v ± 02333	y = 1.35047x - 18667 y = .68516x + .17245 y = .90131x + .06609 y = .97301x + .02276 y = .99202x + .00625		
v = 07735v + 02324	x = .99548y00340 x = .96034y + .02333 x = .94449y + .02586	v=1 01725v = 00156		
y = 1,18972x - 0.8933 y = 1,18972x - 0.8933 y = .62602x + .20977 y = .85993x + .09121 y = .94508x + .03534 y = .97735x + .02324 y = .91024x + .07397 y = 1.07575x03500	x = .91860y + .03537 x = .82974y + .09899 x = .94211y + .04900	y = 1.01725x00156 y = .99544x + .02025		
v = 1.07525x03500	x = .82974y + .09899	y=1.13837x 07595		
y = 1.07525x03500 y = .94266x + .02659	x = .94211v + .04900	y = 1.00030x01155		
y = 1.01478y01951	x = .92927y + .05517	y = 1.04500y - 03914		
y = 1.01478x01951 y = 1.08113x + .02403 y = .60087x + .27473		y=1.04500x03914 y=1.24107x07836		
v = .60087x + .27473	x=1.35223v23722	y = .66660x + .22765 y = 1.36372x22073 y = 1.00296x + .00317		
v = 1.25581x14465	x = .67526y + .20484	v = 1.36372x22073		
v = .95228x + .04071	x = .94667y + .03443	y = 1.00296x + .00317		
y = .86211x + .05583	x = .95695y + .07715	y = .94916x00912		
y = .70536x + .19285	x = 1.19403y11997	v = .76860x + .14864		
y = .,60087x + .27473 y = .1.25581x14465 y = .95228x + .04071 y = .86211x + .05583 y = .70536x + .19285 y = .81234x + .13695 y = .81234x + .08110 y = .863682x + .08113 y = .863682x + .0751 y = .79267x + .16250 y = .79267x + .16250 y = .93597x + .04272 y = .1,16474x13460	x=1,01927+1,1313 x=1,35223y-2,23722 x=67526y+20484 x=94667y+0,3443 x=95695y+0,7715 x=1,19403y-11997 x=1,03854y-0,33497 x=1,27572-10526	y=1.002903700317 y=.94916x00912 y=.76860x+.14864 y=.88442x+.08750 y=.78559x+.13355 y=.89547x+.05944 y=.94139x+.02114 y=.92201x+.02440 -80125x+.00003		
y = .72675x + .17439	x=1.17757y10526 x=1.07730y03986	y = .78559x + .13355		
y = .86384x + .08110	x=1.07730y03986	y == .89547x+.05944		
y = .89358x + .05333		y = .94139x + .02114		
y = .88682x + .04751	x = 1.04319y00038 x = .99679y02945	y = .92201x + .02440		
y = .79267x + .16250	x = .99679y02945	v = .89175x + .09993		
y = .93597x + .04272	x = .84931y + .09969	y = 1.04977x03274		
y = 1.16474x13460	x = .84931y + .09969 x = .63060y + .25904 x = .32714y + .39410	y=1.35906x26206		
$y \approx 2.20674x66032$	x = .32714y + .39410	y = .89175x + .09493 y = .89175x + .09993 y = 1.04977x03274 y = 1.35906x26206 y = 2.59721x91038 y = 1.3023x2420		
y = 1.23178x20072	x = .62916y + .29235	y=1.39922x32430		
	x = 1.09/40y04335	v = .84366x + .08759		
y = .78109x + .13212				
y = 1,9339/A + .04216 y = 1,16474x13460 y = 2,20674x66032 y = 1,23178x20072 y = .78109x + .13212 y = .78521x + .07261 y = .98144x00599	x = .62916y + .29235 x = 1.09740y04335 x = 1.05333y + .04146 x = .88247y + .08672	y=1.3922x32430 y= .84366x+.08759 y= .86340x+.01928 y=1.05459x05048		

TABLE 8—American Railroad Bond Yields', Quarterly, January 1857-January 1936. Mathematical Functions and Equations

an. 1857 April 1857 1900 19138 05520 055971 05520 059911 00991	Dates Grou	OF I	DENTI BON	CAL bs ²	ARITHMETIC OF LOGS OF	AVERAGES F YIELDS	STANDARD OF LOGS	DEVIATIONS OF YIELDS	Sigma Equations ² of Straight Lines fitted : Logarithms of Yields
Description Description			y (la dat	ter e)	Mx	Му	σx	σу	$y = a + \frac{\sigma_y}{\sigma_x} x$
Description Description	an 1	857 3	nril	1857	.90277	.90200	.05577	.05520	y = .98971x + .00852
		" I	uly		,90200	.91738	.05520	.06091	y = 1.10343x07791
		" (Oct.		.91738	.99308		.06918	y=1.13578x04886
	Oct.		an.	1858	.99308	.93300	.06918	,06620	y = .95694x01732
	an. 1	858 3	\pril		.93493	.89673			y = .86929x + .08400
1	Anril	" IJ	uly		.89673	.88627	.05627	.05868	y = 1.04290x04893
1	uly	- 15	Oct.		.88627		.05868	.05090	y = .86841x + .10082
1	Oct.			1859	.87047	.86427		.04900	y = .902/1x +.02626
1								05788	y=1.03809x03539
1	prii	1	miy.		97003	97000	05398	05281	V = 00850v = 00700
1				1860	87080	87007	05281		v = 1 12296v - 10780
1				1000	87007		05930		y = .86331x + 10759
1	nril	1 4	nly	"	85873	.83953	.05119	.04848	v = .94705x + .02627
1	ulse	" 6	Oct	"	.83953		.04848	.05116	v = 1.05514x04436
1				1861	.84147	.86380	,05116	.05494	y = 1.07388x03984
1		861 4	April	44	.86600	.86107	.05407	.05222	y = .96565x + .02482
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		" J	uly		.86107	.86747	.05222		y = 1.04302x03064
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	úlv	" (Oct.		.86747	.87887	.05446	.05282	y = .96985x + .03755
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	ct.	"]]	an.	1862	.87887	.85327	.05282	.04/04	y = .89056x + .07058
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	an. 1	.862 A	April		.87218	.85453		.04539	y = .91055x + .06036
1		13	uly		.85455	.82212			y = .90788x + .04631
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	uly	- 15	Jet.		77050				y = 1.013911 = .03301
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Ct.			1003	74552	75510	04625	04320	V = 93404v ± 05884
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		600	Color	"	75519	76238	04320	04452	v = 1 03064v - 01505
an, 1864 April $^{\circ}$ 7,7968 7,74373 8,03383 0,3398 9, $^{\circ}$ 1,0484 $^{\circ}$ 2,0737 1,74373 1,7		" 6	Oct.	u	76238	.75938		.03697	v = .83033x + .12635
an, 1864 April $^{\circ}$ 7,7968 7,74373 8,03383 0,3398 9, $^{\circ}$ 1,0484 $^{\circ}$ 2,0737 1,74373 1,7	let.	" 1	Ion	1864	.75938	.78100	.03697	.03567	v = .96494x + .04824
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	an. 1	864	April	44	.77968	.74373	.03537	.03708	y = 1.04849x07376
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		44	July		.74373	.70395	,03708	.05425	y = 1.46276x38395
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	uly	" 10	Oct.		.70395	.76914	.05425	.04277	y = .78837x + .21417
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			an.	1865	,76914	.79309	.04277	.03458	y = .80869x + .17109
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	an. 1	865	April		.79232	.83247			y = .92767x + .09746
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	pril	1	uly		.83247	.83953	.03398	.03504	y=1.04909x03381
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$,83955			.02894	y= .5119/x+.16/91
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Jet.		an.	1900	,04930				y = .50406x + .11337
Det Section	211. 1	800	April					02925	y = 1.20200x = .17334
Det Section		" 1	Dest.	"	85463	84568	02025	03235	V=1 10573v = 00031
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		" i	lan.	1867	84568	85168	03235	02867	v = 88622x + 10222
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	an. 1	867	April	"	.85230	.85725	02851		v = 1.09554x07648
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	pril	"]]	fulv		.85725	.85000	.03124	,03264	y = 1.04481x04566
$ \begin{array}{llllllllllllllllllllllllllllllllllll$		" (Oct.		.85000	.85500	.03264	.03235	y = .99104x + .01262
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	ct.		an.	1868	.85500	.85430	.03235		y = .89680x + .08754
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	an. 1	1868	April		.85390	.84940		.03115	y = 1.06815x06270
$ \begin{array}{llllllllllllllllllllllllllllllllllll$			July		.84940	.84470	.03115	.02836	y = .91059x + .07124
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	шу	19	Oct.		.844/0	.85425	.02830	.03241	y=1.14270x11104
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	on 1			180>	95952	96305	.03241		y=1.03097x =.02236
$ \begin{array}{llllllllllllllllllllllllllllllllllll$					86395	86124	02634	02783	v=1 05648v - 05151
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	n lar	"	Oct		86124	87052	02783	02939	v = 1.05607v - 03901
$ \begin{array}{llllllllllllllllllllllllllllllllllll$		"	Ian.	187C	.87052	.87048	.02939	.03075	v = 1.04612x04019
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	an.	1870].	April	44	.87376	.85638	.02716	.02303	y = .84795x + .11548
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	pril	"	July		.85638	.84814	02303	.01985	y = .86168x + .11021
pril # Tule # 94922 84181 02520 02450 - 06000- 1 0107	uly	**	Oct.		.84814	.85462	01985		y=1.15226x12266
oril # Tribe # 84822 84181 02520 02450 - 06000- 1 0107	rct.			1871	.85462	.85400	,02287	.02231	y = .97580x + .02006
oril # Tribe # 84822 84181 02520 02450 - 06000- 1 0107					.85400	.84900	.02231	.01832	y = .82090x + .14795
pril # Tule # 94922 84181 02520 02450 - 06000- 1 0107					04474	04074	01764	02312	y = .9029/X + .02720
oril # Tribe # 84822 84181 02520 02450 - 06000- 1 0107									y = 1.31130x25919
pril # Tule # 94922 84181 02520 02450 - 06000- 1 0107	217. 1	1872	April	10/2			02454		V = 86074v + 11044
oril # Tribe # 84822 84181 02520 02450 - 06000- 1 0107	nril	u	Inly		.84283	83448	.02113	02613	v=1.23708v - 20817
oril # Tribe # 84822 84181 02520 02450 - 06000- 1 0107	ulv	4	Oct.	**	.83448	.84670	.02613	.02571	v = .98374x + .02579
oril # Tribe # 84822 84181 02520 02450 - 06000- 1 0107	Oct.		ian.	1873			.02571	.02418	y = .94048x + .04966
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	an. 1	1873	April	**			.02355	.02529	y = 1.07367x06055
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	April	"	July		.84833	.84181	.02529	.02450	y = .96900x + .01978
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	uly	"	Oct.		.84181	.87305	.02450		y = 1.27805x20283
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Oct.	**	lan.	1874	.87305	.84790	.03131	.02641	y = .84350x + .11148
April " July " .83790 .83829 .02839 .03336 y=1.17514x1463	an. 1	1874	April		.84576	.83790	.02553	.02839	y = 1.11171x10234
uly "Oct. " 83829 83210 03336 03497 y=1.04837x - 0467		"	July		.83790	.83829	.02839		y=1.17514x14636

TABLE 8—American Railroad Bond Yields', Quarterly, January 1857-January 1936. Mathematical Functions and Equations—(Continued)

								(Continued)
		IDENT OF BON		ARITHMETIC OF LOGS			DEVIATIONS OF YIELDS	SIGMA EQUATIONS OF STRAIGHT LINES FITTED TO LOGARITHMS OF YIELDS
x (ea dat	rlier e)	y (la	e)	М×	My	$\sigma_{\mathbf{x}}$	σy	$y = a + \frac{\sigma_y}{\sigma_x} x$
	1874	Jan.	1875	.83210 .82057	.82033 .81110	.03497	.03266	y = .04394x + .04320 y = 1.04391x09447 y = 1.03890x + .04477 y = 1.03890x + .04477 y = 1.03823x02783 y = .95790x + .02116 y = .05790x + .02116 y = .10732x09054 y = .87371x + .10273 y = 1.0449x15738 y = .0449x15738 y = .0449x04730 y = .047314003954 y = .04140x03954 y = .01146x + .06824 y = .04146x + .06824 y = .04146x04824
Jan. Apri	1912	April	44	.82037	.80638	.03680	.03680	y = 1.10391X09474
Tuly	"	July Oct.	"	.80638	.80462	.03456	.03568	y = 1.03233x02783
Oct.	"	Tan.	1876	.80462	.79195	.03568	.03418	y = .95796x + .02116
Jan.	1876	April July	"	.79195 .78643	.78643 .78029	.03418	.03136	y ≈ .91768x+.05967
Apri July	**	Oct.	**	.78029	.78448	.03130	.03034	y = 1.10/32x09034 y = 87371y \(\perp \) 10273
Oct.	**	Tan.	1877	.78448	.77967	.03034	.03624	y = 1.19449x15738
Jan.	1877	April	**	.78145 .79125	.79125 .77745	03623	.02916	y = .80504x + .16215
April July		July Oct.	"	.79125	.77745	.02916	.03027	y=1.03782x04373
Oct.	**	Jan.	1878	.78265	.77755	.03076	.03212	v=1.04401x03954
Jan.	1878	April	**	. 78045	.77959	.03216	.02931	y = .91146x + .06824
April	"	July	"	.77959	.77082	.02931	.03054	y =1.04198x04150
July Oct.	"	Oct. Jan.	1879	.77082 .77073	.77073 .75659	.03054	.03101	y=1.01550x01204
Jan.	1879	April	"	.75752	.75252	.02458	.02220	v = .90323x +.06831
April	**	July Oct.	"	.75252	.73417	.02220	.02475	y = 1.11466x10463
July	"	Oct.		.73417	.74026	.02475	.02403	y = .97087x + .02748
Oct. Jan.	1880	Jan.	1880	.74026 .74288	.73126 .73728	.02403	.03093	y = .97877x ± .00672
April	"	July	**	.73728	.72572	.03093	.03597	y = 1, 04198x - ,04150 y = 1, 01550x - ,01204 y = ,91203x + ,05366 y = ,90323x + ,06831 y = 1, 11460x - ,10463 y = ,9787x + ,00672 y = ,9787x + ,00672 y = ,9442x + ,03569 y = 1, 16290x - ,13166 y = ,06256x + ,03021
July	"	Oct.	"	. 72572	.71424	.03597	.03390	y = .94256x + .03021 y = .97558x00368 y = 1.01055x
Oct.	4004	lan.	1881	.71424 .69692	.69312	.03390	.03307	y = .97558x00368
Jan. April	1881	April	"	. 70427	.68565	.03547	.03830	y = 1.01055x y = 1.07967y 07473
Tuly	**	July Oct.	"	,68565	70154	.03830	.03676	y = 1.07967x07473 y = .95976x + .04348
Oct.	**	Jan.	1882	.70154	.70058	.03676	.03929	y = 1.06885x04926
Jan.	1882	April	"	.70379	. 70364	.03939	.03828	y = .97177x + .01972
April July	"	July Oct.	"	.70364	.70296	.03796	.03790	v = 96737v ± 02639
Oct.	** }	Jan.	1883	.70296	,70121	.03672	.03256	y = .95976x + .05348 y = 1.06885x04926 y = .97177x + .01972 y = .99170x + .00159 y = .96737x + .02639 y = .86862x + .07781 y = .96575x + .02654 y = .97531x + .01993 y = .113203x10199
Jan.	1883	April	"	.70145	,70397	.03227	.03116	y = .96575x + .02654
April		July	"	.70397 .70274	.70274 .70532	.03116	.03046	y = .97761x + .01453
July Oct.	"	Oct. Jan	1884	.70532	.69652	.02971	.03363	y = .97.31x+.01993 y = 1.13203x0192 y = .84225x+.09946 y = 1.17986x10432 y = .96080x+.02114 y = 1.09809x07697 y = 1.04846x04261 y = 1.02578x02796
Jan.	1884	April	"	.69647	.68606	.03310	.02788	y = .84225x + .09946
April	"	Iulv	"	.68606	.70513	.02788	.03290	y=1.17986x10432
July Oct.		Oct.	1885	.70513	.69863	.03290	.03101	y = .90080x +.02114 y = 1 09809y - 07697
Jan.	1885	Jan. April July	"	.69103	.68191	.03480	.03649	y=1.04846x04261
April	"	July	"	68191	.67153	.03649	.03743	y = 1.02578x02796
July		Oct.	1886	.67153	.66497 .65241	.03743	.03598	y = .96114x + .01954
Oct. Jan.		Jan. April	1000	.66497	.64414	.03281	.03085	v = 94017x + .03100
April	"	July	и	.64414	.63684	.03085	.03118	y = 1.01069x01419
July	"	Oct.	"	.63684	.64476	.03118	.03014	y = .96649x + .02926
Oct. Jan.		Jan . April	1887	.64476	.64489	.03014	.03023	$\begin{array}{c} y=1.02578x02796\\ y=9.0114x+.01954\\ y=.9014xx+.04766\\ y=.90917x+.03.100\\ y=1.01069x01419\\ y=.96649x+.02926\\ y=1.0367x00182\\ y=.97349x+.02926\\ y=.97349x+.02026\\ y=.97349x+.02026\\ y=.97349x+.02026\\ y=.97349x00182\\ y=.106282x+.3927\\ y=1.01682x01122\\ y=1.01682x01122\\ y=1.10468x09237\\ \end{array}$
April	"	July	"	.64870	.64984	.02950	.03156	v=1.06987x04418
July	"	Oct.	"	.64984	.66495	.03156	.03038	y = .96282x + .03927
Oct.	**	an.	1888	.66495	.65249	.03038	.03108	y=1.02291x02769
Jan. April		April July	"	.65414	.65392 .64424	.02865	.03227	v = 1.12645x09237
July	"	Oct.	"	.64424	.64800	.03227	.03542	y=1.12645x09237 y=1.09757x05910 y=1.00089x00855 y=1.02469x02071
Oct.		Jan.	1889	.64800	.64003	.03542	.03545	y=1.00089x00855
	1889	April	"	.63850	.63355	.03523	.03610	y=1.02409x02071
April July	"	July Oct.	"	.62642	.63295	.03205	.03046	y = 1.02499x02071 y = .88767x + .06404 y = .95043x + .03758 y = .97179x + .02130
Oct.	"	Jan.	1890	.63295	.63639	.03046	.02960	y = .97179x + .02130
	1890	April	"	,63989	.64211	.02969	.03005	y=1.01193x00541
April July		July Oct.	"	.64211	.64503 .65379	.03005	.02916	v=1 01342x+.00010
Oct.	"	Jan.	1891	.65379	.65421	.02955	.02956	y=1.00036x+.00018
Jan.	1891	April July	"	.65500	.66136	.02958	.02955	y = .99872x + .00720
April	" }	July	"	.66136	.66979	.02955	.02947	y = .97179x + .02130 y = 1.01193x00541 y = .97049x + .02187 y = 1.01342x + .00010 y = 1.00036x + .00018 y = .99872x + .00720 y = .99731x + .01021 y = .90613x + .05634 x = 1.00048x01263
July Oct.	- 1	Oct. Jan.	1892	.66979 .66326	.66326	.02947	.02671	v=1.00048x01263
Jan.	1892	April	1392	.65090	.64674	.02730	.02626	y=1.00048x01263 y=.96181x+.02070
	-	,						

TABLE 8—American Railroad Bond Yields', Quarterly, January 1857-January 1936. Mathematical Functions and Equations—(Continued)

July 188 .	892 J	y (la			OF YIELDS	of Logs o	DEVIATIONS OF YIELDS	SIGMA EQUATIONS OF STRAIGHT LINES FITTED TO LOGARITHMS OF YIELDS
July 188 .	"	dat		Mx	My	σχ	σχ	$y = a + \frac{\sigma_y}{\sigma_x} x$
July 188 .	"	July	1892	.64674	.64136	.02626	.02645	y = 1.00733x01012
Yan. 188 April 189 April 190 April 189 April 190 April 1		Oct.		.64136	.64626	.02645	.02712	y = 1.00733x01012 y = 1.02519x01126
April 1900. April 183. April 185. April 186. April		Jan.	1893	.64626	.64644	.02712	.02679	v = .98797x + .00705
July 180	023 2	April July	66	.64714	.64714 .67338	.02786	.02786	y = 1.02275x01406
Oct. " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 189 April " Jan 190 April " July " Ju	" (Oct.	"	.67338	.66465	.03382	.02908	y=1.02275x01406 y=1.21399x11224 y=.85988x +.08562
Jan. 188 April 181 Jan. 189 April 181 Jan. 189 April 181 Jan. 189 April 181 Jan. 189 April 181 July 18	"]]	lan.	1894	.66465	.64789	.02908	.02861	y = .98365x00589
April a 100ct. a 120ct. a 120c	894	April	u	.64783	.63381	.02910	.02836	y = .98365x00589 y = .97433x + .00261
Cott. 4 Jan. 139 Jan. 139 April 1 July 1 Jul	"	luly	44	.63381	.63658	.02836	.02995	y = 1.05000x03272
Jan. 189 April 199 April 190 April 1		oct.	1895	62708	62450	02917	.02917	y = .97408x + .00700
April " 100 189 19	895 3	April	44	,62650	.63297	.03076	.03107	v = 1 00000v ± 00027
July 188 July 188 July 188 July 188 July 188 July 188 July 188 July 188 July 188 July 188 July 188 July 188 July 188 July 188 July 198 July	""j	uly oct.	"	63297	.61755	.03107	.02936	v = .94500x + .01939
189 April 190 April	" C	Oct.		.61755	.61429	.02936	02944	y = 1.00266x00490
April April		an.	1896	.61429	.62853	.02944	.03356	y =1.13999x07175
July 188 July 188 July 188 July 188 July 188 July 188 July 198 July	890	\pril [uly	44	.62735 .62300	.62300 .62916	.03323	.03043	y = .91573x + .04852
Oct. 48 April 41 Jan. 180 April 51 Jan. 180 April 61 Jan. 180 April 61 Jan. 180 April 61 Jan. 180 April 61 Jan. 190 April 61 Jan. 190 April 61 Jan. 190 April 61 Jan. 190 April 70 Jan. 190 Oct. 61 Jan. 190 Oct. 61 Jan. 190 Oct. 61 Jan. 190 Oct. 61 Jan. 190 Oct. 61 Jan. 190 Oct. 61 Jan. 190 Oct. 61 Jan. 190 Oct. 61 Jan. 190 Oct. 61 Jan. 190 Oct. 62 Jan. 190 Oct. 63 Jan. 190 Oct. 64 April 61 Jan. 190 Oct. 64 Jan. 190 Oct. 65 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 Jan. 190 Oct. 67 April 67 Jan. 190 Oct. 67 April 67 Jan. 190 Oct. 67 April 67 Jan. 190 Oct. 67 April 67 April 67 Jan. 190 Oct. 67 April 67 April 67 Jan. 190 Oct. 67 April 67 April 67 Jan. 190 Oct. 67 April 67 Jan. 190 Oct. 67 April 67 April 67 Jan. 190 Oct. 67 April		Dut.	44	62916	63735	.03362	.03362	y=1.10503x05927
Jan. 1808 April 1809 A	"]]	an.	1897	.63735	.61635	.03396	.03133	v = .92242x + .02845
April " 100 189 18	897	\pril	"	.61525	.60744	.03139	.03267	y = .97408x + .00700 y = 1.02120x01587 y = 1.00990x + .00027 y = .94500x + .01939 y = 1.00266x00490 y = 1.19999x07175 y = .91573x04852 y = 1.00266x00490 y = 1.00406x00366 y = 1.00406x00366 y = 1.0157x01650 y = 1.01157x01650 y = 1.01157x01650 y = 1.01157x01650
July 4 April 190		uly		.60744	.59797	.03267	.03304	y = 1.01157x01650
Jan. 180 April " July		Oct.	1898	.59797 .60156	.60156 .59144	.03304	.03335	y = 1.00922x00192 y = .93088x + .03146
April " 100ct. 189 April 808 7	an. April	44	.58980	61006	.03353	.03104	y = .93088x +.03146	
July " 100ct. 189 July " 189 July " 189 July " 190 July	" 1	uly	44	.61006	.59383	.03526	.03460	v = .98113x01018
Oct. 189 April " July " Oct. " July " Oct. " July " Oct. " July " Oct. " July " Oct. " July " Oct. " July " Oct. " July " Oct. " July " Oct. " July " Oct. " July " Oct. " July " Oct. " April " July " Oct. " April " July " Oct. " April " July " Oct. " April " July " Oct. " April " July " Oct. " April " July " Oct. " Oct. " April " July " Oct. " Oct. " April " Oct. " Oct. " April " Oct. " Oct	" (let.	**	.59383	.58920	.03460	.03140	y = 1.05161x01018 y = .98113x00472 y = .90766x + .05020
April " July " July " July " July " April " April " July " April " July " April " July " April " July " July " July " July " July " April " July " April " July " April " July " April " July " April " April " April " April " April " April " April " April " April " April " April " April " April " April " April " Oct. " April " Oct. " April " Oct. " April " Oct. " April " Oct. " April " Oct. " April " Oct. " April " Oct. " Oct. " April " Oct. " Oct. " Oct. " April " Oct.		an.	1899	.58920	.57486	.03140	.03312	y = 1.05459x04650 y = 1.01828x01429
July " Oct. " Jan. 190 April " July " Oct. " April " July " Oct. " April " July " Oct. " April " July " Oct. " April " July " April " July " April " July " April " July " April " July " April " July " April " July " April " Jan. 190 April " Jan. 190 April " April " April " April " April " April " April " April " Jan. 190 Oct. " April " Jan. 190 Oct. " April " Jan. 190 Oct. " April " Jan. 190 Oct. " April " Jan. 190 Oct. " April " Jan. 190 Oct. " April " Jan. 190 Oct. " April " Jan. 190 Oct. " April " Jan. 190 Oct. " April " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " Jan. 190 Oct. " April " Apri		April uly	"	.57368 .56988	.56988 .56724	.03341	.03402	y = 1.01828x01429
Jan. 1900 April "April	" C	Oct.	- 61	56724	.57779	.03303	.03303	y = .97091x + .01394 y = 1.01838x + .00012
Jan. 1900 April "April		an.	1900	.56724 .57779	58059	.03363	.03501	v = 1.01838x + .00012
April " July " April " July " April " July " April " April " April " April " April " April " April " April " July " April "	900 1	April	"	. 58276	57527	.03561	.03431	y = .96356x + .01375
July 4 Jan. 190 Oct. 191 Jan. 190 Oct. 191 July 4 July 4 July 4 July 5 July 5 July 6 July 6 July 6 July 7 July 7 July 7 July 7 July 7 July 8 J	" IJ	uly		.57527	.57992	.03431	.03493	y=1.04838x+.00012 y=1.04099x02088 y=.96356x+.01375 y=1.01790x00565 y=.94050x+.03467 y=.95375x+.01867 y=.98972x+.00401 y=.98972x+.0050
Jan. 190 April " July "	. 10	Det.	1901	.57992 .58008	.58008 .57192	.03493	.03285	y = .94050x + .03467
April " July " J		\pril	- 44	.57192	57005	.03133	.03133	y = .953/5X + .0186/
July " Oct. " Jan. 190 April " July " Oct. " July " July " Oct. " July " July " Oct. " July "	" 1.1	ulv	44	.57005	.57370	.03101	.03009	v = .93972x + .00401 v = .97044x + .02050
Jan. 190 April " July " April " July " April " July " April " July " July " July " July " July " July " July " July " July " July " July " July " July " April " July " April " July " April " July " April " July " April " July " April "		Ct.	44	.57370	57541	.03009	.03046	y = 1.01221x00529
Äpril " July " July " April " July " Oct. " Jan. 190 April " July " Oct. Jan. 190 April " April " July " Oct. " Jan. 190 April "		lan.	1902	.57541	.57059	.03046	.02961	y = .97214x + .01121
July "Oct. "Jan. 190 April July "Oct. "Jan. 190 April July "Oct. "Jan. 190 April July "Oct. "Jan. 190 April July "Oct. "April July "April "Jan. 190 April "Jan. 190 April "April		April July	u	.57124 .56905	.56905 .57416	.02948	.02891	y = .98063x + .00887
Oct. 190 Jan. 190 Oct. 4 Jan. 190 April 4 July 4 Oct. 4 Jan. 190 April 5 Jan. 190 April 4 July 4 Oct. 191 July 4 Oct. 191 April 4 April 4 April 5 April 6 April 7 April 7 April 7 April 7 April 7 April 8 April 8 April 8 April 8 April 8 April 8 April 8 April 8 April 8 April 8 April 8 April 8	" (Oct.	и	.57416	.58126	.02580	.02580	y = .89253x + .00627
Jan. 190 April " July " Oct. Jan. 190 April July " July " Jan. 190 April " July " Oct. Jan. 190 April " July " April " Jan. 190 April " April " April " April " April " April " April " April " April " April " April " April "	"]]	lan.	1903	.58126	.58361	.02565	.02466	v = .96133x + .02483
April " July " April " July " Oct. 19 July " Oct. 19 Jan. 190 April " July " Jan. 190 April " July " Oct. " Jan. 190 April " April " April " April " April " April " April " April " April " April " April " April " April " Oct. "		April	"	.58338	.59362	.02437	.02200	y = .90297x + .06685
July Oct. " Jan. 190 April " July " Oct. " Jan. 190 April July " Oct. " Jan. 190 April July " Oct. " Jan. 190 April " April " Oct. " April " Oct. " April " Oct. " April " Oct. " Oct. " April " Oct. "		luly Jet.	"	.59362	.60014	.02200	.02142	y = .97351x + .02224
Jan. 190 April " July " Oct. Jan. 190 April July " Oct. Jan. 190 April July " Oct. " Jan. 190 April " April " April " April " April " April " April " April "		an.	1904	60043	.60043 .59630	.02142	.02255	y = 1.05288x03145
April "July "Oct. Jan. 190 April "July "Oct. "Oct. "Upin "Jan. 190 April "Jan. 190 April "Jan. "July "April "April "April "April "April "April "April "April "April "April "April "April "April "April "April "April "April "	904	April	"	59697	.59672	.02183	.02191	y = .97044x + .02050 y = .97044x + .02050 y = .97214x + .0112x + .0829 y = .97214x + .00827 y = .9805x + .00887 y = .9613x + .00887 y = .9613x + .00885 y = .9613x + .02483 y = .90297x + .06885 y = .97172x + .01285 y = .97172x + .01285 y = .9865x + .06148 y = .94706x + .0215 y = .99406x + .0215 y = .90406x + .0215 y = .97646x + .01481 y = .07646x + .01481 y = .07646x + .01481
July Oct. " Jan. 190 April " July " Oct. " Jan. 190 April " July " Oct. " July " Oct. " Jan. 190 April "	" J	uly Oct.	"	,59672	.58828	.01958	.01854	y = .94706x + .02315
Jan. 190 April " July " Oct. " Jan. 190 April " July " Oct. " July " Oct. " Jan. 190 April "			1905	.58828	.58642	.01854	.01840	y = .99244x + .00259
April " July " Oct. " Jan. 190 April " July " Oct. " Jan. 190 April " April "	13	an. April	1905	.58642	.58067	.01840	.01872	y = 1.01762x01608
July " Oct. " Jan. 190 April " July " Oct. " Jan. 190 April "	" 1	spru fuly	и	.58570	.58440	.02115	.02066	y = .97640x + .01481
Oct. " Jan. 190 April " July " Oct. " Jan. 190 April "	" 10	Oct.	**	. 58440	.58495	.02066	.01978	y = 1.00015x00139 y = .95728x + .02552
April " July " Oct. " Jan. 190 April "	13	an.	1906	.58495	.58775	.01978	01996	y = 1.00940x00270
July " Oct. " Jan. 190 April "		April	"	.58872 .59692	.59692	.02001	.01989	y = .99386x + .01181
Oct. " Jan. 190 April "		fuly Oct.	44	.59900	.59900 .60336	.01989	.01923	y = .96669x + .02196
Jan. 190 April "	" 11	lan.	1907	.60336	.60551	.01762	.01762	y = ,91028x + ,03451
April "	907 3	April	"	.60551	.61526	.01853	.01939	v=1.04655x01844
	. 13	July	"	.61526	.62262	.01939	.02246	y = 1.15810x08991
July	1	Oct.	1908	.62262	.64121	.02246	.02530	y = 1.12637x06009
Oct.	. 13	Jan. April	1908	.64121 .63105	.63105	.02530 .02502	.02502	y = .98923x00325
April "	" 1	fuly	44	.62967	.62246	.02595	.02595	y = 1.03/10X02483
July "	"	July Oct.	**	.62246	.61326	.02369	.01958	v = .82654x + .09877
Oct. "	" IJ	lan.	1909	.61326	.60482	.01958	.01714	y = .87563x + .06783
Jan. 190	909	April	**	.60709	.60577	.02068	.02032	y = ,93728x + ,02552 y = 1,09340x - ,0270 y = ,99386x + ,01181 y = ,9669x + ,02196 y = ,11628x + ,03436 y = ,11628x + ,03436 y = 1,18410x - ,08991 y = ,18410x - ,08991 y = ,98923x - ,00325 y = ,98923x - ,00325 y = ,98236x + ,06787 y = ,87563x + ,06787 y = ,87563x + ,06787 y = ,98236x + ,00783 y = ,98236x + ,00783 y = ,98236x + ,00783
	"	July Oct.		.60577	.60648	.02032	.01908 .01909	y = .93909x + .03761 y = 1.00064x + .00445 y = .97637x + .01640
Oct. '		Jan.	1910	.61132	.61327	.01909	.01864	y = 1.00004X + .00445

TABLE 8—American Railroad Bond Yields¹, Quarterly, January 1857-January 1936. Mathematical Functions and Equations—(Continued)

							QUALITORS	(Continued)
		IDENT OF BON	DS"	ARITHMETIC of Logs o	Averages F Yields	STANDARD OF LOGS	DEVIATIONS OF YIELDS	SIGMA EQUATIONS ³ OF STRAIGHT LINES FITTED TO LOGARITHMS OF YIELDS
x (ea		y (la dat		Mx	My	σz	σy	$y = a + \frac{\sigma_y}{\sigma_x} x$
Jan.	1910	April	1910	.61355	.62066	.01889	.01955	v = 1.03463x01414
April	"	July	"	.62066	.62636	.01955	.02147	y=1,03463x - 0,0144 y=1,09836x - 0,533 y=,88867x + 0,6133 y=,96354x + 0,6133 y=,95700x + 0,02688 y=,95700x + 0,02688 y=,95700x + 0,02689 y=1,09854x + 0,0512 y=,9835x + 0,00068 y=,9835x + 0,00068 y=,99181x + 0,1079 y=1,0805x - 0,0068 y=,99181x + 0,1079 y=1,0805x + 0,00068 y=,96231x + 0,0013 y=1,0013x + 0,0013
July	"	Oct.	1911	.62636	.61798 .61975	.02147	.01908	y = .88867x + .06135
Oct.		Jan. April	1911	.61798	.62093	.01908	.01838	y = .96354x +.02430
Jan. April	**	July	**	. 62093	.62111	.01790	.01713	v = 95700v ± 02688
July	44	Oct.	и	.62111	.62327	.01713	.01877	v=1.09544x 05712
July Oct.	**	lan.	1912	.62327	.62105	.01877	.01824 .01839	y = .97189x + .01530
Jan.	1912	April		.62170 .62350	.62350 .62652	.01861	.01839	y = .98857x + .00891
April July	"	July Oct.	u	.62652	.63091	.01893	.01877	y = 1.02894x01502
Oct.	**	Jan.	1913	. 63091	.63086	.01877	.01893	v=1.00860x00548
Jan.	1913	April	"	.63056	.64419	.01904	.01888	y = .99181x + .01879
April	"	July Oct.	"	.64419	.65360	.01888	. 02094	y = 1.10875x06065
July	"	Oct.	1914	.65360	.64912 .64793	.02094	.02015	y = .96231x + .02015
Oct. Jan.		Jan. April	46	.64912 .64870	.64414	.01940	.01968	y = .9406/x +.03/32
April	"	July	"	.64414	.64767	.01968	01965	y = 1.01448x01395 y = .99827x + .00464
July	**	July Jan.	1915	.64767	.66251	.01965	.02208	
Jan.	1915	April	u	.66172	.66026	.02296	.02336	y=1.01717x01282 y=1.02241x00373 y=1.01504x01483 y=1.01504x01483 y=1.05110x00786 y=1.05110x00786 y=1.05110x00786 y=1.0512x03154 y=1.05467x02478 y=1.05467x02478 y=1.0547x02478 y=1.0547x02478 y=1.0547x02478 y=1.0547x02478 y=1.0547x02478 y=1.0547x02478 y=1.0547x03735 y=8.0547x03735 y=8.0547x03735 y=8.0547x03735 y=1.0541x03298 y=1.0541x03298 y=1.05404x03194 y=1.75680x + .14814 y=1.75680x + .14814 y=1.75680x + .03464
April	"	July Oct.	"	.66026	.67133	.02336	.02388	y = 1.02241x00373
Tuly	"	Oct.		.67133	.66658	.02388	.02424	y=1.01504x01485
Oct.		Jan. April	1916	.66658	.65037	.02424	.02297	y = .94/61x + .018/1
Jan. April	1910	July		65200	.65498	.02307	.02500	v = 1.08362x = .05154
July	"	Oct.	11	. 65498	.65007	,02500	.02387	y = .95467x + .02478
Oct.	"	Jan. April	1917	.65007	.63998 .66193	.02387	.02433	y = 1.01917x02255
Jan.	1917	April	"	.64020 .66193	.66193	.02484	.02706	y=1.08932x03545
April July	**	July Oct.	44	.68315	.69954	.02706	.02708	y = .98530x +.03093
Oct.	**	Jan.	1918	.69954	.71617	.02708	.03083	v=1.13814x08000
Jan.	1918	April		.71617	.72312	.03083	.02737	y = .88793x + .08721
April	"	July	"	.72312	.72702	.02737	.02893	y = 1.05705x03735
July	"	Oct. Jan.	1919	.72702	.72139 .70505	.02893	.02565	y = .88049X +.07089
Oct. Jan.		April	**	70505	.71861	.02055	.02323	v=1.13041x07839
April	"	Ilulv	**	.72139 .70505 .71861	.71983	.02323	.02220	y = .95581x + .03298
July	"	Oct.	"	. 71983	.72624	.02220	.02572	y = 1.15849x10768
Oct.	••	Han.	1920	.72624 .74076	.74076 .77127	.02572	.02802	y=1.08949x05047
Jan. April	1920	April July	**	77127	78295	.03304	.03450	y=1.17903x10213
July	"	Oct.	44	.78295	.74068	.03450	.02611	y = .75680x + .14814
Oct.	"	Ian.	1921	.74068	.74612	.02611	.02811	y = 1.07646x05119
Jan.	1921	April	"	.74612	.75554	.02811	.02718	y = .96700x + .03404
April July	**	Oct	4	.75554 .75561	.75561 .73978	.02718	.02299	y=1.00256x00186 y=.84380x+.10220
Oct.	**	July Oct. Jan.	1922	.73978	.69907	.02299	,02668	y=1,16027x -,15927
Jan.	1922	April	""	.69907	.68695	.02668	.02197	y = .82374x + .11110
April	"	July Oct.	"	.68695	.67500	.02197	.02380	y=1.08308x06902
July Oct.	"	Oct. Jan.	1923	.67500 .68007	.68007 .68595	.02380	.01998	y = .83938x +.11349
Jan.		April	"	.68595	.70285	.02050	.02070	v=1.00973x+.01023
April	**	July	44	.70285	.69754	.02070	.02163	y = 1.04467x03671
Tulv	"	July Oct.	44	.69754	.70020	.02163	.02003	y = .92605x + .05424
Oct.	1004	Jan. April	1924	.70020 .69417	.69417 .69251	.02003	.01813	y = .90539x + .06022
Jan. April	1924	July	44	.69251	.67561	.01703	.01703	v = .97812x00175
July	**	Oct.	**	.67561	.67629	.01665	.01597	y = 1, 00250x - 00189 y = 1, 16027x - 0189 y = 1, 16027x - 1, 15027 y = 1, 832374x + 1, 11110 y = 1, 83238x - 1, 1143 y = 1, 83238x - 1, 1143 y = 1, 00250x - 00602 y = 1, 00250x - 00602 y = 1, 00250x - 00602 y = 1, 00250x - 00642 y = 1, 100250x - 00623 y = 1, 100250x - 00623 y = 1, 00650x - 00623 y = 1, 006
Oct.	"	Ian.	1925	.67629	. 67888	01597	.01425	y = .89228x + .07544
Jan.	1925	April	"	.68471	.67962 .67911	.01854	.02152	y = 1.16085x11523
April	**	July Oct.	"	.67962 .67911	.68182	.02152 .01891	.01891	y = .8/884X + .08183
July Oct.	"	llan.	1926	.68182	.67258	.01628	.01660	y=1.01952x02255
Jan.	1926	April		.67344	.66482	.01774	.01773	y = .99956x00832
April	"	July	u	.66482	.66369	.01773	.01585	y = .89394x + .06938
July	"	Oct.	1927	.66369	.66380	.01585 .01552	.01552 .01670	y = .97924x +.01389
Oct. Jan.	1925	Jan. April July Oct.	14	.66380	.65511 .64700	.01749	.01963	v=1.12249x=.0907
April		July	**	.64700	. 64984	.01963	.02009	y=1.02336x01227
July	**	Oct.	"	.64984	.63718	.02009	.01829	y = .91052x + .04549

A138

APPENDIX

TABLE 8—American Railroad Bond Yields¹, Quarterly, January 1857-January 1936. Mathematical Functions and Equations—(Concluded)

		IDENT:		ARITHMETIC OF LOGS O	Averages of Yields		DEVIATIONS OF YIELDS	SIGMA EQUATIONS OF STRAIGHT LINES FITTED TO LOGARITHMS OF YIELDS
x (ea		y (l da	ater .te)	Mx	My	σx	σу	$y = a + \frac{\sigma_y}{\sigma_x} x$
Oct.	1927	Ian.	1928	.63718	.63004	.01829	.01613	y = .88153x+.06835
Ian.	1928		и	.63144	.63600	.01638	.01431	y = .87383x + .08423
Apr.	44	July	"	.63600	.65672	.01431	.01589	y = 1.11024x04939
July	45	Oct.	"	.65672	.65630	.01589	.01463	y = .92069x + .05166
Oct.	44	Ian.	1929	.65630	.66302	.01463	.01460	y = .99836x + .00780
Ian.	1929	Apr.	"	.66302	.67051	.01460	.01535	y = 1.05123x02648
Apr.	"	July	"	.67051	.67905	.01535	.01553	y = 1.01134x + .00094
July	44	Oct.	"	.67905	.67623	.01553	.01381	y = .88972x + .07207
Oct.	**	Jan.	1930	.67623	.66328	.01381	.01533	y = 1.10980x08720
Jan.	1930		и	.65593	.65143	.00936	.00860	y = .91858x + .04891
Apr.	и	July	"	.65143	.64218	.00860	.01017	y = 1.18275x12830 y = 1.18034x12781
July	**	Oct.	"	.64218	.63018	.01017	.01200	
Oct.	**	Jan₊	1931	.63018	.62939	.01200	.01272	y = 1.05979x03847 y = 1.12983x07896
Jan.	1931	Apr.	44	.64041	.64459	.02114	.02389	
Apr.	"	July	"	.64459	.64390	.02389	.05307	
July	"	Oct.		.64390	.71349	.02893	.05491	y = 1.83413x46751 y = 1.03468x + .01467
Oct.		Jan.	1932	.71349	.75290	.05307	.04876	v = 1.16126x09958
Jan.	1932	Apr.	61	.73806	.75750	.04199	.05858	v = 1.20142x14139
Apr.	"	July	"	.75750	.76869	.04876	.04266	
July	- 66	Oct.		.76869	.71272	.05858	.05875	y = .72832x + .15287 y = 1.37703x27303
Oct.		Jan.	1933	.71272	.75835	.05698	.06489	v = 1,13882x05198
Jan.	1933	Apr.	"	.71155	.68545	.05698	.04367	v = .67298x + .17510
Apr.	"	July	"	.75835	.08345	.04367	.05580	y = 1.27780x17284
July	"	Oct.		.68545	68790	.05580	.03380	y = .86149x + .08225
Oct.		Jan.	1934	.70303	.63918	.04557	.03338	v = .73254x + .13951
Jan.	1934	Apr.	"	.63918	62579	.03338	.03535	v = 1.05907x05115
Apr.	"	July	"	.62579	.63636	.03535	.03333	v = 1.10718x05650
July	"	Oct.	1935	.63636	.60821	.03914	.03934	v = 1.00517x03144
Oct.		Jan.	1935	.60821	.61239	.03914	.05105	y = 1.00317x03144 y = 1.29756x17680
Jan.	1935	Apr.	**	.61239	.59964	.05105	.04401	v = .86215x+.07167
Apr.	44	July Oct.	**	.59964	.61125	.03103	.04483	v = 1.01853x + .00050
July Oct.		Jan.	1936		59093	.04483	.04149	y = .92555x + .00030
OCL.		jall.	1930	01123	,59093	09900	.04149	3 - 172000X T.02019

Note 1. These are the yields in Table 3.

Note 2. The variables are the logarithms of bond yields. The first two columns give, of course, only the dates to which the yields relate.

Note 3. For a description of the nature of these equations see Ch. IV.

Month 10 Month Slopes $\binom{\sigma y}{\sigma x}$ of 'Sigma Lines' Fitted to the Logarhums of the Yields of American Railroad Bonds Month 1036. TABLE 9

Month to Month Slores $\left(\frac{ey}{ex}\right)$ of 'Sigma Lines' Fitted to the Locarthuss of the Vields of American Railroad Bonds January 1936 TABLE 9 (Concluded)

 . 99707 1.12336 1.9329 1.02340 1.07343 1.121094 1.14488 1.121094 1.14488 1.121094 1.159413 1.25041
1.01268 1.002676 1.00469 1.05506 1.05506 99707 93420 1.21094 1.25031

TABLE 10

SHORT TIME INTEREST RATES, BOND YIELDS AND STOCK PRICES

- Col. 1 Call Money Rates at the New York Stock Exchange.
- Col. 2 90-day Time Money Rates in New York City.
- Col. 3 Commercial Paper Rates in New York City. (January 1857 to December 1923 'choice 60-90 day two name paper'; January 1924 to January 1936 '4 to 6 month prime double and single name paper').
- Col. 4 Unadjusted Index Number of the Yields of American Railroad Bonds.
- Col. 5 Adjusted Index Number of the Yields of American Railroad Bonds.¹
- Col. 6 Index Number of the Prices of American Railroad Stocks weighted by the number of shares outstanding at the beginning of each year.

The long time reonomic 'drift' has been eliminated from this index number. The month to month movements are almost identical with the month to month movements of the unadjusted index given in Column 4, whereas the long time movements are the long time movements of the '4.50 Sigma' index given in Table 6.

TABLE 10

Date	1 Call Money	2 Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1857 J F M A M J J A S O N D	8.00 8.75 9.25 7.88 7.38 6.60 6.75 9.50 15.00 18.00 8.00 7.00		8.81 8.81 9.25 9.00 8.19 7.90 8.50 10.00 18.00 24.00 11.50 8.00	9.644 9.577 9.592 9.627 9.731 9.949 9.991 10.086 11.128 11.926 11.105	6.621 6.577 6.592 6.619 6.696 6.849 6.882 6.952 7.674 8.230 7.668 7.367	21.22 20.83 20.82 20.41 20.10 18.87 18.61 17.70 15.14 12.83 14.65 15.27
1858 F M A M J A S O N D	6.50 4.88 4.44 4.20 3.50 3.60 3.50 4.12 3.55 4.05 4.00		7.50 5.75 5.50 5.19 3.64 4.31 3.71 4.05 4.44 4.69 4.69	10,376 9,857 9,525 9,478 9,377 9,323 9,260 9,255 9,149 8,907 8,802 8,774	7.175 6.820 6.595 6.566 6.566 6.467 6.425 6.427 6.356 6.192 6.122 6.107	15.69 17.16 17.45 16.56 16.82 16.10 15.17 15.98 15.78 16.25 16.16
1859 J F M A J J A S O N D	4.31 5.00 4.54 4.50 5.88 5.96 6.38 5.96 6.03 5.25 5.81		4.62 5.50 5.17 5.28 6.47 6.89 6.62 7.04 6.54 6.75 6.19 6.75	8.776 8.758 8.757 8.726 8.887 9.120 9.110 9.047 8.868 8.992 8.969 8.935	6.111 6.101 6.105 6.086 6.202 6.368 6.364 6.323 6.199 6.240 6.275 6.255	15.93 15.73 15.66 15.28 14.80 14.91 14.98 15.10 15.70 15.40
1860 J F M A M J J A S O N D	6.69 5.88 5.50 5.25 5.31 4.75 5.25 5.63 6.50 6.75 7.13 7.25		8.00 7.10 5.90 5.60 5.80 5.50 6.10 7.00 6.80 11.10 12.90	8.920 8.855 8.779 8.671 8.507 8.357 8.288 8.258 8.274 8.333 8.731 9.115	6.247 6.206 6.156 6.084 5.973 5.872 5.828 5.812 5.828 5.875 6.163 6.440	15.11 15.21 15.85 16.68 16.97 17.20 17.73 18.81 19.28 18.62 16.57 15.49

TABLE 10 (Continued)

Date	1 Call Money	Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1861 J F M A M J J A S O N D	5.75 5.50 5.75 5.13 6.25 5.50 4.50 5.75 6.50 6.50 6.50		8.00 7.30 6.10 6.20 8.10 6.50 6.50 6.30 6.80 6.30 7.00	8.781 8.687 8.604 8.676 9.130 9.055 8.812 8.833 8.963 9.042 8.971 8.952	6.210 6.153 6.101 6.160 6.492 6.449 6.285 6.310 6.415 6.482 6.442 6.440	17.09 17.02 17.41 16.09 14.86 15.01 15.63 15.30 15.27 15.86 16.06 15.59
1862 J F M A M J J A S O N D	6.50 6.00 5.50 5.50 4.60 4.10 5.40 4.00 4.30 6.30 6.00		6.30 5.90 6.30 6.10 5.00 4.50 5.50 4.50 5.00 4.50 5.50	8.513 8.172 8.235 8.164 7.734 7.519 7.569 7.400 7.149 6.863 6.700 6.741	6.136 5.902 5.959 5.920 5.621 5.476 5.525 5.414 5.244 5.045 4.939 4.981	16.54 17.12 17.65 17.51 18.34 19.23 18.80 19.44 20.83 22.89 23.08 23.54
1863 J F M A M J J A S O ND	6.10 6.30 6.10 5.20 5.30 6.10 6.00 6.60 0.50 7.00		5.30 5.70 5.30 5.30 5.40 5.60 5.60 5.70 6.60 6.80	6.189 5.979 6.059 6.325 6.324 6.381 6.432 6.450 6.440 6.379 6.506 6.617	4.585 4.440 4.510 4.721 4.730 4.785 4.835 4.863 4.863 4.863 5.032	26.60 27.53 27.04 27.36 29.96 29.01 29.69 31.79 31.83 32.69 32.78 32.49
1864 J F M A M J J A S O N D	7.00 6.10 5.90 6.80 5.60 6.70 0.80 6.90 7.00 6.80 6.90 6.60		7.30 6.50 5.60 6.70 6.90 6.80 6.50 7.70 9.00 9.20 8.30 7.80	6.702 6.645 6.424 6.170 6.145 6.024 5.651 5.660 6.074 6.549 6.658	5.107 5.076 4.917 4.734 4.724 4.642 4.363 4.379 4.710 5.089 5.045 5.194	33 .86 35 .48 37 .99 38 .68 36 .99 37 .69 37 .34 37 .62 33 .14 34 .88 34 .58

TABLE 10 (Continued)

Date	1 Call Money	Time Money	3 Coml. Paper	Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1865 J F M A M J J A S O N D	7.00 6.10 7.00 5.60 5.40 4.90 5.50 5.90 6.00 7.00 6.80 6.80		8.00 8.50 9.00 8.50 7.20 6.70 7.30 7.70 7.10 7.60 8.00 7.80	6.908 7.100 7.468 7.577 7.537 7.846 7.701 7.734 7.781 7.871 7.993 8.050	5.401 5.562 5.860 5.957 5.935 6.190 6.086 6.121 6.166 6.247 6.353 6.408	32.93 32.16 29.17 28.75 29.39 28.83 30.07 29.73 30.95 31.84 32.12 31.65
1866 J F M A M J J A S O N D	5.50 6.06 5.56 5.38 5.40 4.88 4.13 4.19 4.35 6.00 6.38		7.37 7.28 7.32 6.69 6.05 5.56 5.89 5.25 5.45 6.69 6.88	8.143 8.189 8.272 8.202 8.039 7.990 7.873 7.804 7.751 7.718 7.668 7.790	6.491 6.534 6.607 6.558 6.434 6.400 6.311 6.259 6.222 6.197 6.160 6.259	30.20 29.44 29.54 30.03 30.65 31.05 31.59 32.80 32.95 33.45 32.78
1867 J F M A M J J A S O N D	7.18 5.81 6.06 6.19 4.80 6.19 4.50 4.25 5.63 10.76 7.22 6.50		7.40 7.06 7.19 7.17 6.67 7.38 6.55 6.50 7.12 8.40 8.56 7.94	7.822 7.844 7.856 7.913 7.932 7.928 7.784 7.768 7.784 7.875 7.953	6.288 6.307 6.317 6.364 6.380 6.375 6.259 6.245 6.257 6.330 6.390 6.415	31.51 31.22 31.01 30.33 30.68 31.74 32.88 33.03 32.98 32.91 32.81 33.29
1868 J F M A M J J A S O N D	5.65 4.69 9.35 11.53 5.50 3.50 4.15 3.75 4.87 9.04 17.03 11.40		7.06 6.50 7.67 8.00 6.62 5.72 6.50 6.62 6.75 7.44 10.00 8.25	7.859 7.770 7.743 7.780 7.725 7.699 7.692 7.711 7.788 7.869 7.959 8.031	6.312 6.239 6.216 6.245 6.109 6.176 6.169 6.183 6.245 6.308 6.308 6.380 6.437	34.50 35.30 35.12 34.91 36.12 36.72 36.34 36.66 37.21 36.16 36.88

TABLE 10 (Continued)

Date	1 Call Money	Time Money	3 Coml. Paper	Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1869 J F M A M J J A S O N D	12.02 6.74 9.02 9.73 6.75 23.67 9.79 6.38 19.54 5.63 6.25 7.96		8.31 7.69 9.40 9.88 7.81 9.65 10.25 9.56 10.94 10.38 11.94 10.17	8.036 8.048 8.103 8.133 8.021 8.003 8.084 8.065 8.150 8.264 8.350	6.439 6.449 6.494 6.518 6.428 6.418 6.483 6.471 6.545 6.630 6.676 6.717	38.23 38.52 38.23 38.89 40.59 40.96 40.87 41.44 38.75 38.44 38.16 37.52
1870 J F M A M J A S O N D	6.19 5.50 5.15 5.63 4.56 4.20 5.06 4.70 5.50 5.25 5.50 11.45		9.00 7.38 7.50 7.19 6.38 5.46 6.38 7.18 7.25 7.28 7.25 8.75	8.263 8.006 7.901 7.934 7.862 7.797 7.781 7.862 7.888 7.903 7.919 7.959	6.651 6.451 6.371 6.403 6.350 6.304 6.297 6.368 6.394 6.412 6.413 6.468	38.07 39.29 39.05 39.66 41.22 41.54 40.27 39.54 39.89 40.06 39.61
1871 J F M A M J A S O N D	6.49 4.13 4.20 5.84 3.55 3.00 3.25 2.80 4.44 12.36 6.35 10.25		7.22 6.62 6.25 6.78 5.50 5.06 4.90 5.52 6.66 10.03 9.28 9.94	7.890 7.841 7.819 7.797 7.741 7.730 7.720 7.681 7.654 7.797 7.850 7.788	6.418 6.383 6.369 6.355 6.312 6.307 6.307 6.270 6.250 6.368 6.412 6.359	39.70 40.11 40.97 42.05 43.00 42.69 41.91 42.18 40.25 40.58 41.38
1872 J F M A M J A S O N D	8.78 6.93 8.44 13.68 6.20 4.50 3.65 3.81 10.33 6.43 7.73 20.06		8.30 7.56 8.62 8.66 7.20 6.00 6.45 7.56 10.00 10.80 11.62 10.83	7.562 7.522 7.614 7.600 7.601 7.556 7.462 7.541 7.619 7.672 7.727 7.742	6.174 6.139 6.213 6.199 6.196 6.155 6.074 6.181 6.189 6.224 6.262 6.266	42.29 42.55 43.87 45.20 45.03 44.56 44.19 43.57 43.03 42.95 42.68 43.82

TABLE 10 (Continued)

	1	2	3	4	5	6
Date	Call Money	Time Money	Coml. Pape	Unadj. Bonds	Adjust. Bonds	Stock Prices
1873 J F M A M J J A S O N D	7.20 10.30 13.26 27.52 6.09 4.63 3.80 4.63 61.23 14.91 9.40 7.88		9.28 9.38 10.12 11.40 8.12 6.83 6.44 7.06 14.28 16.50 14.50 9.80	7.658 7.640 7.657 7.657 7.692 7.671 7.576 7.589 7.734 8.150 8.179 7.953	6.190 6.166 6.170 6.187 6.160 6.118 6.062 6.062 6.166 6.486 6.497 6.304	44.25 44.79 44.42 43.66 43.73 43.36 43.21 42.98 39.74 36.42 35.11 38.28
1874 J F M A J J A S O N D	5.50 4.13 4.00 4.15 3.13 2.50 2.75 2.50 2.70 2.94 3.80		7.44 6.00 6.14 6.25 5.66 5.61 5.44 6.25 5.81 5.62 6.00	7.685 7.570 7.568 7.553 7.620 7.557 7.557 7.557 7.525 7.456 7.350 7.338	6.080 5.979 5.966 5.943 5.985 5.927 5.921 5.900 5.872 5.809 5.720 5.703	40.36 41.47 40.73 39.62 38.60 38.23 38.29 38.52 39.09 38.96 39.05 39.10
1875 J F M A J J A S O N D	2.75 2.50 3.95 3.50 2.75 2.35 2.50 2.19 2.35 3.31 4.00 5.17		5.25 5.19 5.90 5.44 4.56 4.55 4.31 4.94 5.89 6.31 6.39 6.61	7.255 7.214 7.195 7.105 7.056 7.091 7.024 7.006 6.956 6.947 6.867	5.631 5.595 5.573 5.499 5.458 5.480 5.425 5.410 5.369 5.400 5.299	39.41 39.27 39.64 40.06 38.33 37.62 37.65 37.80 37.42 36.90 37.38 37.38
1876 J F M A J J A S O N D	5.83 3.63 3.75 3.69 3.20 2.56 2.06 1.70 1.94 3.00 3.85 5.00		6.44 5.33 5.39 5.50 5.05 4.75 3.81 3.60 4.75 5.44 5.88	6.795 6.722 6.674 6.705 6.736 6.699 6.616 6.575 6.672 6.675 6.658 6.652	5.243 5.188 5.152 5.177 5.204 5.178 5.117 5.089 5.169 5.175 5.165	38 . 29 38 . 87 39 . 02 37 . 48 35 . 93 35 . 62 33 . 65 31 . 71 31 . 39 30 . 72 30 . 55

TABLE 10 (Continued)

	To (Continued)							
Date	Call Money	2 Time Money	3 Coml. Paper	Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices		
1877 J F M A J J A S O N D	5.37 3.31 2.94 3.69 2.45 1.75 1.75 3.40 4.31 6.10 5.38 6.00		5.55 4.50 4.44 4.38 4.00 4.06 4.14 5.64 6.38 7.25 6.19 5.62	6.607 6.649 6.737 6.749 6.690 6.605 6.538 6.569 6.588 6.618 6.596 6.547	5.135 5.172 5.247 5.260 5.220 5.159 5.112 5.143 5.164 5.193 5.182 5.149	30 .29 28 .39 27 .05 25 .07 24 .99 23 .59 24 .39 25 .97 27 .70 28 .48 27 .97 27 .84		
1878 J F M A J J A S O N D	9.76 4.75 4.88 6.18 3.50 2.56 1.75 1.81 2.31 5.00 3.81 4.38		5.85 5.31 5.12 5.36 4.53 3.81 3.60 3.81 4.62 5.45 5.12	6.543 6.533 6.534 6.529 6.486 6.404 6.399 6.440 6.431 6.397 6.349 6.322	5.152 5.149 5.156 5.157 5.127 5.069 5.069 5.105 5.103 5.079 5.043 5.026	27. 84 27. 28 27. 75 28. 61 28. 62 29. 39 29. 91 29. 56 30. 20 29. 91 29. 80 29. 69		
1879 J F M A J J A S O N D	3.05 3.06 4.50 4.40 3.81 3.31 2.95 7.85 5.50 12.34 8.73 5.80		4.33 3.81 5.06 5.45 4.44 4.25 3.90 5.56 5.78 5.94 6.25 5.95	6.188 6.018 6.118 6.117 5.974 5.918 5.864 5.857 5.961 5.945 5.921 5.876	4.922 4.789 4.869 4.870 4.758 4.715 4.673 4.668 4.751 4.739 4.720 4.685	31.15 32.33 31.66 32.66 34.33 34.86 35.46 35.95 37.25 41.17 43.29 43.43		
1880 J F M A M J J A S O N D	5.00 4.63 7.28 6.55 4.06 3.00 2.50 2.70 2.88 6.05 11.20		5.38 5.31 5.50 5.50 5.19 4.55 4.44 5.03 5.25 5.12 5.44 6.00	5.824 5.750 5.734 5.747 5.736 5.691 5.600 5.543 5.505 5.453 5.326 5.243	4.643 4.585 4.571 4.580 4.572 4.535 4.463 4.417 4.486 4.344 4.243 4.176	45.26 46.22 46.97 46.35 42.59 42.62 44.61 46.52 46.49 48.14 51.12 53.69		

TABLE 10 (Continued)

Date	I Call Money	2 Time Money	3 Coml. Paper	Unadj. Bonds	5 Adjust. Bonds	Stock Prices
1881 J F M A M J A S O N D	4.81 15.91 7.48 4.44 3.38 3.15 3.44 4.65 5.25 5.44 5.20 6.00		5.25 5.38 5.55 5.19 4.06 3.50 4.00 4.95 5.69 6.25 6.30 6.25	5.194 5.249 5.302 5.283 5.144 5.064 5.066 5.100 5.199 5.250 5.221 5.250	4.137 4.181 4.224 4.209 4.099 4.036 4.038 4.071 4.147 4.189 4.168 4.192	56.38 55.77 56.51 58.51 59.00 50.80 55.74 56.12 55.25 55.61 54.03
1882 J F M A M J A S O N D	5.43 4.50 4.65 4.06 3.00 3.56 3.00 3.95 7.25 5.50 7.80 4.63		5.50 5.47 5.64 5.06 4.85 5.12 4.62 5.65 6.75 6.67 6.50 5.88	5.242 5.273 5.288 5.240 5.209 5.212 5.190 5.226 5.246 5.232 5.255 5.255	4.187 4.214 4.236 4.192 4.170 4.174 4.159 4.190 4.208 4.200 4.221 4.219	53.12 51.89 51.60 50.98 50.68 53.68 55.86 54.46 52.18 52.50
1883 J F M A M J J A S O N D	4.50 4.13 10.38 6.06 3.55 2.00 2.13 2.50 2.44 2.70 2.00 2.13		5.50 5.38 6.38 5.81 5.35 5.50 4.78 5.61 6.00 6.00 5.69 5.50	5.205 5.241 5.259 5.233 5.228 5.223 5.219 5.258 5.262 5.249 5.211 5.185	4.185 4.217 4.234 4.216 4.213 4.211 4.210 4.243 4.249 4.240 4.210 4.192	52.35 51.05 51.73 52.95 51.88 52.36 51.40 49.11 49.72 48.45 49.10 48.13
1884 J F M A M J A S O N D	1.90 1.88 1.75 2.10 14.98 3.44 1.90 1.75 1.75 1.95 1.44 1.50		4.89 4.75 4.62 4.72 5.06 5.75 5.95 5.50 5.50 5.50 5.50 5.00	5.149 5.095 5.052 5.021 5.115 5.238 5.253 5.171 5.179 5.172 5.172 5.133	4.163 4.120 4.087 4.063 4.140 4.239 4.252 4.187 4.195 4.196 4.159	46.74 48.01 47.85 46.04 42.26 39.20 40.31 42.77 41.17 39.84 38.93 38.93

TABLE 10 (Continued)

Date	Call	Time	Coml.	4 Unadj.	5 Adjust.	6 Stock
	Money	Money	Paper	Bonds	Bonds	Prices
1885 J F M A J J A S O N D	1.19 1.44 1.31 1.35 1.44 1.19 1.35 1.50 2.13 2.69 2.75		4.69 4.47 3.97 3.68 3.55 3.50 3.68 3.75 4.00 4.44 4.50	5.076 5.033 4.987 4.974 4.953 4.892 4.856 4.846 4.829 4.732 4.749 4.723	4.113 4.079 4.042 4.033 4.017 3.967 3.939 3.931 3.918 3.880 3.853 3.853 3.833	38.12 39.13 39.29 39.22 38.63 38.33 39.98 42.10 41.55 43.82 46.61 46.43
1886 J F M A M J A S O N D	2.13 2.06 2.65 2.38 2.88 3.35 2.25 5.31 5.90 5.66 5.63 8.70		4.31 3.90 3.87 4.25 4.06 3.85 3.94 5.19 5.81 6.06 5.92 5.97	4.643 4.562 4.558 4.558 4.554 4.517 4.482 4.495 4.562 4.562 4.562 4.592	3.768 3.703 3.690 3.690 3.697 3.687 3.638 3.648 3.703 3.703 3.702 3.726	46.64 47.38 46.60 45.95 45.10 47.13 47.84 48.30 49.45 50.81 51.88 50.70
1887 J F M A M J A S O N D	4.19 3.56 5.05 6.13 5.13 7.20 4.75 5.15 5.13 4.19 4.60 5.00		5.50 4.81 5.35 5.38 5.21 5.13 6.19 6.35 6.94 6.38 5.75 6.00	4.564 4.575 4.595 4.595 4.601 4.586 4.592 4.615 4.656 4.745 4.777 4.734 4.715	3.708 3.710 3.725 3.729 3.715 3.718 3.735 3.765 3.835 3.835 3.835 3.821 3.803	50.11 49.71 50.85 52.20 53.06 51.71 50.38 49.07 48.43 46.57 47.26 47.10
1888 J F M A M J J A S O N D	3.69 2.70 2.75 2.63 1.80 1.50 1.44 1.55 2.81 2.60 2.56 4.13		5.60 4.85 5.22 5.40 4.82 4.25 4.08 4.36 5.28 5.07 4.75 4.97	4.643 4.614 4.638 4.640 4.620 4.595 4.541 4.535 4.572 4.582 4.582 4.564 4.551	3.742 3.716 3.732 3.731 3.731 3.690 3.644 3.637 3.664 3.671 3.655 3.643	47.32 46.92 45.16 45.31 45.88 44.10 45.40 46.02 47.32 46.82 45.39 44.55

TABLE 10 (Continued)

Date	1 Call Money	2 Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1889 J F M A J J A S O N D	3.30 2.31 3.06 3.88 2.55 3.00 3.55 3.88 4.81 8.30 7.13 8.00		4.65 4.25 4.50 4.29 3.85 3.88 4.40 5.16 5.28 6.00 6.00 6.09	4.499 4.445 4.457 4.448 4.396 4.347 4.372 4.383 4.383 4.487 4.475 4.491	3.599 3.555 3.565 3.557 3.516 3.476 3.506 3.512 3.551 3.583 3.597	45.19 45.56 44.31 44.05 45.21 45.71 44.54 45.63 47.20 46.74 46.68 46.47
1890 J F M A J A S O N D	7.70 4.25 4.25 4.30 4.88 4.75 4.60 11.63 6.75 5.00 7.00 5.00	4.80 4.94 5.06 4.50 5.20 5.00 4.85 6.00 6.25 6.00 7.00	5.35 5.03 5.50 5.11 5.06 5.05 5.50 5.75 5.90 6.75 7.33	4.472 4.474 4.494 4.495 4.404 4.512 4.525 4.564 4.590 4.618 4.676 4.732	3.584 3.588 3.607 3.611 3.613 3.632 3.645 3.705 3.733 3.784 3.832	46.93 46.45 46.14 47.14 49.03 48.63 48.14 46.96 46.07 43.96 41.11 40.45
1891 F M A M J A S O N D	3.90 2.88 2.88 3.30 4.38 3.25 2.20 2.13 4.50 4.25 4.38 2.94	5. 22 4. 38 4. 75 4. 20 5. 58 4. 50 4. 55 5. 78 5. 39 5. 00 4. 40	5.83 5.00 5.25 5.08 5.38 5.50 5.60 5.75 5.78 5.58 5.06 4.83	4.622 4.619 4.677 4.691 4.727 4.789 4.789 4.781 4.755 4.709 4.629	3.747 3.750 3.800 3.816 3.849 3.901 3.899 3.901 3.883 3.848 3.848 3.789	42.32 42.72 41.76 43.34 43.30 42.30 41.81 43.59 47.45 47.47 46.50 48.06
1892 J F M A M J A S O N D	2.40 2.00 2.00 2.00 1.50 1.40 1.88 2.05 4.13 5.63 5.15 6.81	3.31 3.12 3.55 2.88 2.62 2.70 3.00 2.95 4.50 5.50 5.50	4.16 3.69 3.98 3.47 3.16 2.95 3.47 3.96 4.71 5.16 5.14 5.50	4.577 4.547 4.554 4.533 4.508 4.492 4.477 4.486 4.531 4.529 4.558 4.556	3.749 3.726 3.734 3.720 3.701 3.689 3.679 3.687 3.725 3.724 3.732 3.746	48.62 48.53 49.14 48.85 48.26 48.32 48.64 47.08 47.93 47.39 46.84

TABLE 10 (Continued)

Date	1 Call Money	Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1893 J F M A M J A S O N D	4.00 3.00 8.20 4.88 3.60 8.88 7.75 5.50 3.75 2.38 1.70 1.16	4.88 4.12 5.90 5.86 6.08 8.75 7.40 5.75 4.88 3.40 2.62	5.10 4.97 6.80 5.75 6.69 8.47 10.88 10.60 8.28 5.91 4.38 3.66	4.531 4.498 4.534 4.539 4.594 4.670 4.824 4.940 4.726 4.622 4.554	3.726 3.697 3.727 3.731 3.775 3.836 3.962 4.056 3.930 3.878 3.791 3.734	47.70 46.71 45.12 45.42 42.14 40.17 36.58 35.85 37.85 38.47 39.22 38.08
1894 J F M A J A S O N D	1.02 1.00 1.09 1.13 1.10 1.00 1.00 1.00 1.00 1.00 1.03 1.44	2.61 2.56 2.50 2.50 2.00 1.88 2.00 2.45 2.38 2.00 2.39 2.38	3.48 3.30 3.03 3.10 2.93 2.91 3.00 3.07 3.28 2.76 2.79 2.88	4.547 4.493 4.452 4.403 4.408 4.413 4.430 4.405 4.374 4.334 4.303 4.302	3.727 3.681 3.688 3.606 3.607 3.611 3.623 3.602 3.576 3.542 3.516 3.514	37.31 37.80 38.90 39.22 37.63 36.95 36.33 37.68 38.53 37.32 37.22 36.77
1895 J F M A M J A S O N D	1.35 1.50 2.25 2.25 1.32 1.16 1.40 1.08 1.58 2.17 1.97	2.55 3.19 3.38 3.41 2.40 2.00 2.39 2.50 2.69 2.85 2.50 4.12	3.10 3.62 3.91 3.97 2.77 2.62 2.94 3.47 4.03 4.78 4.13 4.75	4.310 4.351 4.367 4.374 4.318 4.251 4.220 4.170 4.177 4.189 4.208 4.271	3.520 3.551 3.562 3.566 3.519 3.462 3.435 3.392 3.396 3.404 3.418 3.467	36.26 35.73 35.45 36.93 38.86 39.77 40.42 41.05 41.38 40.85 39.50 37.14
1896 J F M A M J J A S O N D	4.90 3.94 3.50 3.02 2.53 1.94 2.07 4.69 5.45 11.13 6.25 1.95	6.00 5.25 3.88 3.70 3.12 3.12 3.90 7.50 7.89 8.44 4.81 3.10	6.00 5.81 5.22 5.27 4.53 4.25 5.05 7.81 8.30 8.36 5.34 3.73	4.331 4.284 4.289 4.286 4.266 4.253 4.349 4.555 4.477 4.434 4.326 4.275	3.515 3.475 3.479 3.475 3.456 3.456 3.521 3.687 3.622 3.587 3.499 3.456	36.62 38.10 37.29 37.67 37.51 37.00 34.90 33.07 34.54 35.22 37.18

TABLE 10 (Continued)

Date	1 Call Money	2 Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1897 J F M A M J A S O N D	1.78 1.63 1.62 1.50 1.41 1.20 1.19 1.25 2.22 2.50 1.81 2.92	2.62 2.50 2.83 2.50 2.50 2.22 2.00 2.69 3.20 3.19 3.00 3.40	3.31 3.00 3.33 3.53 3.53 3.12 3.40 3.72 4.10 4.19 3.38 3.42	4.222 4.194 4.135 4.147 4.131 4.095 4.059 4.080 4.090 4.092 4.072 4.019	3.413 3.389 3.342 3.350 3.388 3.308 3.279 3.296 3.304 3.305 3.289 3.247	36.09 35.65 35.81 34.68 34.84 36.45 37.85 40.39 42.21 41.13 39.73 40.77
1898 J F M A M J A S O N D	2.50 1.78 2.17 2.97 1.95 1.25 1.70 3.78 2.25 2.10 2.41	2.88 2.69 4.60 5.81 3.72 2.78 2.56 2.95 3.69 2.69 2.90 3.00	3.25 3.12 4.65 5.75 4.65 3.24 3.66 3.64 4.11 3.30 3.03	3.996 4.000 4.093 4.189 4.145 4.083 4.033 4.002 4.021 3.989 3.949 3.911	3.228 3.233 3.308 3.386 3.351 3.302 3.262 3.262 3.238 3.254 3.229 3.168	41.72 41.52 39.63 38.77 41.16 42.66 42.67 44.47 44.65 43.78 44.73 47.26
1899 J F M A M J A S O N D	2.72 2.47 4.10 5.13 3.52 2.63 4.47 8.27 6.38 7.50 7.60	2.89 3.03 4.00 3.88 3.19 3.00 3.62 4.30 5.56 5.35 5.96 6.12	2.90 3.05 3.86 3.69 3.60 8.31 3.66 4.35 4.94 5.19 5.42 5.88	3.859 3.864 3.865 3.826 3.793 3.783 3.803 3.824 3.859 3.897 3.918 3.960	3.127 3.132 3.134 3.103 3.078 3.071 3.089 3.107 3.138 3.170 3.190 3.226	51.25 53.25 53.07 53.81 51.90 51.14 53.08 54.30 53.69 53.42 54.52 51.78
1900 J F M A M J J A S O N D	4.15 2.25 3.94 3.06 2.00 1.69 1.53 1.30 1.61 3.57 5.06 5.13	4.80 4.25 4.56 3.50 3.00 3.06 3.36 3.61 3.88 4.95 4.33 4.78	4.93 4.40 4.88 4.25 3.70 3.68 4.03 4.19 4.34 5.05 4.40 4.75	3.923 3.889 3.875 3.856 3.860 3.900 3.898 3.897 3.898 3.898 3.898 3.898 3.898	3.197 3.172 3.164 3.150 3.178 3.192 3.192 3.194 3.199 3.202 3.183 3.160	52.30 53.43 54.77 55.79 53.57 52.23 51.95 52.45 51.53 53.29 56.90 61.06

TABLE 10 (Continued)

Date	1 Call Money	Time Money	3 Coml. Paper	Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1901 J F M A M J J A S S O N D	3.07 2.00 2.34 4.30 6.88 4.31 4.30 2.44 4.34 3.55 4.19 6.25	3.83 3.25 3.28 4.14 4.36 3.56 4.33 4.38 5.06 4.65 4.69 5.19	4.03 3.69 3.75 3.97 3.97 3.94 4.30 4.50 4.94 4.65 4.72 4.94	3.824 3.804 3.801 3.808 3.835 3.835 3.838 3.853 3.853 3.853 3.853 3.853 3.853 3.853	3.152 3.140 3.141 3.151 3.172 3.190 3.208 3.217 3.219 3.200 3.205	63.53 66.01 68.29 74.36 71.47 78.33 72.17 73.03 74.44 74.84 77.86
1902 J F M A M J A S O N D	4.57 2.38 3.94 5.10 5.56 2.84 3.52 3.78 10.80 7.63 4.88 6.81	4.53 4.00 4.00 1.25 4.75 4.35 4.60 4.72 7.83 7.44 6.44 6.80	4.50 4.00 4.34 4.48 4.53 4.44 4.62 4.84 5.61 5.94 5.75 6.00	3.8i0 3.801 3.799 3.791 3.804 3.818 3.833 3.848 3.863 3.997 3.996 3.928	3.198 3.197 3.201 3.200 3.217 3.234 3.252 3.271 3.290 3.325 3.339 3.364	77.94 78.52 78.62 81.64 81.95 82.25 85.32 87.91 88.01 85.11 81.89 80.29
1903 J F M A M J J A S O N D	5.75 2.88 6.00 4.19 2.44 3.05 2.50 2.03 2.32 2.69 5.19 5.50	4.97 4.59 5.63 4.96 3.92 4.28 4.58 4.91 5.25 5.00 5.81 5.23	5.12 4.48 5.61 5.22 4.75 5.08 5.44 6.00 5.84 5.97 5.85	3.918 3.932 3.978 4.011 3.991 4.024 4.070 4.115 4.118 4.074 4.040 4.047	3.362 3.380 3.427 3.462 3.451 3.486 3.532 3.578 3.556 3.554 3.530 3.542	84.23 82.75 78.98 75.56 74.35 70.38 68.43 66.42 65.50 64.09 64.35 66.84
1904 J F M A M J A S O N D	2.34 1.81 1.75 1.38 1.55 1.13 1.03 0.90 1.53 2.03 2.80 3.13	4.03 3.69 3.17 2.69 2.61 2.31 2.44 2.35 3.25 3.50 3.75 3.59	4.88 4.78 4.68 4.06 3.92 3.61 3.53 3.88 4.31 4.40 4.13 4.28	4.035 4.044 4.056 4.032 4.016 3.992 3.953 3.941 3.936 3.926 3.926 3.915	3.537 3.550 3.565 3.549 3.539 3.522 3.491 3.484 3.490 3.487 3.480 3.473	67.85 65.83 65.75 67.44 66.03 69.08 71.42 74.64 78.91 82.25 83.53

TABLE 10 (Continued)

Date	1 Call Money	Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	Stock Prices
1905 J F M A J J A S O N D	2.25 2.19 3.20 3.25 2.42 2.50 2.31 2.05 3.56 5.31 7.70 16.50	2.93 3.10 3.24 3.44 3.18 3.07 3.00 3.28 4.28 4.90 5.71 6.00	3.97 3.83 3.93 3.97 3.98 3.75 4.12 4.20 4.72 4.95 5.58	3.885 3.874 3.886 3.893 3.899 3.894 3.882 3.885 3.885 3.912 3.023	3.449 3.441 3.453 3.461 3.467 3.464 3.455 3.458 3.459 3.460 3.483 3.491	86.05 90.39 93.01 91.58 87.13 88.72 91.53 95.46 96.30 97.38 96.18 96.94
1906 J F M A M J A S O N D	8.65 4.63 4.88 9.50 4.15 3.25 2.97 4.44 9.38 5.15 7.50 14.00	5.08 5.25 5.22 5.69 4.95 4.38 4.50 5.39 7.19 6.13 7.19 7.88	5.05 5.03 5.28 5.44 5.32 5.46 5.96 6.50 6.30 6.25 6.25	3.912 3.932 3.966 3.986 4.003 3.990 4.005 4.027 4.056 4.045 4.038 4.054	3.482 3.499 3.529 3.545 3.559 3.557 3.658 3.676 3.600 3.588 3.581 3.594	99.84 99.42 97.61 96.25 93.78 95.57 93.78 100.85 103.95 102.91 102.46 101.57
1907 J F M A M J J A S O N D	6.15 4.38 6.38 2.35 2.31 3.13 4.55 3.06 4.00 21.00 12.25 14.60	5.78 5.25 6.22 4.42 3.97 4.44 5.10 6.41 5.72 8.05 13.50 10.00	6.15 5.94 6.18 5.94 5.47 5.45 6.25 6.81 7.10 7.25 7.83	4.065 4.088 4.159 4.159 4.181 4.233 4.231 4.286 4.340 4.419 4.590 4.474	3.602 3.621 3.683 3.681 3.700 3.745 3.742 3.791 3.840 3.900 4.062 3.959	98.16 94.50 85.02 85.58 82.88 80.67 83.71 78.97 79.01 72.08 67.87 71.03
1908 J F M A M J A S O N	4.75 1.81 1.85 1.72 1.66 1.52 1.22 1.06 1.35 1.44 1.75	5.36 4.22 3.57 2.85 2.91 2.32 2.29 2.56 2.57 3.10 3.31 3.20	6.47 5.06 5.68 4.46 3.94 3.64 3.75 3.60 3.93 4.06 4.03 3.85	4.316 4.302 4.335 4.303 4.261 4.255 4.230 4.185 4.151 4.140 4.102 4.083	3.820 3.810 3.841 3.814 3.779 3.777 3.757 3.757 3.693 3.686 3.657 3.643	73.71 70.93 72.98 76.37 80.74 80.93 83.18 85.95 85.40 94.28

TABLE 10 (Continued)

	1	2 1	3	4	5	1 6
Date	Call Money	Time Money	Coml. Paper	Unadj. Bonds	Adjust, Bonds	Stock Prices
1909 J F M A M J J A S O N D	1.81 2.25 1.85 1.94 1.84 1.87 2.06 2.17 2.69 4.31 4.65 5.03	2.66 2.78 2.65 2.47 2.60 2.55 2.38 3.74 4.75 4.86 4.64	3.72 3.53 3.50 3.50 3.44 3.25 3.38 4.04 4.18 5.03 5.05 5.11	4.058 4.031 4.042 4.046 4.041 4.058 4.052 4.063 4.083 4.097 4.111 4.116	3.625 3.605 3.620 3.627 3.628 3.648 3.648 3.662 3.685 3.702 3.719 3.727	95.52 93.55 94.98 98.63 100.81 102.21 103.88 105.83 105.29 105.01 103.10 104.45
1910 J F M A M J J A S O ND	4.72 2.78 2.88 3.28 3.63 2.77 2.41 1.55 2.00 3.13 3.23 3.38	4.31 3.69 3.90 4.09 3.93 3.40 3.96 3.78 4.22 4.78 4.50 3.91	4.75 4.44 4.50 4.75 4.75 4.92 5.38 5.43 5.53 5.50 4.66	4.116 4.121 4.140 4.183 4.201 4.218 4.240 4.232 4.183 4.158 4.187 4.184	3.732 3.739 3.761 3.804 3.824 3.842 3.866 3.863 3.820 3.801 3.830 3.829	102.59 99.40 101.71 99.66 98.32 93.56 88.91 90.79 91.21 95.00 94.10 91.88
1911 J F M A M J A S O N D	3.18 2.28 2.28 2.30 2.31 2.40 2.36 2.31 2.28 2.33 2.72 4.03	3.38 3.14 2.86 2.75 2.78 2.81 2.88 3.20 3.50 3.62 4.12	3.99 4.06 3.90 3.65 3.62 3.68 3.78 4.19 4.53 4.36 3.94 4.62	4.174 4.177 4.191 4.186 4.173 4.182 4.187 4.200 4.217 4.209 4.188 4.195	3.823 3.827 3.842 3.840 3.829 3.839 3.844 3.857 3.873 3.866 3.847 3.853	94.25 95.43 94.45 94.34 95.95 98.23 98.17 93.71 80.02 90.37 93.80 93.37
1912 J F M A M J A S O N D	2.42 2.28 2.42 3.03 2.75 2.75 2.88 4.63 5.33 6.38 6.50	2.95 2.89 3.44 3.50 3.19 3.12 3.58 4.10 5.50 5.75 5.88 5.87	3.90 3.75 4.19 4.14 4.19 4.00 4.52 5.00 5.56 5.93 5.72 6.00	4.187 4.178 4.195 4.204 4.210 4.224 4.234 4.257 4.279 4.276 4.275 4.291	3.846 3.837 3.852 3.860 3.865 3.876 3.885 3.905 3.923 3.919 3.917 3.931	93.20 92.31 94.17 96.46 95.70 95.25 95.28 97.62 97.10 96.42 93.78

TABLE 10 (Continued)

		1.11	ILLE TO (COL	temacay		
Date	1 Call Money	Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1913 J F M A M J J A S O N D	3.01 3.31 4.19 3.43 2.75 2.28 2.22 2.25 2.89 3.61 3.75 4.58	4.11 4.53 5.37 4.30 3.94 4.13 4.54 4.50 4.62 5.04 4.94 5.03	4.81 4.90 5.76 5.52 5.35 5.88 6.04 6.00 5.81 5.66 5.56	4.276 4.292 4.362 4.413 4.464 4.512 4.510 4.467 4.427 4.427 4.427 4.533	3.916 3.930 3.992 4.037 4.083 4.127 4.124 4.083 4.045 4.078 4.128 4.138	93.22 90.75 88.94 88.76 86.25 82.31 83.35 84.64 84.96 82.94 81.08 80.88
1914 F M A M J A S O N D	2.57 1.78 1.90 1.82 1.78 1.85 2.74 6.25 6.00 6.00 5.41 3.38	3.67 3.03 3.00 2.81 2.44 2.54 3.66 7.63 6.90 6.50 5.22 3.87	4.53 3.85 3.84 3.74 3.88 3.88 4.44 6.34 6.70 6.44 5.50 4.35	4.451 4.383 4.405 4.406 4.394 4.441 * * 4.657	4.062 3.998 4.016 4.014 4.012 4.000 4.041 * * *	83.38 83.99 81.68 79.77 80.28 79.55 75.72 *
1915 J F M A J J A S O N D	2.13 1.97 1.93 2.09 1.94 1.83 1.85 1.76 1.79 1.82 1.88	3.19 2.88 2.85 2.91 2.84 2.70 2.78 2.75 2.75 2.75 2.75 2.75	3.85 3.75 3.38 3.66 3.72 3.65 3.25 3.25 3.28 3.29 3.09	4.595 4.590 4.624 4.580 4.591 4.697 4.733 4.748 4.647 4.507 4.492	4.166 4.158 4.187 4.145 4.152 4.182 4.243 4.243 4.285 4.192 4.064 4.048	73.23 71.96 73.25 77.17 75.09 74.54 72.84 75.04 77.00 81.16 84.70 84.05
1916 J F M A M J J A S O N D	1.88 1.88 1.90 2.10 2.28 2.97 3.13 2.33 2.78 2.63 3.04 4.44	2.75 2.76 2.88 2.88 2.88 3.50 3.97 3.23 3.32 3.36 3.42 4.25	3.12 3.12 3.12 3.12 3.12 3.62 3.97 3.72 3.38 3.38 3.49 3.91	4.476 4.464 4.480 4.499 4.510 4.516 4.530 4.557 4.479 4.441 4.443	4.032 4.019 4.032 4.047 4.055 4.060 4.070 4.086 4.074 4.020 3.984 3.985	82.63 80.75 80.29 79.74 81.95 83.27 82.38 81.77 83.03 85.17 84.53 82.91

*Stock Exchange closed.

TABLE 10 (Continued)

Date	1 Call Money	Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1917 J F M A M J J A S O N D	2.05 2.41 2.28 2.47 3.07 4.69 3.35 2.99 4.53 4.00 4.17 5.16	3.13 4.06 3.75 3.97 4.42 4.91 4.32 4.49 5.50 5.57 5.44 5.56	3.55 4.09 4.12 4.28 4.83 5.00 4.68 4.79 5.18 5.38 5.44 5.50	4.376 4.450 4.495 4.601 4.731 4.784 4.831 4.867 4.964 5.016 5.162 5.252	3.923 3.988 4.026 4.121 4.236 4.282 4.322 4.354 4.440 4.486 4.615 4.695	81.32 77.04 77.99 77.14 74.00 74.96 74.03 72.96 69.88 66.85 61.80 59.74
1918 J F M A M J A S O N D	4 .10 4 .99 5 .20 4 .22 5 .03 5 .00 5 .63 5 .88 6 .00 6 .00 5 .85 5 .39	5.65 5.81 6.00 6.00 5.78 5.72 5.91 6.00 6.00 6.00 5.68	5.57 5.68 5.88 5.91 5.88 5.88 5.88 5.94 6.00 6.00 5.97 5.81	5.215 5.162 5.233 5.297 5.223 5.283 5.345 5.347 5.405 5.274 4.957 4.979	4.661 4.612 4.676 4.732 4.664 4.718 4.773 4.824 4.705 4.422 4.440	62.37 63.12 62.63 61.39 63.37 63.74 63.96 65.51 65.89 68.60 70.32 67.51
1919 J F M A M J A S O N D	4.78 5.06 4.88 5.40 5.25 6.63 6.55 5.13 5.78 7.94 11.06 8.85	5.18 5.31 5.50 5.80 5.50 5.78 6.00 5.94 5.88 6.18 6.50 6.60	5.25 5.18 5.38 5.38 5.38 5.53 5.43 5.38 5.38 5.38 5.38 5.38	5.077 5.126 5.189 5.239 5.186 5.185 5.258 5.435 5.477 5.333 5.473 5.538	4.527 4.570 4.625 4.669 4.617 4.676 4.837 4.837 4.874 4.746 4.869 4.927	05.84 65.86 66.54 66.77 70.41 70.55 70.26 65.77 64.52 63.18 60.42
1920 J F M A M J A S O N	8.19 10.00 8.09 7.29 7.15 7.50 8.29 7.23 7.10 7.75 7.90	7.31 8.12 8.15 8.15 8.25 8.25 8.72 8.28 8.72 8.22 7.94 7.76 7.32	6.00 6.40 6.67 6.82 7.16 7.72 7.84 8.00 7.97 8.00 7.93 7.88	5.517 5.706 5.705 5.923 6.172 6.121 6.085 5.899 5.692 5.513 5.603 5.784	4.907 5.073 5.073 5.265 5.487 5.443 5.411 5.247 5.063 4.905 4.987 5.149	60.59 58.14 61.64 59.44 57.29 56.80 57.58 59.50 63.09 65.89 64.00 58.11

TABLE 10 (Continued)

Date	1 Call Money	2 Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
1921 J F M A M J A S O N D	6.71 7.26 6.82 6.45 6.79 6.00 5.60 5.57 5.14 5.28 5.03 5.14	6.60 6.81 6.75 6.66 6.65 6.68 6.12 5.98 5.59 5.59 5.20 5.12	7.82 7.75 7.62 7.56 6.93 6.71 6.28 5.95 5.88 5.62 5.17 5.12	5.584 5.608 5.672 5.707 5.722 5.862 5.707 5.611 5.525 5.502 5.266 5.110	4.974 4.997 5.057 5.091 5.109 5.238 5.103 5.021 4.949 4.933 4.726 4.591	59.77 59.02 56.25 55.17 57.43 53.97 56.25 57.23 57.86 56.93 58.54 58.62
1922 J F M A M J J A S O N	4.55 4.90 4.23 3.97 3.91 3.70 3.86 3.76 4.34 4.73 4.89 4.66	4.75 4.87 4.74 4.41 4.17 4.12 4.06 4.08 4.47 4.79 4.99 4.91	4.91 4.88 4.79 4.56 4.28 4.03 3.94 3.88 4.19 4.39 4.61 4.62	5.011 5.013 4.966 4.870 4.840 4.833 4.740 4.674 4.793 4.879 4.862	4.506 4.513 4.475 4.393 4.372 4.370 4.291 4.251 4.242 4.355 4.439 4.429	58.36 60.35 62.65 65.80 67.11 66.44 68.99 72.30 73.30 73.21 69.24 67.62
1923 F M A M J A S O N D	4.32 4.82 5.14 4.87 4.70 5.00 4.97 4.93 4.76 4.81 4.86	4.67 4.91 5.28 5.32 5.07 4.91 5.12 5.24 5.47 5.28 5.03	4.62 4.68 5.03 5.12 5.12 4.91 4.95 5.03 5.12 5.10 4.88	4.857 4.850 5.024 5.050 4.967 4.983 4.991 4.960 5.000 5.019 4.982 4.994	4.431 4.467 4.595 4.625 4.555 4.576 4.576 4.568 4.610 4.633 4.605 4.623	67.56 69.72 70.04 68.98 66.47 65.85 63.24 62.89 63.17 62.66 63.62 63.58
1924 J F M A M J J A S O N D	4.39 4.33 4.04 4.21 3.34 2.25 2.10 2.00 2.07 2.32 2.42 3.49	4.80 4.75 4.69 4.33 3.97 3.31 2.85 2.72 2.96 2.88 3.12 3.55	4.88 4.78 4.62 4.62 4.19 3.97 3.52 3.25 3.12 3.22 3.23	4.949 4.965 4.968 4.930 4.878 4.804 4.742 4.782 4.775 4.749 4.753 4.787	4.586 4.606 4.613 4.584 4.538 4.475 4.422 4.463 4.461 4.440 4.448 4.484	64.52 65.06 64.60 65.46 65.58 67.42 70.71 72.53 72.03 71.27 76.15 80.10

TABLE 10 (Continued)

Date	1 Call Money	2 Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	Stock Prices
1925 J F M A M J J A S O N D	3.32 3.60 3.97 3.86 3.82 3.97 4.09 4.19 4.62 4.87 4.74 5.32	3.62 3.65 4.07 4.01 3.78 3.85 3.93 4.35 4.41 4.82 4.91 4.99	3.62 3.62 3.91 3.93 3.88 3.88 3.90 3.97 4.15 4.38 4.38 4.38	4.776 4.759 4.741 4.724 4.667 4.670 4.716 4.772 4.728 4.744 4.725 4.687	4.478 4.466 4.452 4.440 4.390 4.396 4.444 4.500 4.402 4.479 4.465 4.432	\$9.79 80.93 78.63 76.46 78.49 78.89 79.68 \$2.32 \$3.17 \$4.34 \$6.78 90.59
1926 J F M A M J A S O N D	4.33 4.85 4.55 4.06 3.81 4.15 4.27 4.52 5.02 4.75 4.56 5.16	4.78 4.64 4.74 4.22 4.06 4.13 4.36 4.66 4.91 4.99 4.68 4.67	4.35 4.15 4.28 4.19 4.03 3.88 3.94 4.22 4.49 4.53 4.43 4.40	4,645 4,609 4,614 4,554 +,516 4,517 4,542 3,555 +,550 4,543 4,562 4,485	4.395 4.864 4.372 4.318 4.285 4.285 4.315 4.325 4.325 4.225 4.229 4.278	90.66 89.09 85.33 85.84 86.75 93.29 92.09 94.67 97.49 94.54 95.24
1927 J F M A M J A S O N D	4.32 4.03 4.13 4.18 4.26 4.33 4.05 3.68 3.80 3.90 3.60 4.38	4.55 4.42 4.42 4.38 4.36 4.40 4.41 4.08 4.17 4.34 4.15 4.19	4.19 3.91 4.00 4.09 4.12 4.12 4.06 3.90 3.91 4.00 3.93 3.93	4.454 4.452 4.411 4.355 4.387 4.380 4.384 4.342 4.305 4.257 4.206 4.183	4.251 4.253 4.217 4.168 4.165 4.200 4.209 4.174 4.143 4.101 4.057 4.040	98.36 102.61 103.69 106.14 108.47 110.22 112.10 113.47 115.39 115.15 114.23 116.58
1928 J F M A M J A S O N D	4.24 4.38 4.47 5.08 5.70 6.32 6.05 6.87 7.26 6.98 6.67 8.60	4.35 4.55 4.61 4.88 5.17 5.76 5.93 6.34 7.06 7.10 6.88 7.47	3.88 3.99 4.19 4.55 4.72 5.09 5.59 5.51 5.59 5.51	4.187 4.208 4.213 4.231 4.275 4.371 4.437 4.496 4.442 4.435 4.395 4.468	4.049 +.073 4.082 4.104 4.151 4.249 4.317 4.327 4.329 4.329 4.287 4.360	114.79 111.84 115.66 120.49 122.41 116.52 114.85 116.57 119.60 118.42 124.37

TABLE 10 (Continued)

	TABLE 10 (Consided)								
Date	1 Call Money	2 Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices			
1929 J F M A M J A S O N	7.05 7.06 9.10 8.89 8.91 7.70 9.23 8.23 8.50 6.43 5.44 4.83	7.65 7.69 7.97 8.72 8.77 8.10 7.84 8.87 8.94 7.80 5.50 4.82	5.50 5.56 5.69 5.88 6.00 6.00 6.00 6.08 6.12 6.12 5.41 5.00	4.501 4.548 4.599 4.579 4.597 4.649 4.670 4.662 4.694 4.638 4.581 4.504	4.393 4.434 4.464 4.460 4.477 4.520 4.516 4.512 4.575 4.546 4.445 4.398	130 . 53 128 . 95 128 . 54 126 . 90 128 . 40 133 . 56 146 . 61 152 . 76 154 . 42 135 . 68 122 . 20 125 . 02			
1930 J F M A M J J A S O N D	4.64 4.32 3.69 4.60 3.12 2.62 2.20 2.21 2.19 2.00 2.00 2.23	4.70 4.65 4.12 4.12 3.54 2.90 2.78 2.62 2.59 2.45 2.18 2.24	4.90 4.62 4.10 3.88 3.68 3.44 3.15 3.00 3.00 2.97 2.85	1.504 1.522 4.437 4.454 4.441 4.417 4.375 4.317 4.262 4.292 4.366 4.488	4.386 4.375 4.300 4.352 4.319 4.287 4.237 4.176 4.116 4.096 4.138 4.200	124.18 130.53 131.34 128.76 122.54 115.09 115.01 111.95 109.98 101.77 93.31 85.38			
1931 J F M A M J J A S O N D	1.57 1.50 1.55 1.52 1.45 1.50 1.50 1.50 2.10 2.50 2.70	2.10 1.88 2.12 2.12 1.66 1.41 1.42 1.50 1.69 3.19 3.53 3.40	2.82 2.50 2.53 2.40 2.12 2.12 1.95 1.88 1.88 3.35 4.00 4.00	4.322 4.324 4.319 4.365 4.381 4.362 4.492 4.732 5.146 5.248 5.886	4.078 4.083 4.095 4.081 4.002 4.016 4.009 4.056 4.120 4.350 4.492 4.736	90.69 96.12 89.89 79.92 70.56 67.78 69.26 61.25 51.47 45.18 41.08			
1932 J F M A M J J A S O N D	2.65 2.50 2.50 2.50 2.50 2.50 2.08 2.00 2.00 1.35 1.00	3.56 3.62 3.13 2.69 1.59 1.50 1.44 1.38 1.26 .97 .50	4.00 3.88 3.52 3.38 3.00 2.78 2.56 2.18 2.12 1.94 1.74	5.637 5.636 5.524 5.906 6.362 6.513 6.077 5.458 5.286 5.319 5.443 5.557	4.735 4.793 4.691 4.837 4.848 4.898 4.798 4.540 4.456 4.456 4.456 4.458 4.375	32.01 31.86 29.44 21.27 15.57 13.46 15.87 25.67 31.23 26.16 24.37 23.26			

TABLE 10 (Concluded)

		TAB	LE 10 (Cor	icluded)		
Date	1 Call Money	Time Money	3 Coml. Paper	4 Unadj. Bonds	5 Adjust. Bonds	6 Stock Prices
IOSS J F M A M J J A S O N D	1.00 1.00 3.32 1.37 1.00 1.00 1.00 .98 .75 .75	.50 .66 2.94 1.25 1.04 .93 1.16 1.08 .64 .69 .83 1.09	1.38 1.38 2.78 2.56 2.08 1.50 1.50 1.25 1.25	5.290 5.390 5.681 5.907 5.485 5.162 4.964 4.921 5.159 5.576 5.417	4.174 4.173 4.337 4.515 4.357 4.205 4.128 4.076 4.111 4.240 4.200	25.14 23.81 23.75 25.46 34.64 40.36 45.93 45.56 42.99 35.50 35.40 37.34
1934 J F M A M J A S O N D	1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00	1.09 .91 .88 .88 .88 .88 .88 .88 .88 .88	1.25 1.22 1.00 1.00 .90 .75 .75 .75 .75	4.997 4.695 4.597 4.515 4.407 4.403 4.379 4.494 4.592 4.491 4.401 4.307	4.084 3.996 3.926 3.865 3.812 3.728 3.721 3.771 3.826 3.762 3.680 3.681	41.68 46.05 44.37 44.87 40.31 40.32 35.93 32.82 32.08 32.95 32.53 33.47
1935 J F M A J J A S O N D	1.00 1.00 1.00 1.00 .64 .25 .25 .25 .25 .25 .25 .75	.88 .88 .88 .56 .25 .25 .25 .25 .25 .25 .25	.75 .75 .75 .75 .75 .75 .75 .75 .75	4.209 4.148 4.225 4.262 4.206 4.173 4.129 4.178 4.214 4.243 4.232 4.612	3.523 3.438 3.409 3.411 3.438 3.417 3.397 3.451 3.467 3.479 3.443 3.414	32.39 30.55 26.73 27.54 29.05 30.10 31.71 33.52 34.10 32.00 35.61 38.36
1936 J F M A J J A S O N D	.75 .75 .75 .75 .93 1.00 1.00 1.00 1.00 1.00	1.00 1.00 1.00 1.00 1.19 1.25 1.25 1.25 1.25 1.25	.75 .75 .75 .75 .75 .75 .75 .75 .75	4.047 3.941 3.882 3.995 3.895 3.875 3.881 3.877 3.843 3.828 3.796 3.747	3.360 3.312 3.251 3.245 3.215 3.200 3.220 3.220 3.240 3.211 3.200 3.170 3.170	41.38 46.59 45.55 43.51 42.08 44.26 47.52 50.10 51.37 54.06 53.06 50.31
1937 J	1.00	1.25	.75	3.764	3.146	51.44

TABLE 11

An Adjusted Arithmetic Average Index Number¹ of the Yields of American Railroad Bonds, Monthly, January 1857-January 1936

- Col. 1 Logarithms of Index.
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).

For the nature of the graduations given in columns 2 and 3 see Appendix D. $\,$

See Table 10.

TABLE 11

Date	1	2	3	4	Date	1	2	3	4
1857 JF M AM J ASOND	.8209 .8180 .8190 .8208 .8258 .8356 .8377 .8421 .8850 .9154 .8847	.8249 .8268 .8301 .8346 .8401 .8518 .8568 .8604 .8624 .8624	.8255 .8261 .8264 .8266 .8265 .8264 .8262 .8260 .8258 .8254 .8249 .8249	0006 +.0007 +.0037 +.0080 +.0136 +.0196 +.0256 +.0308 +.0346 +.0370 +.0375 +.0358	1862 J F M A M J J A S O N D	.7879 .7710 .7752 .7723 .7498 .7385 .7423 .7335 .7197 .7029 .6936 .6973	.7920 .7854 .7775 .7682 .7578 .7464 .7344 .7224 .7109 .7001 .6905 .6824	.7452 .7426 .7397 .7369 .7343 .7318 .7292 .7268 .7245 .7223 .7203 .7184	+.04 +.04 +.03 +.03 +.02 +.01 +.00 01 01 02 02 03
1858 J F M A M J J A S O N D	.8558 .8338 .8192 .8173 .8129 .8107 .8079 .8080 .8032 .7918 .7869 .7858	.8558 .8494 .8413 .8321 .8225 .8131 .8047 .7978 .7926 .7882 .7875 .7870	.8237 .8230 .8222 .8216 .8208 .8200 .8193 .8186 .8178 .8170 .8162 .8155	+.0321 +.0264 +.0191 +.0105 +.0017 0069 0146 0208 0252 0278 0287 0285	1863 J F M A M J J A S O N D	.6613 .6474 .6542 .6740 .6749 .6799 .6844 .6872 .6869 .6838 .6933 .7017	.6761 .6719 .6699 .6700 .6722 .6759 .6806 .6854 .6895 .6923 .6933	.7166 .7152 .7138 .7126 .7113 .7105 .7099 .7097 .7093 .7097 .7100	04 04 04 03 03 02 02 01 01
1859 F M A M J I A S O N D	.7861 .7854 .7857 .7843 .7925 .8040 .8037 .8009 .7923 .7952 .7976	.7874 .7884 .7899 .7916 .7934 .7953 .7970 .7982 .7988 .7984 .7969	.8146 .8137 .8128 .8119 .8109 .8099 .8088 .8076 .8064 .8053 .8040 .8027	0272 0253 0229 0203 0175 0146 0118 0076 0069 0071 0083	1864 J F M A M J J A S O N D	.7082 .7055 .6917 .6752 .6743 .6667 .6398 .6414 .6730 .7066 .7029	.6895 .6855 .6810 .6766 .6734 .6720 .6728 .6761 .6821 .6904 .7009	.7104 .7112 .7121 .7132 .7148 .7161 .7178 .7197 .7221 .7244 .7269 .7294	02(02: 03 03 04 04 04 04 03 03 03
1860 JF M A M J A S O N D	.7957 .7928 .7893 .7842 .7762 .7688 .7655 .7643 .7655 .7690 .7898 .8089	.7912 .7875 .7838 .7804 .7776 .7755 .7744 .7742 .7749 .7767 .7793 .7828	.8010 .7997 .7981 .7964 .7945 .7927 .7908 .7888 .7868 .7868 .7868 .7868	0098012201430160016901720164011900810032 +0026	1865 J F M A M J A S O N D	.7325 .7452 .7679 .7750 .7734 .7917 .7843 .7868 .7900 .7957 .8030 .8067	.7259 .7391 .7520 .7640 .7745 .7835 .7909 .7968 .8013 .8047 .8071	.7320 .7348 .7378 .7407 .7438 .7469 .7501 .7532 .7567 .7599 .7632 .7666	000 +.001 +.011 +.023 +.030 +.041 +.044 +.044 +.044 +.044
1861 JF M A M J J A S O N D	.7931 .7891 .7854 .7896 .8124 .8095 .7983 .8000 .8072 .8117 .8090 .8089	.7869 .7914 .7960 .8001 .8036 .8061 .8075 .8076 .8067 .8046 .8015 .7973	.7778 .7754 .7728 .7703 .7676 .7649 .7622 .7595 .7566 .7539 .7511 .7482	+.0091 +.0160 +.0232 +.0298 +.0360 +.0412 +.0453 +.0481 +.0501 +.0507 +.0504 +.0491	1866 J F M A M J J A S O N D	.8123 .8152 .8200 .8168 .8085 .8062 .8001 .7965 .7939 .7922 .7896 .7965	.8096 .8097 .8093 .8084 .8070 .8053 .8034 .8015 .7996 .7980 .7969	.7697 .7729 .7759 .7758 .7816 .7843 .7869 .7894 .7916 .7939 .7959 .7980	+.030 +.033 +.025 +.025 +.016 +.016 +.016 +.000 +.000

TABLE 11 (Continued)

Date	1	2	3	4	Date	t	2	.3	4
1867 F M A M J A S O N D	.7985 .7998 .8005 .8037 .8048 .8045 .7965 .7955 .7964 .8014 .8055 .8072	.7963 .7969 .7980 .7993 .8006 .8017 .8025 .8026 .8023 .8014 .8002 .7987	.7994 .8008 .8023 .8036 .8048 .8059 .8070 .8077 .8082 .8088 .8093	0031 0039 0043 0043 0042 0042 0051 0059 0074 0091 0109	1872 JF MAA MJJ AASO ON D	.7906 .7881 .7933 .7923 .7921 .7892 .7835 .7875 .7916 .7941 .7967 .7970	.7947 .7937 .7929 .7922 .7918 .7914 .7911 .7908 .7906 .7903 .7903 .7903	8018 8012 8006 7098 7992 7984 7977 7968 7959 7950 7930 7931	007 007 007 007 006 006 005 004 003
1868 JF M A M J A S O N D	.8002 .7951 .7955 .7955 .7923 .7907 .7902 .7912 .7955 .7999 .8048 .8087	.7973 .7959 .7949 .7944 .7945 .7952 .7962 .7962 .7975 .7991 .8009 .8029	.8098 .8100 .8102 .8102 .8101 .8100 .8100 .8098 .8095 .8093 .8091 .8088	0125 0141 0153 0158 0159 0155 0148 0136 0120 0102 0082 0059	1873 JF M A A J J A S O N D	.7917 .7900 .7903 .7915 .7866 .7866 .7826 .7826 .7900 .8127 .7996	.7906 .7910 .7916 .7922 .7928 .7933 .7935 .7935 .7932 .7926 .7917 .7905	.7918 .7907 .7894 .7882 .7869 .7857 .7843 .7829 .7813 .7708 .7767	001: +.000: +.002: +.004: +.005: +.007: +.010: +.011: +.013:
IS69 F M A M J A S O N D	.8088 .8095 .8125 .8141 .8081 .818 .8118 .8110 .8159 .8221 .8245 .8272	.8052 .8075 .8098 .8121 .8141 .8157 .8169 .8175 .8176 .8172 .8164 .8153	.8084 .8082 .8080 .8078 .8075 .8073 .8072 .8071 .8070 .8069 .8069	0032 0007 +.0018 +.0043 +.0066 +.0084 +.0097 +.0106 +.0106 +.0102 +.0095 +.0085	1874 JF M A M J J A S O N D	.7839 .7766 .7757 .7757 .7771 .7728 .7724 .7713 .7688 .7641 .7574 .7561	.7889 .7868 .7843 .7814 .7781 .7746 .7710 .7674 .7608 .7578 .7549	.7740 .7732 .7714 .7697 .7680 .7661 .7642 .7624 .7608 .7589 .7571 .7553	+.014 +.013 +.012 +.011 +.010 +.005 +.005 +.003 +.000 000
1870 J F M A M J A S O N D	.8229 .8096 .8042 .8064 .8028 .7996 .7991 .8040 .8058 .8070 .8083 .8103	.8139 .8124 .8108 .8092 .8078 .8064 .8053 .8045 .8039 .8038 .8038 .8038	.8068 .8068 .8067 .8067 .8066 .8065 .8064 .8063 .8063 .8062 .8060 .8059	+.0071 +.0056 +.0041 +.0025 +.0012 0001 0018 0024 0024 0022 0018	1875 J F M A M J J A S O N D	.7506 .7478 .7461 .7403 .7370 .7388 .7344 .7332 .7299 .7324 .7292 .7242	.7520 .7491 .7466 .7436 .7407 .7379 .7352 .7323 .7298 .7274 .7251	.7534 .7517 .7490 .7481 .7462 .7446 .7428 .7411 .7394 .7377 .7361 .7345	001- 002- 003. 004- 005- 006- 008- 009- 010- 011-
1871 J F M A M J J A S O N D	.8074 .8050 .8041 .8031 .8002 .7998 .7994 .7973 .7959 .8040 .8070 .8034	.8043 .8046 .8045 .8042 .8037 .8029 .8019 .8008 .7995 .7982 .7970	.8058 .8056 .8054 .8051 .8049 .8047 .8044 .8036 .8031 .8027 .8023	001500100009000900120018002500320041004900570065	1876 JF M A M J J A S O N D	.7196 .7150 .7120 .7141 .7163 .7142 .7090 .7066 .7134 .7139 .7131	.7204 .7182 .7161 .7144 .7130 .7120 .7115 .7114 .7117 .7122 .7128 .7135	.7330 .7316 .7301 .7288 .7272 .7259 .7245 .7232 .7220 .7208 .7198 .7186	012 013 014 014 013 013 011 008 007 005

TABLE 11 (Continued)

Date	1	2	3	4	Date	1	2	3	4
ISTT J F M A M J A S O N D	.7105 .7137 .7199 .7210 .7177 .7126 .7086 .7112 .7130 .7154 .7145 .7117	.7141 .7146 .7150 .7152 .7152 .7151 .7150 .7144 .7139 .7133 .7128 .7124	.7174 .7165 .7154 .7143 .7132 .7122 .7111 .7101 .7090 .7079 .7068 .7057	0033 0019 0004 + .0009 + .0029 + .0039 + .0043 + .0049 + .0054 + .0060 + .0067	1882 J F M A M J J A S O N D	.6219 .6247 .6270 .6274 .6201 .6201 .6202 .6241 .6232 .6241 .6232 .6254	.6208 .6217 .6224 .6230 .6232 .6233 .6232 .6230 .6229 .6229 .6236	.6248 .6242 .6238 .6233 .6230 .6227 .6223 .6220 .6218 .6216 .6313 .6211	0040 0025 0014 0003 + .0002 + .0006 + .0010 + .0011 + .0013 + .0019 + .0025
1878 JF M AM J I AS OND	.7120 .7117 .7123 .7124 .7099 .7049 .7080 .7078 .7058 .7027 .7012	.7121 .7118 .7116 .7116 .7113 .7107 .7099 .7086 .7069 .7046 .7020 .6991 .6959	.7044 .7033 .7020 .7008 .6992 .6979 .6965 .6949 .6931 .6914 .6897	+.0077 +.0085 +.0096 +.0105 +.0115 +.0120 +.0121 +.0120 +.0115 +.0106 +.0094 +.0080	1883 J F M A M J J A S O N D	.6217 .6250 .6267 .6249 .6246 .6244 .6243 .6277 .6283 .6274 .6243	.6243 .6251 .6258 .6262 .6263 .6261 .6254 .6245 .6234 .6223 .6213 .6204	.6208 .6204 .6202 .6199 .6196 .6192 .6187 .6182 .6173 .6168	+ .0035 + .0047 + .0056 + .0067 + .0067 + .0063 + .0056 + .0056 + .0045
1870 JF M AM J ASOND	.6921 .6802 .6874 .6875 .6774 .6735 .6696 .6691 .6768 .6757 .6739	.6926 .6893 .6861 .6830 .6802 .6777 .6756 .6738 .6724 .6712 .6702	.6861 .6842 .6823 .6804 .6784 .6765 .6743 .6722 .6701 .6680 .6659	+.0065 +.0051 +.0038 +.0026 +.0018 +.0012 +.0013 +.0016 +.0023 +.0032 +.0043 +.0052	1884 F M A M J J A S O N D	.6194 .6149 .6114 .6088 .6170 .6273 .6286 .6219 .6227 .6222 .6228 .6190	.6199 .6196 .6196 .6197 .6200 .6204 .6207 .6209 .6208 .6203 .6194 .6180	.6155 .6149 .6141 .6133 .6125 .6116 .6107 .6068 .6089 .6080	+ .0044 + .0047 + .0053 + .0056 + .0073 + .0188 + .0111 + .0113 + .0125 + .0125
FM AM J ASOND	.6668 .6613 .6600 .6609 .6601 .6566 .6496 .6451 .6421 .6379 .6277	.6676 .6658 .6634 .6606 .6564 .6526 .6484 .6440 .6394 .6357 .6312	.6615 .6594 .6572 .6551 .6530 .6508 .6488 .6467 .6450 .6430 .6412	+.0061 +.0064 +.0062 +.0055 +.0034 +.0018 0004 0027 0056 0073 0100 0127	1885 J F M A M J A S O N D	.6142 .6106 .6066 .6056 .6039 .5985 .5954 .5945 .5931 .5888 .5858	.6170 .6136 .6108 .6077 .6043 .6008 .5973 .5939 .5903 .5831 .5796	.6046 .6034 .6022 .6011 .5997 .5984 .5971 .5958 .5944 .5931 .5917	+ .0124 + .0102 + .0086 + .0046 + .0044 + .0022 0015 0041 0086 0106
1881 FM AM I ASOND	.6167 .6213 .6257 .6242 .6127 .6059 .6062 .6097 .6177 .6221 .6199 .6224	.6230 .6197 .6170 .6152 .6141 .6138 .6141 .6148 .6159 .6172 .6184 .6197	.6379 .6363 .6349 .6336 .6321 .6308 .6296 .6287 .6277 .6277 .6268 .6261	014901660179018401800170015501390118009600770056	1886 JF M A M J J A S O N D	.5761 .5685 .5670 .5682 .5678 .5643 .5669 .5621 .5685 .5686 .5684	.5762 .5732 .5707 .5685 .5669 .5657 .5650 .5647 .5653 .5660 .5671	.5889 .5875 .5862 .5848 .5835 .5822 .5808 .5795 .5770 .5758 .5746	0127 0143 0155 0166 0166 0158 0138 0137 0098 0075

TABLE 11 (Continued)

An Adjusted Arithmetic Index Number of the Yields of $\Lambda_{\rm MERICAN}$ Railroad Bonds.

Date	1	2	3	4	Date	1	2	3	4
1887 J F M A M J A S O N D	.5685 .5694 .5711 .5716 .5699 .5703 .5723 .5723 .5758 .5838 .5865 .5822 .5801	.5684 .5698 .5713 .5728 .5728 .5756 .5766 .5774 .5779 .5780 .5778	.5732 .5721 .5709 .5699 .5688 .5679 .5661 .5661 .5652 .5646 .5639 .5632	0048 0023 + .0004 + .0029 + .0055 + .0077 + .0097 + .0113 + .0127 + .0134 + .0139 + .0140	1892 J F M A M J J A S O N D	.5739 .5713 .5722 .5705 .5683 .5669 .5657 .5667 .5711 .5719	.5774 .5751 .5729 .5708 .5690 .5665 .5665 .5665 .5661 .5669 .5683 .5705	.5762 .5765 .5768 .5770 .5770 .5770 .5770 .5769 .5769 .5766 .5762 .5762	+.001. 001. 003. 006. 008. 010. 010. 010. 010. 010. 009. 009. 009. 009.
1888 J F M A M J A S O N D	.5731 .5701 .5719 .5718 .5696 .5670 .5616 .5608 .5640 .5648 .5629	.5763 .5751 .5736 .5720 .5703 .5684 .5666 .5647 .5628 .5608 .5588 .5588	.5625 .5621 .5616 .5612 .5609 .5607 .5605 .5604 .5603 .5603	+.0138 +.0130 +.0120 +.0108 +.0094 +.0077 +.0061 +.0043 +.0025 +.0005 0015 0037	1893 JF M A M J A S O N D	.5712 .5679 .5714 .5718 .5769 .5839 .5979 .6081 .5944 .5886 .5788	.5731 .5760 .5790 .5818 .5841 .5858 .5868 .5869 .5869 .5862 .5846 .5821	.5756 .5751 .5748 .5748 .5748 .5729 .5729 .5722 .5714 .5706 .5698 .5690	0023 + .0004 + .004 + .0104 + .0124 + .0155 + .0144 + .0131 + .0104
1889 J. F. M. A. M. J. A. S. O. N. D.	.5562 .5509 .5520 .5511 .5460 .5411 .5436 .5448 .5455 .5504 .5543	.5547 .5528 .5510 .5494 .5482 .5474 .5470 .5470 .5474 .5482 .5494 .5509	.5604 .5606 .5608 .5609 .5610 .5613 .5616 .5618 .5621 .5623 .5627 .5630	0057 0078 0098 0115 0128 0139 0146 0148 0147 0141 0133 0121	1894 JF MAA JJASOND	.5714 .5660 .5620 .5570 .5572 .5576 .5591 .5566 .5534 .5493 .5461	.5750 .5708 .5664 .5623 .5559 .5539 .5525 .5517 .5511 .5505 .5497	.5671 .5662 .5654 .5645 .5632 .5624 .5613 .5603 .5591 .5582 .5573 .5563	+.0079 +.0040 +.0011 002: 0040 0061 0071 0071 0071 0071 0064
1890 IF M A M J A S O N D	.5544 .5549 .5572 .5576 .5579 .5601 .5617 .5688 .5720 .5720 .5779	.5526 .5545 .5565 .5585 .5604 .5624 .5643 .5663 .5708 .5733 .5760	.5635 .5639 .5644 .5648 .5653 .5658 .5663 .5669 .5674 .5679 .5685 .5691	0109 0094 0079 0063 0049 0034 0020 0006 + .0011 + .0029 + .0048 + .0069	1895 J F M A M J J A S O N D	.5465 .5504 .5517 .5522 .5464 .5393 .5359 .5305 .5310 .5320 .5338 .5400	.5486 .5472 .5455 .5438 .5419 .5402 .5385 .5371 .5360 .5355 .5356	.5551 .5542 .5533 .5523 .5512 .5503 .5493 .5482 .5471 .5460 .5450	006 007 007 008 009 010 011 011 011 010 009 009
J F M A M J A S O N D	.5737 .5740 .5798 .5816 .5853 .5912 .5912 .5912 .5892 .5852 .5852 .5854 .5785	.5788 .5812 .5835 .5853 .5853 .5866 .5872 .5873 .5867 .5856 .5839 .5819 .5797	.5698 .5703 .5710 .5717 .5723 .5729 .5736 .5741 .5746 .5756 .5756	+.0090 +.0109 +.0125 +.0136 +.0143 +.0143 +.0137 +.0126 +.0110 +.0087 +.0063 +.0037	1896 J F M A M J J A S O N D	.5459 .5410 .5414 .5409 .5386 .5372 .5467 .5667 .5590 .5547 .5439 .5386	.5378 .5399 .5423 .5448 .5469 .5485 .5494 .5494 .5485 .5468 .5414	.5429 .5417 .5406 .5395 .5383 .5372 .5361 .5349 .5336 .5325 .5313 .5301	005 0018 +.0011 +.0053 +.0058 +.0113 +.0144 +.0144 +.0143 +.0113

TABLE 11 (Continued)

Date	1	2	3	4	Date	1	2	3	4
ISOT J F M A M J I A S O N D	.5331 .5301 .5240 .5251 .5235 .5196 .5157 .5180 .5190 .5192 .5171 .5115	.5380 .5347 .5308 .5269 .5233 .5203 .5174 .5160 .5153 .5159 .5167	.5290 .5279 .5279 .5268 .5257 .5245 .5235 .5225 .5215 .5204 .5195 .5185 .5175	+ .0090 + .0068 + .0040 + .0012 0032 0051 0055 0051 0042 0026 0008	J F M A M J J A S O N D	.5049 .5047 .5047 .5053 .5052 .5074 .5097 .5122 .5147 .5172 .5236 .5269	.5058 .5063 .5068 .5076 .5087 .5100 .5118 .5138 .5164 .5192 .5223 .5256	.5132 .5143 .5155 .5167 .5178 .5189 .5200 .5212 .5224 .5235 .5257	0074 0084 0085 009 009 0085 007 0066 0044 002
1898 IF M A M I I A S O N D	.5090 .5096 .5195 .5297 .5252 .5188 .5135 .5103 .5124 .5091 .5048 .5008	.5175 .5182 .5186 .5186 .5181 .5172 .5157 .5135 .5109 .5078 .5044 .5010	.5165 .5156 .5157 .5137 .5128 .5118 .5109 .5100 .5091 .5082 .5073 .5065	+.0010 +.0026 +.0039 +.0049 +.0054 +.0048 +.0035 +.0018 0004 0028	1903 J F M A M J J A S O N D	.5266 .5289 .5349 .5379 .5423 .5423 .5480 .5536 .5546 .55507 .5478	.5290 .5323 .5356 .5386 .5415 .5441 .5463 .5482 .5498 .5509 .5515 .5517	.5267 .5277 .5287 .5296 .5305 .5314 .5322 .5330 .5339 .5347 .5360	+.002 +.004 +.006 +.009 +.011 +.012 +.015 +.015 +.016 +.016
J F M A M J A S O N D	.4951 .4958 .4961 .4918 .4883 .4873 .4898 .4924 .4967 .5011 .5038 .5086	.4980 .4954 .4935 .4923 .4919 .4922 .4930 .4943 .4957 .4973 .4990 .5006	.5055 .5048 .5040 .5031 .5023 .5017 .5010 .5003 .4998 .4994 .4990 .4987	0075 0094 0105 0108 0104 0095 0080 0060 0041 0021 .0000 +.0019	1904 F M A M J S O N D	.5486 .5502 .5521 .5501 .5489 .5468 .5430 .5421 .5428 .5424 .5416	.5515 .5509 .5500 .5488 .5476 .5463 .5450 .5438 .5427 .5417 .5408 .5400	.5368 .5375 .5382 .5389 .5397 .5403 .5411 .5418 .5426 .5433 .5440	+.014 +.013 +.011 +.009 +.007 +.006 +.003 +.002 +.000 001 003
1900 JF M A M J A S O N D	.5048 .5013 .5002 .4983 .5021 .5040 .5044 .5050 .5054 .5054 .5028 .4997	.5020 .5032 .5040 .5044 .5044 .5041 .5035 .5027 .5020 .5013 .5008	.4983 .4983 .4983 .4981 .4981 .4982 .4984 .4986 .4992 .5002 .5008	+.0037 +.0049 +.0058 +.0063 +.0063 +.0059 +.0051 +.0041 +.0028 +.0017 +.0006 0002	1905 J F M A M J J A S O N D	.5377 .5367 .5382 .5392 .5400 .5384 .5388 .5389 .5389 .5389 .5381	.5393 .5387 .5383 .5381 .5380 .5382 .5385 .5390 .5398 .5407 .5417 .5429	.5456 .5462 .5470 .5477 .5485 .5492 .5500 .5508 .5513 .5520 .5527 .5532	006 007 008 009 010 011 011 011 011 011 011
IPO1 JF MAAM JAASOND	.4986 .4969 .4971 .4985 .5022 .5013 .5038 .5062 .5075 .5077 .5051	.5005 .5006 .5009 .5013 .5018 .5023 .5028 .5034 .5040 .5045 .5049	.5015 .5023 .5031 .5039 .5048 .5059 .5068 .5078 .5088 .5098 .5109 .5120	0010 0017 0022 0026 0030 0046 0044 0048 0053 0060 0066	1906 JF M A M JA S O N D	.5418 .5439 .5476 .5496 .5513 .5498 .5512 .5534 .5563 .5549 .5540	.5442 .5455 .5469 .5481 .5493 .5503 .5513 .5529 .5538 .5549	.5538 .5543 .5550 .5556 .5561 .5567 .5572 .5578 .5583 .5590 .5596	009 008 007 006 005 005 005 005 005 005 005

TABLE 11 (Continued)

Date	1	2	3	4	Date	1	2	3	4
IPOT F M A M J J A S O N D	.5566 .5588 .5662 .5660 .5682 .5735 .5731 .5788 .5843 .5921 .6087 .5976	.5584 .5609 .5640 .5675 .5714 .5753 .5790 .5825 .5854 .5876 .5890	.5606 .5613 .5619 .5625 .5637 .5642 .5649 .5656 .5661 .5668	0022 0004 +.0021 +.0050 +.0084 +.0116 +.0148 +.0176 +.0198 +.0215 +.0222 +.0224	1912 J F M A M J J A S O N D	.5850 .5840 .5857 .5866 .5871 .5884 .5894 .5916 .5936 .5932 .5930 .5945	.5862 .5864 .5866 .5869 .5872 .5877 .5883 .5893 .5905 .5920 .5039 .5960	.5890 .5900 .5909 .5919 .5929 .5939 .5949 .5958 .5968 .5977 .5986 .5995	0028 0036 0043 0050 0057 0062 0065 0065 0057 0057 0057
1908 JF M A M J A S C N D	.5821 .5809 .5844 .5814 .5774 .5771 .5748 .5706 .5674 .5666 .5631 .5615	.5893 .5881 .5861 .5835 .5803 .5769 .5735 .5702 .5673 .5648 .5628	.5680 .5686 .5692 .5697 .5702 .5707 .5711 .5716 .5719 .5722 .5726	+.0213 +.0195 +.0169 +.0138 +.0101 +.0062 +.0024 0074 0074 0078 0117	1913 J F M A M J A S O N D	.5928 .5944 .6012 .6061 .6156 .6153 .6110 .6069 .6104 .6157	.5983 .6007 .6032 .6056 .6078 .6096 .6109 .6117 .6118 .6114 .6105	.6003 .6010 .6018 .6024 .6030 .6036 .6045 .6045 .6045 .6053 .6058	0020 0003 +. 0014 +. 0032 +. 0069 +. 0072 +. 0069 +. 0069 +. 0069 +. 0048
1000 FMAM JASOND	.5593 .5569 .5587 .5596 .5597 .5620 .5620 .5637 .5664 .5684 .5704	.5602 .5596 .5593 .5594 .5598 .5606 .5618 .5633 .5651 .5672 .5694	.5731 .5735 .5738 .5738 .5740 .5742 .5746 .5747 .5748 .5748 .5749 .5751	0129 0139 0145 0146 0146 0136 0128 0114 0097 0077 0057 0036	1914 J F M A M J J A S O N D	.6087 .6018 .6038 .6036 .6034 .6021 .6065 .6104* .6182* .6220* .6258	.6082 .6072 .6065 .6063 .6065 .6072 .6084 .6100 .6119 .6141 .6165 .6188	.6063 .6067 .6070 .6072 .6075 .6078 .6081 .6083 .6087 .6090	+.0019 +.0005 0005 0009 0010 0006 +.0003 +.0017 +.0051 +.0051
F M A M J A SOND	.5719 .5728 .5753 .5802 .5825 .5846 .5873 .5869 .5821 .5799 .5832 .5831	.5739 .5760 .5779 .5795 .5809 .5820 .5829 .5834 .5838 .5839 .5840	.5756 .5758 .5760 .5762 .5766 .5770 .5775 .5777 .5780 .5785 .5789 .5789	0017 +.0002 +.0019 +.0033 +.0043 +.0050 +.0054 +.0057 +.0058 +.0054 +.0051 +.0047	1915 J F M A M J J A S O N D	.6197 .6189 .6219 .6175 .6183 .6214 .6277 .6308 .6319 .6224 .6089 .6072	.6211 .6229 .6242 .6248 .6247 .6239 .6227 .6211 .6193 .6176 .6159 .6143	.6103 .6108 .6113 .6117 .6121 .6127 .6132 .6136 .6140 .6140 .6150	+.0108 +.0121 +.0129 +.0131 +.0112 +.0015 +.0075 +.0053 +.0030 +.0009
IPII F M A M J J A S O N D	.5824 .5829 .5846 .5843 .5831 .5842 .5848 .5863 .5880 .5873 .5851	.5838 .5838 .5838 .5839 .5841 .5844 .5846 .5849 .5852 .5854 .5857	.5799 .5805 .5811 .5818 .5823 .5830 .5838 .5846 .5854 .5862 .5871 .5880	+ .0039 + .0033 + .0027 + .0021 + .0018 + .0014 + .0008 0002 0008 0014 0021	1916 J F M A M J J A S O N D	.6055 .6041 .6055 .6071 .6080 .6085 .6096 .6113 .6100 .6042 .6003	.6127 .6116 .6095 .6079 .6063 .6048 .6036 .6026 .6019 .6018	.6162 .6168 .6176 .6182 .6189 .6198 .6207 .6216 .6225 .6236 .6248 .6259	,0035 ,0052 ,0081 ,0103 ,0126 ,0150 ,0171 ,0190 ,0206 ,0218 ,0227 ,0228

^{*}Interpolated. Stock Exchange closed.

TABLE 11 (Continued)

	i i		1		1	1		1	
Date	1	2	3	4	Date	1	2	3	4
1917 JFM AM JA SOND	.5936 .6008 .6049 .6150 .6270 .6316 .6357 .6389 .6474 .6519 .6642	.6049 .6075 .6111 .6156 .6209 .6270 .6336 .6405 .6473 .6538 .6598	.6272 .6287 .6302 .6319 .6333 .6351 .6370 .6389 .6409 .6430 .6451	- 0223 - 0212 - 0191 - 0163 - 0124 - 0081 - 0034 + 0016 + 0064 + 0108 + 0178	I 1922 F M A M J J A S O N D	.6538 .6545 .6508 .6428 .6407 .6405 .6326 .6285 .6276 .6390 .6473 .6463	.6633 .6556 .6487 .6429 .6386 .6358 .6346 .6348 .6361 .6384 .6413	.6773 .6762 .6750 .6738 .6725 .6712 .6700 .6688 .6677 .6664 .6653	0140 0206 0263 0309 0339 0354 0340 0340 0280 0280 0240 0196
1918 JF M A M J A S O N D	.6685 .6639 .6699 .6750 .6688 .6738 .6788 .6788 .6834 .6726 .6456	.6692 .6723 .6723 .6752 .6750 .6740 .6723 .6703 .6681 .6660 .6641	.6495 .6518 .6541 .6564 .6587 .6609 .6632 .6654 .6678 .6699 .6720	+ .0197 + .0205 + .0202 + .0188 + .0163 + .0131 + .0091 + .0003 0039 0079 0116	1923 J. F. M. A. M. J. J. A. S. O. N. D.	.6465 .6500 .6623 .6651 .6585 .6605 .6618 .6597 .6637 .6659 .6632	.6480 .6515 .6548 .6578 .6604 .6626 .6642 .6652 .6654 .6654	.6631 .6620 .6609 .6599 .6589 .6570 .6570 .6562 .6553 .6545 .6537	0151 0105 0061 0021 +.0015 +.0047 +.0090 +.0103 +.0109 +.0110 +.0107
1919 FM AM J J ASOND	.6558 .6599 .6651 .6692 .6646 .6644 .6699 .6846 .6879 .6763 .6874	.6614 .6608 .6608 .6615 .6631 .6658 .6695 .6742 .6798 .6859 .6923	.6762 .6782 .6789 .6817 .6833 .6848 .6862 .6874 .6887 .6896 .6905	0148 0174 0191 0202 0190 0167 0132 0089 0037 +.0018 +.0071	1924 JF M A M J J A S O N D	.6614 .6633 .6640 .6612 .6569 .6508 .6456 .6496 .6494 .6474 .6482 .6517	.6623 .6609 .6593 .6577 .6560 .6544 .6529 .6514 .6501 .6490 .6482	.6523 .6517 .6511 .6505 .6500 .6495 .6490 .6485 .6480 .6476 .6471	+.0100 +.0092 +.0082 +.0072 +.0060 +.0049 +.0039 +.0029 +.0021 +.0014 +.0011
1920 JF M AM J J A S O N D	.6908 .7053 .7053 .7214 .7393 .7358 .7358 .7333 .7199 .7044 .6906 .6978 .7117	.7042 .7091 .7128 .7154 .7169 .7174 .7169 .7158 .7143 .7125 .7107 .7091	.6922 .6927 .6930 .6933 .6935 .6934 .6933 .6931 .6928 .6923 .6918	+.0120 +.0164 +.0198 +.0221 +.0234 +.0240 +.0236 +.0227 +.0215 +.0202 +.0189 +.0179	1925 JF MA A J J A S O N D	.6511 .6499 .6486 .6474 .6425 .6431 .6478 .6532 .6495 .6512 .6498 .6466	.6476 .6478 .6482 .9487 .6491 .6493 .6492 .6488 .6481 .6471 .6460	.6461 .6456 .6451 .6445 .6435 .6435 .6429 .6422 .6416 .6403 .6396	+.0015 +.0022 +.0031 +.0042 +.0052 +.0058 +.0063 +.0065 +.0065 +.0065 +.0057 +.0051
1921 J F M A M J A S O N D	.6967 .6987 .7039 .7068 .7083 .7192 .7078 .7008 .6945 .6931 .6745 .6619	.7078 .7068 .7061 .7053 .7043 .7029 .7005 .6970 .6922 .6862 .6791	.6903 .6896 .6888 .6878 .6866 .6856 .6845 .6833 .6822 .6810 .6798 .6786	+.0175 +.0172 +.0173 +.0173 +.0175 +.0177 +.0173 +.0160 +.0137 +.0100 +.0052 0007 0073	1926 JF M A M J J A S O N D	.6430 .6399 .6407 .6353 .6320 .6323 .6350 .6366 .6364 .6360 .6324 .6312	.6433 .6419 .6405 .6390 .6376 .6362 .6350 .6339 .6330 .6322 .6316	.6390 .6383 .6376 .6370 .6364 .6357 .6346 .6342 .6338 .6334	+.0043 +.0036 +.0029 +.0029 +.0001 0001 0007 0012 0018 0022

TABLE 11 (Concluded)

Date	1	2	3	4	Date	1	2	3	4
J F M A M J J A S O N D	.6285 .6287 .6250 .6199 .6196 .6233 .6242 .6205 .6173 .6129 .6082 .6064	.6299 .6287 .6271 .6251 .6228 .6202 .6177 .6153 .6133 .6118 .6110	.6326 .6323 .6320 .6317 .6314 .6311 .6309 .6307 .6306 .6304 .6302 .6301	0027 0036 0049 0066 0086 0109 0132 0154 0173 0186 0192	1932 JF M A M J J A S O N D	.6753 .6806 .6713 .6846 .6856 .6900 .6811 .6571 .6489 .6489 .6521	.6668 .6733 .6778 .6801 .6800 .6777 .6736 .6681 .6618 .6552 .6488 .6429		
J F M A M J A S O N D	.6073 .6099 .6109 .6132 .6181 .6283 .6352 .6412 .6364 .6360 .6322 .6395	.6115 .6128 .6146 .6170 .6199 .6230 .6264 .6300 .6335 .6369 .6402 .6431	.6300 .6299 .6298 .6297 .6296 .6295 .6294 .6295 .6296 .6297 .6299	0185 0171 0152 0127 0097 0065 0030 +.0006 +.0040 +.0073 +.0105 +.0132	1933 J F M A M J A S O N D	.6206 .6204 .6372 .6547 .6392 .6238 .6157 .6102 .6128 .6139 .6274	.6378 .6337 .6307 .6285 .6269 .6256 .6242 .6223 .6200 .6170 .6136		
1929 JF M A M J J A S O N D	.6428 .6468 .6497 .6493 .6510 .6551 .6576 .6544 .6604 .6571 .6479	.6457 .6480 .6499 .6515 .6528 .6537 .6542 .6536 .6524 .6536 .6506	.6301 .6304 .6307 .6310 .6314	+.0156 +.0176 +.0192 +.0205 +.0214	1934 JF MAAM JASOND	.6111 .6016 .5940 .5872 .5812 .5715 .5707 .5765 .5828 .5754 .5658	.6058 .6017 .5975 .5932		
1930 F M A M J J A S O N D	.6421 .6410 .6335 .6387 .6354 .6322 .6271 .6203 .6145 .6124 .6168	.6453 .6421 .6387 .6355 .6324 .6294 .6265 .6236 .6205 .6172 .6138 .6105			1935 MAM JASOND	.5469 .5363 .5326 .5329 .5363 .5336 .5311 .5379 .5399 .5414 .5369			
1931 F M A M J A S O N D	.6105 .6110 .6122 .6108 .6023 .6038 .6030 .6081 .6149 .6385 .6524	.6075 .6053 .6041 .6043 .6063 .6100 .6155 .6225 .6309 .6401 .6495			1936 J	.5263			

CHART 31

NEW ENGLA	ES, COUNTIES AND CITIES WHC ERS, AND THE PERIODS DURING
OR CITY	161 161 161 161 161 161 161 161 161 161
VERMONT WE	
CONNECTION	
BATH, ME.	
RHODE ISLAND	
CARBRIDGE, MASS.	
LYNN, MASS.	
BROOKLYN, N. Y.	
WORCESTER, MASS.	
CHELSEA, MASS.	
FITCHBURG, MASS.	
SPRINGFIELD, MASS.	
BROOKLINE, MASS.	
NEWTON, MASS.	
SOMERVILLE, MASS.	
MANCHESTER, N. H.	
PORTSHOUTH, N. H.	
PROVIDENCE, R. 1.	
HOLYOKE, MASS.	
MALDEN, MASS.	
QUINCY, MASS.	
Middlesex Co., MASS.	
NORTHAMPTON, MASS.	

NEW ENGLAND MUNICIPAL BOND YIELDS, JANUARY INDEX NUMBERS

- 1. An unadjusted chain index number based on simple geometric averages of the yields each January.
- $2. \ \ \,$ An unadjusted chain index number based on simple arithmetic averages of the yields each January.

In both the index numbers (geometric and arithmetic), the chaining is backward from January 1914. The index numbers for January 1914 are therefore the averages (geometric or arithmetic) of the yields of the bonds used in January 1914.

Date	(1) Geometric Index	(2) Arithmetic Index
	%	%
Tomas 1057	5.211	5.198
January 1857		
1000	5.271	5.270
1009	4.854	4.843
1000	4.805	4.794
1901	4.923	4.909
" 1862	5.240	5.226
" 1863	4.410	4.403
" 1864	4.676	4.666
" 1865	5.164	5.153
" 1866	5.757	5.748
" 1867	5.265	5.255
" 1868	5.373	5.367
" 1869	5.318	5.310
" 1870	5.515	5.510
" 1871	5.439	
1011		5.432
1014	5.353	5.345
1019	5.496	5.484
7014	5.652	5.642
10(0	5.336	5.327
1910	4.776	4.767
" 1877	4.530	4.525
" 1878	4.369	4.364
" 1879	4.287	4.285
" 1880	4.199	4.199
" 1881	3.838	3.843
" 1882	3.697	3.700
" 1883	3.619	3,621
" 1884	3.649	3.651
" 1885	3.593	3.595
" 1886	3.419	3.422
" 1887	3.409	
" 1888		3.407
	3.733	3.735
1999	3.589	3.589
1990	3.335	3.336
1891	3.640	3.646
1892	3.655	3.657
1999	3.611	3.613
" 1894	3.667	3.665
" 1895	3.470	3.470

TABLE 12 (Concluded)

Date	Geometric Index	(2) Arithmetic Index
January 1896	3.705	3.705
1897	3.437	3.435
" 1898	3 308	3.307
" 1899	3.123	3.121
" 1900	3.201	3.198
" 1901	3.081	3.081
" 1902	3.173	3.170
" 1903	3.253	3.250
" 1904	3.255	3.469
" 1905	3.400	3.398
" 1906	3.506	3.505
" 1907	3.759	3.760
" 1908	4.224	4.231
" 1909	3.878	3.879
" 1910	3.893	
" 1911		3.893
" 1912	4.008	4.007
	4.003	4.002
" 1913 " 1914	4.239 4.367	4.242 4.372

TABLE 13

New England Municipal Bond Yields, Arithmetic Average Quarterly Index Number, January 1857-January 1914

An unadjusted chain index number based on simple arithmetic averages of the yields each quarter. The January 1914 figure is the arithmetic average of the bonds used in that month.

Date	Index	Date	Index	Date	Index
1857 J A J O	5.198 5.118 5.102 5.382	1866 J A J O	5.748 5.603 5.502 5.230	1875 J A J O	5.327 5.128 4.966 4.868
1858 J A J O	5.270 5.006 4.957 4.921	1867 J A J O	5.255 5.349 5.411 5.362	1876 J A J O	4.767 4.637 4.497 4.476
1859 J A J O	4.843 4.818 4.833 4.798	1868 J A J O	5.367 5.275 5.245 5.258	1877 J A J O	4.525 4.466 4.384 4.407
1860 J A J O	4.794 4.800 4.767 4.806	1869 J A J O	5.310 5.366 5.394 5.462	1878 J A J O	4.364 4.381 4.330 4.301
1861 J A J O	4.909 4.878 5.102 5.270	1870 J A J O	5.510 5.452 5.400 5.409	1879 J A J O	4.285 4.256 4.191 4.146
1862 J A J O	5.226 5.064 4.864 4.508	1871 J A J O	5.432 5.337 5.291 5.243	1880 J A J O	4.199 3.959 3.994 3.937
1863 J A J O	4.403 4.201 4.426 4.457	1872 J A J O	5.345 5.314 5.360 5.458	1881 J A J O	3.843 3.713 3.653 3.654
1864 J A J O	4.666 4.678 4.903 5.060	1873 J A J O	5.484 5.541 5.512 5.675	1882 J A J O	3.700 3.639 3.579 3.611
1865 J A J O	5.153 5.617 5.664 5.736	1874 J A J O	5.642 5.470 5.420 5.412	1883 J A J O	3.621 3.632 3.621 3.665

TABLE 13—(Continued)

Date	Index	Date	Index	Date	Index
1884 J A J O	% 3.651 3.591 3.633 3.627	1893 J A J O	% 3.613 3.631 3.829 3.887	1902 J A J O	% 3.170 3.189 3.262 3.251
1885 J A J O	3.595 3.540 3.505 3.465	1894 J A J O	3.665 3.753 3.700 3.651	1903 J A J O	3.250 3.305 3.483 3.462
1886 J A J O	3.422 3.366 3.363 3.393	1895 J A J O	3.470 3.451 3.469 3.465	1904 J A J O	3.469 3.474 3.459 3.409
1887 J A J O	3.407 3.441 3.535 3.749	1896 J A J O	3.705 3.432 3.579 3.719	1905 J A J O	3.398 3.386 3.458 3.503
1888 J A J O	3.735 3.687 3.654 3.615	1897 J A J O	3.435 3.407 3.380 3.349	1906 J A J O	3.505 3.552 3.661 3.754
1889 J A J O	3.589 3.482 3.410 3.349	1898 J A J O	3.307 3.608 3.279 3.191	1907 J A J O	3.760 3.847 3.905 4.101
1890 J A J O	3.336 3.378 3.427 3.540	1899 J A J O	3.121 3.106 3.068 3.144	1908 J A J O	4.231 3.977 3.994 3.926
1891 J A J O	3.646 3.591 3.674 3.641	1900 J A J O	3.198 3.165 3.139 3.105	1909 J A J O	3.879 3.807 3.845 3.893
1892 J A J O	3.657 3.611 3.583 3.580	1901 J A J O	3.081 3.109 3.136 3.168	1910 J A J O	3.893 3.991 4.085 4.048

TABLE 13—(Concluded)

Date	Index	Date	Index	Date	Index
1911 J A J O	4.007 4.007 4.007 4.000 4.011	1912 J A J O	4.002 4.019 4.093 4.162	1913 J A J O 1914	% 4.242 4.391 4.572 4.403
				J	4.372

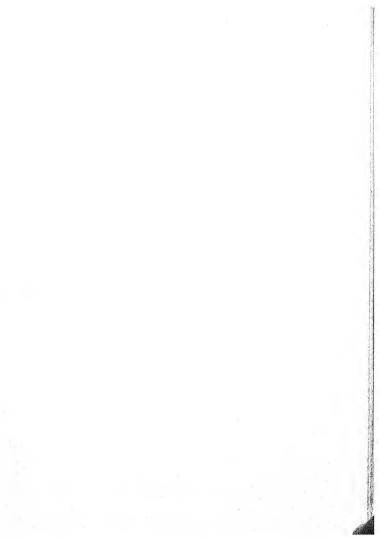


CHART 32

- 0 4 4 10 10 4 10 10 10 10 10 10 10 10 10 10 10 10 10	WEE PERIOD WANTE OF RAVIESOD SACTIONS AND DISC. SACTIONS AND DI	PERIODS DURING WHICH THEIR COMMON STOCK PRICES WERE USED IN CONSTRUCTING INDEX NUMBERS
±8.5.8.8.8	GUI LORD AND NOTHWESTERN CHICARO, ST. PAUL, MINSTAPOLIS & GMAHA HIGHON GENTRAL HIGHOR RIVER HIGHOR RIVER HIGH YORK CENTRAL AND HORDON RIVER HIGH YORK CENTRAL AND HORDON RIVER HIGH YORK CENTRAL AND HORDON RIVER	
\$ 50 50 50 50 50 50 50 50 50 50 50 50 50	THE TABLE AND AND AND AND AND AND AND AND AND AND	

(CONTINUED) STOCKS CHART 32 AMERICAN RAILROAD PITTSBURGH, GINCINNATI, CHICAGO & ST. LOUIS CHICAGO, MILWAUKEE, ST. PAUL & PACIFIC COLUMBUB, HOCKING VALLEY AND TOLEDO ST. PAUL, MINNEAPDLIS AND MANITOBA YORK, NEW HAVEN, AND HARTFORD HILMAUKEE AND PRAIRIE OU CRIEM ---PITTEBURGH, FORT WAYNE & CHICAGO CNICAGO, ST. LOUIS AND PITTSBURGH NEW YORK, CHICAGO AND ST. LOUIS NEW YORK, LAKE ERIE AND WESTERN CHICAGO, MILWAUKER AND ST. PAUL CHICAGO, BURLINGTON AND QUINCY NAME OF RAILROAD

CHART 32

AMERICAN RAILROAD STOCKS (CONCLUDED)										
AMER	KEW YORK, SUSQUENAKHA AND WESTERN ST. LOUIS, IRON WOUNTAIN AND SOUTHERN	BO, GENVER AND RIO GRANDE BI. MESTERN PACIFIC BOT STORM LADVIAND		98, ST.LDUB SOUTHWESTERN 99, LOUSIVILE & MANVILLE ON MANVILLE CULTERNOOD	ATLANTIC COAST LINE	95. OREGON SHORT LINE AND UTAM NORTHERN 95. SOUTHERN PARTIN	96. MOBILE AND ONIO 97. SOUTHERN RAILWAY 98. WISCONBIN CRITARIA	99. CANADIAN PACIFIC 100. OBLUTH, SOUTH SHORE AND ATLANTIC 101. HINNEAPOLIS, ST. PALL AND SAULT STE, MARIE 102. FLINT AND PER EMREUTTE	103. Per Manuelle 105. Only Str. Louis, San Falmeiro 105. Only Southern 107. Instruction and Str. Louis 107. Instruction and Str. Louis 109. Instruction of Netzern 109. Only Control Officers of Netzern 109. Control Officer Western 109. Control Offi	III. GULF, MOBILE AND NORTHERN

RAILROAD COMMON STOCK PRICE RELATIVES, JANUARY 1857-JANUARY 1936

The numbers at the heads of columns are the numbers assigned to the various railroads in Chart 32. For example, the figures of Column 1 refer to the Baltimore and Ohio Railroad. The figures in the single column entitled '51 to 52' refer first to the Chicago, Milwaukee and St. Paul Railway (January 1874 to January 1928) and then (lower down) they refer to the Chicago, Milwaukee, St. Paul and Pacific Railroad (January 1928 to January 1936).

Each relative price in Table 14 is the ratio of the average price of a specified stock in a particular January to the average price of the same stock in the preceding January, after all adjustments have been made for stock dividends, rights, assessments, etc. For example, the first number in the table is .5855. This means that the average price of Baltimore and Ohio Railroad common stock in January 1858 was a little less than three-fifths (.5855) its average price in January 1857.

The blank spaces in the table correspond to periods in which particular stocks were not used in constructing the stock price index numbers.

TABLE 14-RAILROAD COMMON STOCK PRICE RELATIVES

January Dates	1	2	3	4	5	6	7	8	9	10	11
1857-1858	.5855		.9201	.8093	.6706		.6176		1.0464	.9402	1.0664
1858-1859	1.1841		.9098	1.1551	8968		1 1 0337		1 1746	1.2685	1.0551
1859-1860 1860-1861	1.2045		.9235 9619	1.0909	1 0483		1.0294	1.0985 1.0713 1.4901	1.0593		1.2100
1861-1862	.8606		.9965	.9039	.9289		.7566	1.0713	.9671	.9634	.8092
1862-1863	1.7239		1 4236	1 8164	2.2465		1.7191	1.4901	1.2084	1.4028	1.7640
1863-1864	1.2056		1.4253	1.4662	1.5063		2.5704		.9767	1.0297	.9592
1864-1865 1865-1866	1.0585	.8137	1.2703 .8284	1.1463	0702		1 2613		.9941	1.2832	1.0588
1866-1867	1.0426	.8838	1.0469	.9505	1.0012		1.1424	1.0686	1.1225	1,1639	.9647 1.0864
1867-1868	1.0967	1.3280	1 0016	.8369	9450		.8221	.9317	1.0116	1.0498	1.0383
1868-1869	.9451	1.1324	.8714	1.0790	1.1130		1.0745	.9881	1.0191	1.0123	1.0347
1869-1870	1 0447	6998	.9515	.8736	1.0678		1.0551	.8452	1.0668	.9789	9990
1870-1871 1871-1872 1872-1873	1.0804	1.2817	.9775 1.0156	.9947 1.0067	1.0404		1.3280	1.0607	1.0278	.9738 1.0817	1.0380
1872~1873	1.0688	1.0440	.9641	.9282	1.0055		1.1205	.9255	.9022	.9730	.8877
1873-1874	1 0193	.6991	1.0600	1.0515	.9835		.9542	.9854	8353	. 9545	.7489
1874-1875 1875-1876	1,2053	.8908	.9602	1.0515	.9822		1.1585	1.0544	1.1094	.8512	.7062
1875-1876 1876-1877	.9070 .8764	.6961	1.0671 .5350	1.1064	.9650		1.0177	.9883	.9350	.7978 .8614	.2192
1077 1079		1.1382	.7472	.6860	0015		7620	E424			.4561
1877-1878 1878-1879	.6018 1.0747	1.2414	.8504	.9952	8139		.7630 1.0476	.5424 2.4843	.9888 1.1135	1.1416	.8527 2.5990
1879-1880		3.1967	1.8289	1.7338	2.5598			2.0549	1.0902	1.0044	2.5639
1880-1881	1,2451	1.3253	1.3065	1.3574	.8690			1.0802	1.2365	1.1064	1.2241
1881-1882 1882-1883	1.0294 1.0254	.8726 .9210	1.0730 1.0146	1.0760	1.0426			1.0539	1.9848		.9380 1.0624
	9912	71.39	9838	9.301	1.0012			1 1987	1 0673		0722
1884-1885	,8496	.7485	.6596	. 7360	.3077			.4186 1.2117	1.0700		1.2277
1884-1885 1885-1886 1886-1887	1.1013	1.3286	1.3131	1,3829	1.2379			1.2117	1.0814		1.6661
	.9191	1.1424	1.1179	1.1269	1.8493			1.4077	1.1238		1.6819
1887-1888 1888-1889	.6173 .8456	.9036	1.0426	.9659 1.0854	1.6692			1.2552	1.0060		.8941
1889-1890	1.1207	.9117	1.2517	9604	7781			1.2526	1 1771		
1890-1891	,9298	.8760 1.2145	,9799	,9909	,8650			.9087	1.0998		
1891-1892 1892-1893	1 1564	1.2145	9367	1.0593	1.2323			1.0278	,8836		
1892-1893 1893-1894	1.0698	1.0191	1.0824 .9805	1.0659	1.2671			1.1174	1.0693		
1894-1895	. 9320		1.0079	.9778	.5686			7854	1 2621		
1894-1895 1895-1896	.6351		.9623	.9877	.2504			.7854 1.1363	1.0100	1.1064	
1896-1897	.4005		,9143	.9637	.6662			,9901	.9879		
1897-1898 1898-1899	.8921		.9863	.9924		.8386		.9417 1.0725	1.0335		
1898-1899	1.0102		.9961 1.0363	1.0445		1.0170		1.0725	1.0088		
1900-1901	1.5185		1.2448	1.1023		1 6746		1.1776 1.3026	0712		
1900-1901 1901-1902 1902-1903	1.1904		1.23081			1.8578		1.2650	.9897		
1902-1903	.9948		.9883	.9990		1.1492		.9567	1.0021		
1903-1904	1 2717		.9438 1.1256	1.0000		.7079		.8750	.8707		
1904-1905 1905-1906	1.1102		1.2212	1.3699		1.8555		1.1945	0036		
1906-1907	1 0323		0847	1 0629		9663		0492	0251		
1907-1908 1908-1909	,7248		.7233	.9293		.7939		.8093	.8434		
1908-1909	1.2894		1.13191	1.1923		1.3449		1.3332	.9982		
1909-1910	1.0566		1.0000	1.2474		1.1801		1.3189	1.0899		
1910-1911 1911-1912 1912-1913	.9791		1.0214	1.0877		9485		. 8832	8507		
1912-1913	.9927		.9735	1.0474		1.0703			.9624		
1913-1914	.8956		.9343	.9011		1.0290			.5104		
1914-1915 1915-1916	1 2006		.9507 1.0349	1.0402		.8760			.5612		
1916-1917	0010		.9914			1.0/5/			1.3450		
1917-1918	6303		.7253	7447		1.2624			1.1148		
1917-1918 1918-1919	.9018		.9417	1.0249		1 0849			1 3830		
1919-1920	,6862		.9181	1.0125		.9545			1.1765		
1920-1921	1.1125		1.0668	1.1784		1.1182			.6714		
1921-1922 1922-1923	1 2057		1.0750	1.0585		.8583			.6489		
1923-1924	1.3195		.9932	.8905		8639		1.1945 1.1725 9.0482 8.093 1.3332 1.3183 8.832	1.1001		
1924-1925 1925-1926	1.3568		1.2741	1:2584		1.3712			1.5059		
1925-1926	1.1532		1.1434	1.0491		1.1099			2.7868		
1926-1927	1.1921		1.0952	.9680		1.1262			1.1636		
1927-1928 1928-1929	1.0779		1.0322			1.0370			1.0948		
1929-1930	.9787		.8474	1 0707		1.0866			1.7382		
1930-1931 1931-1932 1932-1933	.6472		.8690	.6535		.6860			6106		
1931-1932	.2273		.5103	.2582		.4170			.2026		
1932-1933 1933-1934	2 7320		1.2181	1.0187		.7769			.7514		
1934-1935	.4804		.6242	6201		8054			1.6216		
1934-1935 1935-1936	1.3633		1.0206	.9783		.9985			1 4252		

JANUARY 1857 TO JANUARY 1936

	T				1			1		T	January
12	13	14	15	16	17	18	19	20	21	22	Dates
.7232			.7368			.6819 .8963 .9353 1.1158 .9782 1.3400 1.2289			.8480	.6011	1857~185
.8548			.7395			.8963			1.0747	1.7583	1858-185
1.0404			1.2030			.9353			.8695 1.0760	1.2437	1859-186
0224			7660			0782			1.0760	1.1151	1860-186 1861-186
1 6947			1.4302			1 3400			1.4181	3 2227	1862-186
1.5209			1.3409	1.6807		1.2289	2.6026		1.1524	1 5125	1863-186
.7126			1.0193	.6860			.7143		.8270	.7714	1864-186 1865-186
1.0600			1.1382	.7952			.8759		.8529	.9893	1865-186
1,2379			.9245	1.0529			1.2362		1.1087	1.2238	1866-186
.9904			1.1706	1.5035			1.7002		1.1956	1.6025	1867-186
1.3056			1.1468	.7824			1.5101		1.2826	.9571	1868-186
1.82/4			.9788	1 3505			.8581		1.1202	1.2114	1869-187
1 0235			9605	7725			0710				1870-187
1 0275			.9408	.,,,,,,			1 1596				1872-187
.9241			,8235				.7280	1111111			1873-187
.9976			,9803				.7672				1874-187
1.0375			.9962				.8870				1875-187
.9463			.5852				.8805				1876-187
.9821			1.2776				1.0035				1861-1864 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1864-1866 1870-187 1874
1.2414		1.5279	1.1382				1.5974				1878-187
1.2246		2.4683 1.3277	1.2131		1 4757		1.5783				1879-188
0620		1.0812	1 0212		1 0617		0831	7475			1880-188
G408		9910	1.0912		1.4727 1.0617 .7572		1.0435	1.4408			1882-188
0326		. 9091	1.0280		.5301		.8700	.5997			1883-188
.9170	::::::	.7212	.8998		.9298		.7598	.8245			1884-188
1.2045		1.3864	1.1537		1.5470		1.2238	1.5136			1885-188
. 9767		.000/	.9544		1.6099		1.0493	1.2665			1886-188
.8982			.9475		.6364		.9596	,8086			1887-188
.8717			.9644		1.1161		.9931	.8188			1888-188
.9797			1.0349		.8426		1.0297	1.0404			1889-189
. 1209			1 0024		1 3065		1 0002	1 9790			1890-189
9390			9333		8212		9690	1 0619			1807-180
7589			.8990		.2428		.8903	.6997		1111111	1893-189
.9579			.9376		.7953		.9485	.9291			1894-189
1.0532			1.0942		.9231		1.0209	1.0459			1895-189
1.0342			1.0028				1.0619	1.4525			1896-189
1.3431			1.1259				1.1880	1.5087			1897-189
1.3948			1.1166				1.1918	1.2773			1898-189
.9054			.9544				1.0977	1.2697			1899-190
1.3721			1.1744				1 2173	1.0602			1000-190
1.3459	.4752 1.4987 .6898		1.1468				1.0532	1 1453		1111111	1902-190
	.4752		.8881				,8113	,9006			1903-190
	1.4987		1.1885				1.3552	1.2930			1904-190
	.6898		1.1355				1.1156	1.0347			1905-190
	1.1138		.9270				.9167	.8505			1906-190
	.5293		.7758				.8214	.7742			1907-190
	1.7061		1.1692				1.2465	1.2173			1908-190
• • • • •			.9914				.9791				1909-191
	7812		1 0300				9768				1011-101
	9210		.8903				,9634				1912-19
	.6463		.8898				.9652				1913-191
.9574	.0554		.9775				.9545				1914-191
.9574			.9885				1.0493				1915-191
1.8055			.9842				.9256				1916-19
.4167			.8905				.7677				1917-191
1.1825			1.0332				1.0114				1918-19
1.0186			0057				7077				1020-10
1.1545			1.1236			[::::::]	.9093				1921-19
.0433			1.1176				1.2871				1922-19
.7642			.9195				.6385				1923-19
1.8523			1.1358			[1.4253				1924-192
1.2266			1.0375				1.0619				1925-19
1.2500			1.0118				1.0486				1926-19
			1.1286				1.0602				1927-19
1.2276			1.0271				1.0358				1928-19
.8632			.9133				.9641				1929-19
2206			1752				2410				1031-10
.3714			9366			11111111	.5306				1927-19 1928-19 1929-19 1930-19 1931-19 1932-19 1933-19
.8528							1.8603				1933-10
			.4577				.5441		7:::::		1934-19
,5711			1,3904				.7500				1935-19

TABLE 14--RAILROAD COMMON STOCK PRICE RELATIVES

			TA	BLE 1	4RA	LROAD	COMMO	on Sto	ск Рві	CE REI	LATIVES
Intuary	23	24	25	26	27	28	29	30	31	32	33
1857-1858			. 4621	.5782		. 2339	.5465			1.0030	1.0337
1858-1859			1.8884	.9476		.9970	.7470			1.1408	1.0993
1859-1860			1 7720	1.7017		2.4609	1 7660			1.0409	1.0201
1861-1862			8178	9074		1.3329	1.0894			1.0127	1 0111
1862-1863			2.9696	1,8488		1.3329	2.2925			1.2340	1.3508
1863-1864				1.3568		1.5675	1.4980			1.0462	.9270 1.0411
1864-1865	1			.8583		1.0469	.8659			.9717	.9134
1865~1866				1 0025		1.0508	1 1233	1		1.1041	
1000-1007				1 0385		1 1682	1 0014			1.1041	1 4273
1868-1869				1.1811		1.1535	.9747	.9395			
1869-1870				1.0000				.9054			
1870-1871	1.0268			.9957					1.0561		
1871-1872	1.0550			0552					1 1709		
1873-1874	.9903			.8432					.8590		
1874-1875	.9981			.9605					.9430		
1875-1876	1.0688			.7504	· · · · · · ·				.8431		
1876-1877	.9407			1.0004					1 1054		
1877-1878	1.0428	[:::::		1.2024	1.3558 1.1311 .6740 1.2723 .7568 .5917 1.3351 1.4494				1.1524		
1879-1880	1.1484			1.1051	1.3558				1.4292		
1880-1881	1.1458			1.3602	1.1311				1.2990		
1881-1882	.8727			,7039	1 2723				.8557		
1882~1884	.8922			.9102	.7568				.8544		
1884-1885	.7665			.6443	.5917				.6392		
1985-1886	1.2050			1.2589	1.3351				1.3967		
1880-1887	0.634			.9478	0202				1.0932		
1887-1888 1888-1889 1889-1890	1.0100			1.0207	9465				1 1051		
1889-1890	.9833			1.0945	1.0493				1.0125		
	.9591			.9697 1.1548	.9176				1.0249		
1891-1892 1892-1893 1893-1894	9576			.9918	. 9512				1.0656		
1893-1894	.8975			.9252	.8580				.9509		
1894-1895	1.0018			.9807	1.0053				1.1125		
1894-1895 1895-1896 1896-1897	.9784			.9501	.9528				1.0238		
1807-1808	1.1998			1.1479	1.1801				1 1926		
1898-1899 1899-1900	1.1674				1.1564						
1899-1900	1.0590				1 1400						
1900-1901 1901-1902 1902-1903	1.1910				1.5329						
1902-1903	.9464										
1903-1904	.7802										
1904-1905 1905-1906	1.0922										
1906-1907	.8908										
1907-1908	.7435										
1908-1909 1909-1910	1.3243										
1010~10111	.9228										
1011-1012	.9820										
1912-1913	.9891										
1014-1915	. 8555	9595							• • • • • • • •		
1914-1915 1915-1916 1916-1917		1.2100									
1916-1917		.9481									
1917-1918		.6931									
1010-1020		0.0259									
1920-1921		1.0486									
1921-1922		1.0188									
1922-1923		1.2094									
1924-1925		1.1690									
1925-1926		1.0832									
1916-1917 1917-1918 1918-1919 1919-1920 1920-1921 1921-1922 1922-1923 1923-1924 1924-1925 1925-1926 1926-1927		1.0747						• • • • • • •			
1927-1928		1.1840									
1929-1930		.9319									
1930-1931		.6881									
1931-1932	• • • • • • •	6186									
1933-1934		1.8988									
1926-1927 1927-1928 1928-1929 1929-1930 1930-1931 1931-1932 1932-1933 1933-1934 1934-1935 1935-1936		.5319									

JANUARY 1857 TO JANUARY 1936

34	35	36	37	38	39	40	41	42	43	44	January Janu
	,8959					.8240		.1775			1857-185
	1.0515					1.0817		.9500			1858-185
	.9434					.8723		.7242			1859-186
	1.0464					1.0184		1.4362			1860-186
	1.1458					1.0097		1.6316			1861-186
	1.4635					1.6734	1111111	4.0170			1862-186
	1.1179					1.1074	1.2584	1.7374		1.2067	1863-186
	1,1008					.9/90	1.1207	.8022		1.1855	1864-186
	0371					1 0150	1.0170	1 0222		.8626	1865-186
	.9271					1,0136	1.0102	1.0332		1.0414	1800-180
.037i	,9224					1.0198	1.0202	1.1161		.9287	1867-186
.0371	1 0271					1.0799	1.1752	1.0676		1.1094	1858-180
.0051	1 1104					1.0049	1.3080	1.1205		.8924	1809-187
9811	1 0767					0875		1.1981		9571	1071-107
.9882	1 0250					9643		1.2193		0706	1972-197
.9448	8507					9637				8172	1972-197
9712	8622		1111111			1 1277				1 0457	1874-187
9806	.8800					1 0014				1 0634	1875-187
9565	.6118					.8755				7111	1876-187
.9615	0064					6554				6250	1077 10
0760	1 1474					1 0606				9245	197910
0696	1 0156		8 4411			1 5364				2 4615	1870-18
1045	1 1709		1.0728			1 2812				1 3803	1880-18
9821	8715		1.0544			9252				1 0619	1881-188
0578	9938		.9435			.9974			1 2255	1 1089	1882-188
1182	.7826		.6311			.9700			1.0702	1.0812	1883-18
9646	.5079		.4155			.8632			.9664	.9313	1884-18
0522	1.7266		1.9802			1.0595			1,2682	1,2817	1885-18
1511	1,1403		.7475	1.1709		1.0457			1,1447	1.0852	1886-18
9925	8333		.4786	6627		9776			9574	1 2204	1887-18
.0214	1.1285		.7553 1.8109	1.0483		.9930			1.0235	.8902	1888-18
0704	1.4233		1 8100	.8271		1.0000			.9743	.9229	1889-189
0342		.8745	.6887	1.2921		.9436			.9707	.9359	1890-189
0095		1 1 . 1585	1.4488	1.1943		1.0965			1,1048	1.0418	1891-189
.0529		.8047	.8793	.9816		.9744			1.1636	1.0109	1892-189
			.7419	.6516		.9129			.8873	,9711	1893-189
.0321		1.1089	.9855	.8577		1.0228			.8692	.9777	1894-189
.0067		.8903	.8641	.9855		1.0351			.9609	1.0266	1895-189
.9952		.8309	1.1744	.7436		1.0072			,5873	1.0009	1896-18
.0585		1.2656	1.3222			1.1174			.8205	1.1471	1897-189
.1363		1.4578		4756	1.1787	1.1220			1.6719	1.1741	1898-189
		1 1 . 2003	1.0780		1.1787	1.0177			.7663	1.0522	1899-19
		1.2368	1.3177		1.3388	1.1490				.9928	1900-19
		1.2642	1.1811		1.3388 1.5867 1.4727 .7378 1.1912 1.3125 .9866	1.0787				1.1644	1901-19
		.9943	1.0854		1.4727	1.0351				1.1171	1902-19
		.8111	.6682		.7378	.7916				.7644	1903-19
		1.2184	1.4240		1.1912	1.1439				1.2494	1904-19
		1.1179	1.2089		1.3125	1.0554				1.0193	1905-19
		.8377	.8965		.9866	,9304				1.0025	1900-19
		.6139	.5857		.9866	.8368				.8714	1907-19
		1.2761	1.9050			1.1719				1.2712	1908-19
		1.1321	1.4250			1.0757				1.1445	1909-19
		.8082 .8915	.9594			,9555					1910-19
		.8915	1.8732			.9021					1012 10
		.9304 .7312 .5368 2.0922 1.1492	21.0770			.9939					1012-19
		1312	.0109			0400					1014-10
		2 0022	1 4494			1 0008					1015-10
		1 1402	1 0100			0711					1016-10
		1.11/2	1.0102								1010 10
			.8140			.8104					1917-19
			1.0022			.9720					1910-19
			1.0021			.9200					1020 10
			1.0077			.9000					1021 10
			1 2008			1 3813					1022-10
			1 0060			9402				l	1923-10
			1 3237			1 0884					1924-19
			1.2543			1.1110					1925-19
• • • • •			1.2942			1.0720					1926-19
						1 1224					1027 10
						1.1234					11927-19
• • • • •			1.0831			1.2020					1928-19
			1.0/43			19024					1929-19
			.9001			2307					1021-10
			.0080			8140					1037-19
			1 5060			2 0152					1033-10
			1 0384			7011					1034-10
			1 2497			1 4470					1035-10

TABLE 14-RAILROAD COMMON STOCK PRICE RELATIVES

					;r 1(///	LROAD		N 3100	JK I KI		ATIVES
January Dates	45	46	47	48	49	50	51 & 52	53	54	55	56
1857-1858 1858-1859 1859-1860 1860-1861 1861-1862 1862-1863 1863-1864 1864-1865 1865-1866 1867-1868 1868-1869 1870-1871 1871-1872 1872-1873 1874-1875 1876-1877			. 8182	.4073				.5889			
1858-1859			1.4132	.4098		.8578 1 2391		.8697			
1859-1860			.8942	.1904				.7730			
1860-1861			1.2957	5.2012	4 6100			8200			
1861-1862			1.0849		2 0740			2 1111			
1863-1864			1 3219		1.3855			1,4099			
1864~1865			.8834		.7261			1.0421			
1865-1866			.8354		.9289			1.1447			
1866-1867			1.0363			.8578		1.1692			
1867-1868			. 8066			1.2391		1.2942	.9825		
1868-1869			1.0740			1.4679		1.30//	1.7857		
1869-1870			1 1316			8015		1 0067	7783		
1871-1872			1 0207			1.1008		.0442	.6221		
1872-1873			.9715			.9316		,9360	.8995		
1873-1874			.9968			.8674		.8442	.6403		
1874-1875			1.0325				1 0222	1.0812	.7204		
1875-1876			1.0264				4805	1 0174	6824		
1870-1877			.7032				1 0007	.8736	9220		
1877-1878			.8440				1.0055	1 1125	1 2377		
1870-1880			1 4914				1.8741	1.2598	2.6345	6.4032	
1880-1881		::::::	1.1264				1.4990	1.4578	1.3465	6.4032 1.0330 1.0141	.9822
1881-1882			1.0498				.9671	.8622	1.8763	1.0141	.7632
1876-1877 1877-1878 1878-1879 1879-1880 1880-1881 1881-1882 1882-1883 1883-1884 1884-1885 1886-1887			1.0351			. 8578 1.2391 1.4679 1.1479 1.1008 9316 8674	1.1371	.9316		1.3721	1.3909
1883-1884			1.1102				.8424	.9822		.4081	.7865
1884-1885	1 7649		0608				1 2694	1 1687		1 6823	1 7330
1886-1887	1.2394		1.0044				.9558	1.0023		1.0000	1.4747
1987-1888	7857		0823				8493	9369		.8134	1 2017
1887-1888 1888-1889 1889-1890	1.0634		.9865				.8391	.8498		1.1647	.6468
1889-1890	1.1156		.9669				1.0935	.9767		1.2382	.8392
1890-1891	.8210		.9433				.8201	.8371		.8787	.7444
1891-1892		2.0086	1.0188				1.4122	1.2100		.9612	1.8811
1892-1893		6637	6420				7181	7533		2652	5365
1894-1895		1.1532	9035				.9738	.9389		.7127	.8177
1895-1896		1.0445	1.0671				1.2184	1.0600		1.1722	1.3070
1896-1897		.8184	.8043				1.1038	.9750		.4068	.8307
1897-1898		3.1089	.8417				1.2656	1.3580		1.7081	1.0705
1898-1899		1.8450	1.0325				1.3170	1.3348		1.9616	1.7914
1899-1900		.9572	1 2671				1 2057	1 1700		1 5063	1.3020
1900-1901		1 4391	1 1617				1.1156	1.1790		1.0900	
1902-1903		1.0745	1.1355				1.0930				
1903-1904		.7052	.8894				.8036				
1904-1905		1.1869	1.5035				1.2098				
1905-1906		1.1071	1.4652				1.0001				
1900-1907		.00/9	.9048				7245			7020	. 7632 1.3909 . 7865 . 7327 1.7330 1.4747 1.2017 6.468 8.392 . 7444 1.8811 . 9583 . 5365 . 8177 1.3070 . 8307 1.0705 1.7914 1.3020
1009-1000		1 3016	1 2792				1 3483			1 1374	
1909-1910		1.0975	1.4125				1.0172			9880	
1910-1911		1.0018	1.0292				.8349			.8660	
1911-1912		1.0235	.9712				.8506			.9797	
1912-1913		1.0100	.9485				1.0556	<i>.</i> .		1.0202	
1913-1914		.8358	.9304				9050			.9442	
1915 1916		1.1413	1.1676				1.0942			1.1130	
1916-1917		1.0032	.9920	[.9075			.9403	
1917-1918			.7312				.4959			.7830	
1918-1919			.9727				.8718			1.0797	
1919-1920			.7705				.9548			.8703	
1920-1921			1.2674				.7953			1.0605	
1921-1922			1.0785				1 2274			.9017	
1923-1924			. 9692				7039			7137	
1924-1925			1.9156				.9326			1.3161	
1925-1926			1.0549				.8400			1.0632	
1926-1927			1.3549				.8441			1.1031	
1927-1928			.8315				1.7857			1.1833	
1928-1929			1.0595				1.4844			1.1386	
1929-1930			7940				.0856			.7826	
1931-1932			.7649				3541			3503	
1932-1933			.9064			52	7520			.8020	
1933-1934			1.3097				3.0585			1.7281	
1880-1891 1891-1892 1892-1893 1893-1894 1893-1894 1893-1894 1894-1895 1896-1897 1897-1898 1896-1897 1897-1898 1899-1900 1900-1901 1903-1904 1904-1905 1905-1906 1906-1907 1907-1906 1906-1907 1907-1908 1908-1908			.5945				4556			.7333	

JANUARY 1857 TO JANUARY 1936.

57	58	59	60	61	62	63	64	65	66	67	January Dates
		.9419			1.0271						1857-1858 1858-1859
		1.0750			1.1492						1858-1859
		1.0220			.9993						1859-1860 1860-1861
					.9886						1861-1862 1862-1863
					1.2921		1.4031				1862-1863 1863-1864
					1.0500		1.0430			1.1413	1863-1864
					.8330		1.1487			. 6947	1864-1865 1865-1866
					.9763		1.3970				1866-1867
			1.1869		.8903		1.2328				1867-1868
			1.0952		1.0889		1.2092				1868-1869
			1.0605		.9981		1 0505				1870-1871
			.9879		1.1329		1.0479				1871-1872
			.9670	9000	,9807		.9440				1872-1873
				1.0715	.9724		.9883				1874-1875
				1.1000	.9826		.9691				1875-1876
				1.0219	.9688		.9878				1867-1868 1868-1869 1869-1870 1870-1871 1871-1872 1872-1873 1873-1874 1875-1876 1876-1877
				1.0174	1.0304		1 0772		[1877-1878
				.9797	1.1218		1.2520				1879-1880
1.2549				1.1403	1,1620	1.2972	1.4568				1871-1872 1872-1873 1873-1874 1873-1874 1874-1875 1875-1876 1876-1877 1877-1878 1878-1879 1880-1881 1881-1883 1882-1883 1882-1883 1885-1886 1885-1886
1.2549				.9542 1.0069	.9785 1.0872	.7531	1 0583				1881-1882
. 8680				1.0290	1.0233	.4810	1.0065				1883-1884
.9113				1.0028	1.0580	,9062	.9497				1884-1885
1.3351				1.1556	1.0867	1.7390	1.0897				1885-1886
.9696				1.0186	.9756	.9365	0547				1880-1887
.9060				1.1358	.9736	.9505	1.0074	1.0549			1888-1889
1.1771	1.0233			1.1125	1.0294	1.1647	.9710	.9690			1889-1890
	1.6151			1.0612	.9516	.8359 1,2578	.9636 1.0902	.7108			1890-1891
	1.2170			1.1490		.9237	1.0373	.9214			1892-1893
	.7764			. 7232		8178	9.509	.7945			1893-1894
	1.0000			1.0399		1.0486 .8721	1.1023	.8637			1894-1895
	1.0664			.9840		1.0580	1.0715	.9277			1886-1887 1887-1888 1888-1889 1889-1890 1890-1891 1891-1892 1892-1893 1893-1894 1894-1895 1896-1897
	1,1202			1.0525		1.1251 1.2903	,9996	1.1866			1897-1898 1898-1899 1899-1900
	1.9147			1.0792		1.2903	1.0306	1.1795			1898-1899
	1.0691			1.0678		1.0172	.9861 1.1593	1.6199			1899-1900
	1.0874			.9941		1,0904	.9009	2.3388	1.6757		1901-1902
	1.0957			1.0597		.9657	1.0160	.8731	1.5206		1902-1903
	.8639 1.3842			.8747 1.0275		.6773 1.8867	1.0000	1,5063	1 3596		1903-1904
	1.2844			1.0273		1.2674	.8146	1.5707	1.0486		1905-1906
	1.0116			.9287		.8376	.7634	.8741	.8509		1899-1900 1900-1901 1901-1902 1902-1903 1903-1904 1904-1905 1905-1906 1906-1907
	.7321			.7411		.7537	.5288 4.7457	.4793			1907-1908 1908-1909
	1.1992			1.1992		1.3759	9549	1.8374	3.4562		1908-1909
	.9190			.9584		,8919	.4815	1.0445	.4637		1910-1911
	1.0242			.9215		.9056	.5833	.9225	.5918		1911-1912
	1.0454			.9325		.8580 .8881	, 6055	1.0188	.8889		1912-1913 1913-1914
	,8952			.7020		.8004	. 8883	.8606			1914-1915
	1.0688			1.3490		1.2411	1.1194	1.2112			1914-1915 1915-1916 1916-1917
	.7639			.6460			.4690	.8400			1916-1917 1917-1918 1918-1919 1919-1920 1920-1921 1921-1922 1922-1923 1923-1924 1924-1925 1925-1926 1926-1927
	1.0435			1.0083		.7084 1.0000	,8322	1.9333			1918-1919
	,8533			.8788		.8547	1.0337	.9827			1919-1920
	.9724			.7873 .6828		1.1031	1.0404	1.6842			1920-1921
	1.0191			1.3561		.9495	7396	1.5000			1922-1923
	.7755			.8944		.9248	1.7002	.9687			1923-1924
	1.2238			1.7632		1.3630	1.9552	1.6244			1924-1925
	1.10809			1.3983		1.0700	.8096	1.0715			1926-1927
	1.1474			1.4533		1.1199	1,1914	1 5173			1927-1928
	1.1419	:::::::		1.3777		.9723	2.0186	1.0534			1927-1928 1928-1929
				1.2584		.5032		.9777			1929-1930
	.8785			1.2304		.0002					
	.8785			.7576		.4675		.6097			1930-1931
	.8785 .6613 .3216			.7576 .2966 .6219		.4675 1.1121 1.2850		.0827			1930-1931 1931-1932 1932-1933
	.8785 .6613 .3216			.7576		1.1121		.0827	::::::		1930-1931

TABLE 14-RAILROAD COMMON STOCK PRICE RELATIVES

			TA	BLE 1	4KAI	LROAD	Соммо		K PRI		ATIVES
Innuary Dates Innuary Dates Inst-188 Inst-1	68	69	70	71	72	73	74	75	76	77	78
1857-1858											
1858-1859											
1859-1860											
1861-1862											
1862-1863											
1863-1864											
1864-1865											
1866-1867	1 0104										
1867-1868	1.0544										
1868-1869	1.4135										
1869-1870	.8360										
1870-1871	.9586					1 5353					
1872-1873	1 6009					1.8231					
1873-1874	.7123					.7848					
1874-1875	.3410					.5943				*****	
1875-1870	.2690					6048				6594	
1070-1077	1.5705	0 4077				9607				5462	
1878-1879		1 4309				1.8806				2,3036	
1879-1880		2.7315					1.8531			3.4922	
1880-1881			1.0275				1.1153			1.0762	1.0195
1881-1882			0.112				.8119				8319
1883-1884			4725				.6699				.4498
1884-1885			.3027				.5163		.4392		.7001
1885-1886			2.2151				1.8497		1 6250		1 7396
1007 1007	1		0200				0742		7600		1 0512
1888-1889			.8452				.9890		.9737		1.0116
1889-1890			1.2601				.9600		.8514		1.0181
1890-1891				.7671			.7563		1.1495		.7032
1892-1893				.8179			7715		1.6432		.7603
1893-1894				.5869			.5780		.7737		.7905
1894-1895				.8978			,7086		.9209		1.0937
1896-1897				.9807			.8090		.8827		1.1978
1897-1898				1.1043				.9786	1.4639		1.2246
1898-1899				1.1463				1.0259			1.5951
1899-1900				.8807				.7707			.8406
1900-1901				1.7824				1.4832			1.4784
1902-1903				1.3400				.9804			1.0578
1903-1904				.6744				.6971			.6274
1905-1906				1.0972				1.1855			1.0488
1906-1907				.7404				.7988			.9481
1907-1908				.5453				.4093			.5738
1908-1909				1.9861				1.9879			1.7902
1910~1911				6751				9021			7957
1911-1912				.4107				1.1130			.8099
1912-1913				.5468				.9959			.9884
1913-1914				3287				7570			8267
1915-1916				.1764		1111111		1.7378			.7000
1916-1917					.9680			.8268			2.1004
1917-1918					.5622			.4806			.9456
1918-1919]				.9553			1.0404			1.8302
1920-1921	1	1			1.0390			1 0673			5025
1921-1922					.7806			.6370			1.3731
1922~1923					1.4161			1.2523			.8036
1924-1925					1.8084			1.3428			2 1548
1925-1926					2.1752			1.1471			1.3008
1926-1927]				.9300	1		1.1249			.9521
1927-1928					1.4662			1.5097			1.9372
1929-1930	0	1	11	1:::::::	7292		1	8208			1.5820
1930-1931					.3896			.5431			.8254
1931-1932					.1107			.2419			
1933-1934				1	1.9668		1::::::	3 2278			
1934-1935					.5787			.6600			1.09.73 90060 1.1978 1.2246 1.5951 1.5951 1.6764 1.0274 1.
1935-1936	M		1	J	1.5485	1	1	1.0563	H	J	1

JANUARY 1857 TO JANUARY 1936

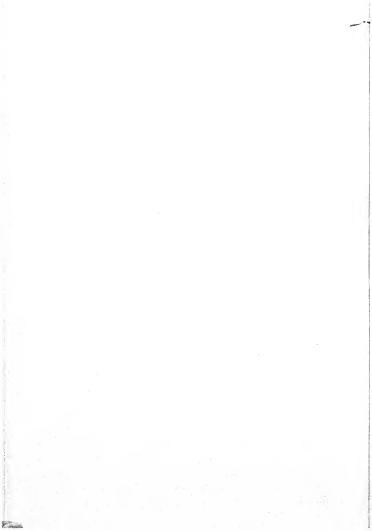
79	80	81	82	83	84	85	86	87	88	89	January Dates 1837-1838 1838-1859 1859-1840 1859-1840 1859-1840 1859-1840 1859-1840 1859-1840 1859-1840 1859-1840 1859-1859 1959-1959 1959-1959 1959-1959
											1857-1858
											1858-1859
											1860-1861
											1861-1862
											1862-1863
											1864-1865
											1805-1866
											1866-1867
											1867-1868
										• • • • •	1868-1869
											1870-1871
							.				1871-1872
											1872-1873
											1874-1875
											1875-1876
						1.4438		.9237			1876-1877
						.0087		1 6150			1877-1878
						1.5038		6.7035		2.8801	1879-1880
						1.1345		1.0894		1.7033	1880-1881
1.1550						.9779		.8418	• • • • • • •	1.0619	1881-1882
.8586						.8852		.6081		.8376	1883-1884
1.0488						1.0209		.7953		.5258	1884-1885
1.1970	1 1107					1.1965		1.8976		1.7037	1885-1886
. 9030	0205		• • • • • • • • • • • • • • • • • • • •			0775		1.0332		0725	1007-1007
. 8469	.7599					.5528		.7672		.9873	1888-1889
1.0137	.9816					.6081		.7758		1.6222	1889-1890
.8654	1.1363			.9927		.9513		.4297		.8763	1890-1891
9750	9622			5706		7043		7615	6428	9401	1892-1893
.3693	.5980			.5949		.3237		.9076	.6667	.5915	1893-1894
1.0935	1.0294			.7738		.3777		.9867	1.0000	1.1959	1894-1895
9051	9551			3822		1 0000		1.2073	9740	1.1492	1896-1897
1.5318	1.0313			4753		1.1056		.9595	9444	1.1497	1897-1898
1.3725	1.5999			2.0659		1.6600		1.0520	2.2070	1.1553	1898-1899
.8925	.8845			1.3900		.9177		.7353	1.1727	1.1973	1899-1900
1.2747	1.4073			1 4645		1.7057	1.2951	1.4781	1.2948	1.1973	1900-1901
1.0713	.9252			1.4581		1.1094	1.7660	1.1169	1.0612	1.2100	1902-1903
.8418	.5252			.7002		.7855 1.2715	.5700	1.7947	.5267 1.7474	.8555	1903-1904
.9682	1.4070			1.0242		1.0720	1.1468	1.2117	.9350	1.1010	1905-1906
.8668	.8721		.7503	.7686		1.1115	.8442	1.0081	.9922	.9147	1899-1900 1900-1901 1901-1902 1902-1903 1903-1904 1904-1905 1905-1906 1906-1907
.4951	.5246		,4438	,4786		.6903 1.3954	.8066	.6489 1.7036	.6115	.6962	1907-1908 1908-1909 1909-1910
1.6214 .9884	1.9852		1.7551	1.6730		1.3954	1.7956	1.7036	1.5213	1.2806	1908-1909
.7065	6474		1 0000	6507		1.2012	,8148	.7305	8708	9604	1910-1911
.8235	.7154		1.1492	.9344		.8719 1.0102	8297	.8459	1.1000	1.0508	1910-1911 1911-1912 1912-1913
1.0387	1.0354		.7157	1.6711		.9988	.9540	.9649	1.1787		
.4013	.3239		. 4552	.4833		.9209	. 8934	.7818	. 7069	.8476	1914-1915
.4912	2.1948		1.8690			1,1110	1.2543	.6261	1.1256	1.0904	1915-1915 1915-1916 1916-1917
2.7893	1.1687		.9432	1.7559		1.0053	.8600	1.4498	1.5657	1.0290	1916-1917
.6945 1.1087	.2793 1.0922			.4375	1.0188	.8027 1,0892	.6941 1,0399	.5881 1.0000	.7227	1 0322	1917-1918 1918-1919 1919-1920
1.0226	1.7789	1.3750 1.2697	.8357	.8859 1.5272	1.4207 .7797	.9012	.8717	1.7116	.7463	9393	1919-1920
.7641		1.1151	. 9827	.8030	1.0708	1,0000	1.2747	.2889	2 1247	.9210	1920-1921 1921-1922 1922-1923
.8683		.5574	.7974	.6565	.7958	1.1508	1.1500	.3271	.7679	1.1125	1921-1922
.6618		1.1269	1.3412	1.3274	1.4976	1.0554 .9852	.8965	1.8361 .8298	1.4666		
3.1761		.9089 2.3137	1.5269	1.8932	1.9706	1.2001	1.8446	2.6098	1.4132	1.2289	1924-1925 1925-1926 1926-1927
1.1051 1.0802		1.7104	1.0037	1.8884	1.6226	1.1223	1.2815	1.3065	1.3539	1.2371	1925-1926
1.0802		.7933	1.4064	1.5762	1.1290	1.2408	.9513	.8210 1.1266	.9409	.9081	1920-1927
1.2150		1.1765	2.1111		1.0771	1.1464	1.3685	1.1266	1.2011	9802	1927-1928 1928-1929
1.3523		.6560	.5960		8282	1,1390	.8452	.9880	.5762	8941	1929-1930
		.5000	.5962		.6147	.8201	.4937	.4590	.4548	.7495	1930-1931 1931-1932
		.2713	.4071		.1712	.4514 .5029	.2772 .8217	.2541 1.1784	.3405	9258	1931-1932
1.30211		2 1428				1.4810	1 6913	1 5357		2.1700	1933-1934
1.2240		.7840	.8466			.7961 1,3310	1.8249	1 2455		1.8084	1934-1935 1935-1936
1.2240		.8/0/	1.0900			1,3310	1.0249	4.4433		1.5056	1933-1936

TABLE 14-RAILROAD COMMON STOCK PRICE RELATIVES

									1		1
January Dates 1857–1858 1858–1850 1859–1860 1861–1862 1861–1862 1863–1864 1863–1866 1866–1867 1867–1868 1869–1869 1870–1871 1871–1872 1873–1874 1875–1877–1875 1875–1877	90	91	92	93	94	95	96	97	98	99	100
1857-1858											
1858-1859											
1859-1860											
1861-1862											
1862-1863											
1863-1864											
1864-1865											
1865-1860											
1800-1007											
1867-1606											
1869-1870											
1870-1871											
1871-1872											
1872-1873											
1874-1875											
1875-1876											
1876-1877			.8803								
1877-1878			1.0691								
1878-1879			.9430								
1879-1880			1.4434				4.5941		2 0040		
1876-1877 1877-1878 1878-1879 1879-1880 1880-1881 1881-1882 1882-1883 1883-1884	1 2117		1.29/5				1 4385		8100		
1882-1883	7192		8666				.5437		.7090		
1883-1884	.8466		.7309				.5000		8413	.9119	
1884-1885	,6863		.6495	1.0242			.8110		1.7084	.7326	
1884-1885 1885-1886 1886-1887	1.3715		1.0829	1.5167			2.1242		1.7084	1.6014	
1886-1887	1.7685		1.1282	1.2005			1.0780				
1887-1888 1888-1889 1889-1890 1890-1891 1891-1892 1892-1893	.9189		.9680 1.1174					::::::	.7323	.9057	
1888-1889	1 2360		1.0539	1 1773	1		1 0165		2.1483	1.4545	
1800-1891	9171		.6695	1.1770	.4060	.7216	1.7595		.6122	.9761	
1891-1892	1.0093				1.4223		1.4019		. 9290	1,2382	
1892-1893	.9888		.8513		.7561	.8529	.9109		.7773	.9672	
1893-1894	.7955		.4641		.2232	.6399	.4902		.3278	.8125	
1894-1895	.9571		5380		.9403 1.1269	.8355 1.1426	1.5027		1.1439	.7674	
1894-1895 1895-1896 1896-1897			1 5094		1,1209	.6962	9565		,6057	1.0233	
1897-1898 1898-1899 1899-1900			0560			1.4282	1 3600		1,1225	1,5754	
1898-1899			2.1067			1.8437	1.2014		.8908	9850	
1899-1900			1.0134			. 9675	1.0985		6492	1.0822	1.5918
1900-1901			1.7877			1.2081	1.4325		.8667	.9704	.9294
1900-1901 1901-1902 1902-1903 1903-1904			1.22/2			1.3375		1.6248	.8667 1.2425 1.3434	1.2700	2.1622
1902-1903			7738			7403		1.0639	.7076	.8779	1.6827
1903-1904 1904-1905 1905-1906 1906-1907			1.4911			.7493 1.4025		.5979 1.6226	1.2048	1 1602	1 5244
1905-1906		1.3262	1.3044			1.0462		1.1434	1.2048	1.3068	1.3944
1906-1907		.7985	1.1405			1.3465		.7489	,7931	1.1825	.8571
1907-1908 1908-1909 1909-1910		.5650 1.5293 1.2037	.6959			.8002		.3800 2.3286	.6565 2.5545 1.2142	.8637 1,1395	.4444
1908-1909		1.5293	1.4693			1.5940		2.3286	2.5545	1.1395	2.2652
1010-1910		0125	8060			8801		1.1992	1.2142	1.0882	.9251
1911-1912		.9125 1.1308	.9641			.9370		.8720 1.0254	.8862	1.1293	.7736
1910-1911 1911-1912 1912-1913 1913-1914		.9853				.9755		.9842	. 9056	1.1251	.8977
1913-1914		.9259	.9984					.9135	.9467	.8765	.6012
1914-1915		.8512 1.1021	.9315			.9074		.6369	.8019	.7593	1.0081
1914-1915 1915-1916 1916-1917		1.0351	1 0700			9586		1.3788	1.0186	1.0817 .9178	1.1000
1017-1010			7040			9542				.91/8	.9762
1918-1910		.7723 1.0723	1 1170			1.2017		.7428 1.1822	.7329 .8528	.8890 1.1125	
1917-1918 1918-1919 1919-1920		.9364	.9671			1.0278		.7982	.9255	.8224	
1920-1921 1921-1922 1922-1923		.9335	,9726			.9645		1.0710		.8952	
1921-1922		1.0191	1.0673			1.0127		.7691		1.0464	
1922-1923 1923-1924		1.3071	1.0/40			1.1087 9832		1.5314		1.1655	
1924-1925		1.3131	1.1604			1 1097		1.5385		1.0384	
1924-1925 1925-1926 1926-1927		1.6661	.9771			9703		1.4812		.9925	
1926-1927		.8260	1.1015			1.0624		1.0622		1.1218	
1927-1928 1928-1929 1929-1930		.9788				1 1210	12	1 1750	9	1.2781	
1928-1929		.9559	1.1522			1.0916		1.0514		1.1704	
1929-1930		.9532	.9983			.9128		.8476		.8165	
1930-1931 1931-1932 1932-1933		.6696				.8174		4287		. 8370	
1932-1932		.6141	9712			.5558		.1855	• • • • • • •	.3298	
		2 1951				1.4157		5.0493		.9345	
1934-1935 1935-1936		.7307	.8841			.6910		.4800		.8591	
1935-1936		.9392	1.0946			1.5756	l	1.0526		.9414	

January 1857 to January 1936

101	102	103	104	105	106	107	108	109	110	111	January Dates
											1857-1858 1858-1859 1859-1850
											1858-1859
											1860-1861
											1860-1861 1861-1862 1862-1863
											1862-1863
											1863-1864 1864-1865 1865-1866
											1865-1866
											1866-1867 1867-1868
											1868-1869
	,										1869-1870
											1870-1871 1871-1872
											1872-1873
											1873-1874 1874-1875
											1874-1875 1875-1876
											1876-1877
											1877-1878
											1878-1879
	1.5329		1.1806								1879-1880 1880-1881
	.8771		.9085								1881-1882
	1.0698		.7857	.5972 .6107	1.4090						1882-1883
	.6111		,9659	1.2257	.5627						1883-1884 1884-1885 1885-1886
	1.0607		1.1187	1.8022	1.7494						1885-1886
	1.6928		1.4398	1.1682	.9443		2.1350				1886-1887
	.8778 1.1561		1.1447	.5875 1.1064	.3884 .7534		.8246 .9742				1886-1887 1887-1888 1888-1889 1889-1890 1890-1891 1891-1892 1892-1893 1893-1894 1894-1895 1895-1896
	.8234		.6666	1.3271	1.1241		1 3122				1889-1890
	.8485			.9055	.8800		7079				1890-1891
	1.2238			1.3443 2.1903	1.7964	1.9829 .7162	1.1010				1891-1892
					.6065	.7042	. 5386				1893-1894
					.3711	.8486	.8320				1894-1895
					1.3756	1.3571	.5220				1895-1896
			1.4220		1.3256	1,2581	1 0452	3 1579			1897-1898
			1.5842		1.5693	1.3092	1.2540	1.1874			1897-1898 1898-1899 1899-1900
i.200i			.8554 2.6002		1.4883	1.0151 2.0216	1.2924	.7193			1899-1900 1900-1901
2.0128	:::::::		2.4044		1.5485	1 6099	1 2886				1901-1902
1.9046			1.2906		1.0069	1.1254	1.3038	1.2017			1901-1902 1902-1903 1903-1904
.8161 1.5474					.5977	1.4080	.7972 1.3292	1.4191			1903-1904
1.6132					1.4099	1.0664	1.1282	.9623			1904-1905 1905-1906 1906-1907
.8152					.7048	.8214	.9917	.7521			1906-1907
.7014					.4340	.4467	.7567	.3822			1907-1908
1.6196 1.0275					2.3736	2.6996 .8150	1.3280	1.4296			1907-1908 1908-1909 1909-1910
,9990					.5443	.7162	1 0624	.6746			
1.0268			7134		.9951	.7250	1.0479	.8174 .9186			1911-1912
.9204			.2642 .4925		.6572		0178	.7745	.9455		1911-1912 1912-1913 1913-1914
.8621			.4925		.8519		.9897	.8620	.7280		1912-1913 1913-1914 1914-1915 1915-1916 1916-1917
1.1036			2.1385				1.1668	1.2156	1.3035		1915-1916
.7227		.3852	.4988				.7727	.5760	.4638		1917-1918
1.0532		1.0000	1.0205				1.0144	1.0000	1 0238		1918-1919
.8134		2.3036	1.4448				1.0309	1.0884	.8852 .9048	.9677	1917-1918 1918-1919 1919-1920 1920-1921
		1.0960	.9558		11111111		.9814	1.0141	.4665	6286	1921-1922
		1.8720	1.0462				1 1 1 371	.7181 .7884	1 8793	2.4763	1921-1922 1922-1923
• • • • • • • •		1.1353	.9284 2.8629				.9357 1.2377	1.0000	1.1965 3.1340	1 1660	11 923-1 924
		1.6162	1.6402				1.1763	1.1408	2.1802	1.2906	1924-1925 1925-1926 1926-1927
		1.4077	1.0476				1.0414	1.1408	.7791	1.1899	1926-1927
		1.0738	1.1215				1.1860	1.1978	.7406	1 3706	1027-1028
		1.2456	1.0659	• • • • • • • • • • • • • • • • • • • •			1.0512	6022	.6866	.9718	1928-1929 1929-1930
	1:::::::	.5145	.4854		I	:::::::	.8856	.4617	.0922	4685	11930-1931
		.1223	.0910				.5821	.5507	.5319	.3846	1931-1932 1932-1933
		.6544 3.5078	2.8908				1.4214	1.5316	4,4516	1	1033-1034
		7511	4913				1.0085	.4854	.5435		1934-1935 1935-1936
	1	1.9036	1.3313		4		1.2797	.9700	1.3333	5'	11935-1936



RAILROAD COMMON STOCK WEIGHTS, JANUARY 1857-JANUARY 1936

The numbers at the heads of columns are the numbers assigned to the various railroads in Chart 32. For example, the figures of Column 1 refer to the Baltimore and Ohio Railroad. The figures in the single column entitled '51 and 52' refer first to the Chicago, Milwaukee and St. Paul Railway (January 1874 to January 1928) and then (lower down) they refer to the Chicago, Milwaukee, St. Paul and Pacific Railroad (January 1928 to January 1936).

Each weight in Table 15 is the ratio of the market value of the total outstanding common stock of a specified railroad in the earlier January of the thirteen months designated in column 1 to the market value of the total outstanding common stock of all the railroads whose stocks in that particular thirteen months' period were used in constructing the railroad common stock price weighted index number. For example, the first figure in the table is .0587. This means that the market value of the total outstanding common stock of the Baltimore & Ohio Railroad in January 1857 was .0587, or a little less than one-seventeenth, of the market value of the total outstanding common stock of all the 27 railroads whose stock prices were used for constructing the railroad stock price index in the period January 1857 to January 1858 inclusive.

From this definition of the meaning of the figures in the table it follows that, for any particular thirteen months' period, the sum of the weights equals unity.

Though the January figures for the weighted index number of railroad stock prices given in Table 16 night be calculated perfectly from the price relatives of Table 14 and the weights of Table 15 they were not in fact so calculated. If from January to January each year, a chain weighted arithmetic average of relative prices index number were constructed by using the relative prices of Table 14 and the weights of Table 15, the movements of such an index number could be shown to be identical with the movements of a chain weighted aggregate of actual prices index number where the prices were dollars per share and the weights were the number of shares outstanding in the earlier January. This latter is how the railroad common stock price weighted index number was actually constructed.

The blank spaces in the table correspond to periods in which particular stocks were not used in constructing the stock price index numbers.

TABLE 15-RAILROAD COMMON STOCK WEIGHTS

						15R					
January Dates	1	2	3	4	5	6	7	8	9	10	11
1857-1858	0587		.0640	.0125	.0621		.0066		.0243	.0088	.0086
1858-1859	.0458		.0784	.0135	.0550		.0055		.0339	.0110	.0110
1859~1860]	.05241.		.0689	.0155	.0472		.0054	03/13	.0373	.0140	.0158
1860-1861	.0660].		.0665	0271	.0383		0046	.0332	.0384	.0135	.0174
1860-1861 1861-1862 1862-1863 1863-1864 1864-1865 1865-1866 1866-1867	0551		.0568	.0333	.0332		.0035	.0360	.0376	.0132	.0143
1862-1864	.0584		.0492	.0397	.0454		.0037		.0277	.0113	.0159
1864-1865	.04691	.0255	.0464	.0459	.0735		.0065		.0179	.0077	.0108
1865-1866	.0492	.0217	.0584	.0782	.0700		0039	0515	.0162	.0096	.0121
1866-1867	.0501	.0182	0479	0500	0692		0073	0504	.0157	.0096	.0123
1867-1868	.0450	.0140	.0433	0383	0565		.0050	.0426	,0145	.0084	.0106
1960-1970	0.332	.0147	.0406	.0355	.0515		.0046	.0361	.0127	.0073	.0097
1870-1871	.0346	.0105	. 0386	.0413	.0578		.0048	.0305	.0136	.0071	.0099
1871-1872	.03341	.0120	.0334	,0364	.0529		.0054	0371	.0160	.0060	.0077
1872-1873	.0319	.0153	.0306	0358	.0584		.0055	.0321	.0137	.0055	.0081
1873-1874	.0336	.0108	.0388	,0390	.0596		.0053	.0328	.0118	.0054	.0063
1875-1876	.0403	.0096	.0370	.0449	.0582		,0063	.0352	.0130	.0046	.0044
1876-1877	.0359	.0065	.0388	,0489	. 0552		.0068	,0344	.0118	.0036	.0010
1877-1878	.0398	.0027	.0262	.0379	.0219		.0079	.0122	.0138	.0059	.0005
	.0284	.0034	.0214	0242	.0233		.0004	01.39	.0142	.0050	.0011
1879-1880	.0242	.0072	.0156	0263	.0267			.0178	.0098		
1881-1882	.0241	.0070	.0171	.0261	.0171			.0141	.0089		.0016
1882-1883	.0252	.0062	.0187	,0286	.0181			.0151	.0089		.0016
1880-1881 1881-1882 1882-1883 1883-1884	.0243	.0054	.0178	.0273	.0149			0147	0102		0017
	.0267	.0039	.0182	.0252	.0063			.0075	.0133		.0025
1886-1887	.0239	.0041	.0197	,0275	.0071			.0071	.0113		.0033
1007 1000	.0199	.0042	.0199	.0280	.0122			.0091	.0115		.0050
1887-1666 1888-1889 1889-1890 1890-1891 1891-1892 1892-1893	.0129	,0040	.0217	.0283	.0211			.0119	.0121		
1889-1890	.0113	,0038	.0283	.0320	.0165			.0150	.0107		
1890~1891	.0114	.0033	.0283	0301	0110			0177	0224		
1891-1892	.0101	,0033	.0264	,0265	.0114			.0181	.0212		
1893-1894	.0108		.0286	.0282	.0146			.0203	.0229		
1893-1894 1894-1895 1895-1896	.0098		.0357	.0390	.0069			.0230	.0218		
1895-1896 1896-1897	0057		.0384	0369	.0040			.0201	.0273		
1897-1898	0007		. 0345	0350		0162		0196	0266		
1898-1899	.0018		.0315	.0321		,0126		.0171	.0254		
1899-1900 1900-1901	.0147		.0240	.0257		,0098		.0140	.0201		
1000-1901	.0154		.0238	.0275		,0075		.0188	.0239		
1901-1902	0314		.0242	0279		.0155		.0209	.0179		
1902-1903 1903-1904 1904-1905	.0448		.0213	.0249		,0160		.0179	.0162		
1904-1905	.0409		.0231	.0286		,0130		.0180	.0164		
1905-1906 1906-1907	.0402		.0234	.0279		,0185		0147	.0134		
1907-1908	0425		.0223	0242		0219		0142	0110		
1907-1908	0406		.0208	.0375		.0223		.0148	.0120		
1908-1909 1909-1910 1910-1911	.0377		.0170	.0322		,0217		.0143	.0088		
1910-1911	.0356		.0152	, 0362		,0229		.0168	.0086		
1911-1912 1912-1913 1913-1914	.0345		.0150	0342		0227			.0098		
1913-1914	.0320		.0142	.0376		.0233			.0077		
1914-1915 1915-1916 1916-1917	.0314		.0145	.0371		.0262			.0043		
1915-1916	.0274		.0159	.0444		.0265			.0028		
1910-1917	.0307		,0143	,0420		.0247			,0032		
1917-1918 1918-1919 1919-1920	.0285		.0145	,0450		,0320			.0037		· · · · • · ·
1019-1020	.0198		.0121	.0419		.0309			.0023		
1920-1921	.0147		.0121	,0462		.0321			.0042		
1921-1922	.0166		.0131	.0552		.0363			.0028		
1921-1922 1922-1923 1923-1924	.0165		.0145	,0030		0204			.0019		
1924-1925	.0248		.0129	,0543		.0303			.0019		
1924-1925 1925-1926	.0270		.0132	,0550		.0245		[.0014		
1926-1927	.0270		.0132	.0499		.0235			.0034		
1927-1928	.0294		.0159	.0442		. 0242			.0037		
1928-1929	.0362		.0135	.0334		0206			.0033		
	CACO.		.0128	.02/0	1	.0194			.0050		
1929-1930	. 0384	1	.0077	.0253							
1929-1930 1930-1931 1931-1932	.0384	:::::::	.0077	.0253		.0170			.0048		
1929-1930 1930-1931 1931-1932 1932-1933	.0384		.0077	.0253		.0170			.0048		
1929-1930 1930-1931 1931-1932 1932-1933 1933-1934 1934-1935	.0384 .0312 .0313 .0313		.0077 .0063 .0063 .0063	.0253 .0206 .0207 .0207		.0170 .0171 .0171			.0048		. 0016 0016 0016 0016 0017 0017 0017 0017

JANUARY 1857 TO JANUARY 1936

12	13	14	15	16	17	18	19	20	21	22	Januar Dates
,0359			.0598			.0463			.1597	.0087	1857-185
.0373	1		.0711			.0421			.1812		
0308			.0705			.0365			.1867	0118	1850-186
.0337			.0864			.0356			.1696	0153	1858-185 1859-186 1860-186 1861-186 1862-186 1863-186 1864-186
.0272			.1092							.0150	1861-18
0254			.0902			.0347			.1685	.0126	1862-186
.0263			.0786	.0041		.0283	.0038		.1470	.0207	1863-18
.0283			.0843	.0046			.0139		.1148	.0292	1864-18
.0200			.0851	.0031			.0164		.0925	.0238	1865-18
.0227			.0983	.0026			.0143		.0796	.0247	1866-18
0261			0783	0023			0149		0074	0256	1067 10
0222			0764	0020			0216		.0074	.0330	1807-18
.0332			0754	0020			0210		.0871	.04/5	1808-18
.0372			0737	0013			0210		.0970	.0450	1809-18
0376			0642	0012			0200				1870~18
.0370			0556	.0013			.0200				18/1-18
.0047			0501				.0178				18/2-18
.0438			0.179				.0193				1873-18
.0420			0466				.0140				18/4-18
.0410			.0466				.0111				1875-18
.0424			.0450				.0097				1876-18
.0507			.0337				.0108				1877-18
.0457		.0019	.0471				.0118				1878-18
.0486		.0024	.0459				.0162				1879-18
0372		.0037	.0348		.0013		.0160	.0079			1880-18
.0498		.0036	.0322		.0024		.0167	.0071		0.932 (0.	1881-18
0489		.0040	.0335		.0026		.0186	.0058			1882-18
0432		.0037	.0344		.0019		.0290	.0085			1883-18
0446		.0037	.0355		.0011		. 0331	.0062			1884-19
0496		.0033	.0388		.0012		.0305	.0062			1885-18
0472		0036	0366		0015		0295	0063			1886-18
0472		.0000	0217		0022		0200	0072			1000-10
0459			.0317		.0022		.0280	.0072			1887-18
.0431			,0393		.0015		.0281	.0061			1888-18
0391			.0395		.0017	• • • • • •	.0290	.0052			1889-18
0344			.03/1		.0013		.0268	.0048			1890-18
0270			.0384		.0012		.0284	.0040			1891-18
0298			.0383		.0013		.0322	.0062			1892-18
.0279			.0358		.0010		.0312	,0000			1893-18
.0270			.0409		.0003		.0354	,0059			1894-18
.0264			.0392		.0003		.0343	.0056			1895-18
.0267			.0432				.0336	.0056			1896-18
0272			.0427				.0351	.0080			1897-18
0337			.0444				.0385	0112			1898-18
0360			.0434				.0352	.0109			1899-19
0315			.0400				.0373	.0134			1900-19
0315			.0408				.0347	.0126			1901-19
0375	.0158 .0086 .0100 .0052		.0435				.0324	.0103			1902-19
	.0158		.0498				.0306	.0106			1903-19
	.0086		.0508				.0328	.0109			1904-19
	0100		.0466				.0343	.0109			1905-19
	.0052		.0399				.0408	.0085			1906-19
	0000		0270				0424	0074			1007 16
	.0000		.0376				0446	.0074			1907-15
	.0041		.0376				0534	.0074			1000 10
	.0031		.03.77				0120				1910-19
• • • • •	.0067		.0310				0.100				1011 10
	.0001		.0312				0390				1911-19
	.0047		.0323				0350				1911-19 1911-19 1912-19 1913-19
	.0042		.0270				0370				1914-19
0032	.0029		0200				0417				1015 1
0030			.0302				0290				1915-1 1916-1
.0030			.0200				.0380				1910-1
.0083			.0262				.0402				1917-19
.0045			.0303				.0401				1918-19
.0050			.0294				.0381				1917-19 1918-19 1919-19
.0060			.0294				.0374				1920-19
.0062			.0297				.0302				1921-19
.0074			.0345				.0284				1922-19
.0066			.0330				.0313				1923-19 1924-19 1925-19 1926-19
,0052			.0344				.0205				1924-19
.0078			.0315				.0235				1925-19
.0083			.0291				.0232				1926-1
0004			0270				0226				1027. 1
.0094			.02/0				0107				1029-1
.0119			.0208				0127				1020 1
			.0240				.017/				1929-1
.0126			.0204				.0237				1930-1
.0126											
.0126			.0165				.0193				1931-19
.0126 .0111 .0091			.0165 .0166		::::::	:::::::	.0193	:::::::	::::::	::::::	1931-19
.0126 .0111 .0091 .0091	0100 0052 0060 0041 0051 0087 0067 0047 0042		.0165 .0166 .0166	. 0041 .0046 .0033 .0026 .0023	::::::		.0193 .0194				1931-19 1932-19 1933-19

TABLE 15-RAILROAD COMMON STOCK WEIGHTS

				L	ABLE	13-1	ALLROA	Coata			
January Dates	23	24	25	26	27	28	29	30	31	32	33
1857-1858			.0094	0.11.1		.0368	0366			.0271	,0345
1857-1858 1858-1859 1859-1860 1860-1861 1861-1862 1862-1863 1863-1864 1864-1865 1866-1867			0058	.0319		0116	.0266			.0362	.0475
1850-1860			.0106	.0292		.0110	.0192			. 0399	.0505
1860~1861			.0072	0211		.0037	.0126			.0451	.0541
1861-1862			.0112	.0293		.0080	.0195				.0497
1862-1863			.0093	. 0269		.0108	.0216			.0319	.0309
1863~1864				.0304		.0178	0425			.0221	.0257
1864-1865				.0281		.0175	0365			.0212	.0291
1966-1967				0250		.0228	.0369			.0197	.0259
1867-1868				0232		0715	0357			.0197	.0350
1868-1869				0228		0210	.0328	.0237			
1869-1870				.0304				.0743			
1870-1871	.1616			.0326					.0637		
1871-1872	.1471			.0390					.0587		
1872-1873	,1369			.0351					0722		
1873-1874 1874-1875	.1365			,0313					0652		
1875-1876	14/0			02:03					.0611		
1876-1877	1511			0178					.0506		
1877-1878	1920								.0552		
1878-1970				.0249					.0667		
1878-1879 1879-1880	1925			,0287	.0146				.0658		
1880-1881	,1383			0199					.0588		
1881-1887	.1160			.0198	.0103				.0559		
1882-1883 1883-1884	.1032			.0142	.0071				0488		
1884-1885	.0932			.0151	.0069				.0433		
1885-1886	0857			01 19	.0051				.0336		
1886-1887	.0816			.0118	.0053				.0370		
1987-1888				0132	0070						
1888-1889 1889-1890	.0793				.0068						
1889-1890	.0834			.0139	.0067				.0442		
18901891	.0735			.0137	.0063				.0401		
1891-1892	.0778			.0146	.6064				.0454		
1892-1893 1893-1894	.0723			.0140	.0004				0.153		
1893-1694 1894-1895	0850			0163	0000				.0548		
1894-1895 1895-1896	0006			.0164	.0068				.0623		
1896-1897	.0844			.0157	.0063				.0612		
1897-1898	.0812			.0147	.0059				.0657		
1898-1899 1899-1900 1900-1901	.0900				.0064						
1899-1900	.0805				.0057						
1900-1901	.0880				.0044						
1901-1902	.0814				.0044						
1902-1903 1903-1904 1904-1905	0716										
1904-1905	.0641										
1905-1906	.0602										
1906-1907	.0538										
1907-1908	,0559										
1908-1909	.0536										
1907-1908 1908-1909 1909-1910 1910-1911	η .0512										
1910-1911	0525									1	1
1012-1913	.0523		1		1	1			1		1
1913-1914	.0491										
1913-1914 1914-1915		.0511									
1915-1916		.0564									
1916-1917		.0653									
1917-1918	3	.0570									
1918-1919		.0519							·····		
1919-1920 1920-1921 1921-1922		0520				1		1	1	1	
1921-1921		.055			1				1	1	
		.058	3					1	1		
1923-1924 1924-1925		.068									
1924-1925		.0770									
1925-1926 1926-1923		082	ś ····							1	
1920-192	J	.090			1	1	1			1	
1927-192	3	1095	1		1	1				1	
1928-1929	ő]	1 .121	1	1111111	1	1	1			1	1
1930-193	1	.074	s	1				1	11		1
1931-193	21										
1932-193	3	.061	1								
1933-193 1934-193	4	.061	0								
1934-193	5	.061				1	4	4	1		1

JANUARY 1857 TO JANUARY 1936

34	35	36	37	38	39	40	41	42	43	44	January Dates
	.0348				1	.0914		0307	-		1857-185 1858-185 1859-186 1860-186 1861-186 1862-186 1863-186 1864-186 1865-186
	.0415					.1003		.0073			1858_185
	.0422					.1049		.0067			1859-186
	.0416					.0963	0222	.0050			1860-186
	.0383					.0863		.0064			1861-186
	0506					.0882	.0222	.0105			1862-186
	0374					.0907	.0222	.0258		.0089	1863-186
	0360					.0878	.0244	.0335		.0102	1864-186
	0238					.0756	.0330	.0334		.0163	1865-186
	0190	.,,,,,,,				0605	.0000	.0297		.0139	1800-180
0516	0146					.0095	.0334	.0265		.0125	1867-186
.0506	0163					.0723	.0284	.0246		.0099	1868-186
.0508	0185					0780	.0286	.0228		.0098	1869-187
.0557	0220					0785		0217		.0091	1870-187
.0492	.0225					.0827		.0310		0074	10/1-10/
.0459	.0215					.0745				0071	1872-187
.0449	.0190					.1117				0062	1874-197
.0438	.0163					.1250				0064	1875_18
.0422	.0141					.1195				.0067	1876-18
.0510	.0109					.1321	- 1			0060	1877-105
.0535	.0119					.0946				0000	1878-107
.0493	.0117		.0008			.0867				.0020	1879-188
.0328	.0140		.0040			.0833				.0045	1880-18
.0287	.0120		.0031			.0881				.0046	1881-188
.0287	.0106		.0034			.0912			.0089	.0056	1882-188
.0286	.0099	.0151	.0027			.0918			.0103	.0058	1883-188
.0321	.0086		.0020			.1009			.0122	.0070	1884-188
.0377	.0053		.0010	.0032		.1057			.0143	.0079	1885-188
.0313	.0072		.0016	.0032		.0920			.0143	.0080	1886-188
.0315	.0075		.0011	.0034		.0941			.0148	.0079	1887-188
.0327	.0065		.0005	.0024		.0961			.0149	.0102	1888-188
.0347	.0076	******	.0025	.0026		.1059			.0190	.0094	1889-189
.0334		.0151	.0094	.0019		.1026			.0166	.0081	1890-189
.0338				.0027		.1073			.0178	.0084	1891-189
.0353		.0143	.0111	.0025		.1005			.0163	.0072	1892-189
.0372		.0115	.0094	.0025		.0978			.0189	.0073	1893-189
.0454		.0098	.0094	.0021		.1130			.0214	.0090	1894-189
,0481		.0084	.0078	.0018		1100			.0190	.0090	1895-189
.0403		.0068	.0090	.0017		.1102			.0173	.0009	1050-195
.0453		.0080	0110	.0013		.1170			.0101	.0088	1897-189
.0443		.0089	.0104		.0017	1029		,]	.0077	.0093	1898-189
		.0104	0108		.0020	1140			,0090	0085	1000-100
		.0111	0123		0023	1145				0106	1900-190
		.0108	0112		0030	1205				0095	1902-190
		.0096	.0113		0039	.1237				.0095	1903-190
		.0089	.0087		.0033	.1465				.0083	1904-190
		.0107	.0095		,0031	.1299				.0112	1905-190
		.0101	.0087		.0030	.1045		. <i>.</i> 1		.0086	1906-190
1		.0102	.0079			.1028				.0089	1907-190
		.0081	.0060			.1108				.0100	1908-190
		,007.5	.0085			.0937				.0091	1909-191
		.0075	.0109			.1111					1910-191
		.0064	.0110			.1233					1911-191
		.0057	.0096			.1180					1912-191
		.0051	.0099			.1227					1913-191
		.0041	.0088			1352					1015-101
		.0025	0070			1294					1016-101
		.0040	.0008			1200					1017 10-
			.0091			1260					1010 101
			.0097			1247	• • • • • • • • • •				1010-191
			.0090			1255					1020-102
			0116			1248					1921-193
			0110			.1066					1922-193
			0128			.1262					1923-192
			.0136			.1230					1924-192
			.0196			.1077					1925-192
			.0274			.1035					1926-192
			0327			1016	1111				1927-10
			0342			1050					1928-10
			0404			1119					1929-19
			0287			.1944					1930-19
			.0932			.1588				[]	1931-193
						1.600					1022-10
			.0936								
			.0936			.1610					1933-19
			.0936		0017 0023 0023 0039 0039 0033 0031 0030	.1610					1933-19 1934-19

TABLE 15-RAILROAD COMMON STOCK WEIGHTS

-											
January Dates	45	46	47	48	49	50	51 & 52	53	54	55	56
1857-1858 1858-1859 1859-1860 1860-1861 1861-1862 1862-1863 1863-1864 1864-1865 1865-1866 1866-1867			.0095	.0199				.0333			
1858-1859			.0112	.0108				.0201			
1859-1860			.0161	.0043				0177			
1860-1861			0108		0029			.0287			
1862-1863					.0048			.0246			
1863-1864			.0176		.0061			.0314			
1864-1865			.0441		.0061 .0060 .0043			0337			
1865-1866			.0351		.0043	0057		.0387			
1866-1867 1867-1868 1868-1869 1869-1870 1870-1871 1871-1872 1872-1873 1873-1874 1874-1875 1875-1876			0403			0063		.0391	.0032		
1867-1868			0407			.0068		.0431	.0025		
1869-1870			.0375			.0103		.0506	.0038		
1870-1871			.0404			.0175		.0439	,0097		
1871-1872			.0400			0127		0423	0083		
1872-1873			0409			.0127	.0115	.0370	,0069		
1874-1875			.0473				.0115	.0328	.0046		
1875-1876			.0535				.0094	.0483	.0033		
1876-1877			.0540				.0095	.0504	.0030		
1877-1878			.0522				.0059	.0650	.0020		
1878-1879			.0483				.0120	.0629	.0025	.0030	
1879-1880			.0338				.0141	.0513	0041		
1881-1882			.0278			.0057 .0063 .0068 .0103 .0175 .0127 .0127	.0154	.0830	.0040	.0148 .0153	.0013
1877-1876 1878-1879 1879-1880 1880-1881 1881-1882 1882-1883			.0298				.0192	.0653		.0153	.0010
1983-1884	0000		.0290				.0251	0767		,0102	.0013
1884-1885 1885-1886	.0007		0423				.0251	.1006		.0087	.0010
1886-1887	.0010		.0324				.0251	.0928		.0116	.0014
	0013		0294				.0275	.0830		,0105	.0019
1887-1888 1888-1889			.0363				.0248	.0813		.0089	.0024
1888-1889 1889-1890 1890-1891 1891-1892 1892-1893 1893-1894 1894-1895	.0011		.0372				.0218	.0719		.0108	.0010
1890-1891	.0011	.0026	.0329				0223	0582		0107	0012
1891-1892		,0051	.0289				,0261	.0584		,0086	,0015
1893~1894	1	,0036	.0337				.0259	.0582		,0059	.0015
1894-1895		.0029	.0275				.0236	.0555		.0020	.0010
1895-1896		.0035	.0254				.0235	.0533		.0015	.0008
			0201				0200	0520		0000	0000
1897~1898 1898~1899 1899~1900		.0028	0160				.0355	.0673		.0156	.0009
1899~1900		.0115	.0127				.0360	.0688		.0235	.0012
1900-1901		.0106	.0120				.0328	.0710		.0248	
1899-1900 1900-1901 1901-1902 1902-1903 1903-1904 1904-1905 1905-1906		.0076	.0131				.0308				
1902~1903		.0084	0120				.0370				
1903~1901		,0065	.0122				.0341				
1905-1906		.0060	.0141				.0318				
1906-1907		.0050	.0156				.0256	/·····		.0750	
1907-1908		.0052	.0144				0304			.0941	,
1908~1909		.0058	0134				.0339			.0779	
1907-1908 1908-1909 1909-1910 1910-1911	1	.0071	.0170				.0354				
1910-1911 1911-1912 1912-1913 1913-1914 1914-1915 1915-1916		.0078	.0220				.0312			.0630	
1912-1913		.0079	.0220				0264			.0615	
1913~1914		.0077	0200			1	.0266			.0621	1
1915~1916		.0068	.0208				.0270			.0654	
1915-1916 1916-1911 1916-1911 1918-1915 1919-1920 1920-1921 1922-1922 1922-1922 1923-1924 1924-1923 1925-1920 1926-1921 1928-1920 1930-193 1931-193 1932-193 1933-193 1933-193 1934-193 1934-193 1935-193		.0152	.0211				.0256			.0633	
1917-1918	3		.0214				.0238			.0609	
1918-1919			,0204				.0153			.0619	
1919~1920			.0186				0130			.0629	
1920~1921			0200	3		1	.0105			.0639	
1922~1923	3		.0223			1	.0068			.0595	
1923-1924	4		.0224				.0071			.0495	
1924-1925			.0223				0052			.0363	1
1925-1920	7	1	.0194		11	1	.0028		1:	0384	
1027-1026			024		1		.0023		1	0252	1
1928-1926	0	1	.016				(.0041			034	s :::::
1929-193	0		.015	0			.0053	3		.0342	4:::::
1930-193	1	4	.018				.0176			.0372	
1931-193	2		.014				52 .014.			.0302	
1932-193	4		.014	8			.0144			030	31
1934-193	5		.014				.0144				51
1935-193	61		.014	8	.1	.l	.0144	£1	J	.0303	\$1

JANUARY 1857 TO JANUARY 1936

	7										
57	58	59	60	61	62	63	64	65	66	67	January Dates
		.0207 .0260 .0270			.0179						1857-1858
		.0270			.0272						1857-1858 1858-1859 1859-1860 1860-1861 1861-1862 1862-1863 1863-1864 1864-1865 1865-1866
					.0302						1860-1861
					.0265						1861-1862
					.0209		.0058	1111111		0060	1863-1863
					.0143		.0054			.0047	1864-1865
				1	.0164		0056				1865-1866
			.0203				0123				1866-1867 1867-1868 1868-1869 1869-1870 1870-1871 1871-1872 1872-1873 1873-1874 1874-1875 1875-1876 1876-1877
			.0200		.0105		.0127				1868-1869
			.0213		.0098		.0160				1869-1870
			.0202		.0089		.0190				1871-1872
			.0180	0240	.0093		.0200				1872-1873
				.0317	.0121		.0171				1873-1874
				.0338			.0168				1875-1876
• • • • • •				.0363			.0160				1876-1877
• • • • • • •				.0524	.0138		.0204				1877-1878
				.0465	.0127		.0158				1879-1880
				.0285	.0094	.0186	.0137				1880-1881
.0196				.0232	.0082	.0136	.0146				1881-1882
.0235				.0219	.0114	.0126	.0139				1883-1884
0184				.0304	.0131	.0067	.0174				1884-1885
.0194				.0277	.0156	.0101	.0174				1876-1877 1877-1878 1878-1879 1879-1880 1880-1881 1881-1882 1882-1883 1883-1884 1884-1885 1885-1886
.0182				.0263	.0159	.0086					1887-1888
.0184				.0280	.0170	.0084	.0159	.0020			1888-1889
.01/4	.0114			.0354	.0168	.0087	.0146	.0019			1899-1890
	.0128			.0415		.0080	.0155	.0015			1891-1892
	.0172			.0465		.0084	.0140	.0020		• • • • • • •	1892-1893
	.0227			.0637		.0080	.0198	,0019			1894-1895
	.0233			.0678	::::::	.0086	.0253	.0017			1885-1886 1887-1888 1887-1889 1889-1890 1890-1891 1890-1891 1891-1892 1892-1893 1893-1894 1894-1895 1895-1896 1896-1897 1897-1898 1899-1900 1901-1902 1902-1903 1904-1905 1905-1906
	0261					.0075	,0269	0015			1890-1897
	.0270			0012		.0078	.0248	.0016			1898-1899
	.0873			.0674		.0077	.0196	.0014	[1899-1900
	.0996			.0596		.0095	.0039	.0015	.0006		1900-1901
	.0914			.0455		.0079	.0027	.0027	.0008		1902-1903
	.0898			0634		.0069	.0025	.0021	.0011		1004-1005
	.0954			.0503		,0078	.0025	.0019	.0011		1905-1906
]	.1076			.0396		.0074	.0016	.0023	.0009		1906-1907
	.0638			.0376		.0064	.0021	.0012	.0008		1907-1908
	.0680			.0360		.0061	.0029	.0017	.0011		1909-1910
	.0579			.0329		.0055	.0017	.0024	.0010		1910-1911
	.0572			.0524		.0046	.0007	.0018	.0003		1912-1912
	.0548			.0468		.0038	.0007	.0017			1913-1914
• • • • • • •	0733			.0301		.0037	.0005	.0013			1914-1915 1915-1916
	.0681			.0249		.0037	,0005	.0013			1916-1917
	.0659			.0165		.0037	.0008	.0012	[1917-1918
• • • • • • •	.0654			.0140		.0034	.0005	.0006	• • • • • • • • • • • • • • • • • • • •		1918-1919 1919-1920
	.0595			.0126		.0030	,0005	.0012			1920-1921
	.0586			.0102		.0033	.0005	.0021			1921-1922
	,0494		::::::	00831		.0031	.0001	.0031	::::::		1923-1924
	.0394			.0076		.0030	,0002	.0065			1924-1925
	.0388			.0108		.0032	.0004	.0086			1925-1926 1926-1927
	0360			0124		.0030	.0003	.0101			1927-1928
	.0348			.0144		.0025	.0002	.0065			1928-1929
	.0344			.0172		.0021		.0058			1929-1930
	.0373			,0191		.0071		.0041			1931-1932
	.0304			.0192		.0071		.0041			$\begin{array}{c} 1905-1906 \\ 1906-1907 \\ 1906-1907 \\ 1908-1909 \\ 1908-1909 \\ 1909-1910 \\ 1910-1911 \\ 1911-1912 \\ 1912-1913 \\ 1913-1914 \\ 1914-1915 \\ 1915-1916 \\ 1914-1915 \\ 1915-1916 \\ 1916-1917 \\ 1916-1917 \\ 1917-1918 \\ 1920-1921 \\ 1921-1922 \\ 1922-1923 \\ 1923-1924-1925 \\ 1925-1926 \\ 1924-1925 \\ 1925-1926 \\ 1921-1921 \\ 1921-1$
	.0304	::::::		.0192		.0071		.0041			1933-1934 1934-1935 1935-1936
	.0304			.0192		.0071		.0041			1935-1936

TABLE 15-RAILROAD COMMON STOCK WEIGHTS

				Т	ABLE	15R	AILROAI	Com	ION ST	OCK W	EIGHTS
January Dates 1837-1838 1838-1836 1838-1836 1838-1836 1836-1836	68	69	70	71	72	73	74	75	76	77	78
1857-1858											
1858-1859											
1859-1860											
1861-1862											
1862-1863											
1863-1864											
1865-1866	.0042								• • • • • • •		
1866-1867	.0081								• • • • • • •		
1867-1868	.0071										
1868-1869	.0062										
1809-1870	0167										
1871-1872	.0142					.0324					
1872-1873	.0185					.0448					
1873-1874	0173					.0620					
1875-1876	.0043					.0366				.0060	
1876-1877	.0012					.0207				.0003	
1877-1878		.0020				.0158				.0052	
1878-1879		.0056				.0149	.0350			.0061	
1880-1881			.0115				.0406			.0133	.0043
1881-1882			.0107				.0331				.0105
1882-1883			.0086				.0249				.0105
1884-1885			.0040				.0185		.0006		.0053
1885-1886			.0015				.0116		.0003		.0045
1886-1887			.0026				.0170		.0008		.0038
1887-1888			.0036				.0198		.0012		.0007
1888-1889			0033				.0186		.0010		.0070
1890-1891	1			.0029			.0160		.0008		.0064
1891-1892				.0025			.0132		.0010		,0050
1892-1893				.0028			.0136		.0018		.0028
1894-1895				.0017			.0100		.0015		.0028
1895-1896	·			.0016			.0073	0132	.0015		.0031
1896-1897]			.0017				0132	.0011		0027
1897-1898	{{			.0016				.0131	.0010		.0032
1899-1900	5	1		.0014				.0103			.0044
1900-190	[]			.0012				.0077			.0036
1901-1902				.0018				.0183			.0060
1903-1904				,0030				.0160			.0057
1904-1905				.0031				.0128			.0041
1905-1900				.0025				.0143			.0042
1007-1009				0022				0106			.0032
1908-1909	5		1	.0015				.0056			.0024
1909-1910				.0022				.0080			.0031
1910-1911				.0026	1			0070			.0026
1894-1892 1895-1892 1896-1892 1896-1892 1896-1892 1896-1992 1901-1993 1901-1993 1903-1990 1903-1990 1905-1990 1905-1990 1906-1991 1906-1991 1906-1991 1906-1991 1906-1991 1908-1990 1908-1990 1908-1990 1919-1918-1919 1918-1	3	1		.0007	.0015 .0015 .0013 .0013 .0016 .0013 .0016 .0022 .0032			.0074	[::::::		.0018
1913-191	1			.0004				.0071			.0017
1914-1913	į			.0004				.0074		1	.0013
1016-101				.0002	0015			0000			.0007
1917-191	3		1		.0015			.0083			,000,
1918-1919	9				.0014			.0052			.0020
1919-1920	9				.0013			.0051		ļ	.0034
1920-192	2				.0016			.0044		1	.0043
1922-192	3				.0013		1	.0031			.0033
1923-192	4				.0016	1		.0034			.0022
1925-192	6		1		.0022		1	.0075	1::::::	1	.0022
1926-192	7				.0061			.0080			.0044
1927-192	8				.0052			.0099			.0038
1928-192	9				. 0062			.0138			.0061
1929-193	1	1			0100		1	0226			0083
1931-193	2				.0081			.0184			
1932-193	3				.0082			.0185			
1926-192 1927-192 1928-192 1929-193 1930-193 1931-193 1932-193 1933-193 1935-193	5				1 .0082			.0185			
1935-193	6				.0082			.018			
		The second second									-

JANUARY 1857 TO JANUARY 1936

	1	1	1	1	1	1					. I
79	80	81	82	83	84	8.5	86	87	88	89	Januar Dhres
		1				-	-			-	
											1858-185
					j						1859-186
											1860-186
											1862-186
											1863-186
	1										1864-186
											1865-186
					l						1000-180
											1868-186
											1869-187
											1870-18
											1871-187
											1873-187
											1874-187
						0015		0027			1875-187
						0027		0027			1876-187
						.0020		.0018			1879-187
						.0206		.0024		.0063	1879-188
0225						.0382		.0102		.0114	1880-188
.0265						0452		.0152		.0141	1881-188
.0254						.0395		.0125		.0113	1883-188
.0241						.0387		.0084		.0126	1884-188
0307	0079					.0480		.0081		.0080	1885-188
0350	0079					.0317		.0121		.0108	1886-188
.0312	.0069					0589		.0114		.0151	1887-188
.0275	.0055					.0339		.0053		.0158	1889-180
.0270	.0048			.0013		.0252		.0037		.0304	1890-189
0208	0049			.0016		.0263		.0052		.0339	1891-189
.0193	.0047			.0015		.0250		0003	00012	0277	1892-189
.0091	.0036			.0012		.0103		.0057	.0007	.0208	1894-189
.0102	.0038			.0009		.0040		.0058	.0007	.0255	1895-189
.0102	.0042			.0015		.0127		.0053	.0007	.0202	1896-189
.0091	0000			.0005		.0103		.0063	.0006	.0229	1896-189 1897-189 1898-189 1899-190 1900-190 1902-190 1903-190 1904-190 1906-190
.0135	.0047			.0009		0134		.0056	.0006	0243	1898-189
.0124	.0040			.0011		.0118		.0033	.0011	.0249	1900-190
.0317	.0061			.0012		.0240	.0024	.0049	.0017	.0248	1901-190
.0316	0000			.0014		.0315	.0023	.0057	.0017	.0249	1902-190
.0294	,0033			.0015		.0282	.0023	,0045	.0010	0264	1903-190
.0294 .0259	.0038			:0012		.0277	.0028	.0063	.0013	.0260	1905-190
.0189	.0040		.0014	.0009		.0225	.0024	.0057	.0009	.0216	1906-190
.0168	,0036		.0011	.0007		.0257	.0021	.0059	.0010	.0202	1907-190
.0107	.0024		.0006	.0004		.0228	.0021	.0049	8000.	.0181	1908-190
.0116	.0035		.0050	.0003		.0397	.0024	.0059	.0010	.0183	1907-190 1908-190 1909-191 1910-191 1911-191 1912-191
.0086	.0024		.0050	.0002		.0374	.0021	.0045	.0010	.0185	1911-191
.0071	.0017		.0061	.0002		.0387	.0017	.0038	.0010	.0193	1912-191
.0070	0017		.0042	.0003		.0413	.0016	.0035	.0012	.0203	1913-191
.0050	.0006		.6019	0002		.0509	.0017	.0016	.0007	0214	1914-191
.0010				.0001		.0510	.0019	.0009	.0007	.0203	1914-191 1915-191 1916-191
.0061	.0013		.0030	.0010		,0528	.0017	.0013	.0011	,0214	1916-191 1917-191 1918-191 1919-192 1920-192 1922-192 1923-192 1924-192 1925-192
.0055	.0005	.0020	.0020	.0009	.0023	.0554	.0015	.0010	.0010	.0238	1918-191
.0057	.0005	.0025	,0016	.0008	.0031	.0570	.0015	.0010	.0008	.0232	1919-192
.0049		.0039	.0016	.0013	.0026	.0562 .0572	.0014	.0018	.0006	.0230	1920-192
0044		.0023	.0013	.0007	.0023	.0685	.0022	.0020	.0011	.0253	1922-192
		.0022	.0015	.0008	.0030	.0634	.00171	.0040	.0014	.0260	1923-192
0025		.0020	.0014	8000.	.0035	.0642	.0016	.0027	.0016	.0289	1924-192
.0061		.0038	.0018	.0012	.0048	.0619	.0024	.0057	.0018	0305	1925-192
0060		.0030	.0020	.0019	.0070	.0683	.0027	.0049	.0021	0271	1027_104
.0060		.0030			.0070	.0683	.0023	.0045	.0018	.0257	1928-192
.0070		.0026	0020	::::::	.0054	.0610	.0035	.0052	. 002.3	.0219	1929-193
.0124		.0090	.0079		.0045	.0362	.0045	.0121	.0026	.0175	1926-192 1927-192 1928-192 1929-193 1930-193 1931-193 1932-193 1933-193 1934-193
.0101		.0073	.0064		.0037	.0295	.0037	.0098	.0021	0142	1931-193
.0101		.0070	.0065			.0297	.0037	.0099		.0143	1933-193
.0101		.0070	,0065			.0297	.0037	.00991		.0143	1934-193
.0101		.0070	.0065			.0297	.0037	.0099		.0143	1935-193

TABLE 15-RAILROAD COMMON STOCK WEIGHTS

										1	7
January Dates	90	91	92	93	94	95	96	97	98	99	100
1857-1858											
1857-1858 1858-1859 1859-1860 1860-1861 1861-1862 1862-1863 1863-1864 1864-1865 1865-1866 1866-1867											
1859-1860											
1860-1861											
1862-1863											
1863-1864											
1864-1865											
1865-1866											
1800-1807											
1866-1867 1867-1868 1868-1869 1869-1870 1870-1871 1871-1872 1872-1873 1873-1874 1874-1875 1876-1876											
1860-1870											
1870-1871											
1871-1872											
1872-1873											
1873-1879											
1875-1876											
1876-1877			.0413								
1877-1878			.0459								
1877-1878 1878-1879			.0536								
	.0067		.0434				.0005				
1880-1881	.0067		.0542				0015		0020		
1880-1881 1881-1882 1882-1883	.0049		.0624				.0016		.0016		
1003-1004			.0508				.0008		.0012	.0327	
1884-1885	.0031		.0411	.0017			.0004		.0011	.0330	
1884-1885 1885-1886 1886-1887	,0026		.0324	.0024			.0004		.0013	.0294	
1880-1887			.0211	,0029			,0007				
1887-1888 1888-1889 1889-1890	.0045		.0283						.0017	.0330	
1888-1889	0043		.0333	.0020			0003			0291	
1890-1891			0315		.0108	.0294	.0006		,0032	.0380	
1890-1891 1891-1892 1892-1893	.0054	::::::	.0234		.0048	.0243	.0012		.0021		
1892-1893	.0063		.0206		.0057	.0338	.0014		.0017	.0420	
1893-1894	.0062	:::::::	.0175		.0043	.0288	.0013		.0013	.0400	
1894-1895 1895-1896 1896-1897					.0012	.0235	.0003		.0003	.0329	
1896-1897			.0029			.0223	.0011		,0004	,0310	
1897-1898 1898-1899						.0153	.0010		.0002	.0312	
1898-1899			.0106			.0202	0013		.0002	.0454	
1898-1899 1899-1900 1900-1901 1901-1902			.0264			.0457	.0012		.0028	.0342	.0003
1900-1901			.0264			.0436	.0012	0127	.0017	.0358	.0004
1002-1003			0438			0470		.0158	.0013	.0294	.0003
1902-1903 1903-1904 1904-1905 1905-1906			.0394			.0460		.0150	.0015	.0403	.0008
1904-1905		.0158	.0531			.0395		.0103	.0013	.0406	.0005
1905-1906		.0165	.0671			.0410		.0129	.0012	.0421	.0006
1906-1907		.0165	.0/12			.0323		.0111	.0012	.0415	.0007
1907-1908 1908-1909		.0145	.0829			.0445		.0085	.0009	.0550	.0005
		.0116	.0745			0727		.0042	.0008	0583	0005
1910-1911 1911-1912		.0150	.0843			.0721		,0075	.0016	.0650	.0004
1911-1912		.0145	.0798			.0677		.0069	.0021	.0650	.0003
		.0196	.0766			.0631		.0071	.0018	.0978	,0002
1913-1914 1914-1915		.0179	.0697			.0591		.0067	.0016	.1277	.0002
1915-1916		.0177	.0676			.0591		.0049	.0015	.1225	.0001
1916-1917		.0170	.0668			.0611		.0059	.0013	.1007	.0001
1917-1918		.0180	.0732			.0599		.0085	.0019	.0946	
1918-1919		.0181	.0745					.0082	.0018	.1093	
1919~1920		.0182	.0783			.0830		.0092	.0015	1143	
1920-1921 1921-1922		.0185	.0823			.1003		.0079	,	.1021	
		.0184	0894			0872		.0086		1001	
1923-1924 1924-1925		.0206	.0822			.0828		0000		.0990	
1924~1925		.0213	.0798			.0905		.0142		.1066	
1925~1926		.0225	.0745			.0873		.0209		.0869	
1926-1927		.0324	.0630			.0737		.0268		.0746	
1927-1928		.0270	.0635	:::::::				.0282		.0766	
1928-1929 1929-1930 1930-1931		.0217	.0613			.0656		.0272		.0908	
1930-1931		.0180	0322	,		.0620		-0248		.0921	
		.0099	.0271	11111111		.0358		0158		1612	
1932-1933 1933-1934 1934-1935 1935-1936		.0099	.04/2			.0461		.0159		.1638	
1933-1934		.0099	.0272					-0159		.1638	
1935-1935		.0099	.0272			.0461		.0159		.1638	
** AAAAA		.0099	.0412			.0461		.0159		.1638	

JANUARY 1857 TO JANUARY 1936

101	102	103	104	105	106	107	108	109	110	111	January Dates
											1857-1858 1858-1859
• • • • • • •											1858-1859
											1860-1861
											1860-1861 1861-1862 1862-1863
											1862-1863
• • • • • • • •											1863-186- 1864-1863 1865-1866
											1865-1866
											1866-1867
											1867-1868
• • • • • •											1867-186 1868-186 1869-187 1870-187 1871-187 1872-187 1873-187 1874-187 1875-187
		;									1809-187
											1871-1872
											1872-1873
• • • • • •											1873-187
• • • • • • •											1874-187
											1876-187
											1877-1878
											1878-1879
	انهيدسا										1879-1880
	.0007		.0053								1880-1881
• • • • • • •	.0007		.0043	0007	.0011						1880-188 1881-188 1882-188
	.0007		.0029	.0004	.0014						1883-1886
	.0008		.0019	.0003							1884-1885
	,0006		.0026	.0004	.0007						1884-188 1885-188 1886-188
• • • • • • •	.0005		.0023	.0006	.0011		.0000				
	.0008		.0029	.0006	.0009						1887-1888
	.0009		.0024	.0004	.0003		0010				1888-1889 1889-1890
	.0006			.0005	.0003		.0016				1890-1891
	.0006			.0005	.0003	.0005	.0012				1891-1892 1892-1893
	.0006			.0006	.0004	.0008	.0011				1892-1893
					.0008	.0006	.0006				1893-1894
					.0007	.0004	.0004				1894-1895 1895-1896
					.0010	.0006	.0002				1896-1897
			.0012		.0010	,0005	,0082	0009			1897-1898
			.0016		.0012	.0006	.0079				1898-1899
.0013			.0019		.0015	.0006	.0074	.0023			1899-1900
.0013			.0016		.0022	.0001	.0147	.0021			1001-100
.0022			,0065		,0026	.0013	.0146	.0026			1900-1901 1901-1902 1902-1903
.0037					.0023	.0013	.0170	.0028			1903-1900
.0035					.0016	.0007	.0155	.0020			1904-1905 1905-1906
.0041					.0012	.0006	.0136	,0023			1906-1907
.0042					.0008	.0005	.0137	.0018			1907-1908
.0045					.0005	,0003	01.34				
.0053					.0008	.0006	.0131	.0009			1909-1910
.0057					.0006	.0004	.0136	.0030			1908-1909 1909-1910 1910-1913 1911-1913
.0060			0015		.0004	.0003	.0229	.0022			1911-191
.0071			.0010		.0007		.0234	.0015	.0014		1913-1914
.0072			.0003		.0005		.0245	.0013	.0015		1914-191 1915-191
.0071			.0002				.0295	.0013	.0013		1915-191
.0068							.0313	.0014			1916-191
.0067		.0034	.0028				.0369	.0014	.0014		1917-191 1918-191 1919-192 1920-192
.0063		.0017	.0018				.0356	.0010	.0009	0002	1919-191
		.0040	.0027				.0355	.0012	.0008	.0003	1920-192
		.0025	.0035				.0371	.0012	,0007	.0003	1921-192
		.0028	.0034				.0390	.0009	.0004	.0002	1922-192
• • • • • • •		.0045	.0031				.0389	.0006	.0006	.0004	1923-192
• • • • • • •		.0069	.0020				.0394	.0010	.0018	.0006	1925-192
		.0073	,0096				.0408	.0010	.0034	.0007	1923-192 1924-192 1925-192 1926-192
	1	.0094	.0092				.0392	.0008	.0024		
					1 1 1 1 1 1 1	l	.0381	.0008	.0015	00009	1928-192
		.0083	.0107								
		.0083	.0097	::::::			.0349	.0012	.0009	.0007	1929-193
		.0083 .0090 .0067	.0097			::::::	.0211	.0068	.0009	.0007	1929-193 1930-193
		.0083 .0090 .0067	.0097 .0098 .0080				.0211	.0068 .0055 .0055	.0009 .0390 .0317	.0007 .0020 .0016	1927-192 1928-192 1929-193 1930-193 1931-193
		.0083 .0090 .0067	.0097				.0211	.0068	.0009		1929-193 1930-193 1931-193 1932-193 1933-193 1934-193

FOUR INDEX NUMBERS OF THE JANUARY PRICES OF AMERICAN RAILROAD COMMON STOCKS¹

- Column 1. Unweighted geometric average index number (one share each stock).
- Column 2. Arithmetic average index number weighted according to the number of shares of each company outstanding at the beginning of each year.
- Column 3. Index based on arithmetic average price of one share of each stock.

Column 4. Unweighted chain arithmetic average of relative prices.

Date	1	2	3	4
Jan 1857	100.00	100,00	100.00	100.00
1858	68.06	73,94	75,00	73.28
" 1859	70.09	75.07	75.08	78.23
" 1860	59.53	71.21	73.24	70.67
" 1861	76.49	80.54	83,23	99.38
" 1862	75.83	77.95	81.39	100.37
" 1863	132.42	125,35	129.07	183.57
" 1864	177.49	159.57	164.30	253.57
" 1865	167.96	155.18	160.14	243.67
" 1866	155.97	142.32	148.72	228.35
" 1867	165.17	148.49	159.35	243.05
" 1868	180.52	162.58	176.04	270.02
" 1869	200.81	180,16	194.73	304.79
" 1870	194.31	179.41	193.61	298.13
" 1871	202.56	187.09	199.44	312.68
" 1872	212.27	199.29	206.95	332.20
" 1873	215.40	208.53	207.67	340.33
" 1874	189.57	190.20	186.34	301.93
" 1875	173.84	185.72	180.27	283.73
" 1876	147.96	180.44	169.57	253.92
" 1877	109.76	142.74	136.82	200.82
" 1878	99.38	131.20	127.00	193.11
" 1879	128.29	146.80	148.88	286.29
" 1880	. 247.25	213.29	219.49	654.94
" 1881	303.27	265.69	278.67	816.02
" 1882	292.75	250.33	269.73	801.12
" 1883	286.02	246.70	271.09	799.10
" 1884	231.23	220.26	245.93	668.81
" 1885	174.27	179.64	205.91	525.90
" 1886	243.89	219.79	254.95	761.03
" 1887	283.93	236.15	281.23	910.12
" 1888	247.77	223.00	262.30	816.21
" 1889	238.01	212.96	255.11	804.64
" 1890	254.69	221.16	274.92	884.91

These indexes have been so adjusted (by multiplication) that January 1857 is, in each case, 100. In constructing these indexes all adjustments were made for rights, stock dividends, etc. For further details concerning the construction of these indexes see Ch. V.

TABLE 16—(Concluded)

Four Index Numbers of the January Prices of American Railroad Common Stocks

Date	1	2	3	4
Jan 1891	221.99	199.43	254.87	789.77
" 1892	272.84	229, 12	288.10	993.12
" 1893	258.10	224.79	289.54	969.17
" 1894	170.09	175.82	227.32	676.03
" 1895	151.75	170.88	222.92	617.02
" 1896	147.58	172.57	225.64	618.02
" 1897	132.89	170.08	220.53	577.17
" 1898	153,41	196.61	251.44	
" 1899	198, 15	241.52	311.90	700.16
" 1900	199.62	246.47	323.80	937.13
" 1901	267.82	301.27	389.94	960.51
" 1902	364.69	367.30	389.94 485.54	1,337.52
" 1903	416.11	396.94		1,866.38
" 1904	305.92		533.95	2,162.22
" 1905	403.84	319.75 405.51	428.12	1,616.59
1200			538.66	2,161.23
1200	467.11	470.50	629.23	2,534.54
1901	424.45	462.58	596.73	2,323.81
" 1908	271.52	347.36	435.46	1,530.03
" 1900	427.49	450.14	592.17	2,542.73
" 1910	438.86	483.46	647.84	2,710.19
" 1911	369.15	444.16	581.15	2,322.20
" 1912	335.59	439.21	570.13	2,146.84
" 1913	324.64	439.30	565.65	2,099.42
" 1914	262.61	392.93	493.29	1,739.00
" 1915	186.16	345.10	421.17	1,327.70
" 1916	209.67	389.40	479.07	1,585.99
" 1917	232.51	383.22	485.94	1,835.69
" 1918	150.85	293.92	354.79	1,233.10
" 1919	160.09	310.27	375.64	1,329.84
" 1920	159.15	285.53	353.04	1,363.95
" 1921	154.88	281.67	354.07	1,381.66
" 1922	132.27	275.02	348.64	1,227.16
" 1923	160.05	318.38	406.63	1,527.92
" 1924	157.25	304.05	393.77	1,548.46
" 1925	245.88	380.73	544.49	2,533.96
" 1926	308.91	427.24	666.61	3,291.55
" 1927	326.54	463.52	715.02	3,523.71
" 1928	395.45	540.95	848.00	4,349.81
" 1929	459,53	615 . 13	959.42	5,162.39
" 1930	398.10	585,20	886.98	4,575.94
" 1931	228.01	427.38	603.35	2,784,01
" 1932	65.55	150.85	197.36	912.33
" 1933	45.36	118.47	151.04	666.07
" 1934	86.78	196.42	254.63	1,419.91
" 1935	54,45	152,64	190.89	906.56
" 1936	65.78	195.00	240.73	1,150,27
1200	UJ./0	125.00	210,10	1,130.21

AN ARITHMETIC AVERAGE INDEX NUMBER OF THE PRICES OF AMERICAN RAILROAD COMMON STOCKS, WEIGHTED ACCORDING TO THE NUMBER OF SHARES OF EACH COMPANY OUTSTANDING AT THE BEGINNING OF EACH YEAR

Monthly, January 1857-January 1936

- Col. 1. Logarithms of Index (see Table 10-Column 6).
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).

For details of the nature of the graduations given in columns 2 and 3 of this table see Appendix D. $\,$

TABLE 17

AMERICAN RAILROAD STOCK PRICES

Date	1	2	3	4	Date	1	2	3	4
1857 F M A M J J A S O N D	1.327 1.319 1.318 1.310 1.303 1.276 1.270 1.248 1.180 1.108 1.108 1.166 1.184	1.3225 1.3129 1.3008 1.2870 1.2722 1.2571 1.2427 1.2294 1.2176 1.2007 1.2007	1.2781 1.2746 1.2711 1.2678 1.2642 1.2609 1.2575 1.2542 1.2510 1.2478 1.2478 1.2413	+.0444 +.0383 +.0297 +.0192 +.0080 0038 0148 0248 0334 0399 0438 0452	1862 J M A M J J A S O N D	1,219 1,234 1,247 1,243 1,263 1,284 1,274 1,289 1,319 1,360 1,363 1,372	1.2126 1.2223 1.2335 1.2462 1.2604 1.2760 1.2926 1.3102 1.3285 1.3471 1.3657 1.3840	1.2904 1.2982 1.3061 1.3138 1.3221 1.3300 1.3383 1.3466 1.3548 1.3628 1.3712 1.3794	0778 0759 0756 0676 0617 0540 0457 0364 0263 0157 0055 +. 0046
1858 JF M AM JASOND	1.196 1.235 1.242 1.219 1.226 1.207 1.209 1.204 1.198 1.211 1.208 1.201	1.1942 1.1952 1.1983 1.2028 1.2079 1.2123 1.2152 1.2160 1.2147 1.2115 1.2070 1.2019	1.2382 1.2349 1.2317 1.2286 1.2257 1.2223 1.2192 1.2161 1.2133 1.2101 1.2071 1.2044	0440 0397 0334 0258 0178 0100 0901 +.0014 +.0014 0001 0025	1863 J F M A M J A S O N D	1.425 1.440 1.432 1.437 1.477 1.463 1.473 1.502 1.503 1.514 1.516	1.4017 1.4182 1.4335 1.4476 1.4603 1.4721 1.4831 1.4937 1.5040 1.5144 1.5247 1.5350	1.3873 1.3951 1.4031 1.4107 1.4180 1.4253 1.4322 1.4390 1.4458 1.4520 1.4584 1.4642	+.0144 +.0231 +.0304 +.0369 +.0423 +.0468 +.0509 +.0547 +.0582 +.0663 +.0708
1859 F M A M J J A S O N D	1,202 1,197 1,195 1,184 1,170 1,173 1,176 1,179 1,196 1,188 1,192 1,188	1.1969 1.1924 1.1885 1.1851 1.1852 1.1797 1.1778 1.1778 1.1772 1.1792 1.1832 1.1890	1.2016 1.1980 1.1962 1.1940 1.1919 1.1897 1.1880 1.1865 1.1854 1.1834 1.1838 1.1835	0047 0065 0077 0089 0097 0100 0102 0097 0082 0052 0096 +.0055	IS64 JF M A M J J A S O N D	1.530 1.550 1.580 1.587 1.568 1.576 1.572 1.575 1.549 1.520 1.543 1.539	1.5448 1.5538 1.5614 1.5672 1.5706 1.5712 1.5686 1.5628 1.5544 1.5438 1.5320 1.5198	1.4697 1.4751 1.4802 1.4846 1.4892 1.4931 1.4969 1.5004 1.5037 1.5064 1.5064 1.5064 1.5092 1.5113	+.0751 +.0787 +.0812 +.0826 +.0814 +.0781 +.0717 +.0624 +.0507 +.0374 +.0228 +.0085
1860 JF M A M J J A S O N D	1,179 1,182 1,200 1,222 1,230 1,236 1,249 1,274 1,285 1,270 1,219 1,190	1.1964 1.2050 1.2140 1.2230 1.2314 1.2386 1.2442 1.2479 1.2492 1.2480 1.2444 1.2384	1.1835 1.1839 1.1846 1.1857 1.1873 1.1891 1.1914 1.1941 1.1972 1.2006 1.2044 1.2087	+.0129 +.0211 +.0294 +.0373 +.0495 +.0528 +.0520 +.0474 +.0400 +.0297	1865 JF M A M J A S O N D	1.518 1.507 1.465 1.459 1.468 1.460 1.478 1.473 1.471 1.503 1.507 1.500	1.5084 1.4983 1.4900 1.4837 1.4793 1.4751 1.4751 1.4753 1.4767 1.4788 1.4815	1.5132 1.5151 1.5164 1.5173 1.5180 1.5185 1.5188 1.5189 1.5190 1.5188 1.5188 1.5188	0048 0168 0264 0336 0387 0420 0437 0442 0437 0421 0397 0367
1861 F M A M J A S O N D	1.233 1.231 1.241 1.207 1.172 1.176 1.194 1.185 1.184 1.200 1.206 1.193	1.2306 1.2217 1.2125 1.2040 1.1968 1.1916 1.1886 1.1879 1.1879 1.1877 1.2044	1,2132 1,2181 1,2232 1,2288 1,2348 1,2409 1,2474 1,2541 1,2609 1,2679 1,2753 1,2827	+.0174 +.0036 0107 0248 0380 0403 0588 0662 0752 0776 0783	1866 J F M A M J J A S O N D	1.480 1.469 1.470 1.478 1.486 1.492 1.500 1.516 1.518 1.531 1.524 1.516	1.4848 1.4883 1.4918 1.4950 1.5003 1.5024 1.5024 1.5055 1.5064 1.5069 1.5068	1.5176 1.5172 1.5167 1.5161 1.5155 1.5150 1.5147 1.5144 1.5143 1.5143 1.5144 1.5144	0328 0289 0249 0211 0176 0147 0123 0103 0078 0076 0080

TABLE 17—Continued

Date	1	2	3	4	Date	1	2	.3	4
1867 JF MA M JI. ASOND	1,498 1,494 1,492 1,482 1,487 1,502 1,517 1,519 1,518 1,517 1,516 1,522	1.5061 1.5049 1.5034 1.5021 1.5014 1.5018 1.5035 1.5068 1.5114 1.5171 1.5234 1.5298	1.5152 1.5158 1.5167 1.5176 1.5187 1.5200 1.5216 1.5233 1.5252 1.5273 1.5252 1.5273	0091 0109 0133 0155 0173 0182 0181 0165 0138 0102 0061 0020	1872 J F M A M J J A S O N D	1.626 1.629 1.642 1.655 1.654 1.649 1.645 1.639 1.634 1.633 1.633	1.6304 1.6323 1.6341 1.6359 1.6379 1.6400 1.6421 1.6442 1.6460 1.6473 1.6478	1.6273 1.6276 1.6278 1.6279 1.6279 1.6279 1.6279 1.6280 1.6280 1.6279 1.6279	+.0031 +.0047 +.0063 +.0160 +.0100 +.0121 +.0142 +.0162 +.0180 +.0200 +.0195
1868 J.F.M.A.M.J.A.S.O.N.D.	1.538 1.548 1.546 1.543 1.558 1.565 1.565 1.560 1.564 1.571 1.558 1.567	1.5358 1.5412 1.5457 1.5495 1.5527 1.5556 1.5585 1.5617 1.5694 1.5739 1.5784	1.5341 1.5367 1.5393 1.5418 1.5448 1.54475 1.5504 1.5532 1.5562 1.55621 1.5650	+.0017 +.0045 +.0064 +.0077 +.0081 +.0081 +.0085 +.0092 +.0104 +.0118 +.0134	1873 JF M A M J A S O N D	1.646 1.651 1.648 1.640 1.641 1.637 1.636 1.633 1.599 1.561 1.545 1.583	1,6457 1,6431 1,6395 1,6352 1,6302 1,6248 1,6192 1,6134 1,6077 1,6022 1,5971 1,5929	1.6275 1.6273 1.6270 1.6266 1.6261 1.6255 1.6247 1.6238 1.6229 1.6216 1.6203 1.6288	+.0182 +.0158 +.0128 +.0086 +.0041 0005 0104 0152 0104 0232 0232
1869 FM AM JASOND	1.582 1.586 1.582 1.590 1.608 1.612 1.611 1.617 1.588 1.585 1.585 1.582	1.5828 1.5868 1.5901 1.5928 1.5946 1.5957 1.5962 1.5962 1.5959 1.5953 1.5948 1.5943	1.5676 1.5704 1.5731 1.5757 1.5784 1.5808 1.5834 1.5858 1.5884 1.5906 1.5906 1.5929	+.0152 +.0164 +.0170 +.0171 +.0162 +.0149 +.0128 +.0104 +.0075 +.0047 +.0019 0009	1874 JF M A M J J S O N D	1.606 1.618 1.610 1.598 1.587 1.582 1.583 1.586 1.592 1.591 1.592	1.5896 1.5875 1.5868 1.5871 1.5383 1.5901 1.5919 1.5934 1.5943 1.5945 1.5939 1.5928	1.6171 1.6151 1.6131 1.6131 1.6109 1.6085 1.6059 1.6032 1.5003 1.5970 1.5937 1.5937	0273 0276 0265 0237 0153 0153 0069 0027 +.00069 +.0037 +.0069
1870 JF M A M J A S O N D	1.581 1.594 1.592 1.598 1.615 1.618 1.605 1.597 1.601 1.603 1.603 1.598	1.5940 1.5939 1.5942 1.5949 1.5960 1.5976 1.5994 1.6015 1.6036 1.6057 1.6095	1.5977 1.5997 1.6018 1.6040 1.6061 1.6081 1.6099 1.6117 1.6134 1.6150 1.6166 1.6180	0037 0058 0076 0091 0105 0105 0105 0102 0098 0093 0091 0088	1875 I M A M J J A S O N D	1.596 1.594 1.598 1.603 1.584 1.575 1.576 1.577 1.573 1.567 1.573	1,5913 1,5895 1,5877 1,5846 1,5833 1,5823 1,5815 1,5809 1,5803 1,5796 1,5787	1.5828 1.5788 1.5747 1.5706 1.5663 1.5619 1.5574 1.5528 1.5482 1.5435 1.5388 1.5342	+ .0085 + .0107 + .0136 + .0155 + .0214 + .0226 + .0327 + .0367 + .0407
1871 F M A M J A S O N D	1.599 1.603 1.612 1.624 1.633 1.630 1.622 1.625 1.627 1.605 1.608 1.617	1.6105 1.6117 1.6127 1.6138 1.6151 1.6165 1.6183 1.6202 1.6223 1.6244 1.6265 1.6285	1.6192 1.6204 1.6215 1.6225 1.6233 1.6241 1.6248 1.6254 1.6260 1.6265 1.6268 1.6271	0087 0087 0088 0087 0082 0076 0052 0052 0037 0021 0003 +.0014	1876 J F M A M J J A S O N D	1.583 1.590 1.591 1.574 1.555 1.551 1.547 1.527 1.501 1.487 1.485	1.5775 1.5757 1.5759 1.5688 1.5680 1.5550 1.5446 1.5318 1.5171 1.5009 1.4842 1.4678	1.5296 1.5250 1.5250 1.5204 1.5158 1.5115 1.5074 1.5032 1.4992 1.4953 1.4918 1.4885 1.4853	+.0479 +.0502 +.0502 +.0513 +.0513 +.0474 +.0474 +.0474 +.0474 +.04740174

TABLE 17—Continued

Date	1	2	3	4	Date	1	2	3	4
1877 J. F. M. A. M. J. A. S. O. N. D.	1.481 1.453 1.432 1.399 1.398 1.373 1.387 1.414 1.442 1.455 1.447	1.4528 1.4397 1.4290 1.4209 1.4155 1.4125 1.4127 1.4137 1.4174 1.4227 1.4292 1.4364	1.4823 1.4797 1.4774 1.4774 1.4754 1.4737 1.4723 1.4714 1.4709 1.4707 1.4709 1.4706	0295 0400 0484 0545 0598 0598 0594 0572 0533 0482 0424 0362	1882 J F M A M J J A S O N D	1.725 1.715 1.713 1.713 1.707 1.705 1.730 1.743 1.747 1.736 1.718 1.718	1.7262 1.7228 1.7206 1.7196 1.7194 1.7200 1.7211 1.7224 1.7238 1.7249 1.7254 1.7251	1.7294 1.7294 1.7294 1.7290 1.7284 1.7272 1.7259 1.7241 1.7222 1.7190 1.7175 1.7148 1.7119	-,0032 -,0066 -,0084 -,0088 -,0078 -,0059 -,0030 +,0002 +,0039 +,0074 +,0106 +,0132
1878 J F M A M J A S O N D	1.445 1.436 1.443 1.457 1.457 1.458 1.476 1.471 1.480 1.476 1.474 1.474	1.4435 1.4500 1.4556 1.4590 1.4632 1.4657 1.4677 1.4698 1.4722 1.4751 1.4788 1.4788	1.4739 1.4757 1.4780 1.4806 1.4836 1.4836 1.4907 1.4907 1.4997 1.5044 1.5044 1.5099 1.5154	0304 0257 0224 0207 0204 0212 0230 0251 0275 0293 0311 0319	1883 F M A M I I A S O N D	1.719 1.708 1.714 1.724 1.715 1.719 1.711 1.691 1.685 1.691 1.682	1.7241 1.7222 1.7197 1.7168 1.7137 1.7105 1.7071 1.7034 1.6993 1.6944 1.6887 1.6820	1.7087 1.7056 1.7022 1.6990 1.6955 1.6922 1.6888 1.6854 1.6789 1.6757	+.0154 +.0166 +.0175 +.0178 +.0182 +.0183 +.0183 +.0173 +.0155 +.0150 +.0150 +.0093
1879 F M AM J ASOND	1.493 1.510 1.501 1.514 1.536 1.542 1.550 1.556 1.571 1.615 1.636 1.638	1.4895 1.4970 1.5063 1.5176 1.5307 1.5454 1.5611 1.5769 1.6059 1.6179 1.6279	1.5215 1.5277 1.5343 1.5481 1.5481 1.5554 1.5628 1.5704 1.5781 1.5863 1.5942 1.6021	0320 0307 0280 0234 0174 0100 0017 +.0065 +.0140 +.0196 +.0237 +.0258	1884 J F M A M J J A S O NY	1.670 1.681 1.680 1.663 1.626 1.593 1.605 1.631 1.615 1.600 1.590	1.6744 1.6661 1.6573 1.6482 1.6391 1.6299 1.6123 1.6043 1.5972 1.5914 1.5873	1.6696 1.6670 1.6644 1.6619 1.6594 1.6574 1.6555 1.6537 1.6521 1.6508	+.0048 0009 0071 0137 0275 0346 0414 0478 0536 0583 0583 0612
1880 FM AM J ASOND	1.656 1.665 1.672 1.666 1.629 1.630 1.649 1.668 1.667 1.683 1.709	1.6360 1.6425 1.6478 1.6525 1.6571 1.6621 1.6679 1.6750 1.6835 1.6934 1.7045	1.6100 1.6178 1.6257 1.6336 1.6416 1.6493 1.6568 1.6640 1.6709 1.6774 1.6838 1.6897	+.0260 +.0247 +.0221 +.0189 +.0155 +.0128 +.0111 +.01160 +.0126 +.0267	1885 J F M A M J J A S O N D	1.581 1.593 1.594 1.594 1.587 1.584 1.602 1.624 1.619 1.642 1.668 1.667	1.5851 1.5851 1.5872 1.5970 1.6040 1.6119 1.6202 1.6286 1.6369 1.6449 1.6523	1,6479 1,6474 1,6470 1,6467 1,6466 1,6469 1,6473 1,6478 1,6484 1,6491	0628 0623 0598 0554 0496 0427 0350 0271 0115 0042 +.0024
1881 FM AM JASOND	1.751 1.746 1.752 1.750 1.767 1.771 1.754 1.746 1.749 1.742 1.745 1.733	1.7284 1.7395 1.7490 1.7560 1.7601 1.7611 1.7592 1.7550 1.7493 1.7428 1.7365 1.7308	1.6955 1.7006 1.7054 1.7057 1.7139 1.7133 1.7203 1.7230 1.7252 1.7269 1.7281 1.7288	+ .0329 + .0389 + .0436 + .0463 + .0462 + .0438 + .0320 + .0241 + .0159 + .0084 + .0020	1886 J F M A M J J A S O N D	1.669 1.676 1.668 1.662 1.654 1.673 1.680 1.684 1.706 1.715	1.6589 1.6647 1.6697 1.6739 1.6775 1.6809 1.6843 1.6820 1.6920 1.6963 1.7006	1.6507 1.6518 1.6528 1.6539 1.6550 1.6563 1.6576 1.6589 1.6601 1.6615 1.6628	+.0082 +.0129 +.0169 +.0200 +.0225 +.0246 +.0267 +.0319 +.0348 +.0378 +.0405

TABLE 17-Continued

Date	1	2	3	4	Date	1	2	3	4
1887 JF M A M J A S O N D	1.700 1.696 1.706 1.718 1.725 1.714 1.702 1.691 1.685 1.668 1.674 1.673	1.7080 1.7102 1.7111 1.7103 1.7081 1.7045 1.6999 1.6945 1.6887 1.6828 1.6772	1.6657 1.6670 1.6684 1.6696 1.6708 1.6720 1.6730 1.6739 1.6746 1.6754 1.6759	+.0423 +.0432 +.0427 +.0407 +.0325 +.0269 +.0206 +.0141 +.0074 +.0013 0040	JESS AND DESCRIPTION OF THE PROPERTY OF THE PR	1.687 1.686 1.691 1.689 1.687 1.684 1.687 1.673 1.681 1.673	1.6813 1.6848 1.6875 1.6894 1.6906 1.6912 1.6911 1.6900 1.6876 1.6838 1.6783 1.6713	1.6540 1.6528 1.6517 1.6504 1.6486 1.6472 1.6454 1.6436 1.6419 1.6399 1.6379 1.6359	+ .027: + .0326 + .035: + .0396 + .0426 + .0446 + .045* + .0464 + .045*
1888 FM AM J ASOND	1.675 1.671 1.655 1.656 1.662 1.644 1.657 1.663 1.675 1.670 1.657	1.6679 1.6645 1.6621 1.6605 1.6595 1.6590 1.6586 1.6583 1.6573 1.6567	1.6763 1.6764 1.6763 1.6758 1.6758 1.6747 1.6742 1.6734 1.6734 1.6727 1.6719	0084 0119 0142 0156 0163 0161 0159 0156 0154 0152 0150	1893 F M A M J J A S O N D	1.679 1.669 1.654 1.657 1.625 1.604 1.563 1.554 1.578 1.578 1.585 1.594	1.6628 1.6530 1.6423 1.6313 1.6203 1.6000 1.5915 1.5847 1.5796 1.5765	1.6339 1.6316 1.6295 1.6295 1.6224 1.6226 1.6203 1.6179 1.6151 1.6128 1.6103 1.6077	+.0286 +.0214 +.0124 +.0036 0046 0129 026 0303 0333 0336
1889 J F M A M J A S O N D	1.655 1.659 1.647 1.644 1.655 1.660 1.649 1.659 1.674 1.670 1.669	1.6555 1.6550 1.6546 1.6544 1.6545 1.6551 1.6565 1.6666 1.6653 1.6692 1.6730	1.6702 1.6695 1.6687 1.6678 1.6670 1.6664 1.6658 1.6652 1.6646 1.6642 1.6638 1.6638	0147 0145 0141 0134 0125 0113 0093 0066 0030 +.0011 +.0054 +.0094	1894 J F M A M J J A S O N D	1.572 1.577 1.590 1.594 1.576 1.568 1.568 1.576 1.576 1.576 1.571 1.565	1.5752 1.5761 1.5773 1.5778 1.5778 1.5764 1.5740 1.5712 1.5684 1.5663 1.5654 1.5660	1.6051 1.6026 1.6001 1.5976 1.5949 1.5923 1.5808 1.5873 1.5849 1.5824 1.5801 1.5779	0299 0261 0222 0199 0175 0165 0166 0166 0144
1890 JF MAM JASOND	1.671 1.667 1 664 1.663 1.690 1.687 1.683 1.672 1.663 1.643 1.614 1.607	1.6761 1.6781 1.6787 1.6778 1.67752 1.6712 1.6659 1.6597 1.6597 1.6587 1.6456 1.6387	1.6632 1.6630 1.6629 1.6627 1.6626 1.6625 1.6625 1.6624 1.6624 1.6623 1.6622 1.6622	+.0129 +.0151 +.0158 +.0151 +.0126 +.0087 +.0034 0027 0096 0167 0235 0295	1895 F M A M I J A S O N D	1.559 1.553 1.550 1.567 1.590 1.600 1.607 1.613 1.617 1.611 1.597	1.5681 1.5714 1.5757 1.5805 1.5854 1.5940 1.5968 1.5981 1.5981 1.5961 1.5923	1.5756 1.5736 1.5716 1.5697 1.5669 1.5663 1.5649 1.5638 1.5627 1.5618 1.5614	0073 0022 +.0041 +.0107 +.0237 +.0231 +.0356 +.0356 +.0341 +.0311
1891 JF M A M J A S O N D	1.627 1.631 1.621 1.637 1.636 1.626 1.621 1.639 1.676 1.676 1.667	1.6275 1.6243 1.6233 1.6245 1.6281 1.6336 1.6406 1.6485 1.6566 1.6642 1.6711 1.6768	1.6618 1.6616 1.6613 1.6609 1.6604 1.6595 1.6587 1.6579 1.6571 1.6562 1.6552	0343 0373 0380 0364 0323 0264 0189 0102 0013 +.0071 +.0149 +.0216	I 1896 I F M A M I J A S O N D	1.564 1.581 1.572 1.576 1.574 1.568 1.543 1.519 1.538 1.547 1.570 1.558	1.5872 1.5810 1.5744 1.5679 1.5618 1.5564 1.5544 1.5458 1.5458 1.5442 1.5438	1.5611 1.5613 1.5618 1.5626 1.5634 1.5646 1.5659 1.5674 1.5690 1.5708 1.5728	+.026: +.019: +.0126: +.005: 0010: 0136: 0196: 026: 0296: 0300:

TABLE 17—Continued

Date	1	1 2	3 .	4	Date	1	2	J 3	4
J F M A M J J A S O N D	1.557 1.552 1.554 1.540 1.542 1.562 1.578 1.606 1.625 1.614 1.599 1.610	1.5473 1.5512 1.5563 1.5624 1.5690 1.5759 1.5826 1.5889 1.5946 1.5994 1.6035 1.6067	1.5771 1.5795 1.5819 1.5844 1.5870 1.5898 1.5926 1.5956 1.5985 1.6017 1.6050 1.6084	0298 0283 0256 0256 0180 0139 0100 0067 0023 0015 0017	1902 J F M A M J J A S O N D	1.892 1.895 1.896 1.912 1.914 1.915 1.931 1.944 1.945 1.930 1.913 1.905	1.8941 1.8987 1.9041 1.9101 1.9163 1.9221 1.9271 1.9304 1.9316 1.9308 1.9272 1.9210	1.8536 1.8560 1.8583 1.8604 1.8622 1.8643 1.8661 1.8678 1.8697 1.8714 1.8731 1.8749	+.0405 +.0427 +.0458 +.0497 +.0541 +.0578 +.0610 +.0626 +.0619 +.0594 +.0541 +.0461
J F M A M J A S O N D	1.620 1.618 1.598 1.589 1.614 1.630 1.648 1.650 1.641 1.651	1.6091 1.6111 1.6130 1.6153 1.6186 1.6233 1.6297 1.6379 1.6478 1.6589 1.6705 1.6820	1.6117 1.6153 1.6190 1.6229 1.6270 1.6314 1.6358 1.6405 1.6452 1.6502 1.6505 1.6609	0026 0042 0060 0076 0084 0081 0026 +.0026 +.0026 +.0150 +.0211	1903 F M A M J A S O N D	1.925 1.918 1.898 1.878 1.871 1.847 1.835 1.822 1.816 1.807 1.809 1.825	1.9125 1.9022 1.8907 1.8785 1.8663 1.8544 1.8433 1.8333 1.8247 1.8176 1.8123 1.8091	1.8768 1.8785 1.8804 1.8824 1.8844 1.8864 1.8884 1.8904 1.8925 1.8945 1.8945 1.8986	+.0357 +.0237 +.0103 0039 0181 0320 0451 0571 0678 0769 0842 0895
1899 F M AM J J A S O N D	1.710 1.726 1.725 1.731 1.715 1.709 1.725 1.735 1.730 1.728 1.737 1.714	1.6928 1.7026 1.7110 1.7180 1.7236 1.7278 1.7309 1.7326 1.7322 1.7327 1.7311 1.7286	1.6664 1.6721 1.6781 1.6842 1.6904 1.7034 1.7100 1.7166 1.7232 1.7360 1.7368	+ .0264 + .0305 + .0329 + .0338 + .0332 + .0309 + .0275 + .0226 + .0166 + .0095 + .0011 0082	1904 J F M A M J J A S O N D	1.832 1.818 1.818 1.829 1.818 1.820 1.839 1.854 1.873 1.897 1.915 1.922	1.8082 1.8098 1.8139 1.8205 1.8292 1.8397 1.8515 1.8642 1.8774 1.8907 1.9038 1.9166	1.9007 1.9027 1.9046 1.9065 1.9083 1.9101 1.9117 1.9134 1.9148 1.9163 1.9177 1.9191	0925 0929 0907 0860 0791 0704 0602 0492 0374 0256 0139 0025
1900 F M A M J A S O N D	1.719 1.728 1.739 1.747 1.729 1.716 1.720 1.712 1.727 1.755 1.786	1.7257 1.7226 1.7200 1.7183 1.7182 1.7200 1.7242 1.7309 1.7402 1.7517 1.7653 1.7803	1.7436 1.7502 1.7568 1.7633 1.7695 1.7754 1.7814 1.7872 1.7930 1.7984 1.8036 1.8086	0179 0276 0368 0450 0513 0554 0572 0563 0528 0467 0483	1905 J F M A M J J A S O N D	1.935 1.956 1.969 1.962 1.940 1.948 1.962 1.980 1.984 1.983 1.983	1.9287 1.9398 1.9498 1.9584 1.9654 1.9708 1.9772 1.9787 1.9787 1.9798 1.9808 1.9821	1.9204 1.9217 1.9230 1.9243 1.9253 1.9265 1.9276 1.9287 1.9300 1.9311 1.9324 1.9336	+ .0083 + .0181 + .0268 + .0341 + .0401 + .0443 + .0473 + .0485 + .0487 + .0484 + .0485
1901 J M A M J A S O N D	1.806 1.820 1.834 1.871 1.854 1.858 1.869 1.872 1.874 1.891 1.885	1.7962 1.8122 1.8276 1.8416 1.8538 1.8639 1.8717 1.8774 1.8815 1.8846 1.8874 1.8904	1.8131 1.8177 1.8218 1.8258 1.8258 1.8297 1.8332 1.8366 1.8398 1.8430 1.8458 1.8458 1.8458	0169 0055 +.0058 +.0158 +.0241 +.0307 +.0351 +.0376 +.0388 +.0388 +.0392	1906 J F M A M J A S O N D	1.999 1.997 1.989 1.983 1.972 1.980 1.972 2.004 2.017 2.012 2.011 2.007	1.9840 1.9865 1.9894 1.9924 1.9954 1.9978 1.9995 2.0002 1.9997 1.9978 1.9943 1.9889	1.9350 1.9362 1.9375 1.9387 1.9400 1.9412 1.9423 1.9434 1.9448 1.9456 1.9467	+ .0490 + .0503 + .0519 + .0537 + .0556 + .0572 + .0568 + .0549 + .0522 + .0476 + .0412

TABLE 17-Continued

Date	1	2	3	4	Date	1	2	3	4
1907 F M A M J A S O N D	1.992 1.975 1.930 1.932 1.918 1.907 1.923 1.897 1.898 1.858 1.858 1.851	1.9812 1.9712 1.9590 1.9448 1.9294 1.9137 1.8986 1.8852 1.8743 1.8663 1.8615 1.8599	1.9486 1.9494 1.9500 1.9506 1.9511 1.9515 1.9518 1.9520 1.9521 1.9521 1.9521 1.9521	+.0326 +.0218 +.0090 0058 0217 0378 0532 0668 0778 0858 0906 0922	1912 JF M A M J J A S O N D	1.969 1.965 1.965 1.974 1.984 1.981 1.979 1.979 1.990 1.990 1.987 1.984	1.9700 1.9718 1.9744 1.9773 1.9804 1.9830 1.9847 1.9852 1.9843 1.9818 1.9774	1.9755 1.9732 1.9707 1.9684 1.9653 1.9628 1.9599 1.9573 1.9542 1.9516 1.9489 1.9463	0055 0014 +.0037 +.0089 +.0151 +.0202 +.0248 +.0279 +.0301 +.0302 +.0285 +.0261
1908 JF M A M J A S O N D	1.868 1.851 1.863 1.883 1.907 1.908 1.920 1.934 1.931 1.937 1.963 1.974	1.8613 1.8653 1.8716 1.8799 1.8897 1.9003 1.9123 1.9242 1.9358 1.9470 1.9669	1.9521 1.9521 1.9521 1.9522 1.9522 1.9522 1.9528 1.9533 1.9533 1.9540 1.9554	0908 0868 0805 0723 0523 0405 0290 0175 0070 +.0031 +.0115	1913 J F M A M J J A S O N D	1.970 1.958 1.949 1.948 1.936 1.915 1.921 1.928 1.929 1.919 1.909 1.908	1.9660 1.9590 1.9518 1.9448 1.9383 1.9327 1.9280 1.9244 1.9216 1.9195 1.9178 1.9160	1.9436 1.9413 1.9390 1.9367 1.9345 1.9325 1.9305 1.9286 1.9269 1.9253 1.9253 1.9237 1.9221	+.0224 +.0177 +.0128 +.0081 +.0038 +.0002 0025 0042 0053 0059 0061
1900 FMAMILASOND	1.980 1.971 1.978 1.994 2.004 2.009 2.017 2.025 2.022 2.021 2.013 2.019	1.9757 1.9834 1.9909 2.0041 2.0097 2.0147 2.0179 2.0201 2.0198 2.0180 2.0149	1.9562 1.9573 1.9584 1.9584 1.9596 1.9608 1.9621 1.9635 1.9650 1.9667 1.9684 1.9701 1.9717	+ .0195 + .0261 + .0325 + .0382 + .0433 + .0476 + .0512 + .0534 + .0514 + .0479 + .0432	1914 J F M A M J J A S O N D	1.921 1.924 1.912 1.902 1.905 1.905 1.905 1.873* 1.877* 1.867* 1.862* 1.858	1.9138 1.9109 1.9073 1.9030 1.8979 1.8924 1.8865 1.8749 1.8697 1.8653 1.8626	1.9206 1.9191 1.9177 1.9162 1.9148 1.9134 1.9120 1.9106 1.9091 1.9078 1.9064 1.9048	0068 0082 0104 0132 0169 0210 0255 0301 0342 0381 0411
J F M A M J A S O N D	2.011 1.997 2.007 1.999 1.993 1.971 1.949 1.958 1.960 1.978 1.974 1.963	2.0095 2.0030 1.9965 1.9830 1.9773 1.9728 1.9676 1.9679 1.9678 1.9683 1.9699	1.9733 1.9751 1.9767 1.9782 1.9797 1.9811 1.9824 1.9837 1.9849 1.9858 1.9858 1.9867 1.9874	+ .0362 + .0279 + .0198 + .0114 + .0033 0038 0096 0141 0170 0182 0184 0175	1915 J M A M J J A S O N D	1.865 1.857 1.865 1.887 1.876 1.872 1.862 1.875 1.886 1.909 1.928 1.925	1.8612 1.8615 1.8635 1.8671 1.8717 1.8771 1.8784 1.8828 1.8884 1.8936 1.8984 1.9027 1.9065	1.9031 1.9018 1.9003 1.8988 1.8972 1.8959 1.8945 1.8931 1.8916 1.8904 1.8891 1.8891 1.8878	0419 0403 0368 0317 0255 0118 0117 0047 +.0080 +.0136 +.0136
JF M AM J J A SOND	1.974 1.980 1.975 1.975 1.982 1.992 1.992 1.992 1.992 1.972 1.949 1.956 1.972	1.9718 1.9737 1.9752 1.9762 1.9764 1.9758 1.9746 1.9714 1.9700 1.9691	1.9879 1.9881 1.9881 1.9878 1.9875 1.9867 1.9854 1.9839 1.9839 1.9822 1.9807 1.9793 1.9775	0161 0144 0129 0116 0111 0109 0108 0108 0107 0102 0084	1916 JF M A M J J A S O N D	1.917 1.907 1.905 1.902 1.914 1.920 1.916 1.913 1.919 1.930 1.927	1.9101 1.9132 1.9157 1.9157 1.9191 1.9198 1.9199 1.9195 1.9188 1.9177 1.9160 1.9135	1.8865 1.8854 1.8842 1.8829 1.8816 1.8804 1.8791 1.8778 1.8765 1.8752 1.8737 1.8737	+ .0236 + .0278 + .0318 + .0348 + .0399 + .0408 + .0417 + .0423 + .0423 + .0423

^{*}Interpolated-Stock Exchange closed.

TABLE 17—Continued

Date	1	2	3	4	Date	1	2	3	4
1917 F M A M I J A S O N D	1.910 1.887 1.892 1.887 1.869 1.875 1.869 1.863 1.844 1.825 1.791	1.9098 1.9045 1.8975 1.8888 1.8785 1.8670 1.8549 1.8428 1.8312 1.8207 1.8117 1.8044	1.8708 1.8694 1.8678 1.8661 1.8641 1.8624 1.8604 1.8584 1.8560 1.8538 1.8515 1.8489	+.0390 +.0351 +.0297 +.0227 +.0144 +.0046 0055 0156 0248 0331 0398 0445	I922 JF M A M J J A S O N D	1.766 1.781 1.779 1.818 1.827 1.822 1.839 1.859 1.865 1.865 1.840 1.830	1.7799 1.7906 1.8014 1.8120 1.8219 1.8308 1.8385 1.8446 1.8489 1.8512 1.8514 1.8495	1.7884 1.7894 1.7903 1.7915 1.7927 1.7940 1.7953 1.7970 1.7985 1.8002 1.8040	0085 +. 0012 +. 0111 +. 0205 +. 0292 +. 0368 +. 0432 +. 0476 +. 0510 +. 0494 +. 0455
IP IS IS IS IS IS IS IS IS IS IS IS IS IS	1.795 1.800 1.797 1.788 1.802 1.804 1.806 1.816 1.816 1.816 1.836 1.847 1.829	1.7991 1.7959 1.7946 1.7952 1.7975 1.8012 1.8060 1.8115 1.8171 1.8227 1.8237 1.8319	1.8465 1.8439 1.8411 1.8384 1.8355 1.8325 1.8295 1.8295 1.8238 1.8209 1.8182 1.8154	0474 0480 0465 0432 0380 0313 0235 0151 0067 +.0018 +.0095 +.0165	1923 J F M A M J J A S O N D	1.830 1.843 1.845 1.839 1.823 1.819 1.801 1.797 1.801 1.797 1.804	1.8458 1.8406 1.8346 1.8281 1.8217 1.8158 1.8106 1.8063 1.8029 1.8008 1.7999 1.8004	1.8061 1.8084 1.8105 1.8129 1.8152 1.8178 1.8204 1.8232 1.8259 1.8288 1.8317 1.8349	+. 0397 +. 0322 +. 0241 +. 0152 +. 0065 0028 0169 0230 0280 0318 0345
1919 JF MA M JASOND	1.818 1.819 1.823 1.825 1.848 1.849 1.847 1.818 1.810 1.815 1.801 1.781	1.8351 1.8371 1.8378 1.8371 1.8351 1.8317 1.8268 1.8206 1.8135 1.8058 1.7907	1.8122 1.8099 1.8072 1.8045 1.8018 1.7996 1.7974 1.7954 1.7935 1.7917 1.7903 1.7889	+.0229 +.0272 +.0306 +.0326 +.0323 +.0321 +.0294 +.0252 +.0200 +.0141 +.0377 +.0018	1924 J F M A M J S O N D	1,810 1,813 1,810 1,816 1,817 1,829 1,849 1,861 1,858 1,853 1,882 1,904	1.8026 1.8064 1.8119 1.8190 1.8272 1.8361 1.8453 1.8543 1.8627 1.8702 1.8770 1.8829	1.8381 1.8414 1.8448 1.8483 1.8518 1.8555 1.8555 1.8667 1.8706 1.8746 1.8786	035503560329029601390136008600440009 +.0029
1920 JF M A M J A S O N D	1.782 1.764 1.790 1.774 1.758 1.754 1.760 1.775 1.800 1.819 1.806 1.764	1.7844 1.7795 1.7763 1.7747 1.7745 1.7754 1.7769 1.7783 1.7792 1.7794 1.7785	1.7877 1.7866 1.7857 1.7849 1.7843 1.7839 1.7835 1.7835 1.7827 1.7826	0033 0071 0094 0102 0098 0085 0066 0047 0035 0032 0040	1925 F M A M J J A S O N D	1.907 1.908 1.896 1.883 1.895 1.897 1.901 1.916 1.920 1.926 1.938 1.938	1.8883 1.8932 1.8978 1.9020 1.9060 1.9098 1.9136 1.9173 1.9212 1.9253 1.9296 1.9341	1.8827 1.8869 1.8911 1.8954 1.8997 1.9041 1.9086 1.9133 1.9180 1.9228 1.9227 1.9328	+.0056 +.0063 +.0066 +.0066 +.0056 +.0056 +.0034 +.0036 +.0016
1921 F M A M J A S O N D	1.776 1.771 1.750 1.742 1.759 1.732 1.750 1.758 1.762 1.762 1.765 1.767	1,7733 1,7692 1,7644 1,7593 1,7546 1,7506 1,7482 1,7479 1,7499 1,7545 1,7613 1,7699	1.7826 1.7827 1.7830 1.7832 1.7836 1.7839 1.7842 1.7848 1.7854 1.7861 1.7868 1.7868	0093 0135 0186 0239 0290 0333 0369 0355 0316 0255 0175	1926 J F M A M J J A S O N D	1.957 1.950 1.931 1.934 1.938 1.956 1.964 1.976 1.989 1.976 1.979	1.9386 1.9429 1.9470 1.9507 1.9541 1.9576 1.9614 1.9658 1.9771 1.9775 1.9848 1.9929	1.9380 1.9434 1.9488 1.9543 1.9661 1.9719 1.9778 1.9843 1.9907 1.9972 2.0037	+.0006 0005 0016 0036 0066 008 0106 0132 0132 0108

TABLE 17—Concluded

Date	1	2	3	4	Date	1	2	3	4
1927 F M A M J J A SOND	1.993 2.011 2.016 2.026 2.035 2.042 2.050 2.055 2.062 2.061 2.058 2.067	2.0013 2.0090 2.0182 2.0261 2.0335 2.0463 2.0516 2.0595 2.0621 2.0639	2.0100 2.0168 2.0234 2.0300 2.0365 2.0433 2.0499 2.0565 2.0629 2.0694 2.0753 2.0817	0087 0069 0052 0039 0030 0036 0049 0069 0099 0137 0178	1932 J F M A M J J A S O N D	1.505 1.503 1.469 1.328 1.192 1.129 1.201 1.409 1.455 1.418 1.387	1.4818 1.4330 1.3909 1.3566 1.3304 1.3125 1.3032 1.3028 1.3113 1.3278 1.3512 1.3793		
1928 JF MA M JASOND	2.060 2.049 2.063 2.081 2.088 2.066 2.066 2.067 2.078 2.073 2.073 2.095 2.097	2.0650 2.0657 2.0667 2.0667 2.0574 2.0386 2.0703 2.0730 2.0767 2.0817 2.0878 2.0950	2.0876 2.0931 2.0983 2.1031 2.1078 2.1115 2.1149 2.1176 2.1199 2.1211 2.1215 2.1209	0226 0274 0321 0364 0404 0429 0446 0432 0394 0337 0259	1933 JF M A M J J A S O N D	1.400 1.377 1.376 1.406 1.540 1.606 1.662 1.659 1.633 1.550 1.549 1.572	1.4098 1.4407 1.4701 1.4701 1.4972 1.5220 1.5447 1.5657 1.5850 1.6024 1.6168 1.6275 1.6335		
1929 JF MAM J JASOND	2.116 2.110 2.109 2.103 2.109 2.126 2.126 2.126 2.184 2.189 2.133 2.087 2.097	2.1028 2.1108 2.1185 2.1252 2.1309 2.1352 2.1393 2.1393 2.1394 2.1374 2.1339 2.1285	2.1201 2.1177 2.1145 2.1105 2.1056	0173 0069 +.0040 +.0147 +.0253	1934 JF M A M J J A S O N D	1.620 1.663 1.647 1.652 1.605 1.505 1.516 1.516 1.516 1.518 1.512 1.525	1.6342 1.6301 1.6219 1.6107		
1930 J F M A M J A S O N D	2.094 2.116 2.118 2.110 2.088 2.061 2.061 2.049 2.041 2.098 1.970 1.931	2.1212 2.1121 2.1016 2.0900 2.0777 2.0653 2.0528 2.0404 2.0277 2.0144 2.0001 1.9848			1935 JF MA M JA SOND	1.510 1.485 1.427 1.440 1.463 1.479 1.501 1.525 1.533 1.505 1.552 1.584			
1931 JFMAM JASOND	1.958 1.983 1.954 1.903 1.849 1.831 1.840 1.772 1.655 1.614 1.502	1.9681 1.9499 1.9298 1.9067 1.8795 1.8466 1.8074 1.7613 1.7091 1.6525 1.5939 1.5362			1936 J	1.617			

TABLE 18

PRICE OF GOLD IN GREENBACKS JANUARY 1862-DECEMBER 1878¹ MONTHLY AVERAGES

Date		Date		Date		Date		Date	
1862 JF MA MJJASOND 1863 JF MAMJJASOND 1864 JF MAMJJASOND 1865 JF MA M	102. 5 103. 5 101. 8 101. 5 103. 5 115. 5 118. 5 118. 5 118. 5 118. 5 118. 5 118. 5 118. 5 118. 5 119. 5 11	1865 J J AS ON D 1866 1 J F M A M J J AS ON D 1867 1 F M A M J J AS ON D 1868 J F M A M J J AS O	140. 1 142. 1 143. 5 146. 2 147. 0 148. 5 147. 0 148. 1 138. 4 138. 4 138. 1 148. 7 148. 5 148. 3 143. 8 136. 7 137. 6 137. 6 137. 6 137. 6 137. 6 137. 6 137. 6 138. 6 137. 6 138. 6 139. 6 149. 6 14	1868 ND D0 1870 F M A M J J A S O N D D1 1870 N D D N D D 1871 J A S O N D D 1871 J A S O N D D 1871 J A S O N D D 1872 J F M A M J M J M M J M M M M M M M M M M M	134. 4 135. 2 135. 6 134. 3 132. 9 138. 1 136. 1 136. 2 126. 2 121. 5 121. 5 112. 6 113. 1 114. 7 112. 6 113. 1 114. 8 117. 9 114. 8 117. 9 114. 8 111. 5 111. 6 111. 6 111. 5 111. 6 111. 6 11	1872 MA MJ JASONDO 1873 JFM AM JJ ASONDO 1874 JFM AM JJ ASOND 1875 JFM AM JJ JASOND 1875	110. 1 111. 1 113. 7 114. 3 114. 4 113. 5 112. 2 112. 7 114. 1 115. 5 117. 8 117. 8 117. 8 117. 8 117. 8 117. 8 117. 8 118. 4 119. 1 119. 1 110. 0 111. 4 112. 4 112. 4 112. 4 112. 4 112. 4 112. 4 112. 4 113. 1 110. 0 100. 7 110. 0 111. 7 110. 0 111. 7 111. 5 115. 5 117. 8 117. 8 118. 9 119. 1 119. 1	1875 AS OND 1876 1876 MAM J J AS OND 1877 1877 J FM AM J J AS OND 1878 1 FM AM J J AS OND 1878	113.5 8 115.8 116.4 7 113.9 112.5 111.9 112.5 111.9 112.5 111.9 112.5 111.9 112.5 110.0 0.7 109.7 109.1 100.5 100.

¹W. C. Mitchell—Gold, Prices and Wages under the Greenback Standard—pp. 5-13.

TABLE 19

AN UNADJUSTED ARITHMETIC AVERAGE INDEX NUMBER OF THE YIELDS IN Gold OF AMERICAN RATHROAD BONDS, MONTHLY, JANUARY 1857-JANUARY 1879.

- Col. 1. Index
- Col. 2. Logarithms of Index
- Col. 3. Cyclical Curve (logarithms)

For details of the nature of the graduation given in Column 3 of this table, see Appendix D.

 4 For the meaning of gold yield see Appendix C. The nature of this index of yields in gold is such that beginning with January 1879 it is identical with the index given in Table 10, column 4.

TABLE 19

AMERICAN RAILROAD BOND YIELDS UNADJUSTED ARITHMETIC INDEX—GOLD

Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)	Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)	Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)
1857 F M A M J A S O N D	8.173 8.102 8.107 8.124 8.195 8.436 8.393 8.502 9.563 10.295 9.519 9.043	.9086 .9089 .9098 .9136 .9261 .9239 .9295 .9806 1.0126	.9164 .9179 .9211 .9257 .9313 .9373 .9431 .9478 .9509 .9520 .9520 .9527 .9468	IS62 F M A M J A S O N D	6.193 5.996 5.881 5.725 5.594 5.701 6.491 6.277 6.388 6.925 6.986 7.123	.7919 .7779 .7695 .7578 .7477 .7560 .8123 .7978 .8054 .8054 .8404 .8442 .8527	.7788 .7743 .7719 .7724 .7760 .7831 .7935 .8062 .8205 .8353 .8494 .8617	1867 J F M A M J J A S O N D	9.589 9.840 9.693 9.823 9.962 10.036 10.063 10.181 10.424 10.547 10.343 10.001	.9865 .9922 .9984 1.0016 1.0027 1.0078 1.0180 1.0231	1.0005 .9996 .9990 .9987 .9987 .9095 1.0009 1.0029 1.0078 1.0102 1.0123
1858 F M A M 1 1 1 2 8 0 N D	8,715 8,171 7,838 7,773 7,660 7,570 7,505 7,471 7,346 7,113 6,992 6,940	.9123 .8942 .8906 .8842 .8791 .8754 .8734 .8661 .8521 .8446	.9403 .9314 .9205 .9082 .8954 .8713 .8616 .8538 .8482 .8445 .8424	1863 F M A M J J S O N D	7.564 8.402 8.121 8.189 8.042 7.765 6.918 6.585 7.188 8.081 8.232 8.567	.8788 .9244 .9096 .9132 .9054 .8901 .8400 .8186 .8566 .9075 .9155	.8717 .8789 .8832 .8850 .8848 .8835 .8821 .8818 .8839 .8895 .8996	1868 F M A M I A S O N D	10.186 10.358 10.196 10.201 10.245 10.506 10.781 10.741 10.314 10.200	1.0153 1.0084 1.0086 1.0105	1.0138 1.0148 1.0153 1.0154 1.0153 1.0150 1.0148 1.0148 1.0151 1.0159 1.0171 1.0188
1859 F M AM J ASOND	6.890 6.875 6.854 6.802 6.943 7.139 7.112 7.032 6.846 6.877 6.897	.8373 .8359 .8326 .8416	.8413 .8110 .8412 .8417 .8425 .8434 .8440 .8440 .8431 .8410 .8376 .8329	1864 F M A M J S O N D	8,973 9,148 9,263 9,677 9,944 11,927 14,043 13,915 12,925 12,533 14,067 14,011	.9529 .9613 .9668 .9857 .9976 1.0765 1.1475 1.1114 1.0981 1.1482 1.1465	.9352 .9599 .9880 .0176 1.0468 1.0735 1.0958 1.1124 1.1224 1.1257 1.1226 1.1141	1869 F M A M J J A S O N D	10.424 10.358 10.164 10.352 10.814 10.740 10.674 10.514 10.832 10.401 10.092 9.718	1.0180 1.0153 1.0071 1.0150 1.0340 1.0310 1.0283 1.0218 1.0347 1.0171	1.0208 1.0230 1.0249 1.0263 1.0268 1.0260 1.0236 1.0194 1.0136 1.0062 .9975 .9880
1860 F M A M J J A S O N D	6,803 6,712 6,631 6,506 6,327 6,158 6,067 6,012 6,009 6,043 6,387 6,729	.8327 .8269 .8216 .8133 .8012 .7894 .7830 .7790 .7788 .7813 .8053 .8280	.8271 .8207 .8142 .8080 .8025 .7980 .7945 .7922 .7910 .7911 .7923 .7946	1865 M A M J A S O N D	13,680 13,308 11,712 10,020 9,048 9,670 9,702 9,868 9,972 10,204 10,479 10,503	1.1361 1.1241 1.0686 1.0009 .9566 .9854 .9869 .9942 .9988 1.0088 1.0203 1.0213	1.1014 1.0856 1.0681 1.0500 1.0325 1.0167 1.0034 .9935 .9871 .9844 .9850 .9882	1870 J F M A M J A S O N D	9.621 9.219 8.467 8.554 8.641 8.769 8.954 8.758 8.758 8.738 8.561 8.480 8.397	.9832 .9647 .9277 .9322 .9366 .9254 .9430 .9520 .9409 .9325 .9284 .9241	.9782 .9683 .9590 .9505 .9432 .9372 .9327 .9294 .9274 .9264 .9261
1861 I F M A M I J A S O N	6.386 6.286 6.123 6.233 6.614 6.537 6.291 6.288 6.384 6.432 6.351 6.312	.8084	.7977 .8013 .8048 .8078 .8098 .8104 .8094 .8067 .7970 .7909 .7846	1866 F M A M J A S O N D	10.110 10.021 9.480 9.143 9.385 10.722 10.812 10.594 10.323 10.536 10.154 9.717	1.0048 1.0009 .9768 .9611 .9724 1.0303 1.0339 1.0251 1.0138 1.0227 1.0066 .9875	.9929 .9981 1.0028 1.0064 1.0083 1.0088 1.0082 1.0068 1.0051 1.0037 1.0024 1.0013	187I F M A M J A S O N D	8.344 8.371 8.316 8.265 8.308 8.385 8.385 8.385 8.350 8.541 8.571 8.437 8.177	.9199 .9172 .9195 .9238 .9235	.9263 .9262 .9259 .9252 .9242 .9230 .9217 .9205 .9195 .9186 .9178

TABLE 19-(Concluded)

American Railroad Bond Yields Unadjusted Arithmetic Index—Gold

Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)	Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)	Date	Data	Loga- rithms of data	Cyclica curve (loga- rithms)
1872 J F M A M J A S O N D	7.932 8.011 8.095 8.181 8.428 8.419 8.362 8.459 8.464 8.523 8.500	.8994 .9037 .9082 .9128 .9257 .9253 .9223 .9273 .9276 .9294 .9306 .9294	.9165 .9160 .9158 .9159 .9165 .9178 .9198 .9225 .9255 .9288 .9320 .9350	1875 J F M A M J J A S O N D	8.226 8.363 8.433 8.291 8.342 8.495 8.242 8.116 8.265 8.379 8.182 8.031	.9152 .9224 .9260 .9186 .9213 .9292 .9160 .9093 .9172 .9232 .9129 .9048	.9174 .9183 .9192 .9199 .9203 .9201 .9193 .9179 .9159 .9134 .9106 .9075	IS78 J F M A J J A S O N D	6.765 6.745 6.669 6.607 6.576 6.507 6.471 6.514 6.494 6.468 6.394 6.311	.8303 .8290 .8241 .8200 .8180 .8134 .8110 .8139 .8125 .8108 .8058	.8307 .8278 .8250 .8224 .8198 .8173 .8145 .8116 .8083 .8048 .8010 .7972
1873 F M A M J A S O N D	8.471 8.577 8.723 8.973 8.957 8.830 8.704 8.692 8.591 8.636 8.680 8.680	.9279 .9333 .9407 .9529 .9522 .9460 .9397 .9391 .9340 .9363 .9385 .9345	.9374 .9394 .9408 .9417 .9422 .9423 .9420 .9414 .9403 .9388 .9368 .9344	1876 JF M A M J A S O N D	7.887 7.857 7.892 7.825 7.825 7.832 7.790 7.658 7.568 7.568 7.563 7.541 7.483 7.374	.8969 .8953 .8972 .8935 .8939 .8915 .8841 .8790 .8787 .8774 .8741	.9043 .9009 .8975 .8940 .8905 .8870 .8836 .8803 .8770 .8739 .8709 .8679	1879 J F M A M J A S O N D	(see paper index)	(see paper index)	.7932 .7893 .7856 .7820 .7789 .7761 .7738 .7719 .7705 .7693 .7683 .7671
1874 F M A M J A S O N D	8.459 8.429 8.427 8.534 8.516 8.363 8.263 8.214 8.189 8.151 8.145 8.220	.9273 .9258 .9257 .9312 .9302 .9224 .9171 .9146 .9132 .9112 .9109 .9149	.9318 .9290 .9263 .9238 .9215 .9196 .9181 .9170 .9163 .9160 .9161 .9166	1877 J F M A M J A S O N D	7.185 7.116 7.177 7.316 7.330 7.111 7.047 7.048 6.911 6.896 6.875 6 835	.8564 .8522 .8559 .8643 .8651 .8519 .8480 .8481 .8395 .8386 .8373 .8347	.8651 .8623 .8595 .8569 .8542 .8516 .8488 .8460 .8431 .8400 .8369 .8337	1880 J F M A M J J A S O N D	(see paper index)	(see paper index)	.7658 .7640 .7618 .7590 .7557 .7519 .7478

TABLE 20

AN INDEX NUMBER OF THE GOLD PRICES OF AMERICAN RAILROAD COMMON STOCKS, JANUARY 1862-DECEMBER 1878

This index number was constructed by multiplying the monthly paper index figures (see Table 10) by the monthly average prices of greenbacks in gold (compare Table 18).

Col. 1. Index

Col. 2. Logarithms of Index

Col. 3. Cyclical Curve (logarithms)

For details of the nature of the graduation given in Column 3 of this table, see Appendix D.

TABLE 20

Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)	Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)	Date	Data	Loga- rithms of data	Cyclica curve (loga- rithms)
1860 J F M A M J A S O N D	(see paper index)	(see paper index)	1.2441 1.2475 1.2488 1.2476 1.2439 1.2379	1865 J F M A M J A S O N	15.25 15.66 16.77 19.35 21.66 20.58 21.17 20.72 21.51 21.87	1.183 1.195 1.225 1.287 1.336 1.313 1.326 1.316 1.333 1.340 1.339 1.335	1.2042 1.2186 1.2364 1.2561 1.2761 1.2952 1.3121 1.3268 1.3369 1.3436 1.3436 1.3436	1870 F M A M J A S O N D	31.37 32.89 34.68 35.06 35.94 36.80 34.47 33.53 34.74 35.53 35.77	1.497 1.517 1.540 1.545 1.556 1.566 1.537 1.525 1.541 1.551 1.556 1.554	1.5076 1.5149 1.5221 1.5288 1.5350 1.5405 1.5454 1.5495 1.5559 1.5556 1.5556
1861 JF M AM J JASOND	(see paper index)	(see paper index)	1.2302 1.2212 1.2119 1.2034 1.1963 1.1912 1.1886 1.1884 1.1904 1.1943 1.1907 1.2061	1866 J F M A M J A S O N D	21.56 21.29 22.63 23.60 23.26 20.87 20.85 22.04 22.64 22.88 23.25 23.99	1.334 1.328 1.355 1.373 1.367 1.320 1.319 1.343 1.355 1.359 1.366 1.380	1.3471 1.3461 1.3453 1.3449 1.3455 1.3468 1.3531 1.3531 1.3550 1.3565 1.3577	1871 F M A M J A SO ND	35.86 35.98 36.91 38.01 38.57 37.99 37.30 37.54 37.00 35.54 36.48	1,355 1,556 1,567 1,580 1,580 1,572 1,574 1,568 1,551 1,562 1,578	1.5609 1.5622 1.5634 1.5650 1.5667 1.5667 1.5707 1.5729 1.5751 1.5772 1.5772
I 862 F M A M J J A S O N D	16.14 16.54 17.33 17.25 18.06 16.28 16.97 17.58 17.81 17.61 17.81	1.208 1.219 1.239 1.237 1.249 1.257 1.212 1.230 1.245 1.251 1.246 1.250	1.2130 1.2197 1.2257 1.2306 1.2340 1.2360 1.2368 1.2370 1.2374 1.2385 1.2459	1867 J F M A M J J A S O N D	23.41 22.73 22.98 22.35 22.40 23.07 23.57 23.45 22.99 22.94 23.49	1.369 1.357 1.361 1.349 1.350 1.363 1.372 1.370 1.362 1.361 1.371 1.393	1.3585 1.3592 1.3598 1.3605 1.3615 1.3628 1.3646 1.3671 1.3703 1.3741 1.3783 1.3829	1872 J F M A M J A S O N D	38.78 38.59 39.83 40.68 39.63 39.67 38.67 38.08 37.91 37.92 37.81	1.589 1.586 1.600 1.609 1.598 1.592 1.587 1.581 1.579 1.579 1.578 1.578	1.5829 1.5846 1.5863 1.5878 1.5892 1.5905 1.5913 1.5918 1.5918 1.5908 1.5893 1.5893
1863 F M A M J A SOND	18.33 17.15 17.49 18.06 20.13 20.07 22.74 25.27 23.71 22.13 22.15	1.263 1.234 1.243 1.257 1.303 1.357 1.403 1.375 1.345	1.2529 1.2621 1.2735 1.2869 1.3017 1.3172 1.3326 1.3466 1.3581 1.3657 1.3684 1.3652	1868 J F M A M J A S O N D	24.91 24.96 25.18 25.17 25.86 26.21 25.74 24.97 25.52 27.13 26.90 27.29	1.401 1.401 1.413 1.418 1.411 1.397	1.3876 1.3921 1.3964 1.4005 1.4046 1.4129 1.4176 1.4226 1.4279 1.4334 1.4388	1873 F M AM J ASOND	39.25 39.24 38.47 37.07 37.17 37.20 37.33 37.26 35.25 33.43 32.34	1.594 1.594 1.585 1.569 1.570 1.571 1.572 1.571 1.542 1.510 1.542	1.5846 1.5815 1.5780 1.5742 1.5702 1.5659 1.5616 1.5573 1.5532 1.5494 1.5464
1864 J F M A M J A S O N D	21.77 22.39 23.33 22.40 20.97 17.90 14.45 14.82 15.90 16.01 14.93 15.22	1.350 1.368 1.350 1.322 1.253 1.160 1.171 1.201	1.3561 1.3414 1.3219 1.2992 1.2750 1.2512 1.2295 1.2115 1.1985 1.1911 1.1897 1.1943	1869 J F M A M J J A S O N D	28.18 28.66 29.13 29.25 29.14 29.66 30.04 30.87 28.33 29.52 30.22 30.88	1.440 1.457 1.464 1.466 1.466 1.472 1.478 1.490 1.452 1.470 1.450	1.4440 1.4488 1.4532 1.4574 1.4614 1.4654 1.4698 1.4747 1.4802 1.4863 1.4931 1.5002	1874 F M A M J J A S O N D	36.20 36.95 36.33 34.94 34.35 34.41 35.65 35.45 35.45 35.22 35.03	1.568 1.560 1.543 1.536 1.537 1.542 1.542 1.552 1.550	1.5428 1.5424 1.5430 1.5441 1.5456 1.5472 1.5484 1.5489 1.5487 1.5484 1.5484 1.5484 1.5484

TABLE 20—(Concluded)

American Railroad Stock Prices—Gold

Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)	Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)	Date	Data	Loga- rithms of data	Cyclical curve (loga- rithms)
1875 J F M A M J A S O N D	35.04 34.28 34.33 34.89 33.08 32.13 32.83 33.30 32.33 31.70 32.60 32.82	1.545 1.535 1.536 1.543 1.520 1.507 1.516 1.522 1.510 1.501 1.513 1.513	1.5390 1.5351 1.5311 1.5274 1.5241 1.5215 1.5197 1.5187 1.5183 1.5184 1.5188 1.5192	1877 J F M A M J J A S O N D	28.47 26.91 25.81 23.62 23.37 22.39 23.15 24.72 26.81 27.71 27.21 27.09	1.454 1.430 1.412 1.373 1.369 1.350 1.365 1.393 1.428 1.443 1.435 1.435	1.4218 1.4111 1.4028 1.3969 1.3934 1.3922 1.3931 1.4010 1.4074 1.4153 1.4239	1879 J F M A M J A S O N D	(see paper index)	(see paper index)	1.4879 1.4959 1.5058 1.5176 1.5311 1.5460 1.5616 1.5773 1.5923 1.6059 1.6178 1.6278
1876 F M A M J A S O N D	33.92 34.28 34.14 33.17 31.91 31.65 31.49 30.25 28.82 28.63 28.17 28.29	1.530 1.535 1.533 1.521 1.504 1.500 1.498 1.481 1.460 1.457 1.450 1.452	1.5193 1.5190 1.5179 1.5156 1.5117 1.5060 1.4980 1.4879 1.4758 1.4623 1.4482 1.4344	1878 J F M A M J J A S O N D	27,26 26,73 27,42 28,44 29,15 29,76 29,41 30,08 20,76 29,74 29,66	1.427 1.438 1.454 1.454 1.465	1.4326 1.4408 1.4481 1.4540 1.4586 1.4620 1.4647 1.4670 1.4695 1.4725 1.4765 1.4814	1880 F M A M J A S O N D	(see paper index)	(see paper index)	1.6359 1.6424

TABLE 21

CALL MONEY RATES AT THE NEW YORK STOCK EXCHANGE

Monthly Averages, January 1857 - January 1936

- Col. 1. Logarithms of Data Adjusted for Seasonal Fluctuations.
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).
- Col. 5. Changing Seasonal Fluctuations (logarithms).

For details of the nature of the graduations given in Columns 2 and 3 and of the seasonal given in Column 5 of this table, see Appendix D

TABLE 21

CALL MONEY RATES

Date	1	2	3	4	5	Date	1	2	3	4	5
1857 IF M M JASOND	.874 .927 .969 .936 .906 .876 .860 .985 1.122 1.225 .880 .823	.8813 .9040 .9279 .9501 .9682 .9798 .9828 .9763 .9604 .9351 .9012 .8603	.8353 .8300 .8249 .8159 .8150 .8099 .8051 .8004 .7958 .7913 .7869 .7828	+.0460 +.0740 +.1030 +.1302 +.1532 +.1699 +.1777 +.1759 +.1646 1438 +.1143 +.0775	+.029 +.015 003 039 036 031 007 +.054 +.030 +.023 +.022	I862 J F M A M J A S O N D	.775 .776 .734 .759 .689 .653 .756 .639 .640 .642 .757	.7523 .7427 .7320 .7212 .7109 .7022 .6963 .6935 .6942 .6989 .7072 .7187	.7596 .7616 .7636 .7636 .7652 .7672 .7686 .7700 .7711 .7720 .7728 .7736 .7743	0073 0189 0316 0443 0563 0664 0737 0778 0778 0664 0556	019026040024037007 +.021 +.042
1858 J F M A M J A S O N D	.783 .676 .650 .663 .573 .572 .555 .575 .525 .525 .577	.8136 .7629 .7113 .6616 .6170 .5808 .5558 .5434 .5433 .5547 .5752	.7788 .7749 .7712 .7643 .7611 .7581 .7552 .7524 .7499 .7473 .7449	+.034801200599106114731803202321182091195217211434	+.030 +.012 003 040 029 050 028 011 +.040 +.025 +.025	1863 J F M A M J A S O N D	.745 .801 .775 .721 .757 .827 .811 .826 .830 .791 .800	.7325 .7477 .7625 .7756 .7865 .7943 .7991 .8018 .8032 .8040 .8051 .8071	.7748 .7753 .7758 .7763 .7768 .7772 .7776 .7781 .7786 .7790 .7794 .7798	0423 0276 0133 0007 +.0097 +.0171 +.0215 +.0237 +.0250 +.0250 +.0257	+.040 002 +.010 005 033 042 016 016 +.022 +.045 +.051
I I I I I I I I I I I I I I I I I I I	.603 .689 .659 .693 .792 .820 .772 .820 .749 .758 .691	.6308 .6605 .6884 .7132 .7344 .7512 .7632 .7706 .7735 .7723 .7682 .7626	.7427 .7406 .7387 .7367 .7349 .7332 .7316 .7301 .7286 .7275 .7264 .7253	1119 0801 0503 0235 0005 +.01800 +.0316 +.0405 +.0449 +.0448 +.0418 +.0373	+.031 +.010 002 040 023 045 025 015 +.026 +.022 +.029 +.027	1864 F M A M J A S O N D	.802 .792 .756 .824 .788 .872 .866 .903 .855 .807 .793	.8099 .8135 .8176 .8216 .8250 .8274 .8285 .8279 .8256 .8217 .8163 .8096	.7801 .7802 .7803 .7804 .7803 .7804 .7800 .7796 .7792 .7784 .7776 .7767 .7757	+.0298 +.0333 +.0373 +.0412 +.0447 +.0489 +.0487 +.0472 +.0441 +.0396 +.0339	
1860 F M AM J ASOND	.791 .761 .740 .756 .746 .719 .742 .771 .800 .809 .819	.7569 .7523 .7499 .7501 .7527 .7571 .7627 .7683 .7729 .7761 .7776	.7242 .7237 .7232 .7228 .7226 .7228 .7232 .7237 .7246 .7246 .7258 .7272 .7287	+.0327 +.0286 +.0267 +.0273 +.0343 +.0395 +.0446 +.0483 +.0504 +.0504	+.034 +.008 .000 036 021 042 022 020 +.013 +.020 +.034 +.034	1865 JF M A M J A S O N D	.800 .795 .824 .723 .781 .743 .783 .854 .783 .810 .787	.8023 .7952 .7888 .7840 .7810 .7805 .7816 .7823 .7814 .7717	.7746 .7735 .7724 .7714 .7703 .7695 .7686 .7679 .7673 .7669 .7667	+.0277 +.0217 +.0164 +.0126 +.0107 +.0105 +.0119 +.0137 +.0145 +.0114 +.0051	
1861 J F M A M J A S O N D	.724 .735 .757 .740 .817 .781 .762 .681 .759 .793 .775 .777	.7753 .7728 .7700 .7676 .7662 .7661 .7666 .7676 .7682 .7675 .7647 .7597	.7304 .7325 .7347 .7371 .7394 .7420 .7416 .7472 .7498 .7524 .7548 .7574	+.0449 +.0403 +.0353 +.0353 +.0268 +.0241 +.0220 +.0204 +.0184 +.0151 +.0099 +.0023	+.036 +.005 +.003 030 021 041 022 028 +.001 +.020 +.038 +.036	1866 J F M A M J J A S O N D	.692 .797 .717 .690 .788 .751 .748 .719 .620 .594 .734 .708	.7629 .7520 .7403 .7289 .7192 .7117 .7071 .7056 .7065 .7099 .7150 .7214	.7669 .7674 .7681 .7690 .7701 .7715 .7729 .7746 .7767 .7786 .7807 .7832	0040 0154 0278 0401 0509 0598 0658 0690 0702 0687 0657	+.048 015 +.028 +.041 056 063 103 +.002 +.044 +.044

TABLE 21-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1867 J F M A M J A S O N D	.805 .784 .749 .734 .745 .868 .730 .748 .741 .979 .819 .697	.7287 .7376 .7478 .7589 .7708 .7823 .7919 .7983 .8014 .8004 .7958 .7898	.7860 .7884 .7909 .7936 .7964 .7989 .8014 .8039 .8067 .8089 .8113 .8135	-,0573 -,0508 -,0431 -,0347 -,0256 -,0166 -,0055 -,0056 -,0053 -,0055 -,0155 -,0237	+.051 020 +.033 +.058 064 076 077 120 +.010 +.053 +.040 +.116	IS72 F M A M J A S O N D	.868 .861 .874 1.025 .874 .796 .726 .756 1.002 .720 .838 1.108	.8347 .8472 .8545 .8588 .8599 .8591 .8581 .8590 .8631 .8724 .8888 .9120	.8312 .8301 .8286 .8269 .8247 .8227 .8203 .8176 .8146 .8115 .8080 .8043	+ .0035 + .0171 + .0259 + .0319 + .0352 + .0364 + .0414 + .0485 + .0609 + .0808 + .1077	+.07 02 +.05 +.11 08 14 16 17 +.01 +.08 +.05 +.19
1868 J F M A M J A S O N D	.698 .695 .933 .988 .811 .632 .710 .711 .671 .896 1.195	.7834 .7770 .7727 .7718 .7736 .7794 .7906 .8071 .8293 .8582 .8924 .9292	.8157 .8175 .8194 .8299 .8223 .8234 .8244 .8252 .8257 .8260 .8262 .8260	0323 0405 0467 0491 0487 0440 0338 0181 +.0036 +.0322 +.0662 +.1032	+.054 024 +.038 +.074 071 088 092 137 +.017 +.060 +.036 +.136	1873 F M A M I I A S O N D	.775 1.028 1.068 1.328 1.328 8.66 818 .760 .839 1.788 1.080 .912 .701	.9407 .9729 1.0047 1.0304 1.0474 1.0526 1.0435 1.0210 .9875 .9447 .8949 .8406	.8004 .7959 .7912 .7861 .7805 .7747 .7683 .7611 .7534 .7453 .7370 .7284	+.1403 +.1770 +.2135 +.2443 +.2669 +.2779 +.2752 +.2599 +.2341 +.1579 +.1122	+.08 01 +.05 +.11 08 15 17 00 +.09 +.00
1869 F M A M J A S O N D	1.022 .855 .913 .900 .905 1.475 1.100 .957 1.270 .683 .762	.9664 1.0003 1.0266 1.0422 1.0463 1.0379 1.0172 .9870 .9501 .9084 .8655 .8248	.8256 .8252 .8246 .8238 .8230 .8219 .8211 .8203 .8195 .8188 .8183 .8178	+.1408 +.1751 +.2020 +.2184 +.2233 +.2160 +.1961 +.1667 +.1306 +.0896 +.0472 +.0070	+.058 026 +.042 +.088 076 101 109 152 +.021 +.068 +.034 +.157	IS74 F M A M J A S O N D	.651 .626 .543 .508 .576 .558 .628 .506 .449 .370 .405	.7829 .7232 .6637 .6064 .5540 .5088 .4741 .4499 .4356 .4296 .4298 .4328	.7194 .7099 .7004 .6907 .6805 .6705 .6604 .6502 .6395 .6294 .6193	+.0635 +.0133 0367 0843 1265 1617 1863 2003 2039 1895 1763	+.08 01 +.05 +.11 08 16 16 16 +.07 +.07 +.19
ISTO F M A M J A S O N D	.729 .766 .667 .652 .738 .737 .830 .837 .719 .645 .706	.7881 .7579 .7361 .7231 .7182 .7197 .7251 .7310 .7339 .7315 .7230 .7088	.8175 .8176 .8177 .8181 .8187 .8197 .8207 .8218 .8229 .8241 .8256 .8269	0294 0597 0816 0950 1005 1000 0956 0908 0890 0926 1026 1181	+.063 026 +.045 +.099 079 114 126 165 +.021 +.075 +.034 +.176	1875 F M A M I J A S O N D	.344 .405 .533 .441 .517 .535 .595 .497 .404 .421 .521	.4371 .4419 .4472 .4544 .4647 .4788 .4944 .5106 .5249 .5351 .5396	.5988 .5892 .5794 .5699 .5698 .5522 .5437 .5357 .5280 .5211 .5146 .5086	1617 1473 1322 1155 0961 0734 0493 0251 0031 +.0140 +.0250 +.0314	+.09 00 +.00 +.10 10 15 03 +.09 +.18
1871 F M A M J A S O N D	.743 .640 .575 .658 .631 .606 .657 .619 .628 1.010 .764 .822	.6913 .6742 .6608 .6539 .6551 .6656 .6844 .7091 .7375 .7670 .7937	.8282 .8296 .8307 .8317 .8324 .8331 .8335 .8336 .8337 .8334 .8328 .8322	1369 1554 1699 1778 1675 1491 1245 0962 0664 0391 0157	+.069 024 +.048 +.108 081 129 145 172 +.019 +.082 +.039 +.189	1876 J F M A M J A S O N D	.667 .564 .503 .472 .582 .575 .373 .330 .377 .496	.5365 .5305 .5233 .5159 .5084 .5004 .4915 .4816 .4707 .4600 .4512 .4459	.5032 .4984 .4942 .4909 .4888 .4866 .4857 .4856 .4861 .4873 .4891	+.0333 +.0321 +.0250 +.0196 +.0138 +.0058 0040 0154 0273 0379 0457	+.09 00 +.07 +.09 07 16 20 14 +.10 +.18 +.17

TABLE 21-Continued

Date	1	2	3	4	.5	Date	1	2	3	4	5
1877 JF M AM JJ AS OND	.633 .522 .390 .481 .465 .408 .448 .660 .678 .685 .635	.4461 .4529 .1666 .4866 .5116 .5400 .5697 .5988 .6258 .6490 .6668 .6776	.4945 .4979 .5019 .5068 .5121 .5178 .5237 .5296 .5355 .5418 .5482	0484 0450 0353 0202 0005 +.0222 +.0460 +.0692 +.0903 +.1072 +.1186 +.1232	+.097 002 +.078 +.086 076 165 205 129 044 +.100 +.165	1882 J F M A M J J S O N D	.705 .677 .587 .574 .536 .656 .641 .649 .861 .672 .804	.6229 .6212 .6245 .6314 .6409 .6521 .6654 .6806 .6969 .7121 .7236	.6644 .6572 .6491 .6402 .6308 .6204 .6098 .5985 .5871 .5747 .5623	- 0415 - 0360 - 0246 - 0088 + 0101 + 0317 + 0556 + 0821 + 1374 + 1374 + 14782	+.030 024 +.080 +.035 059 105 164 052 001 +.068 +.088
1878 F M A M J A S O N D	.900 .681 .604 .713 .617 .568 .446 .371 .408 .602 .481	.6803 .6740 .6583 .6336 .6012 .5644 .5267 .4926 .4664 .4520 .4511 .4643	.5607 .5669 .5728 .5787 .5842 .5897 .5949 .5998 .6044 .6090 .6136	+.1196 +.1071 +.0855 +.0858 +.0170 0253 0682 1072 1380 1570 1625 1538	+.089 004 +.084 +.078 073 160 203 113 044 +.097 +.100 +.151	1883 F M A A M J A S O N D	.634 .649 .948 .758 .606 .389 .481 .439 .371 .366 .217	.7210 .7007 .6670 .6211 .5672 .5110 .4579 .4125 .3798 .3612 .3559 .3610	.5372 .5248 .5121 .4996 .4871 .4748 .4632 .4527 .4429 .4333 .4246 .4167	+.1838 +.1759 +.1549 +.1215 +.0801 +.0362 0053 0402 0631 0721 0687 0557	+.019 033 +.068 +.024 056 088 153 041 +.0165 +.084 +.113
1879 FM AM J ASOND	.407 .492 .566 .575 .651 .670 .667 .990 .779 .999 .839	.4902 .5261 .5692 .6158 .6625 .7066 .7451 .7752 .7951 .8026 .7973 .7802	.6227 .6273 .6317 .6363 .6454 .6454 .6588 .6544 .6588 .6631 .6673	1325 1012 0625 0205 +.0217 +.0612 +.0953 +.1208 +.1363 +.1395 1300 +.1088	+.077006 +.087 +.068070150197095039 +.092 +.102 +.141	M A J J A	.274 .318 .191 .307 1.231 .608 .419 .276 .212 .227 .077	.3741 .3902 .4044 .4141 .4162 .4085 .3901 .3616 .3235 .2790 .2326 .1884	.4092 .4027 .3968 .3916 .3869 .3831 .3797 .3767 .3746 .3732 .3721 .3713	0351 0125 +.0076 +.0225 +.0293 +.0254 +.0104 0151 0942 1395 1829	+.005 044 +.052 +.015 055 071
1880 F M AM J ASOND	.639 .677 .774 .759 .675 .614 .584 .476 .462 .375 .683	.7533 .7200 .6848 .6526 .6268 .6101 .6037 .6069 .6178 .6345 .6352	.6753 .6791 .6826 .6859 .6857 .6915 .6938 .6959 .6971 .7002	+.0780 +.040 ³ +.0022 0333 0619 0814 0901 0890 0800 0646 0450 0237	+.060 011 +.088 +.057 066 137 186 078 031 +.084 +.099 +.130	F M A M J J	.077 .212 .033 .125 .212 .134 .260 .204 .145 .265 .350 .323	.1507 .1235 .1098 .1090 .1199 .1403 .1669 .1961 .2263 .2569 .2874	.3709 .3711 .3717 .3729 .3746 .3767 .3792 .3817 .3844 .3876 .3912 .3951	-,2202 -,2476 -,2619 -,2639 -,2547 -,2364 -,2123 -,1856 -,1581 -,1307 -,1038 -,0761	001 054 +.034 +.005 054 058 130 028 +.043 +.063
1881 F M A M J A S O N D	.637 1.220 .789 .600 .592 .619 .712 .731 .739 .661 .622 .657	.6994 .7198 .7360 .7460 .7484 .7425 .7283 .7084 .6856 .6632 .6439	.7012 .7012 .7006 .6995 .6979 .6956 .6931 .6901 .6863 .6820 .6771	0018 +.0186 +.0354 +.0465 +.0505 +.0469 +.0352 +.0183 0007 0188 0332 0410	+.045 018 +.085 +.047 063 121 175 064 019 +.075 +.094 +.121	1886 J F M A M J A S	.333 .380 .407 .379 .513 .576 .471 .750 .713 .639 .671	.3528 .3885 .4254 .4633 .5013 .5380 .5731 .6071 .6391 .6687 .6956 .7192	.3998 .4043 .4094 .4149 .4269 .4334 .4403 .4473 .4547 .4620 .4697	0470 0158 +.0160 +.0484 +.0804 +.1111 +.1397 +.1668 +.1918 +.2140 +.2336 +.2495	005 066 +.016 002 054 051 119 025 +.058 +.065 +.119

TABLE 21—Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
ISST F M A M J A S O N D	.628 .628 .701 .794 .765 .907 .788 .736 .642 .554 .581	.7381 .7524 .7616 .7654 .7634 .7559 .7419 .7205 .6913 .6545 .6104	.4777 .4856 .4937 .5017 .5097 .5177 .5257 .5336 .5411 .5488 .5559 .5627	+ 2604 + 2668 + 2679 + 2637 + 2537 + 2382 + 2162 + 1869 + 1502 + 1057 + 0545 - 0015	006 077 +.002 007 055 050 111 024 +.068 +.068 +.068	J S O N D	.376 .385 .297 .305 .244 .233 .368 .350 .525 .665 .630 .736	.3693 .3476 .3319 .3245 .3271 .3413 .3693 .4112 .4661 .5309 .6013 .6707	.5487 .5391 .5287 .5178 .5067 .4947 .4831 .4715 .4597 .4485 .4367 .4251	1794 1915 1968 1933 1796 1534 1138 0603 +.0064 +.1646 +.2456	+.004 084 +.004 068 087 094 038 +.091 +.082 +.097
1888 JF M A M J A S O N D	.572 .517 .445 .430 .312 .228 .263 .214 .373 .343 .323 .497	.5101 .4601 .4145 .3763 .3474 .3279 .3177 .3166 .3233 .3371 .3582 .3861	.5689 .5747 .5803 .5855 .5901 .5942 .5975 .6003 .6028 .6044 .6056	0588 1146 1658 2092 2427 2663 2798 2837 2795 2673 2474 2203	005 086 006 010 057 052 105 024 +.076 +.072 +.085 +.119	IS93 F M A M J J A S O N D	.596 .556 .897 .683 .624 1.048 .985 .789 .481 .290 .152 031	.7309 .7753 .7988 .7977 .7724 .7259 .6618 .5849 .5004 .4117 .3217 .2341	.4136 .4027 .3924 .3826 .3731 .3642 .3559 .3479 .3404 .3336 .3272 .3216	+.3173 +.3726 +.4064 +.4151 +.3993 +.3617 +.3059 +.2370 +.1600 +.0781 0055 0875	+.006 079 +.017 +.005 068 100 049 +.093 +.087 +.087 +.078
1889 JF MAM JASOND	.523 .453 .495 .601 .467 .535 .650 .614 .600 .842 .765 .787	.4194 .4572 .4976 .5374 .5745 .6079 .6365 .6606 .6821 .7024 .7215 .7402	.6067 .6067 .6063 .6056 .6042 .6033 .6021 .6011 .6002 .5996 .5991	1873 1495 1087 0682 0297 +.0046 +.0344 +.0595 +.0819 +.1028 +.1224 +.1413	004 089 009 012 060 058 100 025 +.082 +.077 +.088 +.116	1894 J F M A M J A S O N D	001 .075 .012 .037 .106 .113 .099 .061 092 088 063	.1528 .0812 .0233 0165 0367 0383 0238 .0018 .0315 .0600 .0842 .1025	.3164 .3119 .3077 .3038 .3003 .2974 .2946 .2920 .2898 .2877 .2858 .2843	- 1636 - 2307 - 2844 - 3203 - 3370 - 3184 - 2902 - 2583 - 2277 - 2016 - 1818	
1890 JF MAM JASOND	.888 .718 .638 .645 .752 .743 .759 1.094 .743 .618 .756 .590	.7580 .7727 .7826 .7873 .7855 .7771 .7637 .7637 .7257 .7033 .6804 .6565	.5990 .5994 .5999 .6006 .6016 .6026 .6036 .6047 .6056 .6063 .6067	+.1590 +.1733 +.1827 +.1867 +.1839 +.1745 +.1601 +.1201 +.0970 +.0737 +.0498	002 090 010 012 064 066 096 028 +.086 +.081 +.089 +.109	1895 F M AM J A SOND	.116 .249 .322 .325 .181 .188 .249 .087 .103 .248 .217 .556	.1165 .1294 .1442 .1623 .1847 .2103 .2370 .2639 .2915 .3205 .3527 .3901	.2828 .2812 .2798 .2787 .2778 .2768 .2761 .2756 .2754 .2756 .2759 .2766	1663 1518 1356 1164 0931 0665 0391 0117 +.0161 +.0768 +.1135	
ISO1 J F M A M J I A S O N D	.590 .546 .466 .529 .707 .587 .437 .359 .564 .554 .367	.6327 .6101 .5887 .5684 .5498 .5320 .5137 .4938 .4718 .4473 .4210 .3943	.6063 .6055 .6039 .6017 .5991 .5956 .5914 .5864 .5803 .5733 .5659	+.0264 +.0046 0152 0333 0493 0636 0777 0926 1085 1260 1449 1635	+.001 087 007 010 066 075 031 +.089 +.084 +.087 +.101	F M A M J A S O N D	.671 .671 .511 .443 .457 .421 .423 .760 .649 .961 .716	.4330 .4793 .5257 .5673 .5982 .6144 .6145 .5979 .5666 .5248 .4762 .4238	.2776 .2791 .2811 .2836 .2870 .2903 .2945 .2992 .3042 .3098 .3156 .3214	+.1554 +.2002 +.2446 +.2837 +.3112 +.3241 +.3200 +.2987 +.2624 +.2150 +.1606 +.1024	

TABLE 21—Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
J F M A M J A S O N D	.227 .292 .176 .131 .198 .219 .189 .202 .263 .313 .170	.3712 .3213 .2758 .2377 .2095 .1928 .1886 .1969 .2155 .2404 .2673 .2920	.3280 .3341 .3409 .3479 .3550 .3614 .3680 .3744 .3808 .3862 .3916 .3967	+.0432 0128 0651 1102 1455 1686 1794 1775 1653 1458 1243 1047	+.023 080 +.034 +.045 049 140 113 105 +.083 +.085 +.088 +.134	1902 J F M A M J J A S O N D	.602 .495 .577 .676 .792 .602 .683 .760 .991 .811 .536	.5914 .6003 .6154 .6351 .6583 .6824 .7043 .7208 .7300 .7298 .7204 .7032	.5721 .5667 .5609 .5550 .5429 .5365 .5305 .5243 .5127 .5071	+.0193 +.0336 +.0545 +.0801 +.1093 +.1395 +.1678 +.1903 +.2057 +.2113 +.2077 +.2113	+.05: 11: +.01: +.03: 04: 14: 13: 18: +.04: +.07: +.15: +.26:
1898 J F M A M J A S O N D	.368 .340 .302 .422 .334 .242 .215 .355 .501 .268 .223 .221	.3108 .3218 .3254 .3230 .3170 .3106 .3062 .3057 .3112 .3242 .3455 .3756	.4014 .4054 .4094 .4129 .4160 .4189 .4216 .4241 .4269 .4294 .4322 .4352	0906 0836 0840 0899 0990 1083 1154 1184 1157 1052 0867 0596	+.030 090 +.034 +.051 044 145 118 125 +.076 +.084 +.079 +.161	I 1903 F M A M J A S O N D	.694 .576 .765 .601 .442 .630 .536 .495 .336 .362 .352	.6795 .6521 .6238 .5959 .5688 .5431 .5179 .4918 .4639 .4334 .3999	.5020 .4970 .4925 .4886 .4850 .4819 .4772 .4772 .4743 .4737 .4739	+ .1775 + .1551 + .1313 + .1073 + .0838 + .0612 + .0386 + .0146 0117 0409 0738 1102	+.06 11 +.01 +.02 05 14 13 18 +.02 +.06 +.16
1899 F M A M J A S O N D	.398 .494 .582 .656 .589 .567 .773 .659 .736 .793 .770 .859	.4144 .4611 .5137 .5689 .6229 .6709 .7085 .7323 .7401 .7309 .7063	.4384 .4422 .4459 .4500 .4543 .4595 .4648 .4704 .4765 .4830 .4898 .4971	0240 +.0189 +.0678 +.1189 +.1686 +.2114 +.2437 +.2636 +.2479 +.2165 +.1716	+.037 101 +.031 +.054 042 147 123 144 +.069 +.082 +.111 +.188	1904 J F M A M J J A S O N D	.296 .368 .234 .131 .256 .194 .151 .142 .167 .243 .213	.3263 .2896 .2553 .2261 .2042 .1901 .1849 .1887 .2003 .2189 .2440	.4748 .4760 .4777 .4796 .4822 .4853 .4886 .4924 .4965 .5009 .5057	1485 1864 2224 2535 2780 2952 3037 3037 2962 2820 2820	+.07 11 +.00 +.00 06 14 13 18 +.01 +.06 +.16
1900 JFM AM JASOND	.573 .464 .568 .435 .342 .376 .313 .275 .146 .473 .580	.6207 .5664 .5101 .4561 .4082 .3706 .3462 .3368 .3431 .3644 .3974 .4384	.5048 .5121 .5200 .5279 .5359 .5436 .5509 .5580 .5649 .5709 .5766 .5817	+.1159 +.0543 0099 0718 1277 1730 2047 2212 2218 2065 1792 1433	+.045 112 +.028 +.051 041 148 128 161 +.061 +.080 +.124 +.216	1905 J F M A M J A S O N D	.272 .440 .501 .513 .460 .534 .501 .497 .544 .660 .715	.3095 .3486 .3912 .4360 .4818 .5276 .5713 .6115 .6477 .6795 .7064	.5153 .5203 .5253 .5304 .5356 .5407 .5456 .5502 .5549 .5593 .5635 .5676	2058 1717 1341 0944 0538 0131 +.0257 +.0613 +.1202 +.1202 +.1429 +.1624	+.08 10 +.00 07 13 13 +.00 +.06 +.17 +.30
1901 J F M A M J J A S O N D	.435 .418 .346 .590 .881 .783 .766 .561 .585 .473 .482 .552	.4830 .5258 .5623 .5904 .6088 .6174 .6181 .6055 .5972 .5911 .5886	.5859 .5891 .5917 .5935 .5944 .5930 .5912 .5888 .5853 .5816 .5771	1029 0633 0294 0031 +.0144 +.0233 +.0251 +.0222 +.0167 +.0119 +.0095 +.0115	+.052 117 +.023 +.043 043 149 133 174 +.052 +.077 +.140 +.244	M M J A S	.852 .753 .690 .992 .703 .642 .605 .827 .971 .647 .703 .842	.7512 .7697 .7850 .7962 .8015 .7987 .7877 .7691 .7449 .7192 .6967 .6804	.5715 .5751 .5785 .5816 .5844 .5869 .5892 .5910 .5927 .5938 .5948	+ .1797 + .1946 + .2065 + .2146 + .2171 + .2118 + .1781 + .1781 + .1522 + .1019 + .0850	

TABLE 21—Continued

Date	i	2	3	4	5	Date	1	2	3	4	.5
907 JFM AM JJASOND	.703 .715 .815 .395 .453 .619 .784 .655 .605 1.256 .917 .868	.6724 .6742 .6842 .6988 .7153 .7308 .7416 .7452 .7407 .7257 .6986 .6591	.5954 .5952 .5942 .5942 .5926 .5904 .5874 .5838 .5798 .5758 .5699 .5639	+ .0770 + .0790 + .0900 + .1062 + .1249 + .1434 + .1578 + .1654 + .1558 + .1347 + .1019	+.086 074 010 024 086 123 126 169 003 +.066 +.171 +.296	1912 F M A M J A S O ND	.362 .418 .429 .521 .500 .509 .524 .533 .654 .654 .685	.3967 .4143 .4378 .4963 .5270 .5552 .5788 .5961 .6064 .6101	.4766 .4799 .4828 .4853 .4871 .4884 .4890 .4890 .4892 .4873 .4856 .4837	0799 0656 0450 0195 +.0092 +.0386 +.0662 +.0898 +.1079 +.1191 +.1245 +.1239	+.02 06 04 04 06 07 06 08 +.01 +.07 +.12 +.18
908 FM AM JASOND	.506 .324 .286 .269 .311 .296 .201 .178 .134 .089 .079 .185	.6072 .5429 .4694 .3919 .3153 .2458 .1895 .1509 .1310 .1298 .1449 .1719	.5495 .5416 .5329 .5239 .5145 .5051 .4951 .4853 .4758 .4659 .4565 .4476	+ .0577 + .0013 0635 1320 1992 2593 3056 3344 3448 3361 3116 2757	+.081 066 019 033 091 114 115 153 004 +.069 +.164 +.277	1913 F M A M J A S O N D	.476 .579 .669 .576 .490 .415 .395 .415 .442 .487 .467	.6000 .5882 .5727 .5529 .5292 .5017 .4711 .4401 .4118 .3892 .3753 .3720	.4810 .4787 .4757 .4757 .4724 .4688 .4654 .4618 .4583 .4547 .4511 .4475 .4439	+.1190 +.1095 +.0970 +.0805 +.0604 +.0363 +.0093 0182 0429 0619 0722 0719	+.00 05 04 05 05 06 +.00 +.07 +.10 +.15
909 FMAM JASOND	.185 .414 .294 .325 .352 .376 .419 .470 .434 .561 .512 .443	.2065 .2453 .2850 .3236 .3009 .3964 .4296 .4602 .4876 .5105 .5278 .5387	.4395 .4317 .4242 .4176 .4114 .4059 .4014 .3977 .3946 .3922 .3904 .3894	2330 1864 1392 0940 0505 0095 +.0282 +.0625 +.9930 +.1183 +.1374 +.1493	+.073 062 027 037 087 104 105 134 004 +.073 +.155 +.259	1914 F M A M J A S O N D	.425 .304 .327 .301 .292 .310 .470 .847 .757 .714 .640 .396	.3793 .3953 .4175 .4430 .4686 .4918 .5115 .5264 .5377 .5317	.4402 .4367 .4331 .4295 .4258 .4224 .4189 .4157 .4123 .4092 .4061 .4031	0609 0414 0156 +.0135 +.0694 +.0926 +.1107 +.1231 +.1285 +.1285	01 05 04 04 03 05 +.02 +.02 +.09 +.13
910 JFM AM JASOND	.617 .503 .494 .555 .639 .535 .475 .306 .301 .421 .363 .292	.5428 .5397 .5301 .5148 .4951 .4731 .4512 .4308 .4140 .4018 .3944 .3912	.3889 .3890 .3896 .3906 .3921 .3941 .3964 .3991 .4021 .4056 .4094 .4134	+.1539 +.1507 +.1405 +.1242 +.1030 +.0790 +.0548 +.0317 +.0119 0038 0150 0222	+.057 059 035 039 079 093 161 .000 +.075 +.146 +.237	1915 F M A M I J A S O N D	.354 .342 .332 .360 .324 .292 .283 .286 .231 .206 .196 .175	.4894 .4532 .4091 .3610 .3139 .2727 .2416 .2230 .2178 .2244 .2403 .2624	.4002 .3977 .3954 .3934 .3915 .3903 .3892 .3886 .3884 .3887 .3896 .3912	+.0892 +.0555 +.0137 0324 0776 1176 1656 1706 1643 1493 1288	-,02 -,04 -,04 -,03 -,03 -,01 -,04 +,02 +,05 +,07 +,11
911 FM AM JASOND	.462 .419 .399 .402 .433 .462 .452 .461 .353 .292 .302	.3916 .3939 .3967 .3988 .3992 .3973 .3934 .3883 .3834 .3801 .3803 .3856	.4179 .4225 .4275 .4325 .4379 .4431 .4483 .4535 .4588 .4637 .4685 .4727	0263 0286 0308 0337 0458 0549 0652 0754 0836 0882 0871	+.040 061 041 040 082 079 097 +.005 +.075 +.153	1916 JF MAA MJ ASOND	.310 .312 .321 .360 .388 .492 .500 .402 .422 .376 .418	.2877 .3132 .3376 .3600 .3796 .3963 .4102 .4212 .4293 .4351 .4395 .4434	.3936 .3965 .4001 .4042 .4088 .4144 .4203 .4270 .4348 .4427 .4514 .4606	1059 0833 0625 0442 0292 0181 0101 0058 0055 0076 0119	036 038 036 036 019 004 +.022 +.044 +.065

TABLE 21—Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1917 JF M AM J A SOND	.350 .409 .393 .428 .513 .686 .525 .506 .636 .567 .567	.4477 .4539 .4626 .4742 .4892 .5076 .5285 .5517 .5762 .6009 .6249	.4709 .4816 .4925 .5038 .5152 .5277 .5402 .5529 .5650 .5784 .5917 .6048	0232 0277 0299 0296 0260 0201 0117 0012 +.0225 +.0332 +.0426	038 027 035 035 026 014 .000 030 +.020 +.035 +.053 +.077	IP22 J F M A M J A S O N D	.673 .661 .627 .617 .598 .597 .602 .593 .636 .662	.6561 .6402 .6273 .6178 .6118 .6093 .6103 .6145 .6214 .6305 .6411	.7355 .7273 .7192 .7109 .7028 .6948 .6868 .6789 .6711 .6637 .6563 .6493	0794 0871 0919 0931 0910 0855 0765 0765 0644 0497 0332 0152 +.0033	015 +.029 001 018 029 015 018 +.001 +.004
1918 FMAM JJASOND	.651 .714 .744 .659 .724 .709 .749 .763 .750 .724 .668	.6678 .6856 .7006 .7129 .7224 .7201 .7333 .7350 .7343 .7318 .7284 .7249	.6176 .6312 .6444 .6578 .6704 .6838 .6964 .7086 .7199 .7309 .7309 .7420	+.0502 +.0544 +.0562 +.0551 +.05520 +.0453 +.0369 +.0264 +.01044 +.0009 0136 0276	038 016 028 034 022 010 +.002 025 +.013 +.043 +.064	M A M	.646 .650 .710 .702 .675 .729 .726 .714 .691 .666 .677	.6641 .6753 .6860 .6958 .7045 .7116 .7162 .7171 .7128 .7019 .6835 .6576	.6423 .6359 .6295 .6295 .6177 .6124 .6072 .6026 .5981 .5941 .5903 .5869	+.0218 +.0304 +.0565 +.0722 +.0868 +.0992 +.1145 +.1147 +.1078 +.0932 +.0707	011 +.033 +.001 014 003 030 022 018 +.002 +.012 +.012 +.005 +.041
1919 JFM AM JASOND	.714 .708 .707 .764 .741 .830 .815 .731 .752 .879 1.011	.7230 .7239 .7288 .7387 .7534 .7727 .7956 .8204 .8453 .8689 .8893 .9055	.7624 .7712 .7799 .7877 .7950 .8012 .8068 .8120 .8167 .8203 .8236 .8264	0394 0473 0511 0490 0416 0285 0112 +.0084 +.0286 +.0486 +.0657 +.0791	035 004 019 032 021 008 +.001 021 +.010 +.021 +.033 +.053	1924 J F M A J J A S O N D	.651 .604 .604 .633 .525 .380 .350 .319 .313 .355 .381	.6251 .5876 .5477 .5082 .4719 .4410 .4175 .4027 .3972 .4015 .4151 .4374	.5835 .5806 .5780 .5756 .5736 .5718 .5704 .5690 .5670 .5666 .5666	+ .0416 + .0070 0303 0674 1017 1308 1529 1663 1706 1655 1515	009 +.032 +.002 009 001 028 018 +.003 +.010 +.003
1920 JF M AM JASOND	.942 .993 .919 .892 .870 .889 .919 .879 .846 .872 .873 .800	.9167 .9227 .9237 .9205 .9140 .9051 .8951 .8850 .8755 .8668 .8589	.8285 .8304 .8315 .8319 .8311 .8301 .8289 .8275 .8249 .8220 .8186	+.0882 +.0923 +.0922 +.0886 +.0821 +.0740 +.0650 +.0480 +.0419 +.0369 +.0330	029 +.007 011 029 016 014 000 020 +.005 +.017 +.025 +.045	1925 J F M A J J A S O N D	.529 .531 .597 .592 .581 .620 .638 .640 .662 .682 .674	.4667 .5010 .5375 .5731 .6049 .6309 .6496 .6610 .6663 .6639	.5660 .5663 .5669 .5678 .5688 .5703 .5723 .5746 .5773 .5804 .5840	0993 0653 0294 +. 0053 +. 0361 +. 0606 +. 0773 +. 0864 +. 0859 +. 0799 +. 0799	008 +.025 +.002 005 +.001 021 026 018 +.003 +.006 +.002 +.042
1921 F M A M J A S O N D	.848 .843 .839 .836 .842 .798 .754 .765 .710 .708 .687	.8444 .8366 .8276 .8170 .8044 .7898 .7732 .7548 .7350 .7146 .6941 .6743	.8149 .8106 .8057 .8001 .7943 .7878 .7811 .7741 .7669 .7591 .7513 .7433	+.0295 +.0260 +.0219 +.0169 +.0101 +.0020 0079 0193 0319 0445 0572 0690	021 +.018 005 026 010 020 006 019 +.001 +.015 +.015 +.042	1926 J F M A J J A S O N D	.645 .671 .657 .611 .580 .631 .647 .674 .699 .673 .657	.6570 .6543 .6524 .6512 .6505 .6502 .6502 .6508 .6517 .6526 .6531	.5926 .5976 .6029 .6088 .6150 .6219 .6288 .6360 .6435 .6515 .6594	+.0644 +.0567 +.0495 +.0424 +.0355 +.0214 +.0148 +.0082 +.0011 0063 0154	009 +.015 +.001 002 +.001 013 017 019 +.002 +.004 +.002

TABLE 21-Concluded

Date	1	2	3	4	5	Date	1	2	3	4	5
1927 J F M A M J A S O N D	.645 .602 .616 .622 .629 .639 .617 .586 .579 .589	.6491 .6434 .6352 .6247 .6131 .6020 .5930 .5873 .5862 .5905 .5909	.6754 .6838 .6914 .6990 .7063 .7131 .7195 .7264 .7310 .7357 .7396 .7428	0263 0404 0562 0743 0932 1111 1265 1391 1448 1452 1397 1285	010 +.003 .000 001 .000 003 010 020 +.001 +.001 +.001	1932 F M A M J J A S O N D	.433 .408 .398 .398 .398 .318 .321 .301 .130 .000 040	.3914 .4036 .4039 .3929 .3720 .3432 .3099 .2746 .2392 .2045 .1719 .1414			010 010 .000 .000 .000 .000 .000 020 .000 .00
1928 J F M A M J A S O N D	.637 .647 .650 .706 .756 .801 .785 .857 .861 .844 .824	.6330 .6550 .6791 .7048 .7311 .7573 .7832 .8082 .8328 .8555 .8766 .8953	.7456 .7474 .7486 .7489 .7484 .7470 .7451 .7427 .7307 .7357 .7357 .7312	1126 0924 0695 0441 0173 +.0103 +.0381 +.0658 +.0931 +.1198 +.1454 +.1689	010 006 .000 .000 .000 003 020 .000 .000 .000 .000 +.040	1933 F M A M J A S O N D	.010 .010 .521 .137 .000 .000 .000 .011 125 125 125 067	.1126 .0864 .0631 .0422 .0242 .0089 0047 0174 0291 0490 0494 0555			010 010 .000 .000 .000 .000 020 .000 .000 .0
1929 J F M A M J A S O N D	.858 .859 .959 .949 .950 .886 .965 .935 .929 .808 .736 .644	.9110 .9231 .9312 .9344 .9321 .9239 .9091 .8870 .8580 .8222 .7801 .7332	.7210 .7148 .7083 .7012 .6940	+.1900 +.2083 +.2229 +.2332 +.2381	010 010 .000 .000 .000 .000 .000 020 .000 .00	1934 F M A M J A S O N D	.010 .010 .000 .000 .000 .000 .000 .020 .000 .000 .000	0560 0497 0359 0152			010 010 .000 .000 .000 .000 020 .000 .000 .0
1930 F M A M J A S O N D	.677 .645 .567 .602 .494 .418 .342 .364 .301 .301	.6833 .6321 .5813 .5326 .4868 .4439 .4037 .3659 .3299 .2956 .2637 .2351			010 010 .000 .000 .000 .000 .000 020 .000 .00	1935 J F M A M J J A S O N D	.010 .010 .000 194 602 602 582 602 538 125 165				010 010 .000 .000 .000 .000 020 .000 .000 .0
1931 F M A M J A S O N D	.206 .186 .190 .182 .161 .176 .176 .196 .176 .322 .398	.2108 .1921 .1803 .1760 .1795 .1916 .2116 .2383 .2703 .3053 .3053 .3690			010 010 .000 .000 .000 .000 .000 020 .000 .00	1936 J	115				010

TABLE 22

90-Day Time Money Rates in New York City

Monthly Averages, January 1890-January 1936

- Col. 1. Logarithms of Data Adjusted for Seasonal Fluctuations.
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).
- Col. 5. Changing Seasonal Fluctuations (logarithms).

For details of the nature of the graduations given in Columns 2 and 3 and of the seasonal given in Column 5, see Appendix D.

TABLE 22

Date	1	2	3	4	5	Date	1	2	3	4	5
1890 JF M AM JASOND	.699 .742 .717 .683 .757 .741 .716 .736 .737 .730 .794 .803	.6089 .7105 .7212 .7305 .7378 .7427 .7451 .7456 .7446 .7448 .7410 .7394	.6888 .6889 .6890 .6893 .6895 .6895 .6904 .6907 .6911 .6916 .6916	+.0101 +.0216 +.0322 +.0412 +.0483 +.0528 +.0547 +.0549 +.0535 +.0514 +.0404 +.0478	018 048 013 030 041 042 030 +.022 +.059 +.048 +.051 +.042	1895 J F M A M J A S O N D	.423 .526 .504 .520 .416 .356 .432 .374 .356 .401 .404 .618	.4014 .4086 .4149 .4209 .4274 .4344 .4417 .4510 .4610 .4758 .4960 .5226	.5005 .4993 .4981 .4969 .4958 .4949 .4940 .4932 .4932 .4932 .4913 .4913	0991 0907 0832 0760 0684 0605 0523 0431 0316 0160 +.0047 +.0316	01 02 +.02 +.01 03 05 05 +.02 +.07 +.05 00
FM AM JASOND	.740 .697 .685 .645 .791 .696 .687 .720 .609 .682 .670 .615	.7383 .7376 .7365 .7344 .7302 .7230 .7120 .6969 .6776 .6550 .6300 .6038	.6913 .6911 .6904 .6895 .6878 .6862 .6839 .6815 .6787 .6787	+.0470 +.0461 +.0461 +.0424 +.0368 +.0281 +.0154 0011 0204 0419 0643	022 046 008 022 044 043 029 +.025 +.063 +.050 +.029 +.028	1896 J F M A M J J A S O N D	.792 .744 .561 .551 .527 .555 .650 .855 .823 .872 .678 .492	.5553 .5917 .6287 .6623 .6879 .7030 .7063 .6975 .6780 .6503 .6166 .5785	.4908 .4907 .4908 .4909 .4911 .4918 .4926 .4937 .4948 .4964 .4981	+.0645 +.1010 +.1379 +.1714 +.1968 +.2112 +.2137 +.2038 +.1832 +.1539 +.1185 +.0783	01 02 +.02 +.01 03 06 05 +.02 +.07 +.05 +.00
1892 F M A M J A S O N D	.542 .533 .549 .471 .461 .475 .507 .443 .586 .689 .721	.5779 .5538 .5331 .5171 .5079 .5069 .5155 .5345 .6016 .6452 .6912	.6635 .6592 .6543 .6490 .6431 .6375 .6316 .6257 .6197 .6197 .6195 .6075	0856 1054 1212 1319 1352 1306 1161 0912 0559 0119 +.0377 +.0897	022 039 +.001 012 043 044 030 +.027 +.067 +.051 +.010	J F M A M J A S O N D	.429 .428 .424 .381 .429 .413 .361 .416 .432 .449 .460	.5384 .4985 .4610 .4289 .4052 .3922 .3910 .4019 .4227 .4496 .4787 .5060	.5024 .5048 .5075 .5103 .5132 .5164 .5194 .5223 .5249 .5278 .5302 .5326	+.0360 0063 0465 0814 1080 1242 1284 1204 1022 0782 0515 0266	01 03 +.02 +.01 03 06 +.01 +.07 +.05 +.01 +.00
1893 F M AM J J AS ON D	.709 .646 .760 .773 .810 .831 .977 .841 .690 .636 .533 .413	.7348 .7716 .7985 .8129 .8136 .8012 .7769 .7422 .6991 .6495 .5952 .5384	.5957 .5899 .5841 .5785 .5728 .5675 .5621 .5569 .5517 .5469 .5422 .5378	+.1391 +.1817 +.2144 +.2344 +.2408 +.2337 +.2148 +.1853 +.1474 +.1026 +.0530 +.0006	021 031 +.011 002 042 047 +.028 +.070 +.052 002 +.005	1898 J F M A M J A S O N D	.468 .467 .637 .750 .601 .518 .467 .463 .497 .375 .428 .462	.5279 .5423 .5493 .5491 .5431 .5330 .5200 .5054 .4911 .4789 .4707 .4688	.5348 .5367 .5385 .5401 .5427 .5428 .5446 .5459 .5459 .5468 .5477	0069 +.0056 +.0108 +.0090 +.0017 0097 0238 0392 0541 0670 0761 0789	00 03 +.02 +.01 03 07 05 +.00 +.07 +.03 +.01
1894 JF M A M J A S O N D	.437 .433 .379 .392 .340 .325 .346 .362 .305 .248 .386 .378	.4824 .4301 .3849 .3502 .3280 .3185 .3207 .3317 .3475 .3644 .3799 .3923	.5333 .5293 .5255 .5218 .5185 .5153 .5125 .5100 .5077 .5054 .5036 .5019	-,0509 -,0992 -,1406 -,1716 -,1905 -,1968 -,1918 -,1783 -,1602 -,1410 -,1237 -,1096	020 025 +.019 +.006 039 051 045 +.027 +.072 +.053 008	I899 J F M A M J A S O N D	.468 .523 .580 .583 .535 .558 .612 .633 .679 .672 .727	.4749 .4894 .5118 .5404 .5723 .6041 .6325 .6550 .6700 .6773 .6776	.5489 .5499 .5514 .5531 .55575 .5602 .5630 .5662 .5669 .5738	0740 0605 0396 0127 +.0171 +.0466 +.0723 +.0920 +.1038 +.1074 +.1038 +.1074	00 04 +.02 +.00 03 08 05 06 +.06 +.06 +.04

TABLE 22—Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1900 JF M AM JASOND	.686 .672 .643 .549 .510 .572 .572 .565 .538 .637 .576	.6621 .6490 .6340 .6179 .6018 .5870 .5745 .5656 .5612 .5616 .5664	.5823 .5870 .5918 .5970 .6024 .6080 .6135 .6187 .6288 .6337 .6383	+.0798 +.0620 +.0422 +.0209 0006 0210 0531 0625 0672 0673 0632	005 044 +.016 005 033 086 046 007 +.061 +.057 +.060 +.049	I 1905 F M A M J A SO ND	.463 .517 .525 .567 .564 .582 .567 .545 .593 .612 .650	.4823 .4960 .5108 .5265 .5430 .5605 .5788 .5977 .6170 .6366 .6560 .6752	.6236 .6263 .6288 .6313 .6335 .6360 .6384 .6407 .6429 .6451 .6471	1413 1303 1180 1048 0905 0755 0596 0430 0259 0885 +.0089 +.0262	+.00 02 01 04 06 09 07 02 +.03 +.07 +.10 +.12
1901 JFM AM JJASOND	.587 .555 .505 .632 .677 .642 .681 .655 .649 .609	.5861 .5978 .6086 .6179 .6246 .6290 .6314 .6326 .6331 .6342 .6364	.6424 .6465 .6501 .6532 .6555 .6577 .6595 .6607 .6622 .6622	0563 0487 0415 0353 0309 0287 0281 0284 0280 0258 0215	004 043 +.011 015 038 071 045 014 +.055 +.058 +.073 +.069	1906 JF M A M J A S O N D	.609 .746 .737 .796 .761 .735 .760 .822 .703 .747	.6940 .7120 .7287 .7434 .7551 .7630 .7662 .7650 .7650 .7526 .7452 .7452	.6507 .6526 .6541 .6555 .6567 .6580 .6592 .6601 .6618 .6625	+.0433 +.0594 +.07-46 +.0879 +.0984 +.1050 +.1049 +.0990 +.0990 +.0827 +.0770	+.00 02 01 04 06 09 08 02 +.03 +.11 +.12
1902 J F M A J A S O N D	.659 .641 .599 .653 .722 .732 .711 .695 .843 .811 .725	.6463 .6550 .6659 .6787 .6928 .7072 .7206 .7322 .7411 .7465 .7486	.6608 .6597 .6584 .6569 .6530 .6508 .6485 .6485 .6432 .6405	0145 0047 +.0075 +.0218 +.0378 +.0542 +.0608 +.0837 +.0753 +.1033 +.1081 +.1102	003 039 +.003 025 045 074 048 021 +.051 +.034 +.088	1907 JF M A M J A S O N D	.754 .748 .818 .687 .668 .740 .791 .833 .722 .815 1.020 .876	.7386 .7421 .7508 .7632 .7777 .7917 .8029 .8089 .8081 .7993 .7819	.6633 .6635 .6634 .6632 .6626 .6617 .6604 .6588 .6569 .6543 .6516	+.0753 +.0786 +.0874 +.1000 +.1151 +.1300 +.1425 +.1501 +.1512 +.1450 +.1303 +.1074	+.00 02 02 04 06 09 08 02 +.03 +.09 +.11 +.12
IPO3 FMAM JASOND	.696 .697 .755 .728 .643 .726 .716 .716 .674 .634 .671	.7443 .7390 .7328 .7260 .7183 .7099 .7000 .6880 .6733 .6554 .6342	.6345 .6316 .6287 .6258 .6230 .6203 .6179 .6156 .6138 .6118	+.1098 +.1074 +.1041 +.1092 +.0953 +.0826 +.0821 +.0724 +.0595 +.0436 +.0236 +.0004	.000 035 034 033 050 055 025 +.046 +.045 +.093 +.103	1908 J M A M J A S O N D	.721 .656 .583 .497 .535 .454 .439 .430 .375 .395 .411	.7220 .6813 .6354 .5869 .5387 .4936 .4544 .4235 .4021 .3906 .3883 .3936	.6446 .6407 .6361 .6311 .6257 .6201 .6142 .6081 .6020 .5958 .5897 .5834	+.0774 +.0406 0007 0442 0870 1265 1598 1846 1999 2052 2014 1898	+.00 03 03 04 07 08 07 02 +.03 +.09 +.10 +.11
1904 F M A M J A S O N D	.603 .596 .510 .468 .473 .460 .453 .399 .470 .473 .474	.5836 .5563 .5294 .5045 .4832 .4664 .4549 .4489 .4482 .4520 .4596	.6090 .6087 .6088 .6091 .6095 .6105 .6117 .6131 .6149 .6167 .6189	0254 0524 0794 1046 1263 1441 1568 1642 1667 1593 1512	+.002 029 038 056 056 066 028 +.042 +.071 +.100 +.115	J F M A M J A S O N D	.420 .479 .458 .435 .486 .491 .447 .534 .537 .579 .582	.4046 .4194 .4359 .4535 .4711 .4888 .5066 .5248 .5433 .5620 .5803 .5974	.5770 .5708 .5650 .5595 .5546 .5496 .5452 .5415 .5379 .5349 .5323 .5301	1724 1514 1291 1060 0835 0608 0167 +.0054 +.0271 +.0480 +.0673	+.00 03 03 04 07 08 07 01 +.03 +.09 +.10

TABLE 22-Continued

Date	1	2	3	4	5	Date	1	2	3	4	.5
IPIO JF M A M J J A S O N D	.634 .605 .630 .653 .665 .608 .653 .588 .588 .581	.6123 .6240 .6317 .6349 .6331 .6269 .6171 .6044 .5960 .5750 .5602	.5283 .5272 .5263 .5256 .5256 .5261 .5269 .5280 .5292 .5313 .5334 .5359	+ .0840 + .0768 + .1054 + .1091 + .1075 + .1098 + .0902 + .0764 + .0698 + .0437 + .0268 + .0101	.000 038 039 041 071 075 011 +.037 +.098 +.098	I915 J F M A J J A S O N D	.536 .485 .490 .488 .491 .445 .450 .434 .396 .392 .402 .404	.5967 .5715 .5404 .5064 .4732 .4142 .4225 .4096 .4057 .4094 .4187	.5455 .5437 .5419 .5405 .5392 .5380 .5371 .5365 .5362 .5363 .5365 .5365	+.0512 +.0278 0015 0341 0660 0938 1146 1269 1305 1269 1178 1059	03 02 03 02 03 01 00 +.01 +.04 +.04 +.03 +.00
1911 J F M A M J A S O N D	.540 .536 .499 .479 .513 .516 .502 .507 .505 .463 .470	.5331 .5216 .5115 .5031 .4964 .4914 .4883 .4872 .4881 .4963 .5039	.5389 .5419 .5455 .5494 .5534 .5577 .5619 .5661 .5705 .5749 .5790 .5830	0058 0203 0340 0463 0570 0663 0736 0789 0824 0838 0827 0791	- 011 - 039 - 043 - 040 - 069 - 067 - 043 - 002 + 039 + 096 - 089 + 088	1916 J F M A M J A S O N D	.470 .457 .478 .475 .484 .547 .600 .493 .494 .498 .513 .626	.4444 .4572 .4691 .4801 .4904 .5007 .5112 .5217 .5322 .5425 .5527 .5631	.5380 .5393 .5412 .5462 .5462 .5530 .5571 .5620 .5671 .5728 .5791	0936 0821 0721 0634 0558 0487 0418 0354 0298 0246 0201 0160	03 01 02 01 02 00 00 +.01 +.02 +.02 +.02 +.02
J F M A M J A S O N D	.491 .499 .581 .582 .569 .549 .587 .608 .699 .666 .692	.5136 .5257 .5399 .5560 .5735 .5920 .6106 .6295 .6464 .6616 .6750 .6862	.5868 .5905 .5938 .5966 .5989 .6007 .6022 .6034 .6043 .6044	0732 0648 0549 0406 0254 0087 +.0084 +.0261 +.0421 +.0708 +.0708 +.0826	021 038 044 038 065 055 033 +.005 +.041 +.077 +.063	1917 J W A M J J A S O N D	.525 .616 .595 .608 .659 .687 .634 .637 .724 .722 .749	.5741 .5862 .5997 .6148 .6315 .6495 .6681 .6868 .7048 .7215 .7364 .7493	.5857 .5927 .6003 .6082 .6162 .6249 .6338 .6426 .6516 .6610 .6702	0116 0065 0006 +.0066 +.0153 +.0246 +.0343 +.0442 +.0532 +.0605 +.0662 +.0694	02 00 02 00 01 +.00 +.01 +.01 +.01 +.01
1913 F M AM J A SOND	.642 .692 .773 .668 .653 .656 .680 .644 .623 .612 .632 .663	.6942 .7002 .7026 .7005 .6932 .6805 .6627 .6414 .6187 .5971 .5790	.6027 .6012 .5998 .5979 .5958 .5934 .5909 .5884 .5832 .5805	+.0015 +.0090 +.1026 +.1026 +.0974 +.0871 +.0718 +.0530 +.0139 0015 0105	028 036 043 035 058 040 023 +.009 +.042 +.090 +.062 +.039	1918 F M A M J J A S O N D	.778 .766 .791 .783 .782 .754 .756 .761 .771 .772 .770	.7597 .7676 .7731 .7763 .7772 .7761 .7736 .7699 .7653 .7603 .7553 .7504	.6895 .6990 .7083 .7178 .7271 .7361 .7449 .7534 .7696 .7767 .7836	+.0702 +.0686 +.0648 +.0585 +.0501 +.0400 +.0287 +.0165 +.0038 0093 0214 0332	02 00 01 00 00 +.00 +.01 +.01 +.00 +.00
1914 J F M A M J J A S O N D	.597 .514 .516 .478 .435 .433 .577 .871 .797 .734 .671	.5611 .5611 .5663 .5753 .5858 .5977 .6091 .6188 .6256 .6282 .6251	.5746 .5718 .5691 .5664 .5638 .5613 .5588 .5564 .5539 .5516 .5494 .5473	0135 0107 0028 +.0089 +.0220 +.0364 +.0503 +.0624 +.0717 +.0757 +.0757	032 033 039 029 048 014 + .012 + .042 + .079 + .047 + .020	1919 F M A M J A S O N D	.735 .723 .747 .764 .738 .753 .778 .767 .770 .789 .809 .828	.7462 .7431 .7416 .7421 .7453 .7514 .7607 .7731 .7883 .8057 .8245 .8438	.7902 .7959 .8015 .8067 .8112 .8150 .8186 .8218 .8239 .8260 .8277 .8288	0440 0528 0529 0646 0659 0636 0579 0487 0356 0203 0032 +.0150	02 +.00 00 +.00 +.00 +.00 +.00 +.00 00

TABLE 22—Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1920 J F M A M J J A S O N D	.881 .904 .911 .906 .911 .902 .921 .940 .919 .901 .889 .870	.8626 .8799 .8946 .9063 .9142 .9183 .9184 .9150 .9084 .8882 .8758	.8293 .8298 .8297 .8293 .8285 .8273 .8259 .8243 .8224 .8224 .8177 .8148	+.0333 +.0501 +.0649 +.0770 +.0857 +.0910 +.0925 +.0907 +.0860 +.0791 +.0795 +.0610	017 +.006 .000 +.004 +.005 +.006 003 +.001 004 001 +.001	1925 J F M A M J J A S O N D	.549 .552 .590 .594 .576 .609 .621 .652 .644 .677 .690	.5198 .5380 .5591 .5813 .6026 .6215 .6369 .6481 .6555 .6597 .6616 .6623	.6018 .6014 .6012 .6013 .6016 .6022 .6031 .6045 .6061 .6083 .6106	0820 0634 0421 0220 +.0010 +.0193 +.0338 +.0494 +.0514 +.0510 +.0489	+.010 +.010 +.020 +.009 +.001 024 027 014 +.000 +.001
1921 F M A M J A S O N D	.831 .826 .823 .815 .817 .825 .796 .784 .753 .717 .707	.8627 .8494 .8362 .8232 .8103 .7971 .7834 .7688 .7530 .7361 .7184	.8112 .8079 .8040 .7997 .7950 .7903 .7853 .7851 .7746 .7689 .7633 .7575	+.0515 +.0415 +.0322 +.0235 +.0153 +.0068 0019 0113 0216 0328 0449 0570	011 +.007 +.006 +.008 +.006 009 007 006 002 001 +.002	1926 JF M A M J A S O N D	.672 .659 .662 .619 .638 .661 .675 .687 .688 .669	.6623 .6621 .6617 .6611 .6633 .6593 .6586 .6582 .6585 .6582 .6602	.6165 .6202 .6242 .6287 .6386 .6389 .6446 .6505 .6505 .6632 .6698	+.0458 +.0419 +.0375 +.0324 +.0267 +.0204 +.0140 +.0077 +.0019 0040 0058	+.007 +.008 +.014 +.006 022 022 007 +.004 +.010 +.001
1922 F M A M J J A S O N D	.681 .679 .661 .633 .613 .622 .630 .625 .656 .681	.6833 .6676 .6545 .6445 .6381 .6353 .6360 .6397 .6459 .6540 .6633 .6734	.7513 .7453 .7392 .7330 .7266 .7203 .7141 .7080 .7018 .6957 .6898 .6839	0680 0777 0847 0885 0850 0781 0683 0559 0417 0265 0105	004 +.009 +.015 +.011 +.007 007 021 014 006 001 +.009	1927 JF M A M J J A S O N D	.656 .640 .638 .637 .640 .662 .664 .614 .610	.6603 .6581 .6542 .6484 .6413 .6338 .6269 .6218 .6192 .6290 .6245 .6327	.6833 .6903 .6970 .7033 .7097 .7157 .7216 .7270 .7320 .7364 .7407 .7445	0230 0322 0429 0550 0685 0821 0948 1053 1127 1163 1160 1115	+.002 +.005 +.007 +.004 001 019 017 003 +.010 +.013 000 +.003
1923 F M A M J J A S O N D	.666 .681 .702 .714 .700 .707 .738 .737 .743 .723 .703 .683	.6838 .6939 .7035 .7124 .7202 .7265 .7307 .7320 .7226 .7228 .7110	.6781 .6723 .6668 .6614 .6565 .6518 .6472 .6426 .6381 .6341 .6304	+.0057 +.0216 +.0367 +.0510 +.0637 +.0747 +.0885 +.0915 +.0894 +.0915 +.0886 +.0673	+.003 +.010 +.021 +.012 +.005 016 029 018 005 .000 001 +.016	1928 F M A M J A S O N D	.642 .655 .660 .685 .714 .775 .786 .804 .834 .835 .838	.6445 .6595 .6773 .6972 .7189 .7418 .7654 .7896 .8140 .8380 .8610 .8824	.7476 .7503 .7524 .7542 .7555 .7561 .7563 .7558 .7558 .7530 .7507	1027 0903 0746 0564 0361 0139 +.0095 +.0341 +.0593 +.0850 1103 +.1103	004 +.003 +.004 +.003 001 015 013 002 +.015 +.016
1924 J F M A M J A S O N D	.674 .667 .648 .624 .596 .542 .485 .452 .474 .456 .494	.6727 .6478 .6206 .5929 .5665 .5427 .5229 .5079 .4985 .4949 .4975	.6236 .6206 .6177 .6153 .6129 .6108 .6090 .6073 .6057 .6044 .6033 .6025	+.0491 +.0272 +.0029 0224 0464 0681 0994 1072 1095 1058	+.007 +.010 +.023 +.012 +.003 022 030 017 003 +.003 +.017	1929 J F M A M J A S O N D	.893 .886 .899 .939 .944 .921 .906 .949 .933 .874 .741	.9011 .9163 .9271 .9326 .9323 .9257 .9126 .8930 .8668 .8347 .7970	.7447 .7407 .7359 .7303 .7245	+.1562 +.1754 +.1910 +.2021 +.2076	009 000 +.002 +.002 001 013 012 001 +.018 +.018 001

TABLE 22-Concluded

Date	1	2 1	.3	1	5	Date	1	2	3	4	5
1930 F M A M J A S O N D	.682 .668 .614 .613 .550 .473 .455 .419 .394 .374 .339	.7097 .6637 .6184 .5757 .5365 .5005 .4672 .4352 .4032 .3764 .3376			010 001 +.001 +.002 001 011 011 001 +.019 +.019 001	1934 F M A M J J A S O N D	.047 040 057 057 055 045 045 055 075 075 075 055	0519 0588 0583 0497			010 001 +.000 +.000 001 011 011 011 +.015 001 001
1931 F M AM J J ASOND	.332 .275 .325 .325 .221 .160 .163 .177 .209 .485 .549	.2781 .2566 .2440 .2420 .2510 .2708 .2997 .3349 .3729 .4100 .4407 .4606			010 601 +.001 +.001 001 011 011 001 +.019 001	1935 J F M A M J J A S O N D	046 055 057 253 601 591 591 601 621 488 .001				010 001 +.001 +.001 011 011 011 +.019 +.019 001 001
1932 FMAM LASOND	.561 .560 .495 .429 .202 .187 .169 .141 .031 -032 -303 -300	.4655 .4523 .4198 .3696 .3055 .2325 .1575 .0869 .0259 -0225 -0560 -0750			010 001 +.001 +.001 001 011 001 +.019 +.019 001	1936 J	.010				010
1933 JFM AM JA SOND	291 179 .467 .076 .018 021 .075 .034 213 180 080	0817 0782 0672 0520 0356 0203 0090 0038 0051 0128 0253 0398			010 001 +.001 +.001 001 011 001 +.019 +.019 001						

TABLE 23

COMMERCIAL PAPER RATES IN NEW YORK CITY¹

Monthly Averages, January 1857-January 1936

- Col. 1. Logarithms of Data Adjusted for Seasonal Fluctuations.
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).
- Col. 5. Changing Seasonal Fluctuations (logarithms).

For details of the nature of the graduations given in Columns 2 and 3, and of the seasonal given in Column 5 of this table, see Appendix D.

¹ January 1857-December 1923 'Choice 60-90 day two name paper'. January 1924-January 1932 '4-6 months prime double and single name paper'.

TABLE 23

Date	1	2	3	4	5	Date	1	2	3	4	5
1857 IF M A M J A S O N D	.933 .929 .979 .979 .932 .927 .960 .997 1.239 1.365 1.040	.9297 .9529 .9787 1.0040 1.0262 1.0427 1.0511 1.0501 1.0392 1.0180 .9868 .9467	.8917 .8868 .8819 .8771 .8724 .8677 .8631 .8589 .8547 .8505 .8547 .8505	+.0380 +.0661 +.0968 +.1269 +.1538 +.1750 +.1880 +.1912 +.1845 +.1675 +.1401 +.1038	+.013 +.017 012 025 019 031 +.003 +.016 +.015 +.021 +.027	1862 J F M A M J J A S O N D	.777 .752 .803 .790 .711 .683 .770 .666 .700 .647 .658 .707	.7788 .7696 .7589 .7469 .7342 .7218 .7108 .7019 .6956 .6922 .6918 .6942	.7833 .7840 .7844 .7848 .7850 .7855 .7857 .7859 .7860 .7863 .7868 .7870	0045 0144 0255 0379 0508 0637 0749 0840 0904 0950 0928	+.02 +.01 00 01 03 03 01 00 +.00 +.01
F M A M J A SO N D	.861 .742 .752 .737 .576 .661 .599 .607 .635 .632 .638	.8980 .8444 .7883 .7335 .6833 .6430 .6137 .5979 .5957 .6060 .6260 .6527	.8396 .8362 .8329 .8300 .8274 .8248 .8224 .8200 .8180 .8160 .8140 .8123	+.0584 +.0082 0446 0965 1441 1818 2087 2221 2223 2100 1880 1596	+.014 +.018 012 022 015 026 030 000 +.012 +.011 +.014 +.029	1863 J F M A M J A S O N D	.701 .739 .724 .724 .732 .766 .779 .740 .751 .748 .800 .798	.6994 .7067 .7184 .7253 .7354 .7444 .7526 .7598 .7664 .7729 .7799	.7873 .7880 .7887 .7895 .7901 .7914 .7925 .7940 .7954 .7973 .7992 .8011	~.0879 ~.0813 ~.0703 ~.0642 ~.0547 ~.0470 ~.0399 ~.0342 ~.0290 ~.0244 ~.0193 ~.0131	+.02 +.01 03 03 03 01 +.00 +.02 +.03
1859 FMAM JASOND	.648 .721 .724 .741 .823 .864 .850 .850 .808 .821 .782 .800	.6825 .7133 .7425 .7690 .7920 .8106 .8240 .8317 .8337 .8337 .83301 .8225 .8128	.8106 .8090 .8074 .8059 .8045 .8030 .8016 .8011 .7986 .7972 .7957 .7957	1281 0957 0649 0369 0125 +.0076 +.0224 +.0316 +.0351 +.0329 +.0268 +.0187	+.016 +.020 010 019 012 025 029 003 +.008 +.009 +.010 +.030	1864 JF M A M J A S O N D	.839 .800 .745 .821 .861 .872 .847 .905 .958 .958 .953 .889	.7975 .8087 .8211 .8346 .8484 .8621 .8750 .8867 .8967 .9046 .9102	.8031 .8053 .8076 .8099 .8123 .8146 .8170 .8194 .8219 .8239 .8262 .8285	~.0056 +.0034 +.0135 +.0247 +.0361 +.0475 +.0580 +.0673 +.0748 +.0807 +.0840 +.0849	+.02 +.00 +.00 02 03 03 00 +.00 +.00 +.00
1860 F M A M J J A S O N D	.884 .831 .780 .763 .773 .766 .760 .791 .841 .826 1.037 1.080	.8032 .7959 .7925 .7940 .8003 .8106 .8238 .8384 .8526 .8654 .8757 .8827	.7925 .7909 .7895 .7881 .7868 .7854 .7842 .7832 .7822 .7813 .7807 .7801	+.0107 +.0050 +.0059 +.0135 +.0252 +.0396 +.0552 +.0704 +.0841 +.0950 +.1026	+.019 +.020 009 015 010 026 028 006 +.004 +.007 +.009 +.031	1865 F M A M I J A S O N D	.879 .920 .948 .921 .884 .871 .899 .909 .855 .866 .863	.9139 .9124 .9092 .9049 .9002 .8954 .8908 .8862 .8812 .8752 .8757 .8586	.8307 .8327 .8345 .8363 .8381 .8397 .8412 .8426 .8440 .8452 .8464 .8476	+.0832 +.0797 +.0747 +.0686 +.0621 +.0557 +.0496 +.0436 +.0372 +.0300 +.0213 +.0110	+.00 +.00 +.00 00 00 00 00 +.00 +
1861 F M A M J A S O N D	.882 .842 .791 .803 .918 .840 .769 .822 .798 .827 .789 .813	.8857 .8848 .8796 .8707 .8593 .8464 .8332 .8210 .8105 .8016 .7939 .7867	.7797 .7794 .7792 .7792 .7795 .7797 .7800 .7804 .7810 .7817 .7824 .7830	+.1060 +.1054 +.1004 +.0915 +.0798 +.0667 +.0532 +.0406 +.0295 +.0199 +.0115 +.0037	+.021 +.021 006 011 010 027 029 +.001 +.006 +.010 +.010	1866 J F M A M J J A S O N D	.843 .858 .856 .814 .815 .797 .809 .795 .723 .717 .776 .793	.8479 .8361 .8237 .8119 .8013 .7925 .7863 .7830 .7826 .7854 .7913	.8487 .8497 .8507 .8517 .8527 .8538 .8548 .8557 .8568 .8578 .8589 .8600	~.0008 ~.0136 ~.0270 ~.0398 ~.0514 ~.0613 ~.0685 ~.0727 ~.0724 ~.0724 ~.0676 ~.0663	+.0 +.0 +.0 +.0 0 0 0 0 +.0 +.0 +.0

TABLE 23—Continued

COMMERCIAL PAPER RATES

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Date	1	2	3	4	.5	Date	1	2	3	4	5
1867 JF MAM JASOND	.846 .851 .847 .842 .863 .925 .858 .841 .853 .899 .875 .851	.8103 .8224 .8351 .8473 .8581 .8668 .8725 .8752 .8751 .8724 .8680 .8627	.8611 .8622 .8632 .8642 .8652 .8662 .8672 .8682 .8692 .8700 .8709 .8718	0508 0398 0281 0169 0071 + .0006 + .0053 + .0070 + .0024 0029 0091	+.023 002 +.010 +.014 039 057 042 028 001 +.025 +.057 +.049	IS72 J F M A M J A S O N D	.899 .900 .930 .923 .916 .854 .879 .916 .978 .978 .993	.8880 .8982 .9077 .9163 .9236 .9295 .9340 .9375 .9447 .9503 .9578	.9080 .9080 .9079 .9076 .9071 .9067 .9059 .9059 .9054 .9029 .9016 .9001	0200 0098 0002 +.0087 +.0165 +.0228 +.0228 +.0325 +.0366 +.0418 +.04187 +.0577	+.020 021 +.007 +.016 059 076 037 +.022 +.061 +.072 +.071
1868 J F M A M J A S O N D	.827 .821 .874 .887 .866 .819 .859 .851 .827 .840 .937 .862	.8572 .8519 .8475 .8443 .8424 .8421 .8439 .8480 .8548 .8649 .8784 .8784	.8729 .8738 .8747 .8756 .8765 .8774 .8783 .8791 .8800 .8807 .8815 .8823	0157 0219 0272 0313 0341 0352 0311 0252 0158 0031 +.0127	+.022 008 +.011 +.016 045 062 030 +.002 +.063 +.063 +.054	1873 F M A M J J A S O N D	.948 .995 1.000 1.043 .970 .911 .883 .886 1.128 1.152 1.091	.9671 .9776 .9880 .9966 1.0022 1.0041 1.0016 .9948 .9844 .9707 .9541 .9349	.8987 .8968 .8949 .8929 .8905 .8879 .8851 .8821 .8788 .8752 .8715	+.0684 +.0308 +.0931 +.1037 +.1117 +.1162 +.1165 +.1127 +.1056 +.0955 +.0826 +.0675	+.020 023 +.005 +.014 060 077 074 037 +.027 +.065 +.070
I 1869 J. F. M. A. M. J. J. A. SO. N. D.	.899 .898 .962 .978 .943 1.052 1.062 1.012 1.033 .977 1.009	.9143 .9351 .9561 .9756 .9920 1.0039 1.0100 1.0099 1.0037 .9917 .9750	.8831 .8840 .8846 .8853 .8859 .8864 .8870 .8876 .8881 .8881 .8887	+.0312 +.0511 +.0715 +.0903 +.1061 +.1175 +.1230 +.1223 +.1156 +.1030 +.0858 +.0653	+.021 012 +.011 +.017 050 067 051 032 +.006 +.039 +.068 +.060	1874 J F M A M J A S O N D	.852 .801 .784 .783 .812 .823 .828 .772 .765 .697 .682	.9131 .8888 .8626 .8355 .8090 .7845 .7637 .7473 .7355 .7277 .7231 .7206	.8632 .8588 .8541 .8439 .8387 .8331 .8276 .8159 .8100 .8038	+.0499 +.0300 +.0085 0137 0349 0542 0694 0803 0861 0382 0869 0869	+.020 023 +.004 +.013 059 079 036 +.031 +.067 +.068 +.071
1870 JF MA M J JA SOND	.934 .884 .865 .840 .859 .808 .863 .890 .848 .814 .789	.9339 .9127 .8932 .8764 .8628 .8524 .8446 .8387 .8335 .8284 .8230 .8173	.8903 .8909 .8915 .8921 .8928 .8935 .8943 .8952 .8962 .8972 .8982 .8982	+.0436 +.0218 +.0017 0157 0300 0411 0497 0565 0627 0688 0752 0819	+.020 016 +.010 +.017 054 071 058 034 +.012 +.042 +.048	1875 J F M A M J J A S O N D	.699 .738 .767 .724 .717 .735 .716 .728 .737 .731 .741	.7192 .7186 .7188 .7202 .7232 .7278 .7337 .7399 .7455 .7493 .7509 .7499	.7973 .7909 .7845 .7782 .7724 .7661 .7602 .7543 .7448 .7426 .7370 .7317	0781 0723 0657 0580 0492 0383 0265 0144 0028 +.0067 +.0139 +.0182	+.021 023 +.004 +.012 058 077 082 034 +.033 +.069 +.065
1871 F M A M J A S O N D	.839 .840 .788 .815 .798 .778 .754 .754 .778 .806 .946 .897	.8118 .8074 .8050 .8051 .8079 .8136 .8216 .8314 .8425 .8541 .8657 .8771	.9002 .9012 .9021 .9030 .9039 .9047 .9054 .9060 .9068 .9071 .9075 .9078	0884 0938 0971 0979 0960 0911 0838 0746 0643 0530 0418 0307	+.020 019 +.008 +.016 058 074 064 036 +.017 +.055 +.072 +.069	1876 J F M A M J J A S O N D	.789 .749 .727 .730 .759 .753 .667 .587 .642 .685 .674	.7467 .7417 .7351 .7271 .7179 .7077 .6856 .6753 .6668 .6610 .6588	.7266 .7217 .7170 .7128 .7087 .7051 .7018 .6987 .6959 .6935 .6916 .6899	+.0201 +.0200 +.0181 +.0143 +.0092 +.0026 0051 0131 0206 0267 0306 0311	+.021 022 +.005 +.010 056 076 086 031 +.069 +.062 +.065

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TABLE 23-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1877 JF M AM J J AS OND	.725 .674 .641 .632 .655 .682 .704 .779 .769 .701 .732	.6604 .6656 .6738 .6842 .6957 .7073 .7183 .7278 .7353 .7404 .7425 .7410	.6884 .6874 .6866 .6860 .6855 .6853 .6852 .6854 .6857 .6863	0280 0218 0128 0118 +.0102 +.0220 +.0331 +.0424 +.0496 +.0545 +.0562 +.0562	+.019 021 +.096 +.099 053 073 087 028 +.036 +.069 +.060	ISS2 J F AI AI J ASOND	.733 .758 .747 .709 .730 .768 .732 .756 .790 .769 .764	.7331 .7393 .7445 .7482 .7505 .7516 .7521 .7528 .7543 .7569 .7607 .7648	.7390 .7399 .7407 .7410 .7411 .7410 .7405 .7398 .7390 .7377 .7363 .7346	0059 0006 +.0038 +.0072 +.0106 +.0116 +.0130 +.0153 +.0192 +.0244 +.0302	+ .007 020 + .004 005 044 059 067 004 + .039 + .056 + .049 + .049
1878 J F M A M J A S O N D	.750 .745 .701 .722 .707 .652 .641 .604 .628 .669	.7359 .7272 .7152 .7008 .6854 .6702 .6566 .6460 .6361 .6360 .6369 .6413	.6873 .6877 .6882 .6886 .6899 .6896 .6896 .6896 .6900 .6904 .6907	+.0486 +.0395 +.0270 +.0122 0035 0120 0339 0509 0544 0538 0497	+.017 020 +.008 +.008 051 071 085 023 +.037 +.067 +.058 +.056	1883 Jr M A M J A S O N D	.734 .735 .803 .773 .772 .796 .738 .749 .738 .725 .708 .697	.7683 .7703 .7699 .7668 .7610 .7533 .7447 .7360 .7283 .7224 .7185 .7167	.7327 .7307 .7285 .7263 .7238 .7215 .7190 .7163 .7138 .7113 .7089 .7066	+.0356 +.0396 0414 +.0405 +.0372 +.0318 +.0257 +.0197 +.0145 +.0111 +.0096 +.0101	+.006 022 +.002 009 044 056 059 .000 +.040 +.053 +.047 +.044
IS79 IF M AM I J AS ON D	.622 .600 .697 .732 .696 .693 .763 .724 .710 .741	.6483 .6572 .6674 .6782 .6890 .6997 .7096 .7184 .7259 .7316 .7353 .7370	.6912 .6918 .6923 .6929 .6934 .6943 .6952 .6961 .6971 .6982 .6994	0429 0346 0249 0147 0054 +.0054 +.0144 +.0223 +.0288 +.0334 +.0359 +.0364	+.014 019 +.007 +.004 049 068 082 018 +.038 +.064 +.056 +.050	1884 F M A M J A S O N D	.685 .701 .666 .686 .747 .813 .827 .736 .700 .689 .670	.7168 .7185 .7212 .7245 .7277 .7301 .7309 .7292 .7243 .7157 .7034 .6879	.7042 .7020 .6998 .6978 .6938 .6938 .6921 .6904 .6888 .6871 .6856	+.0126 +.0165 +.0214 +.0267 +.0319 +.0368 +.0388 +.0355 +.0286 +.0178 +.0037	+.004 024 001 012 043 053 052 +.004 +.040 +.051 +.045 +.044
ISSO F M A M J A SOND	.720 .744 .733 .739 .762 .723 .725 .714 .682 .683 .729	.7369 .7355 .7330 .7300 .7268 .7235 .7200 .7162 .7119 .7071 .7022 .6978	.7019 .7031 .7015 .7059 .7073 .7088 .7103 .7118 .7133 .7149 .7165 .7180	+.0350 +.0324 +.0285 +.0241 +.0195 +.0147 +.0044 0014 0014 0143 0202	+.011 019 +.007 +.007 047 065 078 012 +.038 +.061 +.053 +.049	1885 J F M A M J A S O ND	.669 .630 .653 .615 .609 .601 .589 .560 .533 .553 .604	.6702 .6515 .6333 .6160 .6029 .5920 .5841 .5792 .5771 .5778 .5812	.6829 .6816 .6804 .6794 .6784 .6765 .6758 .6758 .6758 .6747 .6742	0127 0301 0471 0625 0755 0854 0924 0966 0982 0969 0930 0866	+.002 027 003 016 043 051 045 +.046 +.042 +.049 +.043 +.043
I 881 J F M A M J J A S O N D	.711 .750 .738 .717 .655 .606 .675 .703 .716 .738 .748 .750	.6943 .6921 .6916 .6925 .6946 .6975 .7009 .7048 .7092 .7143 .7201 .7265	.7198 .7213 .7231 .7248 .7268 .7268 .7284 .7300 .7318 .7337 .7351 .7365 .7378	0255 0292 0315 0323 0323 0329 0291 0270 0245 0208 0164 0113	+.009 019 +.006 002 046 062 073 008 +.039 +.058 +.051 +.046	I886 J F M A J J A S O N D	.633 .621 .593 .647 .651 .633 .635 .706 .721 .734 .732 .734	.5963 .6077 .6206 .6345 .6484 .6618 .6743 .6861 .6973 .7083 .7192 .7299	.6739 .6738 .6739 .6741 .6744 .6748 .6755 .6761 .6768 .6777 .6787	0776 0661 0533 0396 0130 0112 +.0100 +.0205 +.0306 +.0405 +.0501	+.001 030 005 019 042 048 039 +.009 +.044 +.048 +.040 +.040

TABLE 23—Continued

Date	1	2	3	4	5	Date	1	2	3	1	5
ISST J F M A M J J A S O N D	.740 .714 .735 .752 .759 .756 .826 .792 .795 .758 .722 .737	.7400 .7492 .7571 .7634 .7680 .7711 .7726 .7725 .7708 .7672 .7614 .7535	.6808 .6822 .6835 .6849 .6863 .6881 .6897 .6916 .6934 .6954 .6974	+.0592 +.0670 +.0736 +.0785 +.0817 +.0830 +.0829 +.0774 +.07718 +.0640 +.0540	.000 032 007 021 042 046 +.011 +.046 +.048 +.038 +.041	IS92 J F M A M J A S O ND	.623 .604 .600 .559 .538 .514 .560 .580 .616 .667 .693	.6231 .6020 .5836 .5688 .5591 .5559 .5609 .5752 .5936 .6331 .6744 .7203	.7062 .7038 .7009 .6980 .6942 .6913 .6878 .6841 .6800 .6765 .6729	0831 1018 1173 1292 1351 1354 1269 1089 0804 0434 +.0015 +.0510	00 03 01 03 04 02 +.01 +.05 +.04
1888 JFM AM JJASOND	.749 .720 .725 .755 .725 .673 .640 .626 .675 .658	.7438 .7326 .7206 .7085 .6970 .6862 .6764 .6676 .6533 .6481	.7016 .7036 .7056 .7076 .7076 .7096 .7113 .7127 .7141 .7153 .7161 .7167 .7172	+.0422 +.0290 +.0150 +.0009 0126 0251 0363 0465 0554 0628 0686 0726	001 034 007 023 042 045 029 +.013 +.048 +.047 +.034 +.038	1893 F M A M J A S O N D	.712 .732 .829 .775 .861 .974 1.056 1.007 .860 .726 .626 .555	.7669 .8100 .8458 .8710 .8839 .8839 .8712 .8471 .8131 .7711 .7229 .6709	.6655 .6621 .6587 .6552 .6519 .6487 .6456 .6426 .6396 .6339 .6314	+.1014 +.1479 +.1871 +.2158 +.2352 +.2352 +.2256 +.2045 +.1735 +.1344 +.0890 +.0395	00 03 +.00 01 03 04 +.01 +.05 +.04 +.01
1889 JFM AM JJASOND	.669 .663 .660 .655 .627 .633 .670 .699 .672 .731 .747	.6432 .6442 .6477 .6535 .6611 .6798 .6896 .6992 .7079 .7162 .7236	.7174 .7173 .7171 .7166 .7159 .7152 .7145 .7136 .7129 .7121 .7114 .7109	0742 0731 0694 0631 0548 0451 0347 0240 0137 0042 +.0042 +.0127	002 035 007 023 042 044 026 +.015 +.051 +.031 +.031	J H M A M J A SO N D	.547 .554 .474 .503 .501 .511 .495 .469 .458 .395 .433 .456	.6184 .5683 5241 .4888 .4643 .4507 .4471 .4509 .4589 .4682 .4768 .4837	.6289 .6265 .6244 .6224 .6205 .6188 .6174 .6160 .6149 .6138 .6129	0105 0582 1003 1336 1562 1681 1703 1651 1560 1456 1361 1285	00 03 +.00 03 04 04 +.01 +.02 +.03 +.04 +.05
1890 JFMAM JJASOND	.730 .739 .747 .731 .745 .743 .726 .731 .707 .725 .802 .836	.7301 .7353 .7394 .7419 .7443 .7445 .7445 .7455 .7472 .7500 .7539 .7585	.7107 .7104 .7103 .7105 .7110 .7116 .7123 .7129 .7136 .7144 .7152 .7159	+.0194 +.0249 +.0291 +.0314 +.0323 +.0324 +.0326 +.0336 +.0356 +.0387 +.0426	002 037 007 023 041 044 023 +.016 +.053 +.046 +.027 +.029	1895 J F M A M J A S O N D	.496 .594 .582 .608 .473 .467 .486 .522 .547 .633 .604	.4893 .4949 .5018 .5107 .5219 .5354 .5506 .5673 .5816 .6075 .6316	.6115 .6109 .6103 .6097 .6091 .6087 .6081 .6074 .6056 .6056	1222 1160 1085 0990 0872 0733 0575 0401 0204 +.0019 +.0269 +.0550	00 03 +.01 00 01 +.01 +.05 +.04 +.05 +.06
1891 F M A M J J A S O N D	.769 .736 .724 .727 .771 .784 .769 .743 .706 .701 .681 .662	.7632 .7672 .7696 .7693 .7658 .7585 .7471 .7318 .7132 .6919 .6691	.7166 .7171 .7173 .7175 .7175 .7175 .7172 .7166 .7157 .7143 .7128 .7109 .7087	+.0466 +.0501 +.0523 +.0518 +.0483 +.0413 +.0305 +.0161 0011 0209 0418 0629	003 037 004 021 040 021 +.017 +.056 +.046 +.023 +.022	1896 J F M A M J A S O N D	.784 .799 .707 .729 .685 .679 .722 .876 .862 .876 .715 .569	.6878 .7167 .7428 .7635 .7761 .7793 .7733 .7591 .7384 .7135 .6862 .6575	.6028 .6016 .6006 .5996 .5987 .5978 .5971 .5965 .5959 .5957 .5956	+.0850 +.1151 +.1422 +.1639 +.1774 +.1815 1762 +.1626 +.1425 +.1178 +.0906 +.0619	00 00 +.01 00 02 03 +.01 +.02 +.04 +.00 +.00

TABLE 23—Continued

Date	1	2	3	-1	5	Date	1	2	3	4	5
1897 F M AM J A SOND	.526 .513 .510 .554 .575 .548 .551 .555 .557 .576 .514	.6284 .5909 .5732 .5498 .5318 .5207 .5176 .5225 .5342 .5502 .55677 .5841	.5957 .5960 .5965 .5972 .5982 .5998 .6006 .6018 .6022 .6028 .6034	+.0327 +.0039 0233 0474 0664 0783 0822 0781 0676 0520 0351 0193	006 036 +.012 006 027 054 +.020 +.016 +.056 +.046 +.015 +.005	1902 J F M A M J A S O N	.657 .637 .632 .666 .687 .704 .692 .683 .709 .728 .724 .735	.6526 .6573 .6625 .6682 .6747 .6817 .6891 .6967 .7042 .7114 .7181	.6742 .6752 .6760 .6767 .6771 .6775 .6776 .6775 .6773 .6771 .6767	0216 0179 0135 0085 0024 +.0042 +.0115 +.0192 +.0343 +.0414 +.0480	000 033 +.000 015 03 05 02 +.000 +.044 +.034 +.044
1898 J F M A M J A S O N D	.518 .531 .655 .766 .692 .566 .584 .548 .548 .561 .487 .502	.5969 .6047 .6075 .6055 .5996 .5793 .5660 .5518 .5317 .5253 .5164	.6039 .6039 .6037 .6035 .6031 .6024 .6016 .6007 .5995 .5985 .5974	0070 +.0008 +.0038 +.0035 0118 0223 0347 0477 0608 0721 0799	096 037 +.012 006 025 055 021 +.013 +.053 +.046 +.018 +.012	1903 F M A M J J S O N D	.712 .719 .747 .736 .711 .762 .764 .774 .740 .720 .736 .720	.7390 .7353 .7401 .7444 .7477 .7498 .7501 .7483 .7438 .7364 .7262 .7131	.6756 .6752 .6745 .6737 .6731 .6726 .6720 .6716 .6713 .6713	+.0544 +.0601 +.0601 +.0707 +.0776 +.0772 +.07781 +.0767 +.0725 +.0652 +.0549 +.0417	00: 03: +.00: 01: 03: 05: 02: +.03: +.04: +.04:
ISOO JF MA AM JA SOND	.468 .521 .576 .574 .581 .577 .585 .627 .644 .669 .712	.5130 .5163 .5268 .5439 .5662 .5911 .6161 .6389 .6575 .6709 .6792	.5953 .5946 .5940 .5936 .5932 .5935 .5939 .5945 .5955 .5966 .5984	0823 0783 0672 0497 0270 0024 +.0222 +.0444 +.0620 +.0743 +.0808 +.0821	006 037 +.011 007 025 057 022 +.011 +.050 +.046 +.022 +.019	1904 F M A M J A S O N D	.690 .710 .670 .629 .629 .612 .577 .590 .598 .597 .574	.6978 .6811 .6636 .6464 .6163 .6046 .5957 .5897 .5864 .5857	.6719 .6724 .6732 .6741 .6754 .6765 .6780 .6797 .6815 .6833 .6852	+.0259 +.0087 0096 0277 0450 0602 0734 0840 0918 0969 0995 0999	002 031 020 036 056 029 001 +.036 +.046 +.045
1900 F M A M J A S O N D	.699 .680 .679 .636 .594 .623 .629 .614 .591 .657 .616 .648	.6818 .6776 .6708 .6620 .6519 .6413 .6310 .6218 .6145 .6098 .6078	.6030 .6057 .6086 .6117 .6152 .6186 .6222 .6260 .6341 .6379 .6417	+.0788 +.0719 +.0622 +.0503 +.0367 +.0227 +.0088 0042 0157 0243 0301 0334	006 037 +.009 008 026 057 024 +.008 +.046 +.046 +.027 +.029	1905 F M A M J A S O N D	.600 .612 .596 .621 .639 .627 .644 .625 .639 .703	.5906 .5954 .6017 .6090 .6174 .6267 .6370 .6483 .6604 .6732 .6865	.6891 .6911 .6930 .6949 .6969 .6987 .7004 .7020 .7036 .7050 .7050 .7063	0985 0957 0913 0859 0720 0634 0537 0432 0318 0198 0080	00 02 03 05 02 00 +.03 +.04 +.04
1901 F M A M J A S O N D	.610 .603 .567 .610 .628 .652 .659 .649 .652 .621 .642	.6108 .6146 .6188 .6230 .6268 .6300 .6329 .6357 .6384 .6415 .6449	.6454 .6489 .6522 .6554 .6584 .6611 .6636 .6660 .6681 .6698 .6715	0346 0343 0334 0316 0311 0307 0303 0297 0283 0266 0244	005 036 +.007 011 029 057 026 +.005 +.042 +.042 +.032 +.037	1906 J F M A M J J A S O N D	.703 .729 .727 .759 .766 .771 .766 .776 .783 .753 .751	.7127 .7249 .7361 .7459 .7542 .7668 .7657 .7690 .7708 .7717 .7722	.7085 .7097 .7104 .7111 .7115 .7123 .7123 .7130 .7131 .7136 .7137 .7138	+.0042 +.0152 +.0257 +.0348 +.0427 +.0485 +.0529 +.0560 +.0577 +.0581 +.0585 +.0591	.000 02: 004 05: 05: 00: +.03: +.04: +.04: +.05:

TABLE 23-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1907 J F M A M J J A S O N D	.790 .800 .797 .798 .778 .785 .785 .795 .800 .805 .816	.7746 .7779 .7828 .7893 .7968 .8042 .8102 .8139 .8138 .8092 .7998 .7855	.7139 .7140 .7140 .7139 .7136 .7130 .7126 .7120 .7111 .7100 .7086 .7070	+.0607 +.0639 +.0638 +.0754 +.0912 +.0912 +.0916 +.1019 +.1027 +.0992 +.0712 +.0785	001 026 036 024 040 049 028 +.001 +.033 +.046 +.044 +.050	1912 J F M A M J A S O N D	.607 .599 .637 .640 .648 .626 .664 .682 .717 .739 .734 .749	.6112 .6193 .6281 .6375 .6475 .6582 .6696 .6817 .7077 .7213 .7346	.6740 .6768 .6794 .6816 .6840 .6855 .6868 .6879 .6887 .6887	0628 0575 0513 0441 0365 0273 0172 0062 +.0058 +.0188 +.0326 +.0465	016 025 015 023 026 024 009 +.017 +.028 +.034 +.023 +.029
1908 J F M A M J A S O N D	.813 .729 .762 .674 .608 .600 .552 .561 .563 .563	.7666 .7441 .7188 .6917 .6640 .6371 .6119 .5895 .5711 .5570 .5477	.7052 .7032 .7008 .6982 .6951 .6919 .6886 .6850 .6812 .6775 .6737	+.0614 +.0409 +.0180 0065 0311 0548 0767 0955 1101 1205 1266	002 025 008 025 039 047 026 +.004 +.033 +.046 +.042 +.047	1913 F M A M J A S O N D	.701 .714 .775 .763 .749 .786 .760 .738 .723 .728 .732	.7471 .7581 .7664 .7711 .7714 .7667 .7571 .7435 .7273 .7100 .6935 .6795	.6871 .6857 .6839 .6820 .6798 .6773 .6746 .6717 .6684 .6652 .6618	+.0600 +.0724 +.0825 +.0825 +.0916 +.0825 +.0718 +.0589 +.0448 +.0317 +.0213	019024015021021017005 +.018 +.026 +.030 +.017 +.023
1909 JF M A M J A S O N D	.575 .573 .554 .570 .574 .555 .551 .599 .589 .664 .665	.5427 .5457 .5514 .5588 .5675 .5770 .5873 .5989 .6117 .6261 .6419	.6654 .6617 .6579 .6543 .6543 .6472 .6441 .6412 .6382 .6389 .6339	1227 1160 1065 0955 0828 0702 0568 0423 0265 0098 +.0080 +.0265	004 025 010 026 037 043 022 +.007 +.032 +.045 +.039 +.043	1914 JF MAM JASOND	.677 .607 .599 .591 .605 .596 .648 .783 .805 .786 .729	.6689 .6622 .6594 .6599 .6631 .6679 .6734 .6784 .6817 .6822 .6786 .6698	.6548 .6509 .6475 .6440 .6405 .6371 .6337 .6302 .6267 .6267 .6235 .6203	+.0141 +.0113 +.0119 +.0159 +.0226 +.0308 +.0397 +.0482 +.0550 +.0587 +.0583 +.0527	021 022 015 018 016 009 001 +.021 +.023 +.021 +.011
1910 F M A M J A S O N D	.685 .673 .665 .702 .711 .730 .749 .724 .711 .703 .706 .629	.6752 .6906 .7038 .7135 .7137 .7191 .7202 .7173 .7105 .7006 .6885 .6750	.6306 .6294 .6286 .6282 .6283 .6287 .6295 .6303 .6317 .6335	+.0446 +.0512 +.0752 +.0853 +.0911 +.0919 +.0886 +.0810 +.0703 +.0568 +.0415 +.0252	008 026 012 025 034 038 018 +.011 +.032 +.042 +.034 +.034	1915 J F M A M J A S O N D	.607 .593 .543 .577 .582 .565 .510 .531 .498 .490 .470	.6556 .6362 .6126 .5868 .5611 .5377 .5187 .5050 .4969 .4935 .4939	.6140 .6110 .6083 .6057 .6031 .6008 .5986 .5967 .5949 .5935 .5921	+.0416 +.0252 +.0043 0189 0420 0631 0799 0917 0980 1000 10982 0946	022 019 014 014 011 003 +.002 +.018 +.018 +.018
1911 JF M A M J A S O N D	.612 .635 .605 .506 .589 .598 .590 .608 .626 .600	.6460 .6321 .6193 .6081 .5992 .5927 .5889 .5878 .5891 .5924 .5974	.6372 .6396 .6421 .6448 .6480 .6510 .6542 .6577 .6611 .6646 .6678	+.0088 0075 0228 0367 0488 0583 0653 0720 0722 0704 0672	011 026 014 024 030 032 013 +.014 +.030 +.039 +.039	1916 F M A M J J A S O N D	.516 .510 .505 .504 .500 .557 .596 .557 .516 .517 .541	.5001 .5038 .5078 .5120 .5168 .5227 .5299 .5383 .5478 .5582 .5692 .5807	.5904 .5898 .5897 .5909 .5909 .5918 .5953 .5953 .5953 .6002 .6034	0903 0860 0819 0780 0741 0634 0570 0495 0420 0342 0342	022 016 011 006 +.002 +.003 +.014 +.013 +.012 +.002

TABLE 23—Continued

COMMERCIAL PAPER RATES

Date	1	2	3	4	5	Date	1	2	3	4	5
IPIT F M A M J J A S O N D	.556 .624 .623 .638 .688 .698 .668 .670 .704 .722 .735 .734	.5930 .6061 .6202 .6351 .6508 .6668 .6826 .6978 .7118 .7244 .7355 .7451	.6105 .6151 .6197 .6246 .6305 .6364 .6425 .6491 .6562 .6632 .6705 .6780	0175 0090 +.0005 +.0105 +.0203 +.0304 +.0401 +.0487 +.0556 +.0612 +.0650 +.0671	016 012 008 007 004 +.002 +.011 +.010 +.009 +.002 +.006	I922 J F M A M J J A S O N D	.694 .690 .682 .605 .596 .587 .620 .640	6866 6688 6534 6409 6317 6259 6234 6241 6277 6339 6422 6520	.7483 .7432 .7383 .7329 .7273 .7220 .7167 .7111 .7056 .7002 .6947 .6893	0617 0744 0849 0920 0956 0961 0979 0779 07663 0525 0373	003 002 002 001 000 000 +.002 +.002 +.002 +.003
1918 JF M AM JASOND	.758 .763 .775 .777 .772 .768 .768 .766 .771 .772 .775 .760	.7533 .7602 .7658 .7701 .7730 .7743 .7741 .7722 .7690 .7645 .7591 .7530	.6859 .6935 .7015 .7093 .7170 .7248 .7322 .7395 .7468 .7536 .7601	+.0674 +.0667 +.0643 +.0608 +.0560 +.0495 +.0419 +.0327 +.0222 +.0109 0010 0135	012 009 006 005 003 +.001 +.002 +.008 +.007 +.001 +.001	1923 J F M A M J A S O N D	.667 .672 .703 .701 .710 .691 .695 .701 .708 .708 .707	6627 6737 6842 6940 7025 7094 7144 7170 7168 7135 7067 6961	.6840 .6787 .6734 .6683 .6631 .6581 .6533 .6486 .6440 .6397 .6355	0213 0050 +.0108 +.0257 +.0394 +.0513 +.0611 +.0684 +.0728 +.0738 +.0712 +.0647	002 002 001 001 001 000 +.001 +.001 +.001
1919 J.F.M.A.M.J.A.S.O.N.D.	.729 .720 .735 .735 .733 .742 .734 .726 .726 .739 .766	.7464 .7398 .7336 .7283 .7245 .7245 .7236 .7272 .7339 .7434 .7556 .7699	.7723 .7779 .7828 .7874 .7918 .7954 .7988 .8017 .8042 .8063 .8078 .8091	0259 0381 0492 0591 0673 0726 0752 0745 0703 0629 0522 0392	009 006 004 002 +.001 +.001 +.005 +.005 +.005 +.001	1924 J F M A M J A S O N D	.689 .680 .666 .666 .622 .599 .547 .511 .493 .493 .508	6820 6647 6451 6242 6031 5830 5650 5499 5386 5320 5294 5313	.6275 .6242 .6208 .6176 .6145 .6118 .6093 .6069 .6050 .6032 .6016	+.0545 +.0405 +.0243 +.0066 0114 0288 0443 0570 0664 0712 0722 0691	001 001 001 001 000 000 +.001 +.001 +.001 +.001
1920 J F M A M J A S O N D	.784 .811 .827 .837 .857 .887 .893 .899 .897 .900 .898 .895	.7859 .8030 .8207 .8384 .8554 .8711 .8849 .8960 .9039 .9082 .9086	.8101 .8107 .8111 .8111 .8105 .8100 .8091 .8077 .8062 .8045 .8024 .8001	0242 0077 +.0096 +.0273 +.0449 +.0611 +.0758 +.0883 +.0977 +.1037 +.1062 +.1050	006 005 003 003 002 +.001 +.004 +.004 +.003 +.001 +.002	1925 F M A M J A S O N D	.560 .560 .594 .596 .589 .589 .592 .599 .620 .641 .641	.5374 .5475 .5595 .5758 .5901 .6032 .6138 .6216 .6245 .6268 .6273 .6268	.5993 .5983 .5975 .5976 .5965 .5966 .5968 .5971 .5978 .5986 .5996	0619 0508 0380 0212 0066 +.0067 +.0172 +.0274 +.0274 +.0290 +.0287 +.0272	00 00 .00 .00 .00 +.00 +.00
1921 JF M A M J A S O N D	.898 .892 .884 .881 .842 .827 .772 .766 .747 .713 .707	.8981 .8880 .8753 .8607 .8444 .8269 .8083 .7888 .7685 .7477 .7267 .7061	.7974 .7947 .7916 .7883 .7843 .7806 .7766 .7722 .7676 .7628 .7581 .7532	+.1007 +.0933 +.0837 +.0724 +.0601 +.0463 +.0317 +.0166 +.0009 0151 0314 0471	005 003 002 002 001 +.001 +.003 +.003 +.003 000 +.002	1926 F M A M J J A S O N D	.638 .618 .631 .622 .605 .589 .596 .625 .643 .656 .647	.6260 .6252 .6247 .6245 .6244 .6243 .6243 .6244 .6246 .6250 .6253 .6254	.6007 .6023 .6041 .6061 .6081 .6107 .6135 .6164 .6195 .6229 .6264 .6302	+.0253 +.0229 +.0206 +.0184 +.0163 +.0136 +.0080 +.0051 +.0021 0011 0048	.000 .000 .000 .000 .000 .000 .000 .00

TABLE 23-Concluded

COMMERCIAL PAPER RATES

Date	1	2	3	4	5	Date	1	2	3	4	5
1927 J F M A M J J A S O N D	.622 .592 .602 .612 .616 .616 .609 .591 .592 .602 .594	.6247 .6229 .6197 .6151 .6095 .6034 .5976 .5930 .5904 .5904 .5932 .5990	.6341 .6377 .6416 .6456 .6457 .6534 .6572 .6604 .6637 .6664 .6692	0094 0148 0219 0305 0402 0500 0596 0674 0733 0760 0760	.000 .000 .000 .000 .000 .000 .000 .00	1932 J F M A M J J A S O N D	.602 .589 .547 .529 .477 .444 .408 .338 .326 .288 .241	.5319 .5373 .5373 .5309 .5130 .4852 .4500 .4112 .3726 .3371 .3066 .2826 .2651			.000 .000 .000 .000 .000 .000 .000 .00
JFM AM JA SOND	.589 .601 .622 .634 .658 .674 .707 .734 .747 .741 .731	.6076 .6185 .6311 .6451 .6597 .6745 .6891 .7031 .7162 .7284 .7394 .7493	.6739 .6757 .6773 .6784 .6791 .6796 .6798 .6795 .6790 .6783 .6770	0663 0572 0462 0333 0194 0051 +.0093 +.0236 +.0372 +.0501 +.0624 +.0739	.000 .000 .000 .000 .000 .000 .000 .00	1933 F M A M J A SO N D	.140 .140 .444 .408 .318 .228 .176 .176 .097 .097 .097	.2532 .2458 .2413 .2379 .2340 .2280 .2181 .2033 .1832 .1578 .1281 .0956			.000 .000 .000 .000 .000 .000 .000 .00
1929 J F M A M J A S O N D	.740 .745 .755 .769 .778 .778 .778 .784 .787 .787 .783 .699	.7581 .7658 .7723 .7774 .7808 .7819 .7800 .7745 .7648 .7506 .7318 .7090	.6738 .6716 .6692 .6666 .6638	+.0843 +.0942 +.1031 +.1108 +.1170	.000 .000 .000 .000 .000 .000 .000 .00	1934 F M A M J J A S O N D	.097 .086 .000 .000 046 125 125 125 125 125 125 125	.0623 .0300 0002 0273			.000 .000 .000 .000 .000 .000 .000 .00
1930 F M A M J J A S O N D	.690 .665 .613 .589 .566 .537 .498 .477 .477 .477 .473	.6832 .6557 .6278 .6009 .5756 .5520 .5297 .5077 .4853 .4620 .4379 .4141			.000 .000 .000 .000 .000 .000 .000 .00	1935 F M A M J A S O N D	125 125 125 125 125 125 125 125 125 125 125 125 125				.000 .000 .000 .000 .000 .000 .000 .00
1931 F M A M J J A S O N D	.450 .398 .403 .380 .326 .326 .274 .274 .525 .602	.3918 .3731 .3600 .3538 .3554 .3652 .3826 .4063 .4343 .4642 .4926 .5161			.000 .000 .000 .000 .000 .000 .000 .00	1936 J	125				.000

TABLE 24

Commercial Paper Rates in Boston Monthly 1831-1860

(From Joseph G. Martin's "Seventy-three Years' History of the Boston Stock Market" pages 37 and 38. Martin's table is preceded by the statement that "the following rates are for first-class, three to six months, bankable paper. Loans 'on call' range from 1 to 3 per cent lower." Martin's table goes to 1871. In his later volume "One Hundred Years' History of the Boston Stock Market" it is continued through 1897.)

1831.—Jan., 51/2 per cent, and gradually rose to 7, the rate for last four months of year.

1832.—Opened at 7 per cent; declined to 6 in March; rose to 7 in

May; thence for the year, 6 per eent.

1833.—Opened at 6 per cent; declined to 51/2; rose to 61/2 and to 8, July, Aug., and Sept.; to 10, Oct.; 12, Nov., and 15, Dec.

1834.—In Jan., 15 to 24 per cent; then high and variable, and fell

in Dec. from 10 to 8 per cent. Called a "panic year."

1835.—Rates low, and down to 5 per cent; but elosed in Dec. at 8 to 10. Called the "golden year" for business.

1836.—Opened at 10 per cent; up to 12 in March; 15, April; 18, May; up to 24, Aug. and Sept.; 36, Oct., and 24 to 30, Nov. and Dec.

1837.—Opened at 16 per cent; advanced to 20, and receded to 13; up to 18 in Feb.; 27, March; 30, April; 32, May; then fell rapidly to 6 in June; advanced to 71/2; fell to 6 in Nov., and rose to 10 in Dec. Banks suspended May 10; resumed May, 1838.

1838.—Jan., 11 per cent; Feb., 12; March and April, 12 to 18; fell in May from 10 to 7; thence, 6 to 7 till Dec., and closed at 7 to 9 per cent. 1839.—Opened at 6 to 9, and stationary till July, when it advanced

to 11 and 12; in Aug. to 15; Sept. to 21; Oct. to 30; Nov. to 36, and then rapidly fell to 9 per cent at the close of year.

1840.-Jan., 9 per cent; Feb. and March, 9 to 12, and fell in April

to 7; May, 7; June, 6 to 8; July, fell to 5, and ranged at 6 to 7 for remainder of the year.

1841.—At 6 to 7 per cent till May; then 6 till Sept., and 61/2 to 7, up to 9, in Nov., and 9 to 12 in Dec.

1842.—At 9 to 12 till April; then 8 to Aug.; Sept., 7; declined to

6 in Oct. and Nov., and thence 6 to 9 per cent to close of year. 1843.—Opened at 6 per cent; then 5 to 6 till May; declined in May

to 4½, and 3 in June; "exceptional loans" made as low as 2½; thence 3½ to 4 per cent.

1844.—Opened at 4 per cent; rose to 5 in March, and remained for the year with little change from 5 per cent.

1845.—Opened at 5 per cent, and ranged from 5 to 6 till Aug., and rose to 8 in Nov. and Dec.

1846.—Opened at 8 per cent; rose to 9 in Feb.; declined to 7 in March; thence ranged from 8 and 9 to 12, up to Aug. In Aug., 8 to 9; declined to 6 in Sept.; thence 6, 7, and 8 per cent.

1847.—Opened at 8 per cent; advanced to 12 in Jan. and Feb.; 8 to 10 in March; fell to 6 in June; advanced to 9 and 12 in Oct.; 15 in

Nov., and 18 in Dec.

1848.—Jan., 18 per cent; Feb., 18 to 12; March and April, 12 to 15; May and June, 15 to 18; July and Aug., 12 to 15; Oct., 18; Nov., 18 to 15; Dec., 15 to 12.

1849.—Jan., 12 per cent; Feb., 9 to 12; March and April, 12 to 15; May, 9 to 11; declined to 7 in June; July, 8; Aug., 7½ to 8½; Sept., 9;

Oct., 9 to 10, reaching 10½ in Dec.

1850.—Jan., 9 to 10½ per cent; Feb. and March, receded to 8 and 9; April, May, and June, 7 to 8½; fell to 6½ in July; rose to 9 in Sept.; thence, 7 to 8 per cent.

1851.—Opened at 6 to 7½ per cent; advanced to 7 and 8½ in Feb. and March; April, 8; fell to 6½ in May, and rose to 11 in July and Aug.;

15 in Sept.; and 16, Oct.; thence 9 to 12 per cent.

1852.—Opened at 9 per cent; fell to 714 in Feb.; March, April and May, 6, and $5\frac{1}{2}$ the Summer months. In Sept., 6 to 7; thence, 6 per cent.

1853.—Opened at 6 per cent; advanced to 8, and gradually to 12 in March; fell to 8 in May; then at 9 to 10 in June and July; rose to 12 in Sept.; 15, Oct.; 18, Nov., and fell to 9, Dec.

1854.—Opened at 9 per cent; fell to 7 in Feb.; rose to 10 in March, and 12, April and May; fell to 9 in June; July, 9 to 10; Aug., 12; and

10 to 12, up to 18, in Dec.

1855.—Opened at 15 per cent; fell to 10, and in March to 7; rose to 10 in April; fell to 6½, May; up to 8, and fluctuated from 6 to 8, till Oct.; in Oct., 9, and thence 10 to 15 per cent.

1856.—Opened at 10 to 12 per cent; Feb., 9 to 10; March, 7 to 9;

thence till Nov. at 9 to 10, and in Dec., 10 to 11 per cent.

1857.—Opened at 9 to 10 per cent; Feb., 8½ to 9; March, 9 to 10, and fell to 7 and 8 in April and May; June, July, Aug., 9 to 10, and rose in Sept. from 12 to 36; Oct., 24 to 36; Nov., 15 to 24; Dec., 9 to 15. Banks

suspended Oct. 13, and resumed Dec. 12.

1858.—Jan., 7½ to 9 per cent; fell to 5½ in Feb., to 5 in March, and 4½ in April; thence, 4½ to 4 in Sept. In Aug., "call loans" reported at 2½ in New York, and leading bankers said to be purchasing their own paper at two per cent. Prominent sixty days' acceptances passed at 3 per cent. Oct. and Nov., 4; Dec., 5 per cent.

1859.—Jan., 5 to 6 per cent; Feb., March, and April, 51/2 to 7;

May, $6\frac{1}{2}$ to 8; June to Nov., 7 to 8; Dec., 7 to $8\frac{1}{2}$ per cent.

1860.—Jan. and Feb., 7½ to 9½ per cent; March, 6 to 8; April and May, 6 to 7; June, 5 to 7; July, 5 to 6½; Aug., 6 to 9; Sept., 6½ to 9; Oct., 6½ to 7½; Nov., 7 to 15; Dec., 12 to 18 per cent; the money market being disturbed by the Government as a constant borrower, and the threatening aspect of political matters South.

TABLE 25

COMMERCIAL PAPER RATES IN BOSTON MONTHLY 1831-1860

(From Erastus B. Bigelow's *The Tariff Question* Appendix Table No. 112. Bigelow describes these rates as "street rates on first class paper in Boston.....at the beginning, middle, and end of the month." Both figures and comments are Bigelow's.)

-										
1831 J F M A M J J A S O N D	51-1-1-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2		1834 S O N D 1835 J F M A	tively low 15	10	8	1838 M A M J J A S O N D	10	12 18 9 7 6 6 6 6	18 12 7 6 6 7 7 7
ND 1832 JF MA AM J AA SO ND	7 7 6) <u>2</u> 6, <u>1</u> ,2 7 6 6 6 6 6 6		1835 J F M A M J A S O N D 1836 J F M	Rates comparatively low	8	10 10 10 12	1839 J F M A M J J A S O N D	15 20 18	6 6 6 6 6 11 12 18 21 33 15	9 9 9 9 9 9 12 15 21 30 36
N D 1833 J F M A A M J J A S O N 10 D 12	6 6 6 5 5 5 6 6 6 8 8 8 10 12 15		1836 J F M A M J J A S O N D	16	12 15 15 15 18 24 24 24 24	10 12 15 18 12 18 24 24 36 30 30	1840 J F M A M J J A S O N D	10	9 9 12 6 8 5 6 6 6	9 12 12 7 7 8 5 7 7 7 7
	8 10 12 2 15		1837 J F M A M J A S O N D	16 15 18 27 18	20 21 20 26 27 9	13 18 27 30 32 6 71/2 61/2 9				
1834 J 1 F M 8 M 1 M 1 M 1 M 1 M 1 M 1 M 1 M 1 M 1	unsettled Rates high and	24			7½ 6		1841 J F M A M J J A S O		6 6 6 6	7 7 7 7 6 6 6 6 7 7½
J A	u Rate varia		1838 J F			11 12	S		6 6	7 7⅓

TABLE 25-(Continued)

1841 N D	6 9 9 12	1845 N 6 D	5½ 8 8	1849 N D	8 10 9½ 10½
1842 J F M A M J J A S O N D	9 12 9 12 9 12 8 8 8 7 7 61/2 6 6 9	1846 J F M A J J S O O E N	8 9 8 7 9 12 8 12 12 9 9 66 6 7 6 7	1850 J F M A M J J A S O N	9 101/2 9 8 8 9 81/2 81/2 81/2 81/2 81/2 71/2 8 8 61/2 7 7 8 8 7 8 8 7 8 8 7 8 8 8 8
1843 J F M A M J J A S O N D	6 5 5 5 4 1 4 4 3 1 2 4 4 3 1 2 4 4 3 1 2 4 4 3 1 2 4 4 4 3 1 2 4 4 4 3 1 2 4 4 4 3 1 2 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	1847 J F M A J J A S O N D	8 12 8 10 8 9 7 6 7 6 7 9 9 12 12 15 12 18	1851 J F MI A MI J A S O N D	7 9 12 15 16 12 9 12 9 12
1844 J F M A M J A S O N D	4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	1848 J F 18 M A M J J J A S 2 S 0 O D	18 15 12 12 15 15 15 15 18 15 18 15 18 12 15 12 15 15 18 12 15 12 15 15 18	1852 J F M A J J A S O N D	9 8167 7 7 6 6 6 5 5 1 2 6 6 6 6 6 6 6 6 6
1845 J F M A M J J A S O	51/2 6 51/2 6 51/2 6 51/2 6 51/2 6 51/2 6 6 51/2 6 6 51/2 6 6 51/2 6 6 6 51/2 6 6 6 51/2 6 6 6 51/2 6 6 6 51/2 6 6 6 51/2 6 6 6 51/2 6 6 6 6 6 6 7 8 8 8 8 8 8 8 8 8 8 8 8 8	1849 J F M A M J J A S O	9 12 12 15 12 15 12 15 9 11 7 9 7½ 87 9 10	1853 J F M A M 7 J J 4 S O	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

TABLE 25-(Concluded)

1853 N 15 D 12 1854 J	18 10 9 7	12 9 8 9	1856 M A M J J A S O N D		9 7 7 7 7 8 9 9	10 8 8 8 8 8 8 9 10 10	1858 A S O N D	4 4 41/2 41/2 5	4 4 4 ¹ / ₂ 4 ¹ / ₂ 5	4 4 4 1/2 5
1854 J F M 9 A M J J A S O N D	9 7 8 10 10 9 10 10 10 12 10	8 9 10 12 12 11 9 9 12 10 12 18					1859 J F M A M J J A S O N D	5 1/2 5 1/2 6 1/2 7 7 1/4/4 6 3/4/4 7 1/2	5 6 5 5 1 2 2 3 1 4 8 6 7 7 7 7 7 7 7 7 7 8	51/2 51/2 51/2 51/2 7 7 7 7 7 7 7 7 7 7 7 7 7
D 1855 J F M A M J J A S O N D	15	10 10	1857 J F M A M J J A S O N D	12 36 24	9 8½ 9 8 8 7 9 24 24 18	10 9 10 9 7 8 10 10 36 24 15 9		•		
J S O N D 1856 J F	7 8 61/2 7 6 7 7 7 7 10 12	7 8 8 9 12 15	1858 J F M A M J J	9 6 5 4 4 4 4 4 4 4 4 4	8 6 5½ 4½ 4½ 4½	7 1/2 5 1/2 4 1/2 4 1/2 4 1/2	1860 J F M A M J A S O N D	8 8 6 5 4 1 2 5 1 2 6 6 5 1 2 6 6 5 1 6 1 6 1 6 1 6 1 6 1 6 1 6 1 6 1	9 7 6 334 4 1/2 5 1/2 5 5 1/2 9 15	81/2 61/2 5 41/3 41/3 51/2 6 6 51/2 6 12 12

TABLE 26

AVERAGE MONTHLY¹ RATE ON 90-DAY PRIME BANKERS' ACCEPTANCES

	19182	1921	1924	1927	1930	1933
J M A M J A S O N D	4.00 4.12 4.25 4.25 4.25 4.25 4.25 4.25 4.25 4.31 4.31	5.94 5.97 5.98 5.67 5.69 5.59 5.25 5.00 4.94 4.49 4.27 4.16	4.09 4.07 4.04 3.95 3.29 2.45 2.01 2.33 2.37 2.89	3.69 3.69 3.63 3.63 3.63 3.50 3.13 3.13 3.25 3.25 3.25	3.96 3.77 3.07 2.91 2.48 2.09 1.88 1.88 1.88 1.88	.33 .47 2.49 .81 .50 .38 .48 .45 .25 .25 .39
	1919	1922	1925	1928	1931	1934
J M A M J A S O N D	4.25 4.25 4.25 4.25 4.25 4.25 4.26 4.28 4.25 4.25 4.25 4.95	3.95 4.00 3.73 3.32 3.18 3.07 3.00 3.12 3.72 4.00 4.00	3.00 3.08 3.25 3.14 3.17 3.25 3.25 3.27 3.50 3.50 3.50	3.36 3.51 3.52 3.81 3.94 4.05 4.32 4.62 4.50 4.50 4.50	1.58 1.39 1.50 1.43 1.01 .88 .88 .98 .98 2.47 2.99 3.00	.50 .50 .31 .20 .19 .19 .19 .19 .19 .17 .13
	1920	1923	1926	1929	1932	1935
J M A M J A S O N D	5.37 5.50 6.00 6.00 6.13 6.25 6.25 6.25 6.25 6.25 6.25 6.25	3.98 3.99 4.00 4.14 4.13 4.13 4.13 4.13 4.13 4.13 4.13	3.67 3.63 3.63 3.42 3.20 3.32 3.38 3.57 3.88 3.79 3.88	4.84 5.15 5.34 5.46 5.48 5.49 5.16 5.13 5.13 5.01 4.23 3.90	2.85 2.78 2.51 1.39 .92 .86 .75 .75 .75 .59	.13 .13 .13 .13 .13 .13 .13 .13 .13 .13

¹These rates are monthly averages of daily quotations for the month.

²Rates for 1918 are 'Prevailing Rates' calculated at the Federal Reserve Bank of New York. Monthly averages of daily quotations are not available before January 1919.

TABLE 27

Bank Clearings, Pig Iron Production and Wholesale Prices

PART I

Bank Clearings in New York City, October 1853 - December 1874 (daily averages—thousands of dollars)

- Col. 1 Bank Clearings in New York City, January 1875-January 1919; Bank Debits in New York City, January 1919-January 1937 (daily averages—thousands of dollars)
- Col. 2 Deflated¹ Bank Clearings Outside New York City, January 1875-January 1919; Deflated Bank Debits for 140 Outside Cities, January 1919-January 1937 (daily averages—thousands of dollars)
- Col. 3 Bank Clearings Outside New York City, January 1875-January 1919; Bank Debits for 140 Outside Cities, January 1919-January 1937 (daily averages—thousands of dollars)
- Col. 4 Pig Iron Production in the United States, January 1877-January 1937 (daily averages—thousands of gross tons)
- Col. 5 Carl Snyder's Index of General Price Level, January 1875– January 1937
- Col. 6 United States Bureau of Labor Statistics Index Number of Wholesale Prices of Commodities, January 1890-January 1937.

Deflated by Carl Snyder's index of general price level.

²Estimated by chaining monthly totals, making the percentage movement from each December to the immediately succeeding January be the same as the percentage movement of the totals of the largest number of cities whose clearings were available for the December and the January.

³These figures do not include charcoal pig iron. Monthly figures for 1877-September 1901 were estimated from weekly capacity of furnaces in blast.

TABLE 27 PART I BANK CLEARINGS IN NEW YORK CITY

	27/1.1	K CEBAILINGS	IN IVEW TORK	7111	
1853 J F M A M J A S O N D	11,381 15,688 15,530	1857 J F M A M J A S O N D	21,854 23,769 24,221 25,509 24,856 23,996 23,506 21,573 16,062 9,954 10,716 10,878	1861 J F M A M J A S O N D	16,962 17,009 17,104 17,467 14,239 12,273 12,837 11,861 12,834 16,646 16,615 15,823
1854 J F M A J J A S O N D	15,008 16,008 17,095 17,064 18,742 17,579 15,137 14,789 15,139 15,451 14,904 13,773	1858 J F M A M J J A S O N	11,057 12,731 14,851 14,707 15,206 14,502 13,917 13,455 14,452 16,896 17,850 17,015	1862 J F M A M J A S O N D	14,546 15,601 17,197 22,539 22,052 23,088 20,257 25,537 34,888 29,215 29,793
1855 J F M A M J J A S O N D	13,781 13,681 17,623 14,711 15,744 15,507 14,150 14,750 15,425 17,971 18,457 17,838	1859 J F M A M J A S O N	16,548 17,682 18,872 20,382 20,170 17,171 15,596 15,968 17,926 18,619 19,226 18,826	1868 J F M A M J J A S O N D	39,869 42,832 42,155 30,581 49,201 40,785 40,645 44,491 52,850 62,167 58,950 57,202
1856 J F M A M J A S O N D	17,556 18,764 17,981 20,114 21,452 18,923 19,244 17,667 20,520 22,643 23,167 22,822	1860 J F M A M J J A S O N D	18,952 18,936 21,149 20,963 21,809 19,222 18,910 19,909 20,541 24,221 22,163 15,304	1864 J F M A M J A S O N D	57,107 72,006 88,817 88,158 60,569 63,401 57,347 57,291 69,425 68,531 80,682 78,189

TABLE 27—(Continued)
PART I

-	BAN	k Clearings	IN NEW YORK	JITY	
1865 J F M A M J J A S O N D	83,596 77,356 78,351 51,010 70,397 67,842 68,809 66,225 61,827 82,425 75,193 63,932	1869 J F M A M J A S O N	90,562 92,818 106,585 112,583 116,750 115,208 97,592 81,669 111,103 83,277 83,504 77,455	1873 J F M A M J A S O N D	102,428 113,816 106,062 109,517 89,665 76,901 66,704 78,598 50,139 49,927 63,357
1866 J F M A M J J A S O N D	76,722 71,126 82,195 79,092 87,979 87,981 74,395 81,571 81,060 111,500 115,803 81,344	1870 J F M A M J J A S O N D	76,236 72,649 76,204 73,624 88,642 76,820 82,921 60,488 61,718 69,871 71,004 79,787	1874 J F M A M J J A S O N D	73,673 65,797 68,211 73,658 64,952 66,368 61,424 50,268 64,075 73,286 69,343 72,844
1867 J F M A M J J A S O N D	78,541 67,325 68,338 70,713 71,544 64,479 71,823 62,936 74,780 79,783 78,078 64,927	1871 J F M A M J A S O N	73,603 69,115 90,485 100,267 94,817 93,915 63,393 67,489 89,585 96,795 78,987 88,429		
1868 J F M A M J J A S O N D	82,613 82,665 87,106 83,275 73,314 81,547 73,268 75,138 77,647 109,223 106,118 89,817	1872 J F M A M J A S O N D	97,114 84,854 100,190 118,178 109,505 83,210 72,241 86,032 93,664 125,061 113,184 108,528		

BANK CLEARINGS, PIG IRON AND PRICES A255

TABLE 27—(Continued)

Date	Clear. N. Y.	Def. Cl. outs. N. Y.	Clear. outs. N. Y.	4 Pig Iron	5 Snyder's Prices	B. of L. Prices
1875 J F M A M J J A S O N D	74,771 69,180 73,398 75,580 70,667 71,148 63,997 50,041 59,765 62,576 63,700 64,903	33,118 31,447 35,643 32,452 31,736 36,340 30,553 31,793 29,520 33,043 36,970 33,113	30,800 20,246 33,148 30,180 29,197 33,433 27,803 28,932 26,863 29,739 35,573 29,471		93 93 93 93 92 92 91 91 91 90 89	
1876 J F M A J J A S O N D	65,211 65,210 62,152 55,490 57,309 55,075 48,948 50,461 57,329 65,040 59,195 62,908	35,727 32,433 36,067 30,394 32,369 34,583 30,041 32,292 30,267 33,709 36,992 34,576	31,797 28,541 31,739 26,747 28,161 30,087 25,835 27,771 26,030 28,990 31,813 29,735		89 88 88 87 87 86 86 86 86	
1877 J F M A M J J A S O N D	68,563 69,556 63,897 68,174 63,720 61,244 60,332 61,868 61,571 73,369 64,647 65,800	34,241 32,691 33,586 31,282 35,373 29,889 29,831 30,215 31,301 35,029 37,622 34,107	29,790 28,114 28,548 26,590 29,713 25,107 25,058 25,381 25,980 29,074 30,850 27,968	4.71 4.78 4.83 4.85 4.80 4.72 4.70 4.74 4.84 5.00 5.20 5.43	87 86 85 85 84 84 84 83 83 83 83 82 82	
1878 J F M A M J A S O N D	64,971 53,924 59,963 67,364 60,646 57,211 59,666 56,542 55,074 71,310 67,841 61,307	39,237 30,962 29,175 30,272 32,790 29,796 33,359 28,121 31,966 38,730 33,725 32,625	32,174 25,079 23,632 24,520 26,232 23,837 26,687 22,497 25,573 30,984 26,980 25,774	5.70 5.90 5.98 5.90 5.76 5.63 5.45 5.32 5.25 5.32 5.32 5.40 5.47	82 81 81 81 80 80 80 80 80 80 80	

TABLE 27—(Continued)

	PARI II										
Date	Clear. N. Y.	Def. Cl. outs. N. Y.	Clear. outs. N.Y.	4 Pig Iron	5 Snyder's Prices	B. of L. Prices					
1879 J F M A M J A S O N D	70,985 68,296 60,836 68,341 78,838 63,088 65,669 74,290 76,938 114,187 117,142	37,208 34,001 31,658 37,772 34,724 35,392 38,325 31,715 35,541 50,435 46,444 45,099	29,394 26,861 25,010 29,840 27,432 27,960 30,277 25,055 28,433 40,348 37,620 36,981	5.51 5.54 5.58 5.63 5.74 5.98 6.40 6.84 7.31 7.83 8.33 8.33	79 79 79 79 79 79 79 79 80 80 81 82						
1880 J F M A M J J A S O N D	104,572 100,868 111,972 112,520 197,501 97,803 83,984 77,412 80,841 104,520 135,766 139,434	47,898 43,294 44,270 44,925 41,788 41,241 41,228 39,239 40,735 45,350 51,354 53,111	39,755 35,934 37,187 37,737 34,684 34,239 34,219 32,568 34,217 38,094 43,137 44,613	9.25 9.59 9.75 9.74 9.50 9.07 8.60 8.45 8.89 9.15 9.42	83 84 84 83 83 83 83 83 84 84 84						
1881 J F M A M J J A S O N D	152,117 155,455 135,559 123,535 157,457 140,538 125,335 114,704 113,833 138,103 129,956 137,633	51,359 40,214 47,154 49,208 52,516 53,156 47,002 52,779 53,860 58,821 56,920 56,940	43,655 41,832 40,081 41,827 44,633 49,433 39,952 45,390 46,320 51,174 49,520 48,963	9.71 9.93 10.03 9.97 9.80 9.64 9.44 9.51 9.69 9.95	85 85 85 85 85 85 86 86 87 87						
1882 F M A M J J A S O N	139,159 126,737 143,950 130,254 103,850 111,563 114,336 120,181 131,573 141,442 151,028 125,641	53,852 49,543 49,033 50,663 50,386 51,453 51,001 48,357 52,872 56,144 58,267 54,744	46,813 42,607 42,168 43,570 43,332 44,250 43,861 41,587 45,470 48,284 49,527 46,532	10.93 11.34 11.25 11.03 10.80 10.57 10.30 10.24 10.48 11.15 11.56 11.83	86 86 86 86 86 86 86 86 86 86						

TABLE 27--(Continued)

PART II

Date	Clear. N. Y.	Def. Cl. outs. N. Y.	Clear. outs. N. Y.	4 Pig Iron	5 Snyder's Prices	B. of L. Prices
1883 J F M A M J A S O N D	106,738 107,058 99,838 102,846 103,388 100,401 88,881 96,168 101,400 123,604 96,329 104,202	56,626 52,008 51,799 50,768 53,818 55,964 52,281 50,517 51,590 59,316 56,880 57,188	48,132 44,207 44,029 43,153 45,745 47,010 43,916 41,929 42,820 49,232 47,210 46,894	12.00 12.02 11.88 11.49 11.18 11.08 11.04 10.98 10.92 10.77 10.62 10.38	85 85 85 85 85 84 84 83 83 83 83 83 83	
1884 J F M A M J A S O N D	109,125 102,336 92,747 96,744 107,394 79,890 70,320 66,122 68,549 76,479 69,864 76,739	57,041 51,720 50,860 55,675 56,035 49,163 48,258 44,210 47,159 53,246 49,801 54,324	46,774 42,410 41,197 45,097 45,384 39,330 38,606 35,368 37,727 42,597 42,597 39,343 42,916	9.94 9.67 9.82 10.22 10.45 10.59 10.74 10.23 9.85 9.90 10.09 9.44	82 82 81 81 80 80 80 80 80 79	
1885 J F M A M J A S O N D	70,496 67,884 64,928 62,266 64,446 64,077 76,648 65,842 70,048 102,895 110,632 104,464	53,765 46,392 46,570 50,895 48,371 52,667 53,127 45,827 50,747 60,363 61,570 62,319	42,474 36,650 36,790 40,207 37,729 41,080 41,439 35,745 39,583 47,687 48,640 49,232	9.05 9.80 10.10 9.90 9.71 9.60 9.84 9.90 9.80 10.23 11.20 12.10	79 79 79 79 78 78 78 78 78 79 79	
1886 J F M A M J J A S O N D	92,759 98,054 98,712 80,699 77,753 91,139 79,872 79,167 86,860 104,784 106,065 116,741	58,358 56,171 58,310 56,532 55,399 60,772 60,820 55,027 59,751 66,432 69,384 70,473	46,103 44,375 46,065 44,660 43,765 48,010 48,048 43,471 47,203 52,481 54,813 55,674	12.19 11.96 12.81 14.23 15.03 15.30 15.13 14.78 14.88 15.39 15.63 15.84	79 79 79 79 79 79 79 79 79 79	

TABLE 27—(Continued)

-	ī	Def. Cl.	3 Clear.	4 Pig	5 Snyder's	B. of L.
Date	Clear. N. Y.	outs. N. Y.	outs. N. Y.	Iron	Prices	Prices
1887 J F M A M J J A S O N D	95,571 88,331 91,495 101,096 90,024 98,848 83,717 80,449 89,429 96,095 97,727 88,399	65,426 62,738 68,673 70,228 69,306 75,744 66,468 62,751 67,017 72,486 75,785 70,984	51,032 48,936 54,252 55,480 54,752 59,080 51,845 48,948 52,273 56,530 59,870 56,077	16.26 16.54 16.71 17.03 14.65 12.13 12.97 15.42 17.57 18.35 18.47 17.97	78 78 79 79 79 78 78 78 78 78 78 79	
1888 J F M A J J A S O N	81,328 73,333 76,907 85,745 87,960 78,544 75,622 77,828 83,313 103,033 90,541 96,023	68,334 65,216 63,148 67,185 70,000 69,199 66,982 64,451 66,571 82,181 76,075 75,875	53,984 51,521 49,887 53,077 55,300 54,667 52,916 51,561 53,257 65,745 60,860 60,700	19.26 14.59 14.48 15.17 15.61 15.23 15.19 16.00 16.70 17.58 18.73 19.65	79 79 79 79 79 79 79 80 80 80 80 80	
1889 J F M A J J A S O N D	99,023 96,255 93,218 91,667 99,364 102,379 93,669 88,660 89,996 116,702 105,803 102,032	77,270 72,116 71,056 72,484 75,456 74,654 76,504 68,678 70,521 85,908 83,534 81,243	61,816 57,693 55,845 57,985 60,365 59,723 61,203 54,942 56,417 68,726 66,827 64,994	19.55 19.18 19.23 18.77 17.94 17.67 18.03 18.18 18.75 20.18 21.43 22.16	80 80 80 80 80 80 80 80 80 80 80	
1890 J F M A M J A S O N	105,625 100,767 91,062 97,453 122,211 105,258 91,392 95,488 103,067 115,050 111,699 92,499	85,823 78,139 78,649 85,250 91,460 86,621 86,399 79,476 85,066 97,113 93,275 83,913	08,658 02,511 62,919 68,200 73,168 69,297 69,119 63,581 68,053 77,690 73,687 68,661	22.67 23.23 23.77 24.02 24.24 23.92 22.94 22.65 23.49 23.85 24.07 23.07	80 80 80 80 80 80 80 80 80 80 79	54.7 54.8 55.0 55.1 55.6 55.4 55.7 57.8 58.4 58.1 57.1 56.6

TABLE 27—(Continued)

			PART II			
Date	1 Clear. N. Y.	Def. Cl. outs. N. Y.	Clear. outs, N. Y.	Pig Iron	Snyder's Prices	B. of L. Prices
IS91 J F M A M J J A S O N D	95,387 82,305 78,907 96,530 93,766 84,850 79,939 77,532 110,750 105,874 98,276 105,130	87,039 79,986 77,419 85,616 82,405 83,086 83,954 77,945 89,769 95,830 92,958 92,809	68,761 63,189 61,161 67,637 65,100 64,807 65,484 60,797 70,020 75,706 72,507 73,319	19.95 17.37 15.09 13.92 16.24 20.53 23.04 23.55 24.56 25.93 26.49 26.28	79 79 79 79 79 78 78 78 78 78 79	56.1 56.6 57.8 58.2 57.5 55.8 55.5 55.4 54.8 54.6 54.3 53.8
1892 J F M A M J A S O N D	114,471 111,637 105,182 102,517 96,134 93,568 83,173 81,749 92,616 99,306 106,041 116,202	91,078 91,096 87,958 89,848 88,584 94,971 89,020 86,268 90,794 101,249 103,667 104,324	71,952 71,966 69,487 70,980 69,981 75,027 70,326 68,152 71,727 79,987 81,897 82,416	25.81 25.86 25.55 24.47 23.42 22.93 22.07 20.99 21.20 22.62 23.84 23.95	79 79 79 79 79 79 79 79 79	52.7 52.4 51.6 50.5 50.8 50.7 51.9 52.4 52.5 53.0 54.0 55.0
1893 J F M A M J J A S O N D	114,886 109,532 104,861 93,545 98,564 87,530 77,207 63,162 61,373 71,915 75,228 71,466	102,532 95,710 94,301 96,368 97,973 87,658 78,514 62,542 68,825 80,568 84,991 84,099	81,000 75,611 73,555 75,167 75,439 67,497 59,671 47,582 52,807 61,232 64,593 63,074	23.54 23.76 24.33 24.70 24.45 22.57 17.95 13.01 10.65 10.49 12.45 13.99	79 79 78 78 77 76 76 76 76 76	56.6 57.2 56.2 55.6 55.0 53.2 51.9 50.3 52.0 51.2 50.4
1894 J F M A M J A S O N	69,857 61,573 66,090 67,278 67,521 63,286 59,465 60,374 62,168 73,597 74,716 75,365	85,088 73,891 76,847 79,343 82,250 80,388 76,386 77,323 78,328 91,639 91,104 90,288	63,816 55,418 57,635 59,507 60,865 59,487 56,526 57,219 57,963 67,813 67,417 66,813	14.16 15.10 17.20 17.21 12.44 10.61 14.43 19.11 21.56 22.36 23.50 23.70	75 75 75 75 74 74 74 74 74 74 74 74	49.6 48.6 47.5 47.3 47.0 47.2 47.5 48.3 49.6 48.2 47.5

TABLE 27—(Continued)

111111 11								
Date	Clear. N. Y.	Def. Cl. outs. N. Y.	Clear. outs. N. Y.	4 Pig Iron	5 Snyder's Prices	B. of L. Prices		
1895 J F M A J J A S O N D	77,248 66,587 72,282 79,116 91,415 82,695 81,538 74,736 79,100 94,633 86,440 93,868	91,809 78,118 82,009 88,923 91,325 89,284 91,815 82,172 84,013 103,901 100,036 99,011	67,939 57,807 60,687 65,803 68,494 66,963 68,861 61,629 63,010 77,926 75,027 73,268	23.09 22.14 21.62 21.45 21.35 22.44 24.31 26.47 28.35 30.12 31.21 30.37	74 74 74 75 75 75 75 75 75 75	47.2 46.9 47.2 49.6 50.1 50.4 50.0 49.5 49.0 49.4 49.0 48.3		
1896 J F M A J J A S O N D	\$2,659 \$1,828 74,718 79,782 75,487 80,479 80,013 63,586 68,768 84,317 89,562 85,675	93,418 84,278 82,750 89,239 85,972 88,405 86,990 72,992 78,178 90,166 90,347 93,409	69,129 62,366 61,235 66,037 63,619 65,420 63,503 53,284 57,070 66,723 66,857 69,123	28.81 27.33 26.43 26.30 25.76 24.89 22.96 19.33 16.13 15.85 18.14 20.73	74 74 74 74 74 73 73 73 74 74	48.0 47.5 46.9 46.7 46.0 45.5 45.1 45.3 46.6 48.1 47.6		
1897 J F M A M J A S O N D	83,527 73,040 77,004 74,902 74,682 85,718 91,417 94,738 115,078 107,614 104,048 115,754	\$6,696 \$2,384 \$2,785 \$7,068 \$4,093 \$9,149 \$9,638 \$6,308 97,747 102,431 106,193 106,211	64,155 60,964 61,261 64,430 62,229 65,970 66,332 63,868 73,310 76,823 78,583 79,658	22.36 23.24 24.07 24.30 24.12 23.71 23.40 24.78 27.18 29.22 30.80 31.59	74 74 74 74 74 74 74 75 75 75	46.7 46.3 45.8 45.5 45.0 45.3 47.1 48.5 48.1 47.9 48.1		
IS98 J F M A M J J A S O N D	119,042 125,580 110,258 95,631 101,465 108,862 96,033 113,283 113,799 114,137 132,454 150,076	103,824 100,795 99,480 98,572 98,008 103,257 91,264 93,101 96,303 107,208 114,070 119,414	77,868 75,596 74,610 72,943 73,506 77,443 68,448 69,826 72,227 80,406 86,693 90,755	31.65 31.96 32.16 32.00 31.39 30.53 29.65 29.55 30.37 31.58 32.90 33.61	75 75 75 74 75 75 75 75 75 76 76	48.0 48.6 48.8 48.9 51.8 48.3 48.0 47.8 47.8 47.8 47.8		

TABLE 27—(Continued)

PART II

Date	l Clear. N. Y.	Def. Cl. outs, N. Y.	Clear, outs. N. Y.	Pig Iron	Snyder's Prices	B. of L. Prices
1899						
J	183,572	121,496	93,552	33.59	77	48.9
J F	162,523	116,730	89,882	32.47	77	49.7
M	190,390	122,513	94,335	32.96	77	49.8
	185,897	119,688	93,357	34.40	78	50.6
A M J J	178,215	120,050	93,639	34.92	78	50.7
Ĵ	159,340	120,594	94,063	35.78	78	51.3
Ĵ.	142,592	113,884	89,968	36.71	79	51.9
A	140,592	108,734	85,900	37.16	79	53.0
A S O	146,665	116,756	92,237	38.11	79	54.6
õ	169,566	128,279	102,623	39.64	80	55.4
Ň	165,098	127,184	101,747	40.96	80	55.8
N D	172,525	125,960	100,768	41.42	80	56.7
1900						
J	150,470	122,067	98,874	41.52	81	57.0
F	140,948	112,814	91,379	41.51	81	57.3
M	155,983	114,353	92,626	40.96	81	57.3
	157,208	116,744	94,563	41.05	81	57.2
A J J A S O N D	144,427	116,130	94,065	41.48	81	56.1
J	129,140	118,300	95,823	40.45	81	55.5
J	114,571	110,832	89,774	36.55	81	55.8
A	102,719	104,694	83,755	32.82	80	55.7
8	105,217	105,909	84,727	31.32	80	56.1
0	147,620	124,799	101,087	30.22	81	55.3
N	190,135	127,796	104,793	30.76	82	55.4
D	191,843	126,928	104,081	33.38	82	55.1
1901		1				
J	238,745	134,323	110,145	37.43	82	55.2
F	200,843	122,752	100,657	40.42	82	54.7
M	222,157	126,262	103,535	41.14	82	54.5
A	287,896	141,248	115,823	41.75	82	54.4
M	300,820	140,152	116,326	43.00	83	54.1
J	228,693	134,205	111,390	43.65	83	54.1
J	196,191	131,434	109,090	44.10	83	54.5
A	159,017	122,363 120,792	101,561	43.42	83	55.4
S	168,238	120,792	100,257	43.67	83	56.1 56.1
0	191,952 $212,271$	143,339	118,971	$\frac{44.59}{45.40}$	83 84	56.6
A J J A S O N D	212,271	142,250	119,490	40.85	84	57.7
	203,735	138,054	115,965	40.80	04	31.1
1902	000 501	147 779	194 190	46.38	84	56.8
J	223,531	147,773	124,129 110,904	44.92	84	56.7
F	191,034	132,029		46.61	84	56.5
M	177,643	133,740	112,342 122,883	49.18	84	57.4
A	245,088	146,289	119,155	49.77	85	58.3
IVI	219,539	140,182	111,470	48.23	85	58.8
Į.	165,572	131,141	119,039	46.51	85	59.1
J	212,698	140,046	104,055	47.36	85	58.0
V.	187,643	122,418	115,307	47.29	85	58.7
Ď.	226,819	135,655 149,378	128,465	47.77	86	63.2
A M J J A S O N D	241,834	141,864	122,003	47.76	86	60.7
TA	217,976 $198,905$	143,901	123,755	49.59	86	61.5

TABLE 27—(Continued)

PART II							
Date	Clear. N. Y.	Def. Cl. outs. N. Y.	Clear. outs. N. Y.	4 Pig Iron	5 Snyder's Prices	B. of L. Prices	
1903 J F M A M J J A S O N D	231,810 187,186 193,684 198,146 179,839 191,550 192,832 150,472 143,049 168,816 153,597 177,343	150,210 135,944 136,129 144,663 136,384 146,183 143,623 125,337 134,520 151,763 141,659 146,163	129,181 118,271 118,432 124,410 117,290 125,717 123,516 107,790 115,687 130,516 121,827 125,700	47.51 49.67 51.31 53.61 55.28 55.77 49.88 50.68 51.79 45.99 34.65 27.31	86 87 87 86 86 86 86 86 86 86 86	62.6 62.0 60.3 60.0 59.0 58.6 58.8 59.5 58.7 58.3 58.2	
1904 J F M A J J A S O N D	183,598 152,752 154,967 159,988 156,221 152,350 167,560 150,181 178,490 241,189 277,922 274,224	144,513 135,477 138,117 140,337 130,187 139,073 133,751 129,317 139,108 153,875 164,241 162,255	124,281 116,510 118,781 120,690 111,961 119,603 115,026 111,213 119,633 133,871 142,890 142,784	29.80 41.67 46.82 52.04 49.58 43.19 36.16 37.83 45.26 46.94 49.55 52.13	\$6 \$6 \$6 \$6 \$6 \$6 \$6 \$6 \$6 \$7 \$7	59.7 60.7 60.5 59.3 58.5 58.4 58.5 59.2 59.8 59.9 60.7 61.1	
1905 J F M A M J J A S O N D	249,507 254,226 281,658 289,360 254,324 224,510 220,614 225,186 228,649 258,903 284,755 312,565	154,443 146,826 157,195 157,295 156,778 158,276 149,518 145,592 152,730 168,792 174,770 174,857	135,910 129,207 138,332 138,420 137,965 139,283 133,071 129,577 137,457 151,913 157,293	57.48 57.05 62.46 64.07 63.35 59.78 56.19 59.47 63.32 66.23 67.12 65.99	88 88 88 88 88 88 89 89 90 90	60.6 61.0 60.3 60.4 59.3 59.4 60.1 59.6 59.9 60.1	
1906 J F M A M J J A S O N	362,522 297,301 270,234 284,775 283,646 260,540 234,082 284,942 277,128 301,421 286,933 297,675	185,831 167,673 168,852 164,288 162,088 167,069 160,174 155,491 156,533 187,801 186,151 178,566	169,106 152,582 153,655 149,457 147,500 152,033 145,758 143,052 144,010 172,777 173,120 167,852	66.74 68.00 69.86 69.11 67.70 65.89 64.95 62.15 65.70 70.87 72.92 72.11	91 91 91 91 91 91 92 92 92 92 93 94	61.1 60.8 60.6 61.1 61.3 59.7 61.2 61.7 62.8 63.6 64.3	

BANK CLEARINGS, PIG IRON AND PRICES A263

TABLE 27—(Continued)

PART II

Date	1 Clear. N. Y.	Def. Cl. outs. N. Y.	Clear. outs. N. Y.	4 Pig Iron	5 Snyder's Prices	B. of L. Prices
1907 J F M A M J A S O N D	310,893 261,839 308,460 255,584 236,608 212,306 235,864 222,274 201,008 264,387 183,358 172,579	189,914 174,377 178,648 180,926 177,814 173,539 177,410 163,665 164,574 198,758 154,688 145,908	178,519 163,914 167,929 170,070 167,145 163,127 166,765 153,845 154,700 184,845 142,313 134,235	71.15 73.04 71.82 73.89 74.05 74.49 72.76 72.59 72.78 75.39 60.94 39.82	94 94 94 94 94 94 94 94 94 93 92 92	64.0 64.9 64.3 64.5 65.6 66.1 66.1 66.5 66.9 64.6
1908 J F M A M J A S O N D	217,751 165,829 177,453 182,919 215,156 188,462 213,486 200,811 226,083 233,364 273,034 298,912	105,060 147,740 154,757 158,232 140,902 155,942 161,148 144,004 160,141 175,375 177,040 181,117	151,855 135,921 140,829 145,573 137,910 141,907 146,645 132,484 147,330 161,345 162,877 168,439	33.72 37.16 39.62 38.32 37.60 36.40 39.29 43.87 47.30 50.56 52.60 55.16	92 91 92 91 92 92 91 91 92 92 92 92 92 93	62.3 61.4 61.8 62.2 62.2 62.6 63.1 63.0 63.3 63.5 64.1
1909 J F M A J A S O N D	286,590 245,961 241,510 287,158 201,169 303,728 268,379 280,208 282,612 324,269 302,121 319,572	181,769 170,269 180,673 184,534 170,868 181,359 179,183 167,879 180,161 200,371 201,479 203,105	169,045 158,350 168,026 171,617 160,616 170,477 168,432 157,806 171,153 190,352 193,420 194,981	57.99 60.98 59.10 57.96 60.75 64.36 67.85 72.55 79.51 83.86 84.92 85.02	93 93 93 93 94 94 94 95 95 96 96	64.6 64.9 65.2 66.2 67.3 67.8 67.9 68.2 68.9 70.2 70.9
1910 F M A M J A S O N	362,874 291,112 291,812 278,059 251,834 278,811 254,151 208,460 207,701 254,971 260,477 258,865	200,649 186,801 201,330 197,512 180,013 189,677 184,005 170,079 178,835 198,460 201,446 201,082	192,623 179,329 195,290 191,587 174,613 183,987 176,645 164,977 173,470 192,506 195,403	84.15 85.62 84.45 82.79 77.10 75.52 69.31 67.96 68.54 67.52 63.66 57.35	96 96 97 97 97 97 96 97 97 97 97	71.4 71.3 72.9 73.2 72.0 71.0 71.0 70.8 69.9 67.9 66.4 66.6

TABLE 27-(Continued)

	PART II							
Date	Clear. N. Y.	Def. Cl. outs. N. Y.	3 Clear. outs. N. Y.	4 Pig Iron	Snyder's Prices	B. of L. Prices		
1911 J F M A M J J A S O N D	275,202 260,541 245,858 232,328 256,730 273,884 242,446 233,199 239,499 242,285 269,129 261,671	201,371 184,068 195,518 189,604 187,950 193,972 185,594 176,405 187,209 200,389 206,020 202,232	193,316 178,546 189,652 182,020 180,432 188,153 180,026 171,113 181,593 196,381 201,900 198,187	56.75 64.09 70.04 68.80 61.08 59.59 57.84 62.15 66.57 67.81 66.65	96 97 97 96 96 97 97 97 97 97 98 98	66.1 64.4 64.7 63.3 63.0 63.9 65.5 66.1 65.9 65.9		
1912 J F M A M J J A S O N D	285,019 252,161 271,514 294,330 283,219 265,369 255,519 241,403 247,762 327,065 293,994 284,152	207,667 197,917 200,104 208,267 198,184 192,327 197,861 187,923 191,530 227,853 219,953 219,953	205,590 195,938 198,103 208,267 198,184 192,327 197,861 187,923 191,530 230,132 222,153 215,190	66.38 72.44 77.59 79.18 81.05 81.36 77.77 81.05 82.13 86.77 87.70 89.77	99 99 99 100 100 100 100 100 100 101 101	66.0 66.7 67.5 69.7 70.0 69.0 68.9 69.7 70.5 70.8 70.2		
1913 J F M A J J A S O N D	301,249 278,379 254,395 268,511 256,855 258,451 236,933 218,136 248,531 280,434 252,896 258,065	225.468 210,704 204,497 210,640 201,335 203,283 203,052 184,074 200,433 227,493 213,150 219,129	225,468 210,704 204,497 210,640 201,335 201,250 203,052 184,074 202,437 229,768 213,150 219,129	90.17 92.37 89.15 91.76 91.04 87.62 82.60 82.12 83.53 82.14 74.44 63.99	100 100 100 100 100 100 99 100 101 101 1	70.3 69.8 69.9 69.7 68.9 69.5 69.7 70.6 70.4 70.1		
1914 J F M A M J J A S O N	302,327 258,485 253,203 284,884 233,501 261,473 263,887 147,781 154,271 180,050 179,981 210,635	222,894 203,461 209,106 214,357 193,583 206,132 172,999 180,399 200,039 193,629 199,645	222,894 203,461 209,106 214,357 193,587 205,953 206,132 174,729 182,203 200,039 191,693 199,645	60.81 67.45 75.74 75.67 67.51 63.93 63.15 64.36 62.75 57.36 50.61 48.90	100 100 100 100 100 100 100 101 101 101	68.6 68.3 68.0 67.6 67.4 67.4 67.3 69.6 70.2 68.0 67.5		

TABLE 27—(Continued) PART II

			1 11161 11			
Date	Clear. N. Y.	Def. Cl. outs. N. Y.	Clear, outs. N. Y.	4 Pig Iron	5 Snyder's Prices	B. of L. Prices
1915 J F M A M J A S O N D	235,086 231,494 244,036 293,725 278,553 267,516 280,498 275,401 320,812 410,957 394,314 397,779	202,003 196,018 204,858 206,858 193,414 203,366 199,267 181,497 198,846 225,849 237,897 240,887	202,003 196,018 204,858 208,927 195,348 205,400 203,252 186,942 206,800 241,658 254,550 260,158	51.66 59.81 66.58 70.55 73.02 79.36 82.69 89.67 95.09 100.82 101.24 103.33	100 100 100 101 101 101 101 102 103 104 107 107	68.1 68.6 68.2 68.7 69.0 68.3 69.3 68.6 68.3 70.2 71.7 74.0
1916 J F M A M J A S O N D	397,639 382,991 404,770 387,420 405,191 418,451 368,992 379,591 478,531 506,813 555,112 546,310	229,516 223,653 234,419 227,120 231,307 235,235 224,477 222,272 236,522 265,312 269,323 263,589	252,468 248,255 264,854 258,917 263,690 270,520 258,148 260,058 283,827 323,681 339,347 334,758	102.75 106.46 107.67 107.59 108.42 107.05 104.02 103.35 106.75 113.19 110.39 102.54	110 111 113 114 114 115 115 117 120 122 126 127	77.0 78.5 80.4 81.7 82.5 82.9 83.4 85.1 86.9 91.1 97.4
1917 F M A M J A S O N D	487,979 456,931 459,004 488,408 502,691 569,969 489,849 473,526 462,797 507,206 494,473 471,405	265,313 243,066 258,502 254,272 249,429 249,908 240,071 236,899 238,495 285,284 203,438 269,366	339,600 315,986 341,223 345,810 346,706 354,997 338,500 336,397 338,663 405,103 413,747 385,194	101 .64 94 .47 104 .88 111 .17 110 .24 109 .00 107 .82 104 .77 104 .47 106 .55 106 .86 93 .00	128 130 132 136 139 142 141 142 142 142 142 143	102.1 104.5 107.7 114.1 120.7 122.0 123.0 124.8 123.5 122.2 122.8 122.9
1918 J F M A M J A S O N D	474,809 437,834 446,460 469,783 501,926 495,255 496,813 482,530 455,462 545,652 520,194 537,389	265,329 244,838 269,030 277,497 271,820 271,839 275,975 269,853 265,175 302,069 283,165 278,694	382,074 357,464 395,474 413,470 410,448 415,913 427,761 426,368 424,280 489,352 458,727 457,058	77.80 82.83 103.65 109.61 111.18 110.79 110.35 109.34 113.94 112.48 111.80 110.76	144 146 147 149 151 153 155 158 160 162 162 164	125.0 122.7 126.4 128.3 128.1 129.0 132.0 134.3 137.5 136.3 136.3

TABLE 27—(Continued)

Date	Clear. N. Y.	Def. Cl. outs. N. Y.	Clear, outs. N. Y.	4 Pig Iron	5 Snyder's Prices	B. of L. Prices
1919 J	576,150	288,294	469,919			
1919	"Debit	s to individual	acc'ts"	106.53	163	134.4
J	584,484	332,674 303,261	542,258 488,250	105.01	161	129.8
F M	517,571 538,645	308,085	499,097	99.69	162	131.3
A	577,433	312,256	512,100	82.61	164	133.0
A M	655,806	322,523 345,902	538,613	68.00	167	135.3
J	719,000	345,902	588,033	70.50 78.34	170 174	135.6 141.1
J J A S O N D	723,452	345,365 323,827	600,935 569,935	88.50	176	144.3
A	654,065 681,533	342,538	602,867	82.93	176	141.1
ő	781,484	366,944	653,161	60.12	178	141.6
N	778,367	353,315	639,500	79.75	181	144.5
D	801,935	380,522	700,161	84.94	184	150.5
1920			Wax 225	07.00	100	1
J F	762,452	372,872	701,000	97.26 102.72	188 189	157.7 157.1
F'	622,552	323,554 355,276	611,517 682,129	108.90	192	158.6
Δ IVI	718,871 710,667	345,646	677,467	91.33	196	165.5
M	631,645	320,561	677,467 634,710	96.31	198	167.2
J	660,200	344,070	684,700	101.45	199	166.5
Ĵ	614,935	338,954	671,129	98.94 101.53	198 195	165.8 161.4
A	560,355 586,667	312,721 338,103	609,806 659,300	101.33	195	155.2
$egin{array}{c} \mathbf{M} \\ \mathbf{A} \\ \mathbf{J} \\ \mathbf{A} \\ \mathbf{S} \\ \mathbf{O} \\ \mathbf{N} \\ \mathbf{D} \end{array}$	649,581	350,991	673,903	106.21	192	144.2
Ň	672,367	348,039	650,833	97.83	187	133.4
	722,839	368,101	662,581	87.22	180	120.7
1921		DOM ONE	F00 F10	77.05	177	114.0
J F	646,226 540,357	327,975 303,135	580,516 521,393	77.95 69.19	172	114.0 104.9
M	559 774	314,042	533,871	51.47	170	102.4
	559,774 544,967	317,086	529,533	39.77	167	98.9
M	553,903	301,770	494,903	39.39	164	96.2
Ţ	591,833	326,173 305,948	528,400 489,516	35.49 27.89	162 160	93.4 93.4
A	527,097 489.871	300,625	481,000	30.78	160	93.5
ŝ	489,871 536,733	325,430	517,433	32.85	159	93.4
0	568,065	339,075	539,129	40.22	159	94.1
A J J A S O N D	583,067	334,360	531,633 562,774	47.18 53.20	159 158	94.2 92.9
1922	663,710	356,186	302,114	33.20	100	92.9
J	615,000	328,350	512,226	53.06	156	91.4
F	590,821	323,548	501,500	58.21	155	92.9
M	657,968	344.121	533,387	65.68	155	92.8
A M J J	690,567	334,851 333,238	522,367	69.07 74.41	156 158	93.2
IVI	698,516 735,433	333,238 362,299	526,516 572,433	78.70	158	96.1 96.3
j	635,903	331,569	527,194	77.59	159	99.4
A	589,903	319,536	511.258	58.59	160	98.6
S	640,500	344,854	551,767 594,290	67.79	160	99.3
A S O N	720,065	369,124	594,290	85.09	161	99.6
D	634,233 672,613	352,531 387,611	571,100 631,806	94.99 99.58	162 163	100.5 100.7

TABLE 27—(Continued) PART II

	PART II							
Date	Debits N. Y.	Def. Deb. outs. N. Y.	Debits outs. N. Y.	4 Pig Iron	Snyder's Prices	B. of L. Prices		
1923 J F M A M J A S O N	712,484 679,250 727,129 682,633 667,871 701,367 591,000 522,226 559,967 617,806 666,100 712,290	389,194 368,162 384,047 380,121 376,370 392,209 355,504 338,358 348,707 383,968 371,908 395,783	634,387 603,786 633,677 627,200 624,774 651,007 586,581 558,290 575,367 637,387 617,367 657,000	104.18 106.94 113.67 118.32 124.76 122.55 118.66 111.27 104.18 101.59 96.48 94.23	163 164 165 165 166 166 165 165 165 166 166	102.0 103.3 104.5 103.9 101.9 100.3 98.4 97.8 99.7 99.4 98.4 98.1		
1924 J F M A J J A S O N D	713,355 685,724 695,032 688,467 690,516 730,867 692,548 674,710 691,133 726,000 768,233 881,516	374,425 361,594 372,969 381,111 364,399 372,032 364,848 345,433 368,444 408,837 378,434 419,163	625,290 603,862 619,129 628,833 601,258 610,133 602,000 573,419 607,933 674,581 628,200 704,194	97.38 106.03 111.81 107.78 84.36 67.54 57.58 60.88 68.44 79.91 83.66 95.54	167 167 166 165 165 164 165 166 165 165 166	99.6 99.7 98.5 97.3 95.9 94.9 95.6 97.0 97.1 98.2 99.1		
1925 F M A M J A S O N	892,908 815,714 851,032 798,167 844,484 897,667 821,226 750,484 812,300 932,774 900,300 977,839	425,673 392,921 405,421 408,988 302,032 425,529 409,488 374,816 407,310 450,844 411,503 440,095	719,387 664,036 685,161 687,100 658,613 723,400 696,129 640,935 696,500 775,452 711,900 776,935	108.72 114.79 114.98 108.63 94.54 89.12 85.94 87.24 90.87 97.53 100.77 104.85	169 169 169 168 168 170 170 171 171 172 173 173	102.9 104.0 104.2 101.9 101.6 103.0 104.3 103.9 103.4 103.6 104.5 103.4		
1926 J F M A J J A S O N D	985,097 886,179 1,064,710 976,667 857,129 939,867 892,226 846,226 853,933 927,581 859,667 1,050,871	440,183 417,401 442,520 439,318 404,622 418,109 439,540 391,964 413,488 448,595 418,469 462,045	761,516 717,929 756,710 751,233 691,903 714,967 751,613 670,258 711,200 767,097 719,767 790,097	106.97 104.41 111.03 115.00 112.30 107.84 103.98 103.24 104.54 107.55 107.89 99.71	173 172 171 171 171 171 171 171 172 171 172 171	103.2 102.0 100.6 100.3 100.5 100.4 99.5 99.1 99.7 99.4 98.4 97.9		

TABLE 27—(Continued)

Date	Debits N. Y.	Def. Deb. outs, N. Y.	Debits outs. N. Y.	4 Pig Iron	5 Snyder's Prices	B. of L Prices
1927 J F M A M J J A S O N D	1,008,323 979,964 1,112,645 1,066,900 1,008,710 1,100,267 991,935 1,021,065 1,112,300 1,099,710 1,109,400 1,256,065	445,085 436,576 455,901 465,010 434,023 464,171 435,142 415,922 450,501 468,227 458,632 491,342	756,645 742,179 775,032 785,867 737,839 793,733 739,742 711,226 779,367 810,032 793,433 854,935	100.12 105.02 112.37 114.07 109.39 95.20 95.07 92.50 89.81 88.28 86.96	170 170 170 160 170 171 170 171 173 173 173 174	96.5 95.8 94.7 94.1 94.2 94.3 95.2 96.3 96.4
1928 J F M A M J J A S O N D	1,222,065 1,128,966 1,444,710 1,392,600 1,460,323 1,515,167 1,131,774 1,132,323 1,290,833 1,457,710 1,515,633 1,700,871	466,176 433,625 479,180 480,476 480,153 511,913 437,995 428,904 457,865 504,921 484,644 537,496	806,484 750,172 833,774 840,833 849,871 900,967 770,871 754,871 815,000 893,710 862,667 956,742	92.57 100.00 103.22 106.18 105.93 102.73 99.09 101.18 102.08 108.83 110.08 108.71	173 173 174 175 177 176 176 176 178 177 178 177	96.4 95.8 95.5 96.6 97.5 96.7 97.4 97.6 98.6 96.7 95.8
1929 J F M A M J J A S O N D	1,765,129 1,653,179 1,787,903 1,599,300 1,614,290 1,442,100 1,587,581 1,581,742 1,678,067 2,042,742 1,786,800 1,285,484	506,866 489,126 504,140 499,125 477,924 492,141 506,933 502,286 497,523 574,960 546,341 499,295	907,290 \$75,536 907,452 \$93,433 \$55,484 \$80,933 917,548 914,161 910,467 1,040,677 950,633 868,774	111.04 114.51 119.82 122.09 125.75 123.91 122.10 121.15 116.59 115.75 106.05 91.51	179 179 180 179 179 179 181 182 183 181 174	95.9 96.1 96.1 95.5 94.7 95.2 96.3 96.1 95.1 93.5 93.3
1930 J F M A M J J A S O N D	1,120,387 1,111,321 1,314,194 1,287,700 1,207,194 1,256,333 954,839 908,129 912,767 992,935 749,667 935,516	476,882 444,550 466,418 466,418 457,914 486,134 447,576 407,423 424,211 469,028 407,868 471,764	829,774 769,071 806,903 811,567 787,613 821,567 747,452 676,323 708,433 764,516 656,667 745,387	91.21 101.39 104.72 106.06 104.28 97.80 85.15 81.42 75.89 69.83 62.24 53.73	174 173 173 174 172 169 167 166 167 163 161	92.5 91.4 90.2 90.0 88.8 86.8 84.4 84.3 84.4 83.0 81.3 79.6

TABLE 27—(Continued)

PART II

			1 1111 11			
Date	1 Debits N. Y.	Def. Deb. outs. N. Y.	3 Debit outs. N. Y.	4 Pig Iron	5 Snyder's Prices	6 B. of L. Prices
1931 J F M A M J J A S O N D	792,161 748,143 889,968 894,033 808,774 863,100 677,645 564,548 669,100 667,032 482,133 620,419	445,798 388,626 399,034 421,935 397,597 431,245 399,307 357,783 377,029 406,003 388,078 394,286	699,903 610,143 626,484 654,000 608,323 646,867 594,968 533,097 554,233 584,645 486,833 552,000	55.30 60.95 65.56 67.32 64.33 54.62 47.20 41.31 38.96 37.85 36.78 31.63	157 157 157 155 153 150 149 149 147 144 144 144	78.2 76.8 76.0 74.8 73.2 72.1 72.0 72.1 71.2 70.3 70.2 68.6
1932 J F M A J J A S O N D	570,194 495,897 521,290 518,600 416,548 473,400 410,581 434,129 472,100 417,548 327,167 450,548	371,505 326,318 323,264 357,338 305,425 333,359 312,853 287,317 297,172 304,211 280,385 323,084	512,677 443,793 442,871 478,833 403,161 430,033 403,581 379,258 392,267 398,516 364,500 413,548	31.38 33.25 31.20 28.43 25.28 20.94 18.46 17.12 19.75 20.80 21.04 17.62	138 136 137 134 132 129 129 132 132 131 130 128	67.3 66.3 66.0 65.5 64.4 63.9 64.5 65.2 65.3 64.4 63.9 62.6
1983 J F M A J J S O N D	400,419 429,857 * 400,400 450,871 558,100 559,806 421,806 411,333 428,387 406,800 419,774	306,146 299,568 * 285,377 292,329 337,709 339,149 302,420 306,141 315,959 298,923 324,731	388,806 371,464 * 353,867 371,258 432,267 447,677 399,194 407,167 420,226 397,567 428,645	18.35 19.80 17.48 20.79 28.62 42.17 57.82 59.14 50.74 43.75 36.17 38.13	127 124 123 124 127 128 132 132 133 133 133 133	61.0 59.8 60.2 60.4 62.7 65.0 68.9 69.5 70.8 71.2 71.1 70.8
1934 J F M A J J A S O N D	452,355 472,536 503,484 565,133 472,677 512,933 446,516 396,290 374,067 396,323 378,100 490,774	320,107 309,454 333,895 343,163 338,638 358,978 325,152 313,721 309,041 335,670 319,262 361,774	425,742 420,857 454,097 470,133 460,548 491,800 448,710 432,935 429,567 466,581 446,967 506,484	39.20 45.13 52.24 57.56 65.90 64.34 39.51 34.01 29.94 30.68 31.90 33.15	133 136 136 137 136 137 138 138 138 139 140 140	72.2 73.6 73.7 73.3 73.7 74.6 76.4 77.6 76.5 76.5 76.9

^{*}Not available, complete data not having been reported on account of bank holidays.

TABLE 27—(Concluded)

			1 71101 11			
Date	Debits N. Y.	Def. Deb. outs. N. Y.	Debits outs. N. Y.	Pig Iron	Snyder's Prices	B. of I Prices
1935 JF M A M J J A S O N D	483,806 418,179 512,742 530,167 439,387 522,233 539,903 475,225 467,133 507,516 518,067 570,452	344,635 331,514 362,594 369,625 353,147 368,380 370,568 345,647 343,016 369,703 375,884 407,361	485,935 470,750 511,258 524,867 505,000 530,467 537,323 504,645 504,233 547,161 560,067 606,968	47.66 57.45 57.10 55.45 55.71 51.75 49.04 56.82 59.22 63.82 68.86 67.95	141 142 141 142 143 144 145 146 147 148 149	78.8 79.5 79.4 80.1 80.2 79.8 79.4 80.5 80.7 80.5
1936 J F M A M J J A S O N D	578,226 545,034 633,194 576,167 523,452 620,707 522,548 403,290 521,867 553,903 579,800 730,903	339,914 360,036 381,671 388,822 365,549 414,035 389,966 353,722 375,769 416,501 389,768 471,455	509,871 543,655 576,323 553,233 548,323 609,548 551,806 556,200 649,742 615,833 749,613	65.35 62.89 65.82 80.12 85.43 86.21 83.69 87.48 91.01 96.51 98.25 100.48	150 151 151 150 150 152 154 156 156 156 158	80.6 80.6 79.6 79.7 78.6 79.2 80.5 81.6 81.5 82.4 84.2
1937 J	616,000	408,395	657,516	103.60	161	85.9

TABLE 28

Daily Average Bank Clearings in New York City, Monthly, January 1857 - January 1919, Inclusive; Daily Average Bank Debits in New York City, Monthly, January 1919 - January 1936

- Col. 1. Logarithms of Data (in thousands of dollars) Adjusted for Seasonal Fluctuations.
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).
- Col. 5. Changing Seasonal Fluctuations (logarithms).

For details of the nature of the graduations given in Columns 2 and 3 and of the seasonal given in Column 5 of this table, see Appendix D.

TABLE 28

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Date	1	2	3	4	5	Date	1	2	3	4	5
1857 JF M AM J ASOND	4,357 4,376 4,357 4,380 4,363 4,384 4,387 4,371 4,220 3,999 4,022 4,043	4.3866 4.3884 4.3818 4.3665 4.3432 4.3133 4.2790 4.2426 4.2062 4.1719 4.1417 4.1172	4.2521 4.2519 4.2516 4.2513 4.2509 4.2506 4.2502 4.2499 4.2499 4.2493 4.2488 4.2488	+.1345 +.1365 +.1302 +.1152 +.0923 +.0627 +.0288 0073 0435 0774 1071 1310	017 .000 +.027 +.027 +.032 004 016 037 014 001 +.008 006	1862 J F M A M J A S O N D	4.164 4.184 4.170 4.221 4.335 4.364 4.382 4.358 4.424 4.498 4.434 4.493	4.1848 4.2070 4.2325 4.2607 4.2913 4.3240 4.3580 4.3925 4.4270 4.4605 4.4921 4.5214	4.3479 4.3600 4.3724 4.3848 4.3973 4.4109 4.4245 4.4386 4.4386 4.4525 4.4673 4.4821 4.4973	1631 1530 1399 1241 1060 0869 0461 0255 0068 +. 0100 +. 0241	001 +.009 +.030 +.014 +.018 021 038 051 017 +.045 +.032 019
1858 JF M AM JASOND	4.059 4.101 4.143 4.142 4.151 4.170 4.169 4.169 4.219 4.238 4.240	4.0999 4.0909 4.0907 4.0987 4.1140 4.1344 4.1574 4.1803 4.2010 4.2181 4.2307 4.2393	4.2477 4.2467 4.2457 4.2446 4.2438 4.2420 4.2405 4.2372 4.2372 4.2352 4.2352 4.2306	1478 1558 1550 1459 1298 1076 0831 0586 0362 0171 0023 +.0087	015 +.004 +.029 +.026 +.031 009 025 040 015 +.009 +.014 009	1863 J F M A M J A S O N D	4.600 4.624 4.595 4.586 4.676 4.630 4.648 4.706 4.739 4.746 4.738 4.776	4.5483 4.5729 4.5960 4.6183 4.6403 4.6624 4.6848 4.7071 4.7285 4.7486 4.7670 4.7836	4.5128 4.5289 4.5449 4.5610 4.5764 4.5935 4.6095 4.6245 4.6406 4.6561 4.6719 4.6875	+.0355 +.0440 +.0511 +.0573 +.0639 +.0689 +.0753 +.0826 +.0879 +.0925 +.0951 +.0961	+.001 +.008 +.030 +.011 +.017 019 039 053 016 +.048 +.032 019
IS59 F M A M J L A S O N D	4.231 4.241 4.247 4.285 4.276 4.223 4.223 4.247 4.269 4.250 4.264 4.287	4.2448 4.2481 4.2502 4.2519 4.2534 4.2559 4.2572 4.2589 4.2616 4.2660 4.2721	4.2281 4.2256 4.2229 4.2204 4.2179 4.2155 4.2132 4.2111 4.2092 4.2063 4.2053	+.0167 +.0225 +.0273 +.0315 +.0392 +.0427 +.0461 +.0497 +.0540 +.0597 +.0668	012 +.007 +.029 +.029 +.029 014 030 044 016 +.020 +.020 012	1864 JF M AA J JASOND	4.754 4.852 4.919 4.935 4.766 4.818 4.798 4.812 4.884 4.875 4.875 4.913	4.7982 4.8112 4.8227 4.8323 4.8403 4.8463 4.8501 4.8521 4.8521 4.8523 4.8516 4.8509	4.7022 4.7168 4.7309 4.7445 4.7579 4.7703 4.7828 4.7941 4.8050 4.8151 4.8248 4.338	+.0960 +.0944 +.0918 +.0878 +.0824 +.0760 +.0673 +.0580 +.0477 +.0372 +.0268 +.0171	+.003 +.005 +.030 +.010 +.016 039 054 016 +.049 +.032 020
1860 JF MAM LJASOND	4.287 4.269 4.295 4.302 4.314 4.302 4.311 4.346 4.330 4.352 4.320 4.200	4.2799 4.2892 4.2992 4.3086 4.3164 4.3215 4.3228 4.3118 4.2997 4.2838 4.2651	4.2046 4.2043 4.2046 4.2054 4.2069 4.2111 4.2141 4.2179 4.2218 4.2267 4.2321	+.0753 +.0849 +.0946 +.1032 +.1095 +.1128 +.1117 +.1055 +.0939 +.0779 +.0571 +.0330	009 +.008 +.030 +.021 +.025 018 034 047 017 +.032 +.026 015	1865 J F M A M J J A S O N D	4.917 4.887 4.864 4.723 4.832 4.845 4.877 4.877 4.806 4.868 4.845 4.825	4.8505 4.8502 4.8497 4.8484 4.8464 4.8435 4.8404 4.8379 4.8370 4.8389 4.8443 4.8534	4.8418 4.8495 4.8562 4.8627 4.8682 4.8734 4.8779 4.8819 4.8854 4.8887 4.8914 4.8938	+.0087 +.0007 0065 0143 0218 0299 0375 0440 0484 0498 0471 0404	+.005 +.002 +.030 +.009 +.016 013 039 056 015 +.048 +.031 019
1861 JF MA M JJ ASOND	4,234 4,222 4,203 4,225 4,131 4,110 4,144 4,123 4,126 4,180 4,192 4,216	4.2233 4.2023 4.1829 4.1660 4.1522 4.1426 4.1376 4.1375 4.1423 4.1521	4.2382 4.2448 4.2520 4.2595 4.2674 4.2760 4.2850 4.2945 4.3044 4.3146 4.3251 4.3365	+.0064 0215 0497 0766 1014 1238 1424 1569 1669 1723 1730 1701	005 +.009 +.030 +.017 +.022 021 036 049 017 +.041 +.029 017	A S	4.879 4.854 4.885 4.887 4.926 4.953 4.910 4.970 4.921 5.001 5.037 4.919	4.8659 4.8807 4.8964 4.9118 4.9252 4.9356 4.9449 4.9449 4.9375 4.9284 4.9163	4,8960 4,8980 4,8997 4,9012 4,9037 4,9048 4,9058 4,9066 4,9074 4,9081 4,9088	0301 0173 0033 +.0106 +.0228 +.0319 +.0375 +.0391 +.0366 +.0301 +.0203 +.0075	+.006 002 +.030 +.011 +.018 009 038 058 013 +.046 +.027 019

TABLE 28—Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
IS67 F M A M J A SOND	4.889 4.833 4.805 4.835 4.835 4.814 4.893 4.860 4.866 4.861 4.842 4.829	4.9025 4.8879 4.8737 4.8612 4.8514 4.8450 4.8423 4.8431 4.8472 4.8537 4.8614 4.8697	4.9095 4.9101 4.9108 4.9114 4.9119 4.9126 4.9131 4.9138 4.9142 4.9148 4.9152 4.9158	0070 0222 0371 0502 0605 0676 0708 0707 0611 0538 0461	+.006 005 +.030 +.015 +.020 005 037 061 012 +.041 +.022 017	I872 J F M A M J A S O N D	4.971 4.933 4.975 5.030 5.011 4.921 4.900 5.008 4.983 5.078 5.061 5.033	4.9493 4.9528 4.9584 4.9662 4.9756 4.9862 4.9976 5.0083 5.0174 5.0242 5.0276 5.0263	4.9360 4.9349 4.9336 4.9332 4.9307 4.9291 4.9274 4.9256 4.9239 4.9219 4.9176	+.0133 +.0179 +.0248 +.0340 +.0449 +.0571 +.0702 +.0827 +.0935 +.1023 +.1028 +.1087	+.011 000 +.022 004 074 077 011 +.011 000
IS68 JFM AM JASOND	4.91) 4.924 4.911 4.900 4.842 4.912 4.902 4.939 4.900 5.004 5.012 4.968	4.8776 4.8847 4.8910 4.8968 4.9026 4.9074 4.9276 4.9398 4.9540 4.9692 4.9843	4.9163 4.9168 4.9172 4.9176 4.9180 4.9184 4.9188 4.9192 4.9195 4.9198 4.9202 4.9205	0387 0321 0262 0208 0154 0092 0014 +.0084 +.0203 +.0342 +.0490 +.0638	+.007 007 +.029 +.021 +.023 001 037 063 010 +.034 +.014 015	1873 J F M A M J A S O N D	4.991 5.057 5.001 4.995 4.926 4.889 4.929 4.898 4.682 4.706 4.795	5.0202 5.0089 4.9921 4.9707 4.9461 4.9193 4.8920 4.8661 4.8227 4.8070 4.7961	4.9153 4.9127 4.9100 4.9072 4.9044 4.9013 4.8981 4.8948 4.8913 4.8878 4.8840 4.8802	+.1049 +.0962 +.0821 +.0635 +.0417 +.0180 0061 0287 0487 0651 0770 0841	+.01 00 +.02 +.04 +.02 00 04 07 01 +.01
869 JFMAMJJASOND	4.949 4.976 4.999 5.024 5.041 5.060 5.027 4.978 5.055 4.893 4.915 4.900	4.9981 5.0093 5.0161 5.0186 5.0165 5.0099 4.9994 4.9866 4.9716 4.9556 4.9388 4.9218	4.9209 4.9213 4.9213 4.9222 4.9228 4.9233 4.9240 4.9248 4.9257 4.9266 4.9276 4.9287	+.0772 +.0880 +.0943 +.0964 +.0937 +.0866 +.0754 +.0618 +.0459 +.0290 +.0112 0069	+.008 008 +.029 +.027 +.026 +.001 038 066 009 +.028 +.007	1874 J F M A M J A S O N D	4.843 4.814 4.811 4.824 4.783 4.832 4.775 4.824 4.832 4.775 4.824 4.808 4.808 4.851	4.7895 4.7872 4.7888 4.7931 4.7996 4.8075 4.8156 4.8230 4.8293 4.8340 4.8370 4.8387	4.8761 4.8720 4.8678 4.8636 4.8595 4.8551 4.8551 4.8465 4.8422 4.8379 4.8337 4.8295	0866 0848 0790 0705 0599 0476 0352 0235 0129 0039 +.0033 +.0092	+.02 +.02 +.02 +.04 +.02 06 06 01 +.01
1870 JFMAM LJASOND	4.872 4.869 4.854 4.832 4.920 4.883 4.958 4.799 4.850 4.799 4.850 4.908	4.9053 4.8896 4.8757 4.8647 4.8567 4.8528 4.8524 4.8549 4.8596 4.8658 4.8719 4.8782	4.9298 4.9309 4.9321 4.9333 4.9345 4.9358 4.9369 4.9379 4.9387 4.9387 4.9403 4.9403	0245 0413 0564 0686 0778 0830 0845 0830 0791 0738 0684 0627	+.010 008 +.028 +.035 +.028 +.002 039 069 009 +.023 +.001 006	1875 J F M A M J A S O N D	4.845 4.832 4.844 4.839 4.828 4.863 4.851 4.771 4.796 4.775 4.804 4.798	4.8394 4.8393 4.8385 4.8372 4.8348 4.8310 4.8257 4.8188 4.8102 4.8006 4.7907 4.7811	4.8253 4.8210 4.8169 4.8129 4.8087 4.8050 4.8013 4.7978 4.7942 4.7912 4.7881 4.7853	+.0141 +.0183 +.0216 +.0261 +.0260 +.0244 +.0210 +.0160 +.0094 +.0026 0042	+.02 +.02 +.03 +.03 01 04 07 02 +.02 +.01
1871 F M A M J A S O N D	4.855 4.847 4.930 4.961 4.948 4.972 4.846 4.900 4.966 4.902 4.949	4.8844 4.8908 4.8977 4.9050 4.9129 4.9211 4.9285 4.9349 4.9398 4.9431 4.9451 4.9469	4.9414 4.9418 4.9419 4.9419 4.9416 4.9416 4.9416 4.9498 4.9398 4.9392 4.9383 4.9373	0570 0510 0442 0369 0205 0127 0057 .0000 +.0039 +.0068 +.0096	+.012 007 +.027 +.040 +.029 +.001 040 071 +.020 004 002	1876 F M A M J A S O N D	4.782 4.804 4.774 4.710 4.741 4.756 4.736 4.772 4.781 4.787 4.765 4.782	4.7726 4.7658 4.7658 4.7567 4.7565 4.7565 4.7585 4.7616 4.7659 4.7715 4.7783 4.7783	4.7826 4.7802 4.7782 4.7765 4.7750 4.7737 4.7728 4.7721 4.7717 4.7716 4.7718 4.7722	0100 0144 0174 0188 0185 0169 0143 0105 0058 +.0065 +.0139	+.03 +.01 +.01 +.03 +.01 04 06 02 +.02 +.00

TABLE 28-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1877 F M A M J J A S O N D	4.803 4.830 4.789 4.807 4.791 4.806 4.828 4.857 4.815 4.835 4.797 4.798	4.7944 4.8026 4.8097 4.8153 4.8186 4.8195 4.8181 4.8149 4.8104 4.8052 4.8052 4.8000 4.7951	4.7729 4.7738 4.7750 4.7764 4.7781 4.7800 4.7822 4.7847 4.7872 4.7903 4.7903 4.7968	+.0215 +.0288 +.0347 +.0349 +.0405 +.0395 +.0302 +.0302 +.0232 +.0149 +.0066 0017	+.033 +.012 +.016 +.027 +.013 019 047 066 026 +.031 +.014 +.020	1882 J F M A M J J A S O N D	5.118 5.095 5.161 5.119 5.016 5.071 5.102 5.132 5.156 5.100 5.138 5.065	5.0981 5.0980 5.1002 5.1033 5.1058 5.1058 5.1056 5.1018 5.0956 5.0875 5.0780 5.0674	5.0923 5.0915 5.0898 5.0877 5.0849 5.0817 5.0741 5.0741 5.0695 5.0646 5.0595 5.0541	+.0058 +.0065 +.0104 +.0156 +.0209 +.0251 +.0277 +.0277 +.0229 +.0133	+.02 +.00 00 00 02 04 05 02 +.05 +.04 +.03
1878 F M A M J A S O N D	4.779 4.720 4.766 4.807 4.773 4.779 4.823 4.815 4.770 4.817 4.810 4.765	4.7910 4.7877 4.7856 4.7844 4.7840 4.7853 4.7863 4.7877 4.7896 4.7921 4.7957	4.8002 4.8041 4.8084 4.8131 4.8180 4.8233 4.8291 4.8350 4.8412 4.8480 4.8549 4.8621	0092 0164 02287 0340 0389 0438 0487 0535 0584 0628 0664	+.034 +.012 +.012 +.021 +.021 022 047 063 029 +.036 +.022 +.023	1883 F M A M J J A S O N D	5.005 5.025 5.005 5.019 5.015 5.023 4.992 5.034 5.030 5.039 4.942 4.983	5.0564 5.0454 5.0349 5.0255 5.0179 5.0125 5.0094 5.0085 5.0091 5.0102 5.0104 5.0085	5.0486 5.0428 5.0370 5.0309 5.0248 5.0187 5.0127 5.0067 4.9888 4.9831	+.0078 +.0026 0021 0054 0069 0062 0033 +.0018 +.0085 +.0155 +.0254	+.02 +.00 00 00 02 04 05 +.04 +.03
1879 F M A M J J A SOND	4.817 4.822 4.776 4.821 4.890 4.824 4.863 4.930 4.916 5.018 5.040 4.982	4.8013 4.8094 4.8206 4.8355 4.8538 4.8750 4.8981 4.9218 4.9442 4.9639 4.9800 4.9918	4.8696 4.8773 4.8853 4.8934 4.9018 4.9101 4.9186 4.9274 4.9361 4.9447 4.9533 4.9619	0683 0679 0647 0579 0480 0351 0205 0356 +.0081 +.0192 +.0267 +.0299	+.034 +.012 +.008 +.014 +.007 024 059 030 +.040 +.029 +.025	1884 JFM AM JASOND	5.019 5.007 4.976 4.994 5.032 4.921 4.889 4.871 4.857 4.830 4.803 4.849	5.0037 4.9955 4.9837 4.9687 4.9512 4.9316 4.9108 4.8895 4.8685 4.8490 4.8325 4.8200	4.9777 4.9724 4.9674 4.9623 4.9528 4.9486 4.9443 4.9406 4.9335 4.9305	+.0260 +.0231 +.0163 +.0064 0062 0212 0378 0548 0721 0879 1010	+.01 +.00 00 00 01 04 05 +.05 +.04 +.03
ISSO JFM AM JASOND	4.987 4.993 5.045 5.045 5.027 5.015 4.970 4.945 4.983 4.974 5.098 5.115	4.9993 5.0032 5.0048 5.0052 5.0061 5.0089 5.0143 5.0229 5.0347 5.0492 5.0657 5.0831	4.9705 4.9790 4.9873 4.9957 5.0035 5.0116 5.0192 5.0267 5.0339 5.0408 5.0475 5.0540	+.0288 +.0242 +.0175 +.0095 +.0026 0027 0049 0038 +.0008 +.0182 +.0182 +.0291	+,032 +,011 +,004 +,004 +,004 -,025 -,046 -,036 -,035 +,045 +,035 +,029	1885 J F M A M J A S O N D	4.831 4.830 4.823 4.809 4.823 4.927 4.873 4.958 5.004 4.983	4.8127 4.8113 4.8161 4.8264 4.8408 4.8581 4.8768 4.8951 4.9120 4.9268 4.9390 4.9485	4.9276 4.9251 4.9229 4.9209 4.9191 4.9177 4.9164 4.9154 4.9148 4.9140 4.9140	-,1149 -,1138 -,1068 -,0945 -,0783 -,0596 -,0396 -,0203 -,0028 +,0126 +,0250 +,0345	+.01 +.00 01 01 04 05 01 +.05 +.04
1881 F M A M J A S O N D	5.153 5.182 5.131 5.092 5.195 5.172 5.143 5.085 5.085 5.075 5.108	5.1004 5.1163 5.1296 5.1393 5.1445 5.1452 5.1415 5.1344 5.1252 5.1155 5.1070 5.1011	5.0599 5.0657 5.0708 5.0752 5.0795 5.0830 5.0861 5.0887 5.0926 5.0920 5.0926	+.0405 +.0506 +.0588 +.0641 +.0651 +.0622 +.0554 +.0457 +.0346 +.0235 +.0144 +.0084	+.029 +.010 +.001 000 +.002 024 045 053 029 +.048 +.039 +.031	1886 J F M A M J A S O N D	4.950 4.992 4.985 4.916 4.891 4.973 4.943 4.951 4.954 4.966 4.987 5.032	4.9554 4.9598 4.9619 4.9623 4.9615 4.9603 4.9592 4.9594 4.9645 4.9645 4.9692 4.9748	4.9144 4.9149 4.9157 4.9165 4.9173 4.9183 4.9197 4.9213 4.9230 4.9247 4.9266 4.9287	+.0410 +.0449 +.0462 +.0458 +.0442 +.0420 +.0395 +.0381 +.0382 +.0461	+.01 00 01 04 05 01 +.03 +.03

TABLE 28-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
J F M A M J A S O N D	4.964 4.949 4.976 5.013 4.952 5.006 4.964 4.959 4.965 4.930 4.953 4.953	4.9798 4.9836 4.9853 4.9843 4.9805 4.9743 4.9663 4.9572 4.9479 4.9311 4.9311 4.9244	4.9310 4.9330 4.9352 4.9376 4.9401 4.9423 4.9447 4.9470 4.9495 4.9515 4.9538 4.9559	+.0488 +.0506 +.0501 +.0467 +.0404 +.0320 +.0216 +.0102 0016 0124 0227 0315	+.016 003 015 008 +.002 011 041 053 014 +.053 +.037 +.034	1892 JF M A M J J A S O N D	5.033 5.052 5.035 5.011 4.970 4.976 4.958 4.970 4.984 4.962 4.996 5.035	5.0040 5.0032 5.0009 4.9983 4.9961 4.9953 4.9961 4.9983 5.0015 5.0048 5.0072 5.0079	4.9772 4.9742 4.9741 4.9678 4.9644 4.9609 4.9574 4.9538 4.9503 4.9466 4.9420 4.9392	+.0268 +.0290 +.0298 +.0305 +.0317 +.0344 +.0387 +.0445 +.0512 +.0582 +.0643 +.0687	+.020 001 011 000 +.011 003 053 051 +.033 +.029 +.030
1888 JFM AM JJASOND	4.893 4.887 4.902 4.939 4.939 4.904 4.945 4.962 4.962 4.962 4.922 4.950	4.9192 4.9157 4.9138 4.9139 4.9159 4.9159 4.9253 4.9322 4.9402 4.9402 4.9403 4.9570 4.9651	4.9581 4.9600 4.9618 4.9636 4.9651 4.9667 4.9681 4.9703 4.9703 4.9715 4.9724 4.9734	0389 0443 0480 0497 0492 0470 0428 0372 0301 0230 0154 0083	+.017 004 016 006 +.005 009 041 054 013 +.051 +.035 +.032	1893 J F M A M J A S O N D	5.032 5.044 5.031 4.970 4.981 4.925 4.858 4.807 4.827 4.824	5.0056 5.0000 4.9905 4.9768 4.9595 4.9390 4.9165 4.8709 4.8709 4.8507 4.8336 4.8205	4.9354 4.9315 4.9278 4.9240 4.9203 4.9165 4.9128 4.9091 4.9056 4.9021 4.8986 4.8955	+.0702 +.0685 +.0627 +.0528 +.0392 +.0225 +.0037 0157 0347 0514 0650 0750	+.02 00 01 +.00 +.01 03 05 01 +.03 +.02 +.03
JFM AM J JASOND	4.978 4.988 4.986 4.967 4.988 5.012 5.003 4.968 5.019 4.995 4.978	4.9722 4.9783 4.9833 4.9897 4.9897 4.9916 4.9929 4.9941 4.9956 4.9976 5.0003 5.0037	4.9742 4.9752 4.9762 4.9761 4.9780 4.9790 4.9801 4.9812 4.9824 4.9837 4.9850 4.9864	0020 +.0031 +.0071 +.0100 +.0117 +.0126 +.0129 +.0132 +.0139 +.0153 +.0173	+.018 005 017 005 +.009 008 040 055 014 +.048 +.034 +.034	IS94 JF MA MJ JA SOND	4.814 4.793 4.827 4.825 4.816 4.807 4.810 4.840 4.841 4.841 4.847	4.8115 4.8062 4.8042 4.8046 4.8068 4.8101 4.8143 4.8193 4.8253 4.8326 4.8412 4.8511	4.8924 4.8894 4.8865 4.8838 4.8812 4.8767 4.8746 4.8725 4.8708 4.8693 4.8693 4.8680	0809 0832 0823 0792 0744 0688 0624 0553 0472 0382 0281 0169	+.03 00 00 +.01 03 05 02 +.02 +.02
1890 F M AM J ASOND	5.003 5.009 4.976 4.992 5.076 5.028 5.001 5.037 5.027 5.017 5.016 4.936	5.0076 5.0117 5.0152 5.0180 5.0193 5.0186 5.0159 5.0111 5.0041 4.9953 4.9854 4.9750	4.9878 4.9894 4.9907 4.9921 4.9932 4.9945 4.9955 4.9954 4.9971 4.9978 4.9978 4.9978	+.0198 +.0223 +.0245 +.0259 +.0261 +.0204 +.0147 +.0070 0022 0124 0229	+.021 006 017 003 +.011 006 040 057 014 +.044 +.032 +.030	1895 J F M A M J A S O N D	4.856 4.827 4.864 4.892 4.949 4.923 4.945 4.933 4.922 4.954 4.912 4.942	4.8623 4.8742 4.8861 4.8977 4.9081 4.9168 4.9234 4.9276 4.9293 4.9286 4.9261 4.9221	4.8669 4.8662 4.8657 4.8655 4.8659 4.8667 4.8678 4.8692 4.8711 4.8735 4.8762	0046 +.0080 +.0204 +.0322 +.0427 +.0509 +.0567 +.0575 +.0575 +.0526 +.0459	+.03 00 00 +.00 +.01 03 05 02 +.02 +.02 +.03
1891 F M A M J A S O N D	4.957 4.920 4.912 4.987 4.959 4.934 4.942 4.947 5.059 4.986 5.962 4.992	4.9651 4.9568 4.9511 4.9486 4.9499 4.9549 4.9626 4.9723 4.9823 4.9823 4.9983 5.0025	4.9978 4.9974 4.9968 4.9959 4.9945 4.9932 4.9917 4.9898 4.9875 4.9854 4.9829 4.9801	0327 0406 0457 0473 0446 0383 0291 0175 0052 +.0059 +.0154 +.0224	+.023 005 015 002 +.013 005 039 058 015 +.039 +.030 +.030	1896 J F M A J A S O N D	4.882 4.918 4.875 4.894 4.866 4.914 4.935 4.862 4.864 4.907 4.927 4.902	4.9172 4.9119 4.9067 4.9016 4.8967 4.8920 4.8877 4.8838 4.8836 4.8787 4.8786 4.8810	4.8795 4.8833 4.8873 4.8917 4.8963 4.9014 4.9069 4.9125 4.9182 4.9243 4.9305 4.9369	+.0377 +.0286 +.0194 +.0099 +.0004 0192 0287 0376 0456 0519 0559	+.03 00 00 +.01 03 03 05 02 +.01 +.02 +.03

TABLE 28-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
F M AM J ASOND	4.885 4.870 4.887 4.863 4.862 4.943 4.992 5.091 5.015 4.993 5.033	4.8862 4.8943 4.9055 4.9194 4.9353 4.9526 4.9703 4.9876 5.0032 5.0161 5.0256 5.0314	4.9434 4.9500 4.9566 4.9635 4.97704 4.9772 4.9842 4.9013 4.9983 5.0053 5.0123 5.0195	0572 0557 0551 0441 0351 0246 0139 0037 +.0049 +.0108 +.0133 +.0119	+.037 006 .000 +.012 +.011 031 059 030 +.017 +.024 +.031	1902 J F M A M J A S O N D	5.300 5.292 5.248 5.362 5.331 5.244 5.353 5.330 5.394 5.365 5.317 5.272	5.2855 5.2866 5.2918 5.2998 5.3089 5.3177 5.3249 5.3298 5.3312 5.3279 5.3224	5.2758 5.2760 5.2763 5.2767 5.2773 5.2776 5.2781 5.2786 5.2786 5.2783 5.2800 5.2810 5.2821	+.0097 +.0106 +.0155 +.0231 +.0316 +.0401 +.0468 +.0512 +.0525 +.0512 +.0469 +.0403	+.04 01 +.00 +.01 02 02 03 +.01 +.02 +.02 +.02
1898 F M A M J A S O N D	5.037 5.105 5.040 4.965 4.995 5.049 5.011 5.113 5.089 5.041 5.098 5.146	5.0336 5.0335 5.0322 5.0315 5.0334 5.0392 5.0496 5.0650 5.0846 5.1072 5.1312 5.1550	5.0266 5.0337 5.0408 5.0480 5.0553 5.0624 5.0697 5.0771 5.0847 5.0721 5.0927 5.0721	+.0070 0002 0086 0165 0219 0232 0201 0121 0151 +.0151 +.0478	+.039 006 +.002 +.016 +.011 012 029 033 +.016 +.024 +.030	1903 J F M A M J A S O N D	5.314 5.284 5.285 5.271 5.246 5.308 5.309 5.231 5.194 5.206 5.166 5.223	5.3149 5.3060 5.2958 5.2847 5.2728 5.2605 5.2478 5.2350 5.2223 5.2102 5.1992 5.1905	5.2833 5.2848 5.2864 5.2882 5.2902 5.2923 5.2946 5.2971 5.2099 5.3024 5.3053 5.3082	+.0316 +.0212 +.0094 0035 0174 0318 0468 0621 0776 0922 1061 1177	+.05 01 +.00 +.02 +.00 02 05 03 +.02 +.02 +.02
JFM AM JASOND	5.223 5.218 5.278 5.249 5.239 5.217 5.182 5.207 5.202 5.214 5.194 5.208	5.1769 5.1962 5.2119 5.2237 5.2316 5.2353 5.2349 5.2305 5.2222 5.2106 5.1961 5.1796	5.1150 5.1227 5.1304 5.1381 5.1457 5.1534 5.1609 5.1686 5.1761 5.1836 5.1908 5.1977	+.0619 +.0735 +.0815 +.0856 +.0859 +.0819 +.0740 +.0619 +.0461 +.0270 +.0053 0181	+.041 007 +.002 +.012 015 028 059 036 +.015 +.024 +.029	1904 J F M A M J J A S O N D	5.210 5.196 5.189 5.180 5.187 5.209 5.247 5.229 5.229 5.359 5.424 5.412	5.1849 5.1835 5.1874 5.1969 5.2119 5.2317 5.2551 5.2805 5.3062 5.3305 5.3524 5.3711	5.3115 5.3144 5.3175 5.3206 5.3239 5.3269 5.3299 5.3331 5.3364 5.3393 5.3424 5.3453	1266 1309 1301 1237 1120 0952 0748 0526 0302 0088 +.0100 +.0258	+.05 01 +.00 +.02 02 03 03 +.02 +.02 +.03
1900 JFM AM JASOND	5.134 5.157 5.190 5.172 5.148 5.130 5.086 5.071 5.059 5.153 5.256 5.255	5.1623 5.1458 5.1316 5.1216 5.1171 5.1194 5.1287 5.1450 5.1674 5.1946 5.2246 5.2555	5.2045 5.2111 5.2172 5.2232 5.2238 5.2338 5.2389 5.2434 5.2477 5.2515 5.2550 5.2582	0422 0653 0856 1016 1117 1144 1102 0984 0803 0569 0304 0027	+.043 008 +.003 +.024 +.012 019 027 059 037 +.016 +.023 +.028	1905 J F M A M J A S O N D	5.342 5.418 5.450 5.441 5.401 5.367 5.367 5.397 5.388 5.436 5.469	5.3862 5.3978 5.4061 5.4115 5.4116 5.4167 5.4177 5.4187 5.4203 5.4229 5.4267 5.4317	5.3484 5.3514 5.3543 5.3597 5.3624 5.3650 5.3675 5.3699 5.3724 5.3746 5.3769	+.0378 +.0464 +.0518 +.05544 +.0551 +.0543 +.0527 +.0512 +.0505 +.0521 +.0521 +.0548	+.00 00 +.00 +.00 00 00 00 +.00 +
1901 FM AM J ASOND	5.332 5.313 5.344 5.433 5.466 5.382 5.319 5.259 5.264 5.305 5.305	5.2852 5.3115 5.3325 5.3472 5.3547 5.3551 5.3490 5.3380 5.3242 5.3101 5.2978 5.2892	5.2611 5.2636 5.2636 5.2657 5.2676 5.2706 5.2718 5.2737 5.2745 5.2755	+.0241 +.0479 +.0685 +.0796 +.0853 +.0845 +.0772 +.0652 +.0505 +.0356 +.0228 +.0137	+.046 010 +.003 +.026 +.012 023 026 038 038 +.017 +.022 +.027	J A S	5.503 5.486 5.433 5.439 5.439 5.452 5.439 5.501 5.501 5.479 5.452 5.444	5.4376 5.4440 5.4499 5.4549 5.4584 5.4600 5.4589 5.4568 5.4568 5.4548 5.4548 5.4548	5.3790 5.3812 5.3833 5.3853 5.3872 5.3891 5.3908 5.3924 5.3938 5.3954 5.3954 5.3956 5.3977	+.0586 +.0628 +.0666 +.0696 +.0712 +.0709 +.0692 +.0665 +.0630 +.0589 +.0552 +.0512	+.05 01 +.01 +.02 02 03 +.02 +.01 +.01

TABLE 28-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1907 JF M AM J JASOND	5.437 5.430 5.491 5.395 5.376 5.347 5.394 5.391 5.394 5.394 5.247 5.213	5.4447 5.4389 5.4306 5.4190 5.4040 5.3863 5.3665 5.3455 5.3254 5.3071 5.2918 5.2803	5.3986 5.3995 5.4002 5.4006 5.4009 5.4010 5.4009 5.4008 5.4008 5.4005 5.3996 5.3996 5.3989	+.0461 +.0394 +.0304 +.0184 +.0031 0147 0344 0553 0751 0929 1078 1186	+.056 012 002 +.013 002 021 044 035 +.028 +.016 +.024	1912 J F M A M J A S O N D	5.409 5.410 5.441 5.461 5.457 5.422 5.427 5.428 5.430 5.424 5.453 5.453	5.4162 5.4202 5.4250 5.4301 5.4353 5.4400 5.4440 5.4464 5.4466 5.4441 5.4400	5.4187 5.4167 5.4141 5.4114 5.4086 5.4061 5.4035 5.4011 5.3987 5.3965 5.3946 5.3930	0025 +.0035 +.0109 +.0187 +.0267 +.0339 +.0405 +.0453 +.0453 +.0495 +.0497	+.044 000 000 +.000 000 +.000 024 034 +.031 +.011
1908 J.F.M.A.M.J.A.S.O.N.D.	5.282 5.238 5.252 5.252 5.352 5.350 1.346 5.388 5.339 5.421 5.454	5.2736 5.2714 5.2739 5.2809 5.2918 5.3055 5.3216 5.3390 5.3565 5.3733 5.3890 5.4030	5.3981 5.3974 5.3967 5.3958 5.3951 5.3946 5.3936 5.3933 5.3933 5.3933 5.3933	1245 1260 1228 1149 1033 0891 0724 0546 0368 0199 0043 +.0096	+.056 011 003 +.010 004 015 021 043 +.029 +.015 +.022	1913 F M AM I J A S O N D	5.436 5.455 5.415 5.420 5.417 5.394 5.387 5.424 5.417 5.386 5.392	5.4349 5.4290 5.4230 5.4176 5.4136 5.4114 5.4135 5.4114 5.4135 5.4202 5.4224 5.4222	5.3915 5.3902 5.3894 5.3889 5.3888 5.3889 5.3894 5.3901 5.3914 5.3929 5.3948 5.3970	+.0434 +.0388 +.0336 +.02287 +.02248 +.0226 +.0220 +.0234 +.0274 +.0276 +.0252	+.04 01 00 +.00 00 +.00 01 02 +.03 +.01 +.02
1909 JFMAM JASOND	5.402 5.401 5.387 5.450 5.423 5.450 5.490 5.484 5.482 5.484	5.4152 5.4260 5.4356 5.4443 5.4526 5.4607 5.4682 5.4748 5.4800 5.4831 5.4834 5.4809	5.3936 5.3941 5.3947 5.3954 5.3963 5.3974 5.3987 5.4000 5.4014 5.4029 5.4045 5.4062	+.0216 +.0319 +.0409 +.0489 +.0563 +.0695 +.0748 +.0786 +.0802 +.0789 +.0747	+.055 010 004 +.008 001 011 021 043 033 +.029 +.014 +.021	1914 J F M A M J A S O N D	5.442 5.424 5.413 5.446 5.372 5.409 5.218 5.216 5.227 5.237 5.303	5.4182 5.4100 5.3979 5.3825 5.3649 5.3468 5.3297 5.3150 5.3043 5.2986 5.2987 5.3056	5.3995 5.4020 5.4052 5.4085 5.4123 5.4162 5.4202 5.4246 5.4294 5.4342 5.4343 5.4343 5.4446	+.0187 +.0080 0073 0260 0474 0694 1096 1251 1356 1406 1390	+.03 01 +.00 +.00 +.00 01 02 +.03 +.03 +.03
1910 JFMAMJJASOND	5.507 5.473 5.470 5.437 5.451 5.426 5.363 5.349 5.379 5.402 5.393	5.4753 5.4669 5.4563 5.4444 5.4317 5.4195 5.4086 5.3996 5.3929 5.3888 5.3870 5.3872	5.4080 5.4098 5.4116 5.4135 5.4154 5.4172 5.4191 5.4208 5.4226 5.4242 5.4256 5.4270	+.0673 +.0571 +.0447 +.0349 +.0163 +.0123 0105 0212 0297 0354 0386 0398	+.053 009 005 +.007 006 006 021 044 032 +.030 +.014 +.020	1915 F M A M J A S O N D	5.337 5.380 5.397 5.460 5.447 5.465 5.488 5.532 5.584 5.577 5.577	5.3195 5.3399 5.3659 5.3959 5.4276 5.4587 5.4874 5.5122 5.5324 5.5486 5.5614 5.5720	5.4501 5.4557 5.4616 5.4677 5.4739 5.4802 5.4808 5.5006 5.5079 5.5153 5.5225	1306 1152 0957 0718 0463 0215 +.0006 +.0186 +.0318 +.0407 +.0407 +.0495	+.0. 0 +.00 00 +.00 00 00 +.0. +.0. +.0.
1911 F M A M J A S O N D	5.390 5.424 5.397 5.359 5.415 5.440 5.422 5.354 5.415 5.354 5.415	5.3888 5.3915 5.3944 5.3974 5.4002 5.4024 5.4041 5.4056 5.4071 5.4085 5.4104 5.4130	5.4280 5.4288 5.4293 5.4295 5.4295 5.4291 5.4284 5.4276 5.4263 5.4247 5.4230 5.4211	0392 0373 0349 0321 0293 0267 0243 0220 0192 0162 0126 0081	+.050 008 006 +.007 006 002 021 045 031 +.030 +.015 +.019	1916 J F M A M J A S O N D	5.570 5.600 5.617 5.581 5.610 5.609 5.584 5.626 5.705 5.676 5.725 5.712	5.5815 5.5907 5.6000 5.6092 5.6184 5.6275 5.6364 5.6455 5.6550 5.6647 5.6748 5.6847	5.5300 5.5378 5.5457 5.5538 5.5619 5.5703 5.5786 5.5871 5.5955 5.6040 5.6125 5.6211	+.0515 +.0529 +.0543 +.0554 +.0565 +.0578 +.0578 +.0584 +.0595 +.0607 +.0623 +.0636	+.02 01 +.00 00 +.01 04 02 +.02 +.02 +.03 +.03 +.03 +.03

TABLE 28-Continued

BANK CLEARINGS IN NEW YORK CITY

Date	1	2	3	4	5	Date	1	2	3	4	5
1917 J F M A M J A S O N D	5.672 5.684 5.702 5.740 5.705 5.721 5.690 5.677	5,6933 5,7000 5,7042 5,7055 5,7042 5,7007 5,6958 5,6904 5,6852 5,6852 5,6858 5,6774 5,6750	5.6297 5.6382 5.6465 5.6547 5.6628 5.6707 5.6783 5.6856 5.6929 5.6999 5.7064 5.7124	+ .0636 + .0618 + .0577 + .0508 + .0414 + .0300 + .0175 + .0048 0077 0191 0290 0374	+.026 020 010 +.005 001 +.016 015 046 025 +.028 +.018 +.027	M A M J A S	5.730 5.683 5.711 5.699 5.701	5.6736 5.6730 5.6731 5.6740 5.6756 5.6783 3.6822 5.6873 5.6937 5.7017 5.7112 5.7222	5.7184 5.7242 5.7293 5.7340 5.7385 5.7426 5.7426 5.7465 5.7500 5.7533 5.7564 5.7591 5.7616	0448 0512 0562 0600 0629 0643 0643 0627 0596 0547 0479 0394	+.02: 000 +.000 +.01: 01: 04: 02: +.01: +.02:

BANK DEBITS IN NEW YORK CITY

Date	1	2	3	4	5	Date	1	2	3	4	5
1919 JFM AM JJASOND	5.744 5.738 5.738 5.759 5.817 5.837 5.861 5.858 5.878 5.877 5.873	5.7410 5.7553 5.7712 5.7880 5.8053 5.8220 5.8372 5.8500 5.8594 5.8650 5.8667 5.8648	5.7699 5.7720 5.7740 5.7759 5.7778 5.7795 5.7812 5.7827 5.7842 5.7856 5.7869 5.7869 5.7882	0289 0167 0028 +.0121 +.0275 +.0425 +.0660 +.0673 +.0752 +.0794 +.0798 +.0766	+.023 024 007 +.003 .000 +.020 014 045 025 +.022 +.014 +.031	1922 J F M A M J A S O N D	5.836 5.843 5.842 5,818	5.7856 5.7960 5.8054 5.8135 5.8205 5.8262 5.8368 5.8341 5.8360 5.8362 5.8348 5.8319	5.7997 5.7998 5.7999 5.8002 5.8007 5.8011 5.8017 5.8025 5.8034 5.8045 5.8057 5.8057	0141 0038 +.0055 +.0133 +.0198 +.0251 +.0291 +.0316 +.0316 +.0317 +.0291 +.0249	+.02 02 +.00 +.00 +.02 01 04 02 +.01 +.00 +.03
1920 J F M A M J A S O N D	5.860 5.817 5.861 5.849 5.799 5.798 5.803 5.794 5.794 5.817 5.826	5.8599 5.8528 5.8445 5.8358 5.8273 5.8194 5.8122 5.8055 5.7993 5.7993 5.7869 5.7869	5.7895 5.7906 5.7917 5.7927 5.7938 5.7946 5.7953 5.7961 5.7967 5.7972 5.7976 5.7976	+.0704 +.0622 +.0528 +.0431 +.0335 +.0248 +.0169 +.0094 +.0026 0040 0107 0178	+.022 023 004 +.003 +.001 +.022 014 026 +.019 +.011 +.033	1	5.824 5.820 5.788	5.8278 5.8229 5.8179 5.8134 5.8094 5.8064 5.8034 5.8032 5.8030 5.8060 5.8092	5.8085 5.8103 5.8122 5.8143 5.8166 5.8190 5.8217 5.8247 5.8247 5.8247 5.8307 5.8340 5.8376	+.0193 +.0126 +.0057 0009 0072 0126 0172 0213 0245 0267 0280 0284	+.02 01 +.00 +.00 +.02 01 04 02 +.00 +.00
I P M A M J A S O N D	5.788 5.756 5.750 5.733 5.742 5.748 5.737 5.736 5.736 5.739 5.758	5.7732 5.7660 5.7587 5.7519 5.7464 5.7427 5.7414 5.7431 5.7477 5.7550 5.7643 5.7749	5.7984 5.7988 5.7990 5.7992 5.7993 5.7993 5.7994 5.7994 5.7994 5.7995 5.7996	0252 0328 0403 0473 0528 0566 0579 0563 0517 0444 0352 0247	+.022 023 002 +.003 +.001 +.024 015 046 026 +.015 +.008 +.034	A J A S O N	5.832 5.852 5.833 5.832 5.838 5.857 5.875 5.875 5.868 5.855 5.855 5.855	5.8138 5.8198 5.8269 5.8350 5.8436 5.8522 5.8606 5.8685 5.8758 5.8758 5.8826 5.8891 5.8954	5.8412 5.8448 5.8487 5.8524 5.8563 5.8602 5.8640 5.8678 5.8720 5.8759 5.8759 5.8759 5.8800 5.8841	0274 0250 0218 0174 0127 0080 0034 +.0007 +.0067 +.0091 +.0113	+.02 01 +.00 +.00 +.02 01 04 02 +.00 +.00

TABLE 28-Continued

BANK DEBITS IN NEW YORK CITY

Date	1	2	3	4	5	Date	1	2	3	4	5
1925 JF M A M J J A S O N D	5.931 5.927 5.918 5.895 5.926 5.927 5.932 5.932 5.939 5.966 5.952 5.957	5.9015 5.9076 5.9136 5.9195 5.9253 5.9310 5.9366 5.9421 5.9524 5.9524 5.9528 5.9604	5.8881 5.8925 5.8966 5.9008 5.9051 5.9097 5.9144 5.9193 5.9242 5.9297 5.9351 5.9407	+.0134 +.0151 +.0170 +.0187 +.0202 +.0213 +.0222 +.0227 +.0232 +.0227 +.0217 +.0197	+.020 014 +.012 +.007 +.001 +.026 018 046 029 +.004 +.032 +.033	1930 F M A M J J A S O N D	6.031 6.056 6.099 6.100 6.082 6.074 6.001 5.954 5.990 5.997 5.875 5.941	6.1399 6.1180 6.0943 6.0699 6.0457 6.0228 6.0021 5.9844 5.9697 5.9573 5.9468 5.9373			+.018 010 +.020 +.010 000 +.025 021 047 030 .000 .000 +.030
1926 I F M AM J J AS OND	5.973 5.960 6.012 5.982 5.947 5.969 5.973 5.964 5.964 5.933 5.990	5.9631 5.9647 5.9655 5.9655 5.9650 5.9643 5.9640 5.9645 5.9661 5.9691 5.9786	5.9464 5.9527 5.9527 5.9658 5.9723 5.9723 5.9866 5.9866 5.9937 6.0010 6.0085 6.0162 6.0239	+.0167 +.0120 +.0064 0003 0073 0153 0226 0292 0349 0394 0453	+.020 012 +.015 +.008 +.001 +.026 019 046 025 +.003 +.001	1931 JFM AM JASOND	5.881 5.884 5.929 5.941 5.961 5.852 5.799 5.852 5.852 5.763	5.9279 5.9181 5.9077 5.8962 5.8835 5.8695 5.8537 5.8362 5.8170 5.7967 5.7755 5.7543			+.018 010 +.020 +.010 .000 +.025 021 047 030 .000 .000 +.030
1927 F M A M J J A S O N D	5.985 6.002 6.029 6.019 6.003 6.016 6.055 6.076 6.039 6.044 6.068	5.9849 5.9918 5.9991 6.0069 6.0150 6.0233 6.0319 6.0406 6.0492 6.0576 6.0657 6.0657	6.0311 6.0388 6.0462 6.0534 6.0605 6.0676 6.0743 6.0811 6.0874 6.0936 6.0794 6.1051	0464 0470 0471 0455 0455 0443 0405 0382 0360 0337 0315	+.019 011 +.017 +.002 +.001 +.026 020 046 030 +.002 +.001 +.001	1932 F M A M J A S O N D	5.738 5.705 5.697 5.620 5.630 5.634 5.685 5.704 5.621 5.515 5.624	5. 7336 5. 7139 5. 6954 5. 6781 5. 6624 5. 6485 5. 6368 5. 6279 5. 6188 5. 6188 5. 6188 5. 6186 5. 6204			+.018 010 +.020 +.010 .0000 +.025 021 047 030 .0000 +.030
1928 JF MAM JASOND	6.068 6.063 6.141 6.134 6.163 6.154 6.074 6.101 6.141 6.163 6.181 6.200	6.0815 6.0898 6.0986 6.1078 6.1175 6.1273 6.1368 6.1461 6.1544 6.1648 6.1747 6.1853	6.1104 6.1153 6.1199 6.1242 6.1278 6.1312 6.1339 6.1362 6.1380 6.1392 6.1398 6.1397	0289 0255 0213 0164 0103 0039 +.0029 +.0074 +.0256 +.0349 +.0456	+.019 010 +.019 +.010 +.020 020 047 030 +.001 +.031	1933 J F M A M J A S O N D	5.585 5.643 * 5.592 5.654 5.722 5.769 5.672 5.644 5.632 5.609 5.593	5.6235 5.6275 5.6318 5.6362 5.6408 5.6459 5.6515 5.6573 5.6673 5.6673 5.6701 5.6708			+.018 010 +.020 +.010 +.025 021 047 030 .000 +.030
1929 J F M A M J A S O N D	6.228 6.228 6.232 6.194 6.208 6.133 6.222 6.245 6.255 6.309 6.252 6.079	6.1963 6.2069 6.2165 6.2238 6.2279 6.2281 6.2245 6.2172 6.2065 6.1932 6.1777 6.1598	6.1392 6.1377 6.1357 6.1332 6.1299	+.0571 +.0692 +.0808 +.0906 +.0980	+.019 010 +.020 +.010 .000 +.026 021 047 030 +.001	1934 J F M A M J A S O N D	5.637 5.684 5.682 5.742 5.675 5.685 5.671 5.645 5.603 5.598 5.578	5.6695 5.6664 5.6622 5.6578	-		+.018 010 +.020 +.010 .000 +.025 021 047 030 .000 .000 +.030

^{*}Not available, complete data not having been reported on account of bank holidays.

TABLE 28-Concluded

BANK DEBITS IN NEW YORK CITY

Date	1	2	3	4	5	Date	1	2	3	4	5
1935 JF M A M J A S O N D	5.667 5.661 5.690 5.714 5.672 5.693 5.753 5.724 5.699 5.705 5.714 5.726				+.018 010 +.020 +.010 .000 +.025 021 047 030 .000 +.030	1936 J	5.744				+.018

TABLE 29

DAILY AVERAGE BANK CLEARINGS OUTSIDE NEW YORK CITY, MONTHLY, JANUARY 1875 - JANUARY 1919, INCLUSIVE; DAILY AVERAGE BANK DEBITS FOR 140 OUTSIDE CITIES, MONTHLY, JANUARY 1919 - JANUARY 1936

- Col. 1. Logarithms of Data (in thousands of dollars) Adjusted for Seasonal Fluctuations.
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).
- Col. 5. Changing Seasonal Fluctuations (logarithms).

For details of the nature of the graduations given in Columns 2 and 3 and of the seasonal given in Column 5 of this table, see Appendix D.

¹See Table 27.

TABLE 29

Date	1	2	3	4	5	Date	1	2	3	4	5
1875 F M A M J A SOND	4.458 4.473 4.515 4.490 4.468 4.529 4.470 4.502 4.464 4.400 4.505 4.460	4.4802 4.4796 4.4795 4.4799 4.4806 4.4815 4.4822 4.4822 4.4814 4.4797 4.4771 4.4739	4.4948 4.4927 4.4903 4.4880 4.4853 4.4829 4.4775 4.4746 4.4719 4.4691 4.4664	0146 0131 0108 0031 0047 0014 +.0020 +.0047 +.0068 +.0078 +.0080 +.0075	+.031 007 +.005 010 003 026 041 +.033 +.046 +.009	1880 F M A M J A S O N D	4.568 4.565 4.582 4.583 4.545 4.558 4.556 4.558 4.558 4.558 4.544 4.597 4.623	4.5506 4.5557 4.5590 4.5611 4.5622 4.5631 4.5643 4.5666 4.5705 4.5765 4.5849 4.5954	4.5281 4.5341 4.5402 4.5462 4.5521 4.5584 4.5702 4.5761 4.5818 4.5875 4.5931	+.0225 +.0216 +.0188 +.0149 +.0101 0036 0056 0053 0026 +.0023	+.00 00 00 00 00 00 00 +.00 +
1876 F M AM J ASOND	4.470 4.462 4.500 4.436 4.453 4.484 4.439 4.485 4.446 4.428 4.459 4.460	4.4705 4.4672 4.4644 4.4623 4.4607 4.4595 1.4584 4.4571 4.4556 4.4538 4.4520 4.4502	4.4636 4.4609 4.4583 4.45532 4.4510 4.4487 4.4465 4.4444 4.4426 4.4408 4.4391	+.0069 +.0063 +.0061 +.0055 +.0075 +.0085 +.0097 +.0106 +.0112 +.0112 +.0112 +.0111	+.032 007 +.002 009 003 027 041 031 +.034 +.044 +.013	1881 F M A M J A S O N D	4.611 4.633 4.617 4.626 4.654 4.698 4.624 4.700 4.688 4.672 4.659 4.663	4.6075 4.6205 4.6333 4.6448 4.6544 4.6614 4.6657 4.6675 4.6675 4.6659 4.6634 4.6605	4.5987 4.6038 4.6038 4.6138 4.6185 4.6228 4.6269 4.6307 4.6342 4.6374 4.6402 4.6428	+.0088 +.0167 +.0244 +.0310 +.0359 +.0388 +.0369 +.0333 +.0285 +.0232 +.0177	+.00 00 00 00 00 00 00 +.00 +
1877 F M A M J J A S O N D	4.441 4.456 4.458 4.434 4.477 4.406 4.427 4.446 4.445 4.445 4.429 4.447 4.429	4.4487 4.4477 4.4468 4.4462 4.4453 4.4443 4.1425 4.4402 4.4373 4.4341 4.4309 4.4276	4.4375 4.4363 4.4351 4.4342 4.4333 4.4327 4.4323 4.4322 4.4322 4.4326 4.4331 4.4337	+.0112 +.0114 +.0117 +.0120 +.0122 +.0116 +.0102 +.0080 +.0051 +.0015 0022 0061	+.033 007 002 009 004 028 041 035 +.035 +.042 +.018	1882 F M A M J A S O N D	4.639 4.641 4.641 4.644 4.641 4.649 4.661 4.663 4.679 4.646 4.661 4.661	4.6575 4.6547 4.6524 4.6505 4.6493 4.6489 4.6504 4.6522 4.6522 4.6563 4.6579	4.6451 4.6470 4.6487 4.6500 4.6510 4.6517 4.6522 4.6523 4.6523 4.6521 4.6517 4.6510	+.0124 +.0077 +.0037 +.0005 0017 0028 0019 0010 +.0021 +.0046 +.0069	+.00 00 00 00 00 00 00 +.0. +.0.
1878 J F M A M J A S O N D	4.475 4.406 4.379 4.398 4.423 4.383 4.453 4.454 4.456 4.390 4.390	4.4246 4.4218 4.4193 4.4169 4.4149 4.4133 4.4122 4.4116 4.4119 4.4131 4.4151 4.4183	4.4347 4.4358 4.4373 4.4392 4.4411 4.4435 4.4461 4.4488 4.4517 4.4548 4.4583 4.4620	0101 0140 0180 0223 0262 0302 0339 0372 0398 0417 0432 0437	+.033 007 005 008 004 027 042 028 +.035 +.041 +.021	1883 J F M A M J J A S O N D	4.657 4.660 4.661 4.639 4.664 4.673 4.660 4.652 4.652 4.654 4.641	4.6591 4.6596 4.6596 4.6592 4.6588 4.6582 4.6574 4.6574 4.6562 4.6544 4.6515	4.6502 4.6493 4.6483 4.6459 4.6459 4.6433 4.6421 4.6409 4.6397 4.6385 4.6374	+.0089 +.0103 +.0113 +.0129 +.0138 +.0149 +.0158 +.0165 +.0165 +.0165 +.0141	+.00 00 00 00 00 00 +.00 +.00
1879 F M A M J A S O N D	4.536	4.4226 4.4282 4.4355 4.4446 4.4554 4.4679 4.4816 4.4958 4.5097 4.5227 4.5339 4.5433	4.4662 4.4704 4.4748 4.4795 4.4843 4.4892 4.4943 4.4997 4.5052 4.5167 4.5167	0436 0422 0393 0349 0289 0213 0127 0039 +.0045 +.0118 +.0172 +.0210	+.033 008 009 007 004 026 042 027 +.036 +.039 +.024	1884 I F M A M J J A S O N D	4.648 4.642 4.633 4.657 4.660 4.594 4.602 4.594 4.591 4.563 4.606	4.6486 4.6437 4.6381 4.6316 4.6249 4.6170 4.6103 4.6039 4.5981 4.5981 4.5981 4.5892 4.5867	4.6364 4.6355 4.6347 4.6339 4.6332 4.6322 4.6320 4.6320 4.6320 4.6320 4.6320 4.6320 4.6320	+.0122 +.0082 +.0034 0083 0156 0219 0281 0339 0389 0459	+.00 00 00 +.00 00 +.00 +.00 +.00

TABLE 29-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1885 JF M A M J J A S O N D	4.608 4.580 4.584 4.606 4.579 4.612 4.631 4.598 4.618 4.640 4.656 4.666	4.5860 4.5871 4.5901 4.5946 4.6003 4.6069 4.6140 4.6211 4.6282 4.6351 4.6478	4.6331 4.6338 4.6338 4.6359 4.6371 4.6385 4.6400 4.6417 4.6437 4.6457 4.6457 4.64502	0471 0467 0447 0443 0368 0316 0260 0206 0155 0106 0063 0024	+.020 016 018 002 002 +.002 014 045 020 +.038 +.031 +.026	1890 J F M A M J A S O N D	4.820 4.813 4.817 4.833 4.860 4.838 4.853 4.854 4.854 4.854 4.837 4.813	4.8134 4.8211 4.8283 4.8346 4.8396 4.8429 4.8445 4.8443 4.8424 4.8392 4.8392 4.8392 4.8309	4.8092 4.8119 4.8146 4.8172 4.8198 4.8221 4.8244 4.8267 4.8289 4.8308 4.8328 4.8344	+.0042 +.0092 +.0137 +.0174 +.0198 +.0208 +.0201 +.0176 +.0135 +.0084 +.0024 0035	+.017 018 +.001 +.003 013 046 026 +.036 +.036 +.036
1886 JF M A M J J ASOND	4.646 4.664 4.681 4.652 4.642 4.678 4.695 4.683 4.694 4.708 4.720	4.6534 4.6585 4.6629 4.6670 4.6748 4.6791 4.6842 4.6900 4.6966 4.7038 4.7112	4.6526 4.6553 4.6580 4.6608 4.6665 4.6665 4.6667 4.6729 4.6762 4.6762 4.67830 4.6866	+.0008 +.0032 +.0049 +.0062 +.0073 +.0083 +.0113 +.0138 +.0171 +.0208 +.0246	+.018 017 018 002 001 +.003 013 045 020 +.038 +.031 +.026	1891 F M A M J A S O N D	4.819 4.817 4.804 4.828 4.810 4.829 4.830 4.870 4.844 4.829 4.840	4.8267 4.8232 4.8208 4.8197 4.8200 4.8217 4.8253 4.8291 4.8333 4.8376 4.8416 4.8444	4.8359 4.8372 4.8384 4.8396 4.8404 4.8413 4.8424 4.8426 4.8426 4.8428 4.8429 4.8428	0092 0140 0176 0199 0204 0167 0163 0093 0052 0013 +.0016	+.018016018 +.002 +.003013046025 +.031 +.031 +.035
1887 J.F.M.A.M.J.J.A.S.O.N.D.	4.691 4.707 4.752 4.745 4.738 4.767 4.727 4.735 4.738 4.714 4.747 4.724	4.7183 4.7248 4.7303 4.7343 4.7371 4.7384 4.7371 4.7352 4.7327 4.7302 4.7281	4.6902 4.6939 4.6977 4.7015 4.7054 4.7033 4.7132 4.7171 4.7210 4.7248 4.7286 4.7324	+.0281 +.0309 +.0326 +.0328 +.0317 +.0291 +.0251 +.0079 +.0016 0043	+.017 017 018 001 000 +.004 012 045 020 +.038 +.030 +.025	1892 JF M A M J A S O N D	4.838 4.873 4.859 4.849 4.840 4.873 4.861 4.879 4.882 4.869 4.882 4.891	4.8475 4.8503 4.8533 4.8569 4.8613 4.8666 4.8726 4.8788 4.8882 4.8880 4.8900 4.8884	4.8426 4.8423 4.8419 4.8408 4.8400 4.8393 4.8385 4.8375 4.8366 4.8355 4.8342	+.0049 +.0080 +.0114 +.0157 +.0205 +.0266 +.0333 +.0403 +.0407 +.0514 +.0545 +.0542	+.019016017 +.002 +.002014026 +.031 +.031 +.025
1888 JFM AM JASOND	4.716 4.729 4.716 4.725 4.742 4.734 4.736 4.758 4.747 4.781 4.754	4.7267 4.7264 4.7273 4.7295 4.7329 4.7371 4.7420 4.7473 4.7525 4.7555 4.7620 4.7658	4.7362 4.7399 4.7435 4.7470 4.7503 4.7537 4.7569 4.7659 4.7659 4.7689 4.7718	0095 0135 0162 0175 0174 0166 0149 0127 0105 0084 0069	+.016 017 018 .000 +.001 +.004 012 046 021 +.037 +.030 +.024	1893 Jr M A M J A S O N D	4.888 4.894 4.883 4.873 4.874 4.791 4.723 4.746 4.775 4.779 4.774	4.8834 4.8753 4.8644 4.8506 4.8362 4.8212 4.8065 4.7927 4.7806 4.7708 4.7639 4.7601	4.8329 4.8317 4.8303 4.8289 4.8272 4.8257 4.8239 4.8233 4.8208 4.8193 4.8177 4.8162	+.0505 +.0436 +.0341 +.0217 +.0090 0045 0174 0296 0402 0485 0538 0561	+.020 015 016 +.003 +.004 015 046 021 +.033 +.031 +.026
J F M A M J A S O N D	4.774 4.778 4.773	4.7690 4.7714 4.7733 4.7749 4.7763 4.7763 4.7779 4.7801 4.7872 4.7872 4.7872 4.7924 4.7987	4.7950 4.7978 4.8005 4.8034	0058 0062 0073 0087 0100 0114 0120 0119 0106 0081 0047 0005	+.017 017 018 +.001 +.003 012 046 022 +.037 +.030 +.024	1894 J F M A M J A S O N D	4.784 4.759 4.776 4.771 4.780 4.772 4.768 4.804 4.790 4.800 4.799 4.798	4.7593 4.7611 4.7648 4.7696 4.7747 4.7794 4.7833 4.7864 4.7891 4.7917 4.7947 4.7985	4.8146 4.8130 4.8116 4.8101 4.8089 4.8076 4.8064 4.8052 4.8042 4.8032 4.8022 4.8013	0553 0519 0468 0405 0342 0282 0231 0151 0115 0075 0028	+.021 015 +.004 +.002 016 027 +.031 +.030 +.027

TABLE 29-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
I 895 F M A M J A S O N D	4.810 4.776 4.797 4.814 4.833 4.824 4.854 4.854 4.857 4.862 4.862 4.862 4.845 4.845	4,8030 4,8082 4,8138 4,8194 4,8246 4,8292 4,8330 4,8356 4,8370 4,8370 4,8356 4,8328	4.8006 4.8000 4.7995 4.7995 4.7985 4.7983 4.7981 4.7982 4.7983 4.7983 4.7987 4.7994 4.8002	+.0024 +.0082 +.0143 +.0204 +.0261 +.0309 +.0349 +.0374 +.0387 +.0362 +.0326	+.022 014 014 +.004 +.003 +.002 016 047 028 +.030 +.030 +.028	1900 J F M A M J J A S O N D	4.969 4.972 4.973 4.968 4.975 4.981 4.968 4.970 4.956 4.979 4.995 4.993	4.9758 4.9729 4.9702 4.9682 4.9672 4.9675 4.9674 4.9730 4.9730 4.9783 4.9851 4.9931 5.0017	4.9743 4.9787 4.9830 4.9872 4.9912 4.9952 4.9991 5.0028 5.0063 5.0098 5.0131 5.0164	+.0015 0058 0128 0190 0240 0277 0297 0298 0247 0200 0147	+.02 01 00 +.00 01 04 02 +.02 +.02
1896 J F M A M J A S O N D	1,818 1,809 4,815 4,815 4,802 4,815 2,819 4,774 4,784 4,795 4,796 4,812	1.8288 1.8238 4.8183 4.8183 4.8069 4.8069 4.7971 4.7935 4.7909 1.7894 1.7893 1.7906	4.8011 4.8023 4.8038 4.8054 4.8071 4.8093 4.8114 4.8137 4.8163 4.8189 4.8216 4.8247	+.0277 +.0215 +.0145 +.0071 0076 0143 0202 0254 0295 0323 0341	+.022 014 013 +.005 +.001 016 047 028 +.029 +.029 +.029	1901 F M A M J A S O N D	5.016 5.014 5.020 5.056 5.069 5.047 5.052 5.054 5.029 5.049 5.053 5.041	5.0106 5.0192 5.0272 5.0342 5.0403 5.0451 5.0488 5.0515 5.0533 5.0536 5.0556 5.0567	5.0194 5.0224 5.0252 5.0280 5.0306 5.0332 5.0357 5.0381 5.0402 5.0426 5.0447 5.0467	0088 0032 +.0020 +.0062 +.0097 +.0131 +.0131 +.0134 +.0131 +.0100 +.0100	+.02 01 00 +.00 01 04 02 +.02 +.02
1897 F M A M J A S O N D	4.784 4.798 4.798 4.803 4.793 4.818 4.838 4.853 4.854 4.854 4.867 4.873	1.7934 1.7978 4.8037 4.8109 4.8192 4.8283 4.8376 4.8466 4.8547 4.8616 1.8668 1.8702	4.8279 4.8310 4.8344 4.8378 4.8410 4.8445 4.8479 4.8514 4.8550 4.8584 4.8620 4.8658	0345 0332 0307 0269 0218 0162 0103 0048 0003 +.0032 +.0044	+.023 013 011 +.006 +.001 016 048 029 +.027 +.028 +.028	1902 JF M A M J J A S O N D	5.067 5.055 5.054 5.081 5.081 5.048 5.090 5.063 5.063 5.063 5.071	5.0580 5.0597 5.0617 5.0641 5.0665 5.0690 5.0713 5.0734 5.0752 5.0769 5.0785 5.0801	5.0486 5.0504 5.0523 5.0543 5.0563 5.0582 5.0600 5.0618 5.0637 5.0656 5.0675 5.0675	+.0094 +.0093 +.0094 +.0102 +.0108 +.0113 +.0116 +.0115 +.0110 +.0107	+.00 00 +.00 00 00 00 +.00 +.00
1898 JF M A M J A S O N D	4.867 4.890 4.883 4.857 4.866 4.888 4.851 4.888 4.878 4.911 4.931	4.8721 4.8727 4.8727 4.8727 4.8737 4.8736 4.8795 4.8855 4.8928 4.9024 4.9133 4.9249	4.8696 4.8733 4.8771 4.8810 1.8849 4.8887 4.8929 4.8971 4.9014 4.9057 4.9101 4.9146	+.0025 0006 0044 0083 0112 0131 0116 0086 0033 +.0032 +.0103	+.024 012 010 +.006 .000 +.001 048 029 +.027 +.027	I903 J F M A M J J A S O N D	5.084 5.083 5.075 5.087 5.075 5.105 5.105 5.079 5.090 5.090 5.064 5.078	5.0816 5.0832 5.0847 5.0859 5.0866 5.0868 5.0863 5.0863 5.0850 5.0831 5.0806 5.0779 5.0753	5.0712 5.0731 5.0751 5.0751 5.0772 5.0816 5.0839 5.0864 5.0914 5.0939 5.0966	+.0104 +.0101 +.0096 +.0087 +.0072 +.0052 +.0024 0014 0057 0108 0160 0213	+.0 0 +.0 0 0 0 0 +.0 +.0 +.0
IS99 JFMAM JASOND	4.946 4.966 4.983 4.963 4.972 4.970 4.982 4.994 4.982 4.982 4.977	4.9366 4.9483 4.9586 4.9674 4.9745 4.9830 4.9846 4.9846 4.9834 4.9814 4.9788	4.9190 4.9237 4.9283 4.9329 4.9374 4.9419 4.9467 4.9514 4.9561 4.9606 4.9651 4.9697	+.0176 +.0246 +.0303 +.0345 +.0371 +.0378 +.0363 +.0285 +.0228 +.0163	+.025 012 008 +.007 001 +.001 016 048 029 +.026 +.026	A M J J	5.067 5.076 5.076 5.074 5.057 5.080 5.074 5.091 5.104 5.101 5.133	5.0731 5.0718 5.0717 5.0730 5.0756 5.0756 5.0796 5.0847 5.0906 5.0970 5.1035 5.1100 5.1163	5.0991 5.1018 5.1045 5.1072 5.1101 5.1128 5.1157 5.1184 5.1211 5.1238 5.1265 5.1292	0260 0300 0328 0342 0345 0332 0310 0278 0241 0203 0165 0129	+.00 +.00 +.00 +.00 00 00 +.00 +.00

TABLE 29-Continued

Date	1	2	3	4	5	Date	1	2	3	4	5
1905 J F M A M J A S O N D	5.106 5.121 5.140 5.133 5.149 5.147 5.136 5.157 5.164 5.156 5.175 5.178	5.1222 5.1279 5.1333 5.1385 5.1437 5.1488 5.1537 5.1584 5.1628 5.1669 5.1705 5.1737	5.1319 5.1344 5.1370 5.1396 5.1421 5.1445 5.1449 5.1493 5.1518 5.1541 5.1564 5.1586	0097 0065 0037 0011 +.0016 +.0043 +.0068 +.0091 +.0110 +.0128 +.0141 +.0151	+.027 010 +.001 +.008 009 003 012 044 026 +.022 +.019	1910 J F M A M J A S O N D	5.260 5.263 5.285 5.274 5.256 5.270 5.259 5.261 5.262 5.265 5.265 5.269 5.267	5.2671 5.2685 5.2692 5.2692 5.2687 5.2668 5.2656 5.2644 5.2634 5.2636 5.2626 5.2622	5.2402 5.2426 5.2450 5.2477 5.2502 5.2529 5.2555 5.2581 5.2607 5.2634 5.2660 5.2687	+.0269 +.0259 +.0242 +.0215 +.0185 +.0139 +.0101 +.0063 +.0027 0008 0038 0066	+.025 009 +.006 +.008 014 005 012 044 023 +.028 +.022 +.019
1906 JF M A M J A S O N D	5.201 5.194 5.185 5.167 5.179 5.186 5.176 5.198 5.183 5.210 5.216 5.206	5.1766 5.1790 5.1811 5.1831 5.1850 5.1870 5.1896 5.1930 5.1973 5.2027 5.2089 5.2154	5.1608 5.1630 5.1652 5.1673 5.1692 5.1713 5.1733 5.1752 5.1770 5.1788 5.1807 5.1824	+.0158 +.0160 +.0159 +.0158 +.0158 +.0163 +.0178 +.0203 +.0239 +.0282 +.0330	+.027 010 +.002 +.008 010 004 012 043 025 +.027 +.027 +.019	1911 F M AM J J ASOND	5.262 5.261 5.272 5.252 5.270 5.280 5.267 5.277 5.282 5.265 5.283 5.278	5.2625 5.2632 5.2643 5.2656 5.2674 5.2692 5.2713 5.2736 5.2761 5.2786 5.2815 5.2848	5.2713 5.2739 5.2764 5.2787 5.2809 5.2830 5.2849 5.2868 5.2865 5.2900 5.2926	0088 0107 0121 0131 0135 0138 0132 0124 0114 0098 0078	+.024 +.008 +.008 012 012 044 023 +.028 +.022 +.019
1907 JF MAM JASOND	5.225 5.225 5.222 5.223 5.234 5.217 5.234 5.230 5.213 5.213 5.213 5.213 5.2109	5.2216 5.2266 5.2298 5.2312 5.2280 5.2231 5.2158 5.2066 5.1956 5.1859 5.1755 5.1671	5.1842 5.1859 5.1877 5.1893 5.1908 5.1922 5.1937 5.1950 5.1965 5.1977 5.1990 5.2003	+.0374 +.0407 +.0427 +.0419 +.0372 +.0309 +.0221 +.0116 0009 0118 0235 0332	+.027 010 +.003 +.008 011 004 012 043 024 +.027 +.021 +.019	1912 F M AM J A S O N D	5.290 5.301 5.291 5.311 5.311 5.289 5.308 5.308 5.305 5.333 5.325 5.313	5.2883 5.2921 5.2961 5.3002 5.3043 5.3081 5.3116 5.3144 5.3168 5.3184 5.3194 5.3198	5.2936 5.2943 5.2951 5.2951 5.2961 5.2968 5.2969 5.2969 5.2969 5.2969 5.2969	0053 0022 +.0010 +.0045 +.0116 +.0148 +.0175 +.0199 +.0215 +.0225 +.0228	+.023 +.006 +.006 012 005 012 023 +.020 +.022 +.020
1908 J F M A M J A S O N D	5.155 5.143 5.145 5.156 5.157 5.157 5.165 5.192 5.191 5.191 5.207	5.1593 5.1535 5.1501 5.1494 5.1502 5.1545 5.1597 5.1679 5.1761 5.1844 5.1923 5.2006	5.2015 5.2027 5.2039 5.2051 5.2062 5.2076 5.2088 5.2099 5.2111 5.2124 5.2138 5.2152	0422 0492 0557 0557 0560 0531 0491 0420 0350 0280 0215 0146	+.026 010 +.004 +.007 013 005 011 043 024 +.027 +.021 +.019	1913 F M A M J A S O N D	5.331 5.334 5.306 5.317 5.318 5.308 5.319 5.308 5.328 5.328 5.332 5.332	5.3198 5.3192 5.3189 5.3186 5.3186 5.3189 5.3196 5.3204 5.3215 5.3221 5.3225 5.3222	5.2970 5.2970 5.2972 5.2975 5.2978 5.2982 5.2987 5.2993 5.3001 5.3008 5.3019 5.3031	+.0228 +.0222 +.0217 +.0211 +.0208 +.0207 +.0211 +.0214 +.0213 +.0216 +.0191	+.022 010 +.005 +.007 014 011 043 022 +.029 +.023
1909 J F M A M J J A S O N D	5.202 5.209 5.220 5.227 5.219 5.237 5.238 5.242 5.256 5.252 5.265 5.271	5.2065 5.2126 5.2184 5.2240 5.2298 5.2356 5.2414 5.2470 5.2522 5.2568 5.2607 5.2638	5.2167 5.2182 5.2199 5.2217 5.2234 5.2274 5.2274 5.2274 5.2313 5.2335 5.2356 5.2379	0102 0056 0015 +.0023 +.0102 +.0102 +.0140 +.0176 +.0209 +.0233 +.0251 +.0259	+.026 009 +.005 +.008 013 005 012 044 023 +.028 +.022 +.019	1914 F M A M J A S O N D	5.327 5.319 5.316 5.324 5.301 5.325 5.325 5.282 5.282 5.271 5.260 5.279	5.3211 5.3190 5.3162 5.3124 5.3084 5.3037 5.2989 5.2944 5.2905 5.2871 5.2850 5.2843	5.3045 5.3060 5.3077 5.3096 5.3116 5.3138 5.3163 5.3189 5.3216 5.3246 5.3279 5.3312	+.0166 +.0130 +.0085 +.0028 0032 0101 0174 0245 0311 0375 0429 0469	+.021 011 +.004 +.007 014 003 011 042 021 +.030 +.023 +.021

TABLE 29-Continued

BANK CLEARINGS OUTSIDE NEW YORK CITY

Date	1	2	3	4	5	Date	1	2	3	-4	5
1915 IFM AM JASOND	5.286 5.305 5.308 5.315 5.305 5.314 5.319 5.333 5.335 5.383 5.383 5.393	5.2851 5.2877 5.2923 5.2986 5.3066 5.3157 5.3257 5.3257 5.3465 5.3465 5.3568 5.3670 5.3772	5.3349 5.3386 5.3428 5.3471 5.3516 5.3561 5.3613 5.3665 5.3718 5.3774 5.3833 5.3893	0498 0509 0505 0485 0450 0404 0356 0305 0253 0206 0163 0121	+.019 013 +.003 +.005 014 001 011 041 019 +.030 +.023 +.022	F M A M J A S O N	5.514 5.517 5.532 5.537 5.554 5.548 5.541 5.563 5.546 5.578 5.578 5.596	5.5117 5.5212 5.5298 5.5372 5.5483 5.5482 5.5523 5.5561 5.5601 5.5648 5.5705 5.5774	5.4876 5.4965 5.5055 5.5145 5.5233 5.5326 5.5414 5.5503 5.5592 5.5682 5.5768 5.5851	+.0241 +.0243 +.0227 +.0200 +.0156 +.0109 +.0058 +.0009 0034 0063 0077	+.017 017 +.001 +.002 014 +.002 011 036 016 +.030 +.021 +.024
1916 IF MAAM J JASOND	5.384 5.410 5.421 5.409 5.432 5.432 5.454 5.454 5.454 5.450 5.509 5.502	5.3874 5.3978 5.4083 5.4188 5.4293 5.4397 5.4499 5.4600 5.4703 5.4806 5.4910 5.5015	5.3955 5.4019 5.4086 5.4157 5.4229 5.4307 5.4381 5.4461 5.4537 5.4621 5.4702 5.4789	0081 0041 0041 +.0031 +.0064 +.0139 +.0118 +.0139 +.0166 +.0185 +.0208	+.018 015 +.002 +.004 014 039 018 +.030 +.032 +.022	F M A M I A S O N	5.567 5.572 5.597 5.612 5.626 5.641 5.664 5.644 5.635	5.5852 5.5936 5.6021 5.6104 5.6179 5.6245 5.6301 5.6347 5.6387 5.6423 5.6423 5.6423 5.6458 5.6495	5.5934 5.6014 5.6092 5.6168 5.6241 5.6311 5.6379 5.6441 5.6499 5.6558 5.6611 5.6659	0082 0078 0071 0064 0062 0078 0078 0112 0135 0153 0164	+.015 019 .000 +.001 013 +.003 010 035 014 +.029 +.018 +.025

BANK DEBITS FOR 140 OUTSIDE CITIES

Date	1	2	3	4	5	Date	1	2	3	4	5
1915 MAM LASOZO	5.719 5.709 5.698 5.709 5.744 5.764 5.789 5.790 5.793 5.787 5.787	5.7158 5.7268 5.7269 5.7341 5.7425 5.7520 5.7625 5.7625 5.7734 5.7845 5.7952 5.8052 5.8052 5.8141	5.7324 5.7366 5.7406 5.7443 5.7477 5.7508 5.7537 5.7562 5.7662 5.7640	0166 0158 0137 0102 0052 +.0012 +.0012 +.0172 +.0261 +.0347 +.0429 +.0501	+.015 020 .000 .000 013 +.005 010 034 013 +.027	F M AM J ASON	5.751 5.737 5.726 5.724 5.708 5.715 5.700 5.716 5.725 5.707 5.716	5.7635 5.7509 5.7392 5.7288 5.7201 5.7134 5.7089 5.7064 5.7059 5.7068 5.7089 5.7089 5.7115	5.7685 5.7680 5.7675 5.7668 5.7660 5.7653 5.7646 5.7637 5.7630 5.7623 5.7617	0050 0171 0283 0380 0459 0557 0573 0571 0555 0528 0496	+.013 020 +.001 .000 013 +.008 010 034 011 +.025 +.010 +.029
1920 F M A M J A S O N D	5.832 5.806 5.834 5.831 5.816 5.829 5.837 5.818 5.831 5.802 5.801 5.793	5 .8215 5 .8272 5 .8312 5 .8332 5 .8330 5 .8308 5 .8263 5 .8109 5 .8005 5 .763	5.7652 5.7664 5.7674 5.7682 5.7693 5.7693 5.7697 5.7697 5.7697 5.7694 5.7688	+.0563 +.0608 +.0650 +.0650 +.0615 +.0567 +.0498 +.0412 +.0311 +.0197 +.0075	+.014 020 .000 .000 013 +.007 010 033 012 +.027 +.012 +.028	1922 J F M A J J A S O	5.697 5.720 5.725 5.717 5.733 5.749 5,732	5.7144 5.7175 5.7208 5.7243 5.7285 5.7336 5.7396 5.7396 5.7465 5.7540 5.7616 5.7689 5.7756	5.7606 5.7601 5.7598 5.7595 5.7593 5.7593 5.7594 5.7600 5.7604 5.7604 5.7611 5.7619	0462 0426 0390 0352 0358 0257 0198 0131 0060 +.0012 +.0078 +.0137	+.012 020 +.002 +.002 +.001 012 +.009 010 035 011 +.024 +.008 +.030

TABLE 29-Continued

BANK DEBITS FOR 140 OUTSIDE CITIES

Date	1	2	3	-1	5	Date	1	2	3	4	5
1923 F M A M J I A S O N D	5.791 5.800 5.799 5.795 5.804 5.778 5.783 5.770 5.781 5.785 5.788	5.7813 5.7859 5.7859 5.7852 5.7915 5.7928 5.7931 5.7928 5.7918 5.7904 5.7867 5.7850	5.7628 5.7640 5.7653 5.7667 5.7681 5.7698 5.7717 5.7738 5.7759 5.7782 5.7806 5.7831	+.0185 +.0219 +.0239 +.0247 +.0233 +.0247 +.0233 +.0211 +.0180 +.0145 +.0103 +.0061 +.0019	+.011 019 +.003 +.002 011 +.010 010 036 010 +.023 +.006 +.030	1928 F M A M J A S O N D	5.898 5.890 5.915 5.936 5.936 5.946 5.896 5.918 5.921 5.931 5.933 5.952	5.9039 5.9069 5.9102 5.9134 5.9167 5.9169 5.9228 5.9256 5.9255 5.9353 5.9353 5.9396	5.9225 5.9247 5.9267 5.9286 5.9303 5.9319 5.9332 5.9339 5.9345 5.9346 5.9344 5.9344	0186 0178 0165 0152 0136 0120 0104 0083 0060 0030 +.0098 +.0052	+.009 015 +.006 +.005 007 +.009 040 010 +.020 +.023 +.029
1924 F M AM J ASOND	5.785 5.799 5.788 5.796 5.789 5.775 5.790 5.795 5.794 5.807 5.793 5.818	5.7838 5.7833 5.7838 5.7850 5.7871 5.7898 5.7932 5.7970 5.8012 5.8058 5.8106 5.8158	5.7859 5.7887 5.7916 5.7945 5.7975 5.8005 5.8035 5.8066 5.8098 5.8127 5.8157 5.8187	0021 0054 0078 0078 0104 0107 0103 0096 0386 0369 0051 0029	+.011 018 +.004 +.003 010 010 037 010 +.022 +.005 +.030	1929 JF MA M J ASOND	5.949 5.956 5.952 5.946 5.939 5.936 5.972 6.000 5.969 5.975 5.975 5.910	5.9444 5.9496 5.9546 5.9589 5.9622 5.9641 5.9630 5.9602 5.9602 5.9558 5.9500 5.9430	5,9342 5,9333 5,9320 5,9304 5,9282	+.0102 +.0163 +.0226 +.0285 +.0340	+.009 014 +.006 +.005 007 +.009 040 010 +.019 +.003 +.029
1925 F M AM J ASOND	5.847 5.839 5.834 5.829 5.849 5.852 5.845 5.853 5.869 5.848 5.860	5.8211 5.8266 5.8320 5.8362 5.8410 5.8454 5.8493 5.8526 5.8565 5.8569 5.8609 5.8625	5.8216 5.8245 5.8273 5.8300 5.8326 5.8353 5.8379 5.8404 5.8429 5.8456 5.8456 5.8451 5.8507	0005 +.0021 +.0047 +.0062 +.0084 +.0101 +.0114 +.0122 +.0136 +.0133 +.0128 +.0118	+.010 017 +.004 +.003 010 +.010 009 038 010 +.021 +.004 +.030	1930 JF M A M J A S O N D	5.911 5.900 5.900 5.904 5.902 5.906 5.883 5.870 5.860 5.864 5.815 5.843	5.9349 5.9259 5.9160 5.9056 5.8951 5.8857 5.8657 5.8657 5.8657 5.8424 5.8424 5.8352			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029
1926 F M A M J A S O N D	5.872 5.872 5.874 5.872 5.849 5.844 5.885 5.862 5.863 5.863 5.863	5.8636 5.8643 5.8646 5.8645 5.8643 5.8640 5.8639 5.8641 5.8649 5.8661 5.8679 5.8700	5.8531 5.8558 5.8585 5.8585 5.8611 5.8638 5.8667 5.8725 5.8725 5.8755 5.8787 5.8846 5.8847	+.0105 +.0085 +.0061 +.0034 +.0005 0027 0057 0084 0106 0126 0137 0147	+.010 016 +.005 +.004 009 +.010 039 010 +.021 +.024 +.029	J F M A M J A S O N D		5.8280 5.8202 5.8119 5.8030 5.7935 5.7635 5.7608 5.7608 5.7482 5.7347 5.7205 5.7058			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029
1927 F M A M J A S O N D	5.870 5.887 5.883 5.891 5.876 5.890 5.878 5.891 5.902 5.889 5.897 5.903	5.8725 5.8751 5.8777 5.8803 5.8829 5.8855 5.8881 5.8906 5.8957 5.8983 5.9010	5.8879 5.8910 5.8942 5.8973 5.9004 5.9035 5.9065 5.9094 5.9122 5.9149 5.9175 5.9200	0154 0159 0165 0170 0175 0180 0184 0188 0190 0192 0192 0192	+.009 016 +.006 +.004 008 +.010 009 039 010 +.020 +.003 +.029	1932 F M A M J A S O N D	5.702 5.661 5.639 5.675 5.611 5.625 5.615 5.619 5.604 5.581	5.6909 5.6760 5.6613 5.6470 5.6332 5.6204 5.6088 5.5987 5.5906 5.5846 5.5808 5.5789			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029

TABLE 29-Concluded

BANK DEBITS FOR 140 OUTSIDE CITIES

Date	1	2	3	4	5	Date	1	2	3	4	5
1933 JF M AM J ASOND	5.544 5.576 5.627 5.660 5.641 5.620	5.5788 5.5801 5.5826 5.5859 5.5859 5.5952 5.6010 5.6075 5.6144 5.6213 5.6279 5.6338			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002	1935 J F M A M J A S O N D	5.679 5.687 5.702 5.715 5.709 5.716 5.739 5.743 5.713 5.713 5.719 5.746 5.754				+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029
1934 JF M AM JASOND	5.621 5.638 5.650 5.667 5.669 5.683 5.661 5.643 5.650 5.648 5.650	5.6387 5.6426 5.6458 5.6486			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029	1936 J	5.744				+.008

^{*}Not available, complete data not having been reported on account of bank holidays.

TABLE 30

Deflated Bank Clearings Outside New York City, Monthly, January 1875-January 1919, Inclusive; Deflated Bank Debits for 140 Outside Cities, Monthly, January 1919-January 1936

- Col. 1. Logarithms of Data Adjusted for Seasonal Fluctuations.
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).
- Col. 5. Changing Seasonal Fluctuations (logarithms).

For details of the nature of the graduations given in Columns 2 and 3 and of the seasonal given in Column 5 of this table, see Appendix D.

 $^1\,\mathrm{Deflated}$ by dividing the Clearings Figures of Table 27 by Carl Snyder's "Index of General Price Level."

TABLE 30

DEFLATED BANK CLEARINGS OUTSIDE NEW YORK CITY

Date	1	2	3	4	5	Date	1	2	3	4	5
F M A M J A SOND	4.489 4.505 4.547 4.521 4.505 4.511 4.543 4.543 4.543 4.556 4.512	4.5110 4.5115 4.5127 4.5145 4.5167 4.5167 4.5215 4.5235 4.5249 4.5255 4.52524 4.5253	4.5284 4.5272 4.5260 4.5251 4.5240 4.5228 4.5216 4.5204 4.5192 4.5181 4.5169 4.5158	0174 0157 0133 0106 0073 0031 +.0057 +.0074 +.0083 +.0085	+.031 007 +.005 010 003 005 026 041 031 +.033 +.046 +.009	1880 JF M AM JJ AS ON D	4.649 4.645 4.658 4.658 4.626 4.621 4.639 4.637 4.634 4.620 4.673 4.699	4.6363 4.6393 4.6407 4.6412 4.6411 4.6417 4.6435 4.6471 4.6528 4.6608 4.6706	4.6146 4.6199 4.6252 4.6304 4.6353 4.6407 4.6459 4.6558 4.6557 4.6605 4.6653 4.6701	+.0217 +.0194 +.0155 +.0108 +.0059 +.0004 0073 0073 0086 0075 +.0005	+.03 00 01 00 00 02 02 +.03 +.03
1876 J F M A M J A S O N D	4.522 4.519 4.555 4.492 4.513 4.545 4.505 4.550 4.5512 4.494 4.524 4.524	4,5232 4,5220 4,5211 4,5207 4,5205 4,5203 4,5203 4,5198 4,5191 4,5180 4,5170 4,5161	4.5146 4.5135 4.5126 4.5118 4.5109 4.5103 4.5097 4.5088 4.5088 4.5084 4.5083	+.0086 +.0085 +.0085 +.0089 +.0096 +.0101 +.0103 +.0103 +.0094 +.0086 +.0078	+.032 007 +.002 009 003 006 027 041 031 +.034 +.044	ISSI F M A M J A S O N D	4.682 4.703 4.688 4.697 4.724 4.769 4.765 4.753 4.733 4.719 4.728	4.6819 4.6938 4.7054 4.7156 4.7239 4.7297 4.7329 4.7339 4.7330 4.7308 4.7278 4.7245	4.6748 4.6791 4.6835 4.6876 4.6916 4.6952 4.6987 4.7020 4.7051 4.7078 4.7127	+.0071 +.0147 +.0219 +.0280 +.0323 +.0345 +.0342 +.0319 +.0279 +.0230 +.0175 +.0118	+.03 01 00 00 00 00 +.03 +.03
F M AM J ASOND	4.502 4.521 4.528 4.504 4.553 4.482 4.503 4.521 4.526 4.509 4.533 4.515	4.5155 4.5156 4.5159 4.5167 4.5177 4.5183 4.5185 4.5184 4.5177 4.5166 4.5155 4.5142	4.5083 4.5086 4.5090 4.5095 4.5101 4.5108 4.5118 4.5142 4.5142 4.5158 4.5174 4.5190	+.0072 +.0070 +.0069 +.0072 +.0075 +.0064 +.0054 +.0008 0019 0048	+.033 007 002 009 004 028 041 030 +.035 +.042 +.018	1882 J F M A M J A S O N D	4.704 4.707 4.706 4.710 4.706 4.714 4.727 4.728 4.744 4.711 4.731 4.731	4.7212 4.7184 4.7161 4.7145 4.7137 4.7138 4.7148 4.7165 4.7190 4.7216 4.7244 4.7267	4.7149 4.7167 4.7183 4.7197 4.7209 4.7218 4.7225 4.7230 4.7235 4.7238 4.7240 4.7239	+.0063 +.0017 0022 0052 0072 0080 0077 0065 0025 +.0004 +.0028	+.03 01 00 00 00 00 +.03 +.03
878 JFM AM JASOND	4.561 4.498 4.470 4.489 4.520 4.480 4.550 4.491 4.533 4.553 4.487 4.493	4.5130 4.5119 4.5109 4.5091 4.5091 4.5086 4.5086 4.5089 4.5102 4.5123 4.5123 4.5123 4.5193	4.5210 4.5231 4.5253 4.5280 4.5306 4.5335 4.5366 4.5398 4.5431 4.5465 4.5501 4.5540	0080 0112 0144 0181 0215 0249 0280 0349 0349 0349 0347	+.033 007 005 008 004 027 042 028 +.035 +.041 +.021	1883 J F M A M J A S O N D	4.728 4.730 4.731 4.710 4.735 4.749 4.735 4.748 4.733 4.733 4.735 4.722 4.730	4.7287 4.7302 4.7312 4.7319 4.7328 4.7337 4.7348 4.7360 4.7371 4.7375 4.7364	4.7238 4.7236 4.7235 4.7232 4.7228 4.7224 4.7217 4.7216 4.7214 4.7212 4.7211	+.0049 +.0066 +.0077 +.0087 +.0100 +.0113 +.0128 +.0143 +.0155 +.0162 +.0163	+.03 00 00 00 00 00 00 +.00 +.00
ISTO F M A M J A S O N D	4.538 4.539 4.509 4.584 4.545 4.555 4.609 4.543 4.578 4.667 4.628 4.630	4.5244 4.5306 4.5383 4.5474 4.5577 4.5693 4.5815 4.5938 4.6054 4.6159 4.6246 4.6314	4.5581 4.5622 4.5664 4.5709 4.5754 4.5800 4.5847 4.5895 4.5995 4.5997 4.6048 4.6097	0337 0316 0281 0235 0177 0107 0032 +.0043 +.0109 +.0162 +.0198 +.0217	+.033 008 009 007 004 026 042 +.039 +.039	1884 J F M A M J J A S O N D	4.734 4.729 4.724 4.749 4.751 4.691 4.694 4.688 4.665 4.708	4.7353 4.7321 4.7282 4.7233 4.7180 4.7114 4.7060 4.7008 4.6962 4.6924 4.6897 4.6883	4.7212 4.7214 4.7216 4.7218 4.7222 4.7226 4.7232 4.7240 4.7259 4.7259 4.7270 4.7283	+.0141 +.0107 +.0066 +.0015 0042 0112 0172 0232 0288 0373 0400	+.00 00 00 +.00 +.00 01 01 01 +.03 +.03

TABLE 30-Continued

DEFLATED BANK CLEARINGS OUTSIDE NEW YORK CITY

Date	1	2	3	4	5	Date	1	2	3	4	5
1885 JF M A M J A S O N D	4.710 4.682 4.686 4.709 4.687 4.720 4.739 4.706 4.725 4.743 4.758 4.769	4.6886 4.6906 4.6944 4.6995 4.7056 4.7124 4.7196 4.7266 4.7335 4.7401 4.7461 4.7518	4.7297 4.7312 4.7330 4.7348 4.7368 4.7389 4.7411 4.7434 4.7458 4.7483 4.7508 4.7534	0411 0406 0386 0353 0312 0265 0215 0168 0123 0082 0047 0016	+.020 016 018 002 002 +.002 014 045 020 +.038 +.031 +.026	1890 J F M A M J A S O N D	4.917 4.910 4.914 4.930 4.957 4.935 4.950 4.946 4.953 4.951 4.940 4.915	4.9102 4.9178 4.9250 4.9313 4.9364 4.9399 4.9417 4.9405 4.9380 4.9348 4.9348	4.9074 4.9101 4.9127 4.9153 4.9179 4.9203 4.9226 4.9250 4.9272 4.9292 4.9331 4.9332	+.0028 +.0077 +.0123 +.0160 +.0185 +.0196 +.0191 +.0169 +.0133 +.0088 +.0034 0018	+.01 01 +.00 +.00 +.00 00 00 +.00 +.00 +.00
1886 J F M A M J A S O N D	4.748 4.767 4.784 4.754 4.745 4.781 4.797 4.786 4.796 4.784 4.810 4.822	4.7569 4.7614 4.7653 4.7689 4.7724 4.7761 4.7804 4.7856 4.7917 4.7988 4.8066 4.8146	4.7563 4.7592 4.7622 4.7652 4.7683 4.7713 4.7746 4.7779 4.7811 4.7843 4.7877 4.7913	+.0006 +.0022 +.0031 +.0037 +.0041 +.0048 +.0077 +.0106 +.0145 +.0189 +.0233	+.018 017 018 002 001 +.003 045 020 +.038 +.031 +.026	J F M A M J A S O N D	4.922 4.919 4.907 4.931 4.917 4.937 4.938 4.978 4.947 4.937 4.937	4.9282 4.9257 4.9242 4.9240 4.9249 4.9271 4.9310 4.9388 4.9389 4.9429 4.9489	4.9348 4.9364 4.9379 4.9394 4.9405 4.9417 4.9428 4.9436 4.9444 4.9450 4.9456 4.9456	0066 0107 0137 0154 0156 0146 0118 0088 0055 0021 +.0010 +.0029	+.00 00 +.00 +.00 00 00 +.00 00 +.00 00 +.00
1887 F M A M J A S O N D	4.799 4.815 4.855 4.848 4.841 4.875 4.843 4.846 4.822 4.850 4.826	4.8224 4.8295 4.8355 4.8399 4.8429 4.8444 4.8443 4.8430 4.8409 4.8380 4.8351 4.8325	4.7948 4.7983 4.8019 4.8056 4.8093 4.8130 4.8202 4.8239 4.8274 4.8345	+.0276 +.0312 +.0336 +.0336 +.0314 +.0277 +.0228 +.0170 +.0106 +.0041 0020	+.017 017 018 001 000 +.004 012 045 020 +.030 +.030	1892 JF M A M J J A S O N D	4.940 4.975 4.961 4.952 4.942 4.976 4.963 4.984 4.984 4.985 4.993	4.9514 4.9536 4.9560 4.9589 4.9628 4.9676 4.9733 4.9795 4.9851 4.9894 4.9915	4.9464 4.9466 4.9469 4.9469 4.9468 4.9466 4.9465 4.9462 4.9462 4.9457 4.9457	+.0050 +.0070 +.0071 +.0121 +.0159 +.0208 +.0267 +.0330 +.0389 +.0434 +.0465	+.00 +.00 +.00 +.00 00 +.00 00 +.00
I S S S S S S S S S S S S S S S S S S S	4.819 4.831 4.818 4.827 4.844 4.836 4.838 4.854 4.878 4.851 4.856	4.8305 4.8295 4.8296 4.8310 4.8336 4.8371 4.8413 4.8461 4.8508 4.8554 4.8595 4.8630	4.8381 4.8416 4.8448 4.8481 4.8512 4.8544 4.8574 4.8603 4.8631 4.8659 4.8688 4.8715	0076 0121 0152 0171 0176 0173 0161 0142 0123 0105 0093 0085	+.016 017 018 .000 +.001 +.004 012 046 021 +.037 +.030 +.024		4.991 4.996 4.991 4.981 4.987 4.941 4.910 4.842 4.865 4.873 4.898 4.899	4.9878 4.9811 4.9719 4.9599 4.9475 4.9344 4.9217 4.9098 4.8995 4.8913 4.8860 4.8835	4.9443 4.9440 4.9432 4.9425 4.9414 4.9407 4.9397 4.9388 4.9379 4.9373 4.9365 4.9356	+.0435 +.0371 +.0287 +.0174 +.0061 0063 0180 0290 0384 0460 0505 0521	+++++
J F M A M J A S O N D	4.871 4.875 4.870 4.859 4.875 4.870 4.883 4.870 4.897 4.892 4.886	4.8660 4.8682 4.8700 4.8716 4.8731 4.8748 4.8771 4.8802 4.8843 4.8895 4.8957 4.9027	4.8743 4.8770 4.8798 4.8827 4.8853 4.8882 4.8909 4.8937 4.8963 4.8963 4.99018 4.9046	0083 0088 0098 0111 0122 0134 0135 0120 0095 0061 0019	+.017 017 018 +.001 +.003 012 046 022 +.037 +.030 +.024	A M J J A S O N	4.909 4.884 4.901 4.896 4.911 4.903 4.899 4.934 4.921 4.930 4.929	4.8840 4.8869 4.8916 4.8974 4.9035 4.9091 4.9138 4.9175 4.9206 4.9233 4.9262 4.9296	4.9346 4.9338 4.9331 4.9316 4.9309 4.9305 4.9300 4.9295 4.9292 4.9287 4.9284	-,0506 -,0469 -,0415 -,0348 -,0281 -,0218 -,0167 -,0125 -,0089 -,0059 -,0059 +,0012	+

TABLE 30-Continued

Deplated Bank Clearings Outside New York City

-											
Date	1	2	3	4	5	Date	1	2	3	4	.5
1895 JF M A M J A S O N D	4.941 4.907 4.928 4.945 4.945 4.958 4.949 4.962 4.962 4.952 4.963 4.970 4.968	4.9335 4.9379 4.9426 4.9474 4.9518 4.9558 4.9592 4.9616 4.9631 4.9634 4.9626 4.9607	4.9282 4.9283 4.9283 4.9282 4.9282 4.9284 4.9284 4.9290 4.9296 4.9302 4.9312 4.9324	+.0053 +.0096 +.0143 +.0192 +.0236 +.0274 +.0308 +.0326 +.0335 +.0332 +.0314 +.0283	+.022 014 +.004 +.003 +.002 016 047 028 +.030 +.030 +.028	1900 J F M A M J A S O N D	5.061 5.063 5.064 5.059 5.067 5.073 5.060 5.067 5.053 5.070 5.082 5.080	5.0703 5.0668 5.0636 5.0613 5.0600 5.0616 5.0648 5.0696 5.0757 5.0829 5.0905	5.0743 5.0777 5.0808 5.0838 5.0864 5.0892 5.0919 5.0945 5.0969 5.0969 5.1016 5.1038	0040 0109 0172 0225 0264 0292 0303 0297 0273 0237 0187 0133	+.026 011 006 +.008 002 .000 015 047 028 +.026 +.025 +.024
1896 JF MA M JJASOND	4.948 4.940 4.931 4.946 4.932 4.945 4.955 4.910 4.921 4.926 4.927 4.942	4.9577 4.9538 4.9494 4.9396 4.9390 4.9307 4.9272 4.9245 4.9229 4.9225 4.9234	4.9336 4.9350 4.9366 4.9384 4.9401 4.9423 4.9444 4.9465 4.9489 4.9513 4.9538 4.9565	+.0241 +.0188 +.0128 +.0061 0005 0073 0137 0193 0244 0284 0313 0331	+.022 014 013 +.005 +.002 +.001 046 047 028 +.029 +.029 +.028	A S	5.102 5.100 5.106 5.142 5.150 5.128 5.133 5.135 5.130 5.130 5.129 5.117	5.0983 5.1057 5.1125 5.1183 5.1233 5.1271 5.1298 5.1317 5.1328 5.1335 5.1338 5.1342	5.1051 5.1077 5.1095 5.1114 5.1130 5.1149 5.1165 5.1180 5.1180 5.1221 5.1234	0074 0020 +.0030 +.0069 +.0103 +.0133 +.0137 +.0136 +.0127 +.0117 +.0108	+.026 011 005 +.008 003 .000 014 047 028 +.026 +.024 +.023
1897 F MAM J ASOND	4.915 4.929 4.934 4.934 4.949 4.968 4.983 4.983 4.998 4.998	4.9257 4.9296 4.9350 4.9416 4.9493 4.9578 4.9665 4.9750 4.9827 4.9827 4.9941 4.9972	4.9594 4.9620 4.9651 4.9680 4.9708 4.9736 4.9764 4.9853 4.9853 4.9853	0337 0324 0301 0264 0215 0158 0099 0044 +.0002 +.0039 +.0058	+.023 013 011 +.000 +.001 016 028 +.023 +.028 +.028	F M A M J A S O N	5.143 5.131 5.129 5.157 5.152 5.119 5.160 5.134 5.159 5.148 5.129 5.136	5.1426 5.1431 5.1437 5.1443	5.1246 5.1258 5.1270 5.1285 5.1298 5.1312 5.1324 5.1337 5.1349 5.1364 5.1378 5.1378	+.0102 +.0099 +.0096 +.0096 +.0095 +.0093 +.0089 +.0082 +.0073 +.0065 +.0058	+.027 010 003 +.008 005 001 014 027 +.026 +.023 +.022
·1898 JF MA M J JA SOND	4.992 5.015 5.008 4.988 4.991 5.013 4.976 5.017 5.013 5.003 5.029 5.050	4,9991 4,9998 5,0013 5,0047 5,0099 5,0162 5,0245 5,0338	4.9944 4.9973 5.0003 5.0034 5.0065 5.0094 5.0127 5.0160 5.0194 5.0228 5.0262 5.0297	+,0045 +,0021 -,0011 -,0043 -,0067 -,0081 -,0032 +,0017 +,0076 +,0139	+.026 012 016 +.000 +.001 016 041 021 +.02 +.02	F M A J J A S	5.150 5.143 5.136 5.152 5.140 5.167 5.170 5.144 5.156 5.155 5.129 5.145	5.1470 5.1482 5.1493 5.1500 5.1504 5.1504 5.1492 5.1477 5.1456 5.1433	5.1404 5.1418 5.1433 5.1448 5.1465 5.1481 5.1498 5.1517 5.1536 5.1555 5.1574 5.1594	+.0055 +.0052 +.0049 +.0045 +.0023 +.0024 0025 0059 0099 0141 0185	+.027 010 002 +.008 006 002 013 046 027 +.026 +.022 +.021
I I I I I I I I I I I I I I I I I I I	5.060 5.079 5.090 5.071 5.080 5.072 5.084 5.090 5.082 5.073	5.0630 5.0711 5.0776 5.0824 0.5.0853 2.5.0864 1.5.0860 1.5.0860 1.5.0841 1.5.0812 1.5.0812 1.5.0812	5.0367 5.0402 5.0437 5.0470 5.0505 5.0542 5.0577 5.0610 5.0644 5.0677	+.0204 +.0263 +.0309 +.0339 +.0354 +.0348 +.0322 +.0283 +.0231 +.0168 +.0102 +.0031	+.02 01 00 +.00 00 01 04 02 +.02 +.02	F M A M J A SO N	5.133 5.141 5.139 5.123 5.145 5.139 5.160 5.161 5.190	5.1376 5.1374 5.1384 5.1405 5.1440 5.1485 5.1536 5.1536 5.1592 5.1649	5.1696 5.1715 5.1737 5.1757 5.1776	0225 0258 0280 0290 0291 0275 0252 0221 0184 0146 0110 0077	+.027 010 001 +.008 008 002 013 045 026 +.026 +.022 +.020

TABLE 30-Continued

Deflated Bank Clearings Outside New York City

Date	1	2	3	4	5	Date	1	2	3	4	5
1905 J F M A M J J A S O N D	5.162 5.177 5.195 5.189 5.204 5.202 5.187 5.207 5.210 5.201 5.220 5.224	5.1806 5.1852 5.1894 5.1934 5.1973 5.2011 5.2046 5.2081 5.2112 5.2141 5.2166 5.2187	5.1854 5.1871 5.1890 5.1908 5.1908 5.1926 5.1943 5.1960 5.1976 5.1975 5.2011 5.2027 5.2043	0048 0019 +.0004 +.0026 +.0047 +.0068 +.0105 +.0117 +.0130 +.0130 +.0139	+.027 010 +.001 +.008 009 003 012 044 026 +.026 +.022 +.019	1910 J M A M J A S O N D	5.277 5.280 5.298 5.288 5.269 5.283 5.277 5.274 5.275 5.270 5.282 5.284	5.2842 5.2845 5.2845 5.2835 5.2825 5.2824 5.2792 5.2781 5.2770 5.2770 5.2773	5.2618 5.2636 5.2654 5.2675 5.2693 5.2714 5.2733 5.2752 5.2771 5.2791 5.2810 5.2830	+.0224 +.0209 +.0188 +.0160 +.0132 +.0090 +.0059 +.0029 +.0003 0021 0040 0057	+.025 000 +.000 014 005 013 044 025 +.025 +.025 +.015
1906 J. R. M. A. M. J. A. S. O. N. D.	5.242 5.234 5.226 5.207 5.220 5.227 5.217 5.235 5.220 5.247 5.249 5.233	5.2206 5.2220 5.2231 5.2242 5.2251 5.2260 5.2274 5.2295 5.2323 5.2361 5.2407 5.2457	5.2058 5.2074 5.2090 5.2104 5.2117 5.2132 5.2146 5.2159 5.2170 5.2183 5.2196 5.2207	+.0148 +.0146 +.0141 +.0138 +.0134 +.0128 +.0128 +.0153 +.0153 +.0250	+.027 010 +.002 +.008 010 004 012 043 025 +.027 +.027 +.019	1911 F M A M J A S O N D	5.280 5.274 5.285 5.270 5.288 5.293 5.281 5.291 5.295 5.274 5.292 5.287	5.2780 5.2789 5.2801 5.2812 5.2827 5.2839 5.2851 5.2864 5.2877 5.2888 5.2903 5.2921	5.2850 5.2867 5.2885 5.2920 5.2936 5.2950 5.2963 5.2975 5.2983 5.2994 5.3004	0070 0078 0084 0089 0093 0097 0099 0098 0098 0095 0091	+.024 006 +.006 014 005 012 044 024 +.022 +.021
1907 JF MAM JASOND	5.252 5.251 5.249 5.250 5.261 5.243 5.261 5.257 5.240 5.271 5.168 5.145	5.2504 5.2542 5.2566 5.2575 5.2543 5.2498 5.2433 5.2433 5.2352 5.2256 5.2174 5.2085 5.2016	5.2219 5.2230 5.2243 5.2254 5.2263 5.2274 5.2284 5.2292 5.2301 5.2309 5.2318 5.2326	+.0285 +.0312 +.0323 +.0321 +.0280 +.0224 +.0149 +.0060 0045 0135 0233 0310	+.027 010 +.003 +.008 011 004 012 043 024 +.027 +.021 +.019	1912 F M A M J A S O N D	5.294 5.305 5.295 5.311 5.311 5.289 5.308 5.308 5.305 5.329 5.329 5.320 5.313	5.2940 5.2964 5.2991 5.3018 5.3049 5.3079 5.3108 5.3132 5.3155 5.3171 5.3182 5.3189	5.3011 5.3015 5.3021 5.3025 5.3028 5.3031 5.3034 5.3034 5.3034 5.3034 5.3034 5.3035	0071 0051 0030 0007 +.0021 +.0048 +.0075 +.0098 +.0121 +.0137 +.0148 +.0154	+.02: 00 +.00 +.00 01: 02: 04: 02: +.02: +.02:
1908 JFM AM JASOND	5.192 5.179 5.186 5.192 5.189 5.198 5.218 5.201 5.229 5.227 5.227 5.227	5.1951 5.1904 5.1879 5.1877 5.1888 5.1930 5.1979 5.2056 5.2131 5.2206 5.2276 5.2349	5.2334 5.2343 5.2351 5.2358 5.2367 5.2376 5.2384 5.2391 5.2401 5.2411 5.2411 5.2420 5.2431	0383 0439 0472 0481 0479 0405 0335 0270 0205 0144 0082	+.026 010 +.004 +.007 013 005 011 043 024 +.027 +.021 +.019	1913 J F M A M J A S O N D	5.331 5.334 5.306 5.317 5.318 5.312 5.319 5.308 5.324 5.328 5.326 5.321	5.3191 5.3187 5.3185 5.3184 5.3188 5.3195 5.3202 5.3213 5.3217 5.3219 5.3215	5.3035 5.3035 5.3037 5.3040 5.3042 5.3045 5.3048 5.3052 5.3057 5.3067 5.3067 5.3067	+.0156 +.0152 +.0148 +.0144 +.0142 +.0143 +.0150 +.0156 +.0156 +.0152 +.0141	+.02: 01i +.00: +.00: 01: 00: 01: 02: +.02: +.02:
1909 J F M A M J A S O N D	5.234 5.240 5.252 5.258 5.246 5.264 5.265 5.269 5.279 5.274 5.282 5.282	5.2398 5.2448 5.2495 5.2539 5.2584 5.2629 5.2073 5.2714 5.2751 5.2782 5.2806 5.2822	5.2442 5.2453 5.2467 5.2480 5.2492 5.2507 5.2523 5.2538 5.2552 5.2558 5.2585 5.2585 5.2599	0044 0005 +.0028 +.0059 +.0092 +.0122 +.0150 +.0176 +.0199 +.0214 +.0221 +.0223	+.026 009 +.005 +.008 013 005 012 044 023 +.028 +.022 +.019	1914 J F M A M J J A S O N D	5.327 5.319 5.316 5.324 5.301 5.317 5.325 5.280 5.277 5.271 5.264 5.279	5.3202 5.3180 5.3151 5.3113 5.3074 5.3029 5.2984 5.2942 5.2906 5.2875 5.2857 5.2851	5.3081 5.3089 5.3098 5.3108 5.3116 5.3128 5.3140 5.3151 5.3162 5.3176 5.3191 5.3205	+.0121 +.0091 +.0053 +.0005 0042 0099 0156 0209 0256 0301 0334 0354	+.02: 01: +.00: 01: 00: 01: 04: 02: +.03: +.02:

TABLE 30-Continued

DEFLATED BANK CLEARINGS OUTSIDE NEW YORK CITY

-										-	
Date	1	2	3	4	5	Date	t	2	3	4	5
1915 J F M A M J A S O N D	5.286 5.305 5.308 5.311 5.300 5.310 5.300 5.318 5.324 5.353 5.360	5. 2857 5. 2878 5. 2915 5. 2962 5. 3019 5. 3081 5. 3146 5. 3209 5. 3271 5. 3327 5. 3327 5. 3327 5. 3327 5. 3327 5. 3327	5.3221 5.3237 5.3254 5.3272 5.3293 5.3312 5.3336 5.3359 5.3359 5.3359 5.3403 5.3428 5.3428 5.3453	0364 0359 0339 0310 0274 0231 0190 0150 0108 0076 0046	+.019 013 +.003 +.003 014 001 011 041 019 +.023 +.023	F M A M J A S O N	5,403 5,411 5,403 5,411 5,397 5,391 5,411 5,393 5,425 5,447	5.4011 5.4030 5.4045 5.4055 5.4060 5.4063 5.4067 5.4075 5.4089 5.4113 5.4146	5.3861 5.3896 5.3933 5.3969 5.4002 5.4039 5.4072 5.4105 5.4138 5.4172 5.4203 5.4203	+.0150 +.0134 +.0112 +.0086 +.0058 +.0024 0005 0030 0049 0057 0057	+.017 017 +.001 +.002 014 +.002 016 016 016 +.030 +.021 +.024
1916 MAM JASOND		5.3491 5.3547 5.3606 5.3620 5.3773 5.3820 5.3849 5.3849 5.3932 5.3960 5.3987	5.3479 5.3506 5.3534 5.3564 5.3595 5.3630 5.3659 5.3659 5.3722 5.3725 5.3791 5.3825	+.0012 +.0041 +.0072 +.0100 +.0125 +.0143 +.0161 +.0169 +.0174 +.0169 +.0162	+.018 015 +.002 +.004 014 .000 011 039 018 +.030 +.022 +.023	1918 JF M A M J A S O N D 1919 J	5.408 5.430 5.442 5.447 5.431 5.466 5.438 5.451 5.434 5.420	5.4232 5.4279 5.4321 5.4351 5.4356 5.4396 5.4402 5.4402 5.4403 5.4404 5.4407 5.4404 5.4397 5.4401	5.4261 5.4289 5.4315 5.4340 5.4364 5.4387 5.4410 5.4428 5.4444 5.4461 5.4477 5.4490	0029 0010 +.0016 +.0016 +.0017 0009 0027 0047 0067 0082 0089	+.015 019 .000 +.001 013 +.003 010 +.029 +.018 +.025

DEFLATED BANK DEBITS FOR 140 OUTSIDE CITIES

Date	1	2	3	4	5	Date	1	2	3	4	5
1919 FMAM JASOND	5.508 5.503 5.489 5.495 5.522 5.534 5.548 5.548 5.537 5.533 5.553	5.5035 5.5058 5.5058 5.5132 5.5132 5.5233 5.5288 5.5340 5.5386 5.5423 5.5448 5.5462	5.5121 5.5132 5.5143 5.5153 5.5161 5.5169 5.5177 5.5184 5.5190 5.5198 5.5204 5.5210	0086 0074 0052 0021 +.0019 +.0064 +.0111 +.0156 +.0125 +.0225	+.015 020 .000 .000 013 +.005 010 034 013 +.028 +.015 +.027	J F M A M J J A S O N D	5.502 5.497 5.501 5.493 5.505 5.496 5.512 5.523 5.505	5.5123 5.5090 5.5063 5.5042 5.5029 5.5025 5.5032 5.5032 5.5048 5.5074 5.5105 5.5140	5.5269 5.5273 5.5279 5.5283 5.5288 5.5294 5.5300 5.5305 5.5311 5.5318 5.5325 5.5333	0146 0183 0216 0241 0259 0269 0268 0257 0237 0213 0185	+.01 02 +.00 01 +.00 01 03 01 +.02 +.01 +.01
1920 JFM AM JASOND	5.528 5.541 5.518 5.530	5.5464 5.5457 5.5443 5.5423 5.5399 5.5371 5.5340 5.5305 5.5270 5.5270 5.5231 5.5194 5.5157	5.5212 5.5218 5.5223 5.5223 5.5232 5.5232 5.5238 5.5242 5.5246 5.5251 5.5254 5.5254 5.5254 5.5254 5.5254 5.5254	+.0252 +.0239 +.0220 +.0195 +.0167 +.0133 +.0059 +.0059 +.0019 0023 0065 0106	+.014 020 .000 .000 013 +.007 010 033 012 +.027 +.012 +.028	1922 F M AM J J A S O N D	5,531 5,535 5,524 5,536 5,550 5,532 5,540 5,549 5,543 5,539	5.5206 5.5236 5.5263 5.5289 5.5318 5.5353 5.5394 5.5442 5.5547 5.5547 5.5547 5.5547 5.5548	5.5343 5.5350 5.5361 5.5371 5.5382 5.5393 5.5406 5.5418 5.5433 5.5447 5.5463 5.5477	0137 0114 0098 0082 0040 0012 +.0024 +.0061 +.0100 +.0135 +.0167	+.01 +.00 +.00 +.00 01 +.00 01 +.02 +.00 01 +.00 +.00 +.00 +.00

TABLE 30-Continued

DEFLATED BANK DEBITS FOR 140 OUTSIDE CITIES

Date	1	2	3	4	5	Date	1	2	3	4	5
J F M A M J A S O N D	5.579 5.585 5.581 5.579 5.587 5.584 5.561 5.565 5.552 5.564 5.564	5.5683 5.5713 5.5743 5.5743 5.5744 5.5744 5.5720 5.5704 5.5684 5.5668 5.5654	5.5493 5.5528 5.5528 5.5563 5.5603 5.5603 5.5603 5.56623 5.56641 5.5662 5.5683 5.5703	+.0190 +.0203 +.0205 +.0197 +.0184 +.0160 +.0131 +.0097 +.0063 +.0022 0015 0049	+.011 019 +.003 +.002 011 +.010 010 010 +.023 +.006 +.030	1928 J F M A M J J A S O N D	5.660 5.652 5.674 5.677 5.688 5.700 5.650 5.672 5.671 5.683 5.701	5.6640 5.6657 5.6658 5.6700 5.6723 5.6747 5.6767 5.6786 5.6805 5.6825 5.6825 5.6881	5.6756 5.6772 5.6787 5.6802 5.6817 5.6830 5.6841 5.6849 5.6856 5.6858 5.6859 5.6859	0116 0115 0102 0102 0094 0083 0074 0063 0051 0038 +.0018	+.009 015 +.006 +.005 007 +.009 040 010 +.020 +.023 +.029
1924 JF M AM JJASOND	5.562 5.576 5.578 5.572 5.572 5.572 5.575 5.576 5.576 5.576 5.574 5.590	5.5645 5.5644 5.5653 5.5669 5.5716 5.5748 5.5783 5.5820 5.5829 5.5839 5.5939	5.5726 5.5746 5.5769 5.5792 5.5815 5.5837 5.5858 5.5880 5.5903 5.5923 5.5924 5.5965	0081 0102 0116 0125 0126 0121 0110 0097 0083 0064 0026	+.011 018 +.004 +.003 010 010 037 010 +.022 +.005 +.030	J F M A M J A S O N D	5.696 5.703 5.697 5.693 5.686 5.683 5.715 5.742 5.708 5.741 5.734 5.669	5.6917 5.6958 5.6999 5.7035 5.7065 5.7085 5.7086 5.7086 5.7069 5.7041 5.7002 5.6955	5.6867 5.6865 5.6860 5.6853 5.6842	+.0050 +.0093 +.0139 +.0182 +.0223	+.009 014 +.006 +.005 007 +.009 040 010 +.019 +.003
1925 JFM AM JASOND	5.619 5.611 5.605 5.609 5.603 5.621 5.612 5.633 5.610 5.622	5.5979 5.6019 5.6057 5.6083 5.6116 5.6146 5.6172 5.6195 5.6226 5.6244 5.6259 5.6271	5.5985 5.6005 5.6025 5.6045 5.6064 5.6084 5.6103 5.6122 5.6141 5.6162 5.6162 5.6181 5.6202	0006 +.0014 +.0032 +.0052 +.0069 +.0073 +.0085 +.0085 +.0084 +.0078 +.0069	+.010 017 +.004 +.003 010 +.010 009 038 010 +.021 +.024 +.030	1930 F M A M I J A S O N D	5.670 5.663 5.662 5.664 5.667 5.678 5.650 5.638 5.652 5.609 5.645	5.6900 5.6839 5.6773 5.6703 5.6634 5.6568 5.6508 5.6453 5.6408 5.6371 5.6337 5.6306			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029
1926 JFM AM JJASOND	5.634 5.637 5.642 5.639 5.616 5.611 5.653 5.632 5.632 5.632 5.638	5.6280 5.6286 5.6289 5.6290 5.6291 5.6298 5.6307 5.6321 5.6339 5.6362 5.6362 5.6387	5.6221 5.6243 5.6265 5.6285 6.5306 5.6329 5.6352 5.6374 5.6398 5.6423 5.6424 5.6469	+.0059 +.0043 +.0024 +.0005 0015 0054 0067 0067 0084 0083 0082	+.010 016 +.005 +.004 009 +.010 039 010 +.021 +.021 +.029	1931 F M A M J A S O N D	5.641 5.604 5.594 5.620 5.605 5.626 5.610 5.594 5.587 5.587 5.527	5.6275 5.6238 5.6196 5.6149 5.6097 5.6097 5.5081 5.5914 5.5841 5.5762 5.5675 5.5675			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029
1927 F M A M J A S O N D	5.639 5.656 5.653 5.663 5.646 5.657 5.648 5.658 5.658 5.650 5.658 5.658	5.6414 5.6442 5.6468 5.6492 5.6515 5.6536 5.6555 5.6571 5.6586 5.6599 5.6611 5.6625	5.6494 5.6517 5.6542 5.6566 5.6589 5.6613 5.6637 5.6658 5.6678 5.6678 5.6678 5.6678	0080 0075 0074 0074 0074 0082 0087 0092 0099 0107 0112	+.009 016 +.006 +.008 +.010 009 039 010 +.020 +.003 +.029	1932 F M A M J A S O N D	5.562 5.527 5.502 5.548 5.490 5.514 5.504 5.498 5.483 5.464 5.446 5.481	5.5485 5.5385 5.5283 5.5182 5.5084 5.4994 5.4915 5.4849 5.4799 5.4766 5.4750 5.4747			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029

TABLE 30-Concluded

DEFLATED BANK DEBITS FOR 140 OUTSIDE CITIES

Date	1	2	3	4	5	Date	1	2	3	4	5
1933 F M A M J A S O N D	5.491 5.451 5.472 5.520 5.539 5.520 5.496 5.480	5.4755 5.4771 5.4793 5.4816 5.4844 5.4872 5.4904 5.4937 5.4972 5.5006 5.5039 5.5067			+.008 014 +.007 +.005 006 +.009 009 040 010 +.019 +.002	F M A M I A S O	5.530 5.535 5.553 5.553 5.554 5.558 5.578 5.579 5.546 5.549 5.573 5.573				+.008 014 +.007 +.008 009 009 040 019 +.019 +.002
1934 J. F. M. A. M. J. A. S. O. N. D.	5,504	5.5089 5.5106 5.5120 5.5133			+.008 014 +.007 +.005 006 +.009 040 010 +.019 +.002 +.029		5,568				+.008

^{*}Not available, complete da a not having been reported on account of bank holidays.

TABLE 31

Daily Average Pig Iron Production¹ in the United States, Monthly, January 1877 - January 1936

- Col. 1. Logarithms of Data (see Table 27-Column 4).
- Col. 2. Cyclical Curve (logarithms).
- Col. 3. Trend Curve (logarithms).
- Col. 4. Deviations of Cyclical Curve (logarithms) from Trend Curve (logarithms).

For details of the nature of the graduations given in Columns 2 and 3 of this table, see Appendix \mathbf{D} .

¹ These figures do not include charcoal pig iron.

 $\begin{tabular}{ll} TABLE 31 \\ Pig Iron Production In the United States \\ \end{tabular}$

Date	1	2	3	4	Date	1	2	3	4
1877 JF M A M J J A S O N D	.673 .679 .684 .686 .681 .674 .672 .676 .685 .699 .716 .735	.6661 .6683 .6706 .6733 .6771 .6821 .6886 .6965 .7053 .7147 .7241 .7331	.6627 .6652 .6681 .6715 .6752 .6789 .6831 .6877 .6926 .6977 .7029	+.0034 +.0031 +.0025 +.0018 +.0019 +.0032 +.0055 +.0088 +.0127 +.0170 +.0212 +.0247	1882 JF M A M J J A S O N D	1.041 1.055 1.055 1.051 1.043 1.033 1.024 1.013 1.010 1.020 1.047 1.063 1.073	1.0161 1.0199 1.0239 1.0281 1.0323 1.0363 1.0460 1.0434 1.0467 1.0501 1.0535 1.0569	1.0197 1.0216 1.0233 1.0247 1.0258 1.0266 1.0271 1.0274 1.0274 1.0273 1.0271 1.0267	0036 0017 +.0006 +.0034 +.0065 +.0097 +.0129 +.0160 +.0194 +.0230 +.0268 +.0307
1878 JF M A M J A S O N D	.756 .771 .777 .771 .760 .751 .736 .726 .720 .726 .732 .738	.7410 .7476 .7522 .7548 .7550 .7530 .7490 .7435 .7374 .7317 .7273 .7254	.7140 .7200 .7261 .7324 .7389 .7455 .7524 .7595 .7666 .7740 .7816 .7890	+.0270 +.0276 +.0261 +.0224 +.0161 +.0075 0034 0160 0292 0423 0543 0636	1883 F M A M J A S O N D	1,079 1,080 1,075 1,060 1,048 1,045 1,043 1,041 1,038 1,032 1,026 1,016	1.0600 1.0623 1.0632 1.0632 1.0593 1.0542 1.0476 1.0401 1.0325 1.0256 1.0199	1.0256 1.0248 1.0241 1.0235 1.0229 1.0223 1.0216 1.0211 1.0210 1.0210 1.0213	+.0344 +.0375 +.0391 +.0388 +.0364 +.0319 +.0257 +.0114 +.0046 0011 0057
1879 FM AM LASOND	.741 .744 .747 .751 .759 .777 .806 .835 .864 .894	.7269 .7323 .7421 .7562 .7744 .7059 .8197 .8449 .8700 .8940 .9155 .9338	.7963 .8040 .8119 .8197 .8273 .8352 .8430 .8509 .8587 .8666 .8743	0694 0717 0698 0635 0529 0393 0233 0060 +.0113 +.0274 +.0412 +.0517	1884 JF M AM JA SOND	.997 .985 .992 1.009 1.019 1.025 1.031 1.010 .993 .996 1.004	1.0126 1.0105 1.0092 1.0082 1.0073 1.0063 1.0052 1.0037 1.0016 .9989 .9956	1.0218 1.0224 1.0232 1.0242 1.0254 1.0267 1.0283 1.0299 1.0319 1.0339 1.0362 1.0386	0092 0119 0140 0160 0181 0204 0231 0262 0303 0350 0468
1880 JF M AM J ASOND	.966 .982 .989 .989 .978 .978 .935 .927 .935 .949 .961	.9483 .9588 .9654 .9688 .9696 .9688 .9671 .9654 .9641 .9637	.8896 .8972 .9047 .9120 .9190 .9259 .9328 .9397 .9463 .9528 .9592 .9528	+.0587 +.0616 +.0607 +.0568 +.0520 +.0429 +.0343 +.0257 +.0109 +.0050 +.0050	1885 JF MA M J ASOND	,957 ,991 1,004 ,996 ,987 ,982 ,993 ,996 ,991 1,010 1,049 1,083	.9877 .9840 .9812 .9800 .9813 .9852 .9921 1.0020 1.0144 1.0289 1.0451 1.0624	1.0411 1.0438 1.0466 1.0495 1.0528 1.0560 1.0595 1.0632 1.0670 1.0709 1.0751 1.0793	0534 0594 0695 0715 0708 0674 0612 0526 0420 0306
1881 FM AM JA SOND	.987 .997 1.001 .999 .991 .984 .977 .975 .986 .986 .998	.9682 .9714 .9754 .9798 .9844 .9891 .9937 .9980 1.0020 1.0056 1.0091	.9709 .9767 .9820 .9871 .9918 .9066 1.0069 1.0048 1.0084 1.0117 1.0147	0027 0053 0066 0073 0074 0075 0068 0061 0056 0048	1886 J F M A M J J A S O N D	1.086 1.078 1.108 1.153 1.177 1.185 1.180 1.170 1.173 1.187 1.194 1.200	1.0805 1.0991 1.1179 1.1362 1.1532 1.1683 1.1805 1.1893 1.1946 1.1966 1.1961 1.1942	1.0837 1.0882 1.0929 1.0979 1.1031 1.1081 1.1136 1.1190 1.1249 1.1307 1.1368 1.1427	0032 +.0109 +.0250 +.0383 +.0501 +.0602 +.0669 +.0703 +.0659 +.05593 +.0515

¹ Except charcoal pig iron.

TABLE 31-Continued

PIG IRON PRODUCTIONI IN THE UNITED STATES

Date	1	2	3	4	Date	1	2	3	4
1887 JF MAA MI JAA SO ND	1.211 1.219 1.223 1.231 1.166 1.084 1.113 1.188 1.245 1.264 1.264	1.1921 1.1907 1.1906 1.1917 1.1939 1.1965 1.1988 1.2004 1.2011 1.2009 1.2002	1.1486 1.1546 1.1605 1.1665 1.1727 1.1786 1.1846 1.1905 1.1962 1.2018 1.2072	+.0435 +.0361 +.0301 +.0252 +.0212 +.0179 +.0142 +.0099 +.0049 00070 0134	1892 J F M A M J A S O N D	1.412 1.413 1.407 1.389 1.370 1.360 1.344 1.322 1.326 1.354 1.377 1.379	1.4082 1.4062 1.3992 1.3895 1.3795 1.3718 1.3679 1.3681 1.3714 1.3760 1.3794	1.3276 1.3252 1.3228 1.3204 1.3180 1.3156 1.3132 1.3067 1.3067 1.3063 1.3043	+ .0806 + .0810 + .0764 + .0691 + .05615 + .0547 + .0573 + .0627 + .0695 + .0769
1888 FMAM JASOND	1.211 1.164 1.161 1.183 1.183 1.182 1.204 1.223 1.245 1.273 1.273 1.293	1.1982 1.1978 1.1981 1.1994 1.2020 1.2061 1.2118 1.2191 1.2276 1.2368 1.2459 1.2542	1.2179 1.2230 1.2279 1.2328 1.2373 1.2419 1.2462 1.2504 1.2547 1.2589 1.2630 1.2671	0197 0252 0298 0334 0353 0358 0344 0313 0271 0221 0171	1893 JF M A M J A S O N D	1.372 1.376 1.386 1.393 1.388 1.354 1.254 1.114 1.027 1.021 1.095 1.146	1.3741 1.3630 1.3461 1.3240 1.2976 1.2681 1.2366 1.1736 1.1459 1.1236 1.1092	1.3005 1.2986 1.2968 1.2951 1.2936 1.2921 1.2907 1.2896 1.2885 1.2870 1.2870	+.0736 +.0644 +.0493 +.0289 +.0040 0541 0851 1149 1417 1634 1774
1889 JF MAM JJASOND	1.201 1.283 1.284 1.273 1.254 1.256 1.260 1.273 1.305 1.331 1.346	1.2611 1.2662 1.2697 1.2771 1.2741 1.2764 1.2799 1.2850 1.2924 1.3023 1.3146 1.3291	1.2711 1.2751 1.2792 1.2832 1.2871 1.2912 1.2952 1.2991 1.3030 1.3069 1.3108	0100 0089 0095 01111 0130 0148 0153 0141 0106 +.0038 +.0145	1894 F M A M J A S O N D	1.151 1.179 1.236 1.236 1.095 1.026 1.159 1.281 1.334 1.349 1.371 1.375	1.1042 1.1092 1.1237 1.1459 1.1730 1.2018 1.2298 1.2764 1.2947 1.3105	1,2862 1,2862 1,2865 1,2869 1,2873 1,2881 1,2890 1,2902 1,2918 1,2933 1,2951 1,2972	1820 1770 1628 1410 1143 0863 0592 0353 0154 +.0014 +.0154 +.0274
1890 F M A M J J A S O N D	1.355 1.366 1.376 1.381 1.385 1.379 1.361 1.355 1.371 1.377 1.381	1.3449 1.3606 1.3746 1.3850 1.3903 1.3820 1.3688 1.3515 1.3319 1.3123 1.2949	1.3182 1.3219 1.3252 1.3283 1.3312 1.3340 1.3365 1.3386 1.3402 1.3416	+.0267 +.0387 +.0404 +.0567 +.0553 +.0553 +.0455 +.0302 +.0113 0097 0304 0487	1895 J F M A M J A S O N D	1.363 1.345 1.335 1.331 1.329 1.351 1.386 1.423 1.453 1.479 1.494 1.482	1.3379 1.3509 1.3635 1.3758 1.3879 1.4001 1.4125 1.4251 1.4374 1.4481 1.4557 1.4583	1.2996 1.3019 1.3046 1.3073 1.3101 1.3132 1.3166 1.3200 1.3235 1.3276 1.3316	+.0383 +.0490 +.0589 +.0685 +.0778 +.0869 +.0959 +.1051 +.1139 +.1205 +.1241 +.1226
1891 F M A M J A S O N D	1.300 1.240 1.179 1.144 1.211 1.312 1.362 1.372 1.390 1.414 1.423 1.420	1.2813 1.2729 1.2704 1.2739 1.2832 1.2976 1.3159 1.3367 1.3380 1.3776 1.3936	1.3440 1.3440 1.3432 1.3424 1.3412 1.3400 1.3384 1.3363 1.3345 1.3323 1.3301	0627 0711 0734 0693 0592 0436 0241 0017 +.0216 0431 +.0613 +.0747	1896 J F M A M J J A S O N D	1.460 1.437 1.422 1.420 1.411 1.396 1.361 1.286 1.208 1.209 1.359	1.4547 1.4443 1.4276 1.4061 1.3820 1.3576 1.3353 1.3167 1.3028 1.2944 1.2916	1,3401 1,3499 1,3498 1,3549 1,3600 1,365 1,3712 1,3767 1,3822 1,3832 1,3939 1,3998	+.1146 +.0994 +.0778 +.0512 +.0220 0080 0359 0600 0794 0938 1023 1055

¹ Except charcoal pig iron.

TABLE 31-Continued

Pig Iron Production in the United States

Date	1	2	3	4	Date	1	2	3	4
1897 J F M A M J J A S O N D	1.349 1.366 1.381 1.386 1.382 1.375 1.369 1.394 1.434 1.466 1.489 1.500	1.3024 1.3152 1.3321 1.3518 1.3732 1.3948 1.4152 1.4335 1.4491 1.4618 1.4720 1.4800	1.4051 1.4107 1.4161 1.4216 1.4268 1.4318 1.4367 1.4415 1.4460 1.4505 1.4505 1.4547 1.4589	1027 0955 0840 0698 0536 0370 0215 0080 +.0031 +.0173 +.0173	I 1902 F M A M J A S O N D	1.666 1.652 1.668 1.692 1.697 1.683 1.668 1.675 1.675 1.679 1.695	1.6613 1.6625 1.6636 1.6651 1.6668 1.6690 1.6723 1.6769 1.6832 1.6908 1.6990 1.7069	1.6359 1.6373 1.6389 1.6404 1.6421 1.6437 1.6453 1.6470 1.6485 1.6503 1.6519 1.6538	+.0254 +.0252 +.0247 +.0247 +.0247 +.0253 +.0270 +.0347 +.0405 +.0471 +.0531
1898 LF MAM J ASOND	1.500 1.505 1.505 1.505 1.497 1.485 1.472 1.471 1.482 1.499 1.517	1.4864 1.4913 1.4950 1.4974 1.4985 1.4984 1.4975 1.4964 1.4955 1.4987 1.5029	1.4628 1.4667 1.4704 1.4776 1.4813 1.4851 1.4889 1.4929 1.4971 1.5012	+.0236 +.0246 +.0246 +.0234 +.0209 +.0171 +.0124 +.0075 +.0029 0006 0025 0025	1903 J F M A M J A S O N D	1.677 1.696 1.710 1.729 1.743 1.746 1.698 1.705 1.714 1.663 1.540 1.436	1,7130 1,7163 1,7160 1,7119 1,7042 1,6935 1,6807 1,6664 1,6515 1,6366 1,6226 1,6093	1.6558 1.6579 1.6602 1.6627 1.6653 1.6682 1.6714 1.6747 1.6780 1.6819 1.6858 1.6898	+.0572 +.0584 +.0588 +.0492 +.0389 +.0253 +.0093 0083 0265 0453 0632 0805
1899 F M AM J J ASOND	1.526 1.511 1.518 1.537 1.543 1.5565 1.570 1.581 1.598 1.612 1.617	1.5088 1.5162 1.5251 1.5350 1.5459 1.5576 1.5699 1.5823 1.5940 1.6041 1.6116	1.5098 1.5142 1.5189 1.5238 1.5290 1.5340 1.5343 1.5444 1.5497 1.5549 1.5602	0010 +.0020 +.0062 +.0112 +.0169 +.0236 +.0306 +.0379 +.0443 +.0492 +.0514 +.0503	1904 J F M A M J J A S O N D	1.474 1.620 1.670 1.716 1.695 1.635 1.558 1.578 1.656 1.672 1.695	1.5988 1.5920 1.5898 1.5930 1.6016 1.6150 1.6319 1.6507 1.6697 1.6698 1.7044 1.7195	1.6939 1.6983 1.7029 1.7073 1.7119 1.7163 1.7208 1.7252 1.7252 1.7375 1.7375	0951 1063 1131 1143 1103 1013 0889 0745 0599 0459 0331 0217
1900 J F M A M J J A S O N D	1.618 1.618 1.612 1.613 1.618 1.607 1.563 1.516 1.496 1.480 1.488 1.523	1.6154 1.6111 1.6028 1.5916 1.5788 1.55540 1.5449 1.5375 1.5375 1.5400 1.5466	1.5704 1.5753 1.5800 1.5845 1.5890 1.5931 1.5970 1.6005 1.6041 1.6072 1.6102	+.0450 +.0358 +.0228 +.0071 0102 0273 0430 0556 0649 0697 0702 0663	1905 J F M A M J A S O N D	1.760 1.756 1.796 1.807 1.807 1.777 1.775 1.774 1.802 1.821 1.827 1.827	1.7333 1.7464 1.7591 1.7714 1.7830 1.7933 1.8018 1.8081 1.8123 1.8149 1.8165 1.8177	1.7449 1.7481 1.7512 1.7539 1.7566 1.7586 1.7610 1.7629 1.7647 1.7662 1.7677 1.7662	0116 0017 +.0079 +.0175 +.0264 +.0345 +.0408 +.0476 +.0488 +.0488 +.0485
1901 F M A M J A S O N D	1.573 1.607 1.614 1.621 1.633 1.640 1.644 1.638 1.649 1.657 1.611	1.5566 1.5694 1.5838 1.5989 1.6134 1.6265 1.6375 1.6459 1.6520 1.6561 1.6585 1.6601	1.6152 1.6176 1.6197 1.6216 1.6233 1.6250 1.6282 1.6298 1.6312 1.6328 1.6343	0586 0482 0359 0227 0099 +.0015 +.0109 +.0177 +.0222 +.0249 +.0257 +.0258	1906 JF MA MJJ ASOND	1.824 1.833 1.844 1.840 1.831 1.813 1.793 1.818 1.850 1.863 1.858	1.8190 1.8206 1.8222 1.8236 1.8245 1.8252 1.8250 1.8276 1.8309 1.8364 1.8446 1.8549	1.7703 1.7716 1.7727 1.7738 1.7745 1.7756 1.7765 1.7773 1.7780 1.7780 1.7780	+.0487 +.0490 +.0495 +.0500 +.0495 +.0503 +.0529 +.0576 +.0651 +.0747

¹ Except charcoal pig iron.

PIG IRON PRODUCTION

TABLE 31-Continued

Pig Iron Production in the United States

Date	1	2	3	4	Date	1	2	3	4
1907 J F M A M J J A S O N D	1.852 1.864 1.856 1.869 1.870 1.872 1.862 1.862 1.877 1.785 1.600	1.8661 1.8735 1.8844 1.8873 1.8836 1.8722 1.8531 1.8268 1.7945 1.7584 1.7206 1.6835	1.7809 1.7814 1.7819 1.7822 1.7826 1.7828 1.7827 1.7826 1.7824 1.7824 1.7820 1.7815 1.7809	+.0852 +.0921 +.1025 +.1051 +.1010 +.0894 +.0704 +.0442 +.0121 0236 0609 0974	1912 J F M A M J A S O N D	1.822 1.860 1.890 1.899 1.909 1.910 1.891 1.909 1.915 1.938 1.943 1.953	1.8458 1.8567 1.8679 1.8794 1.8908 1.9019 1.9125 1.9225 1.9316 1.9399 1.9469 1.9525	1.8748 1.8744 1.8740 1.8735 1.8726 1.8714 1.8703 1.8691 1.8680 1.8668 1.8657 1.8649	0290 0177 0061 +.0059 +.0305 +.0422 +.0534 +.0636 +.0731 +.0812 +.0876
1908 J F M A M J A S O N D	1.528 1.570 1.598 1.584 1.575 1.561 1.594 1.675 1.704 1.721 1.749	1.6497 1.6214 1.6001 1.5875 1.5838 1.5890 1.6019 1.6211 1.6444 1.6699 1.6957 1.7205	1.7802 1.7795 1.7786 1.7779 1.7771 1.7764 1.7754 1.7754 1.7749 1.7749 1.7752	1305 1581 1785 1904 1933 1874 1739 1543 1307 1050 0792 0547	1913 F M A M I J A S O N D	1.955 1.966 1.950 1.963 1.959 1.943 1.917 1.914 1.922 1.915 1.872 1.806	1,9562 1,9575 1,9561 1,9518 1,9449 1,9358 1,9252 1,9138 1,9023 1,8911 1,8804 1,8699	1.8640 1.8635 1.8631 1.8628 1.8632 1.8632 1.8637 1.8646 1.8655 1.8667 1.8681 1.8696	+ .0922 + .0940 + .0930 + .0890 + .0820 + .0726 + .0615 + .0492 + .0368 + .0244 + .0123 + .0003
1909 IFMAM IJASOND	1.763 1.785 1.772 1.763 1.784 1.809 1.832 1.861 1.900 1.924 1.929 1.930	1.7435 1.7646 1.7841 1.8024 1.8199 1.8374 1.8546 1.8714 1.8873 1.9015 1.9129	1.7757 1.7764 1.7774 1.7778 1.7801 1.7819 1.7839 1.7862 1.7887 1.7914 1.7977	0322 0118 +.0067 +.0236 +.0398 +.0555 +.0707 +.0852 +.0986 +.1101 +.1185 +.1230	I914 F M AA J ASOND	1.784 1.829 1.879 1.879 1.829 1.806 1.800 1.809 1.798 1.759 1.704 1.689	1.8593 1.8481 1.8362 1.8234 1.8100 1.7965 1.7836 1.7722 1.7631 1.7558 1.7558	1.8713 1.8732 1.8751 1.8772 1.8796 1.8820 1.8845 1.8871 1.8900 1.8929 1.8961 1.8992	0120 0251 0389 0538 0696 0855 1009 1149 1269 1355 1403 1402
1910 JF M A M J J A S O N D	1.925 1.933 1.927 1.918 1.887 1.878 1.841 1.832 1.836 1.836 1.829 1.804	1.9243 1.9230 1.9172 1.9071 1.8937 1.8782 1.8619 1.8459 1.8312 1.8183 1.8077	1.8011 1.8048 1.8086 1.8124 1.8164 1.8207 1.8248 1.8291 1.8337 1.8377 1.8419	+.1232 +.1182 +.1086 +.0947 +.0773 +.0575 +.0371 +.0168 0022 0194 0342 0465	A S O N	1.713 1.777 1.823 1.849 1.863 1.900 1.917 1.953 1.978 2.003 2.005 2.014	1.7676 1.7819 1.8015 1.8259 1.8538 1.8336 1.9136 1.9420 1.9627 1.9889 2.0059 2.0184	1.9129 1.9166 1.9205 1.9244 1.9283 1.9322 1.9364 1.9403	1347 1239 1077 0870 0628 0369 0108 +.0137 +.0352 +.0525 +.0656 +.0741
1911 F M A M J J A S O N D	1.754 1.807 1.845 1.838 1.786 1.775 1.762 1.793 1.823 1.831 1.824 1.819	1.7934 1.7894 1.7874 1.7873 1.7889 1.7921 1.7967 1.8026 1.8095 1.8173 1.8260 1.8356	1.8500 1.8537 1.8574 1.8607 1.8636 1.8662 1.8684 1.8704 1.8721 1.8732 1.8740	0560 0644 0700 0734 0744 0711 0674 0625 055 048 038	M A M J A S O N	2.012 2.027 2.032 2.032 2.035 2.035 2.017 2.014 2.028 2.054 2.043 2.011	2.027 2.025 2.023 2.023 2.024	9 1.9525 1 1.9526 1 1.9607 8 1.9646 5 1.9688 9 1.9729 1.9770 1.9811 4 1.9856 0 1.9898	+.0485 +.0428 +.0378 +.0342

TABLE 31-Continued

PIG IRON PRODUCTION IN THE UNITED STATES

Date	1	2	3	4	Date	1	2	3	4
1917 F M A M J J A S O N D	2.007 1.975 2.021 2.046 2.042 2.037 2.033 2.020 2.019 2.028 2.029 1.968	2.0272 2.0284 2.0286 2.0273 2.0243 2.0198 2.0142 2.0081 2.0021 1.9968 1.9930 1.9912	1.9981 2.0023 2.0064 2.0104 2.0142 2.0176 2.0207 2.0237 2.0262 2.0284 2.0296 2.0302	+.0291 +.0261 +.0222 +.0169 +.0101 +.0022 0065 0156 0241 0316 0366 0390	J F M A M J A S O N D	1.725 1.765 1.818 1.839 1.872 1.890 1.768 1.831 1.930 1.978 1.998	1.6958 1.7357 1.7734 1.8071 1.8365 1.8619 1.8844 1.9049 1.9248 1.9445 1.9643 1.9840	1.8407 1.8427 1.8452 1.8479 1.8511 1.8546 1.8583 1.8623 1.8663 1.8707 1.8753 1.8801	1449 1070 0718 0408 0146 +.0073 +.0261 +.0426 +.0585 +.0738 +.0890 +.1039
1918 F M A M J A S O N D	1.891 1.918 2.016 2.040 2.045 2.045 2.039 2.057 2.057 2.051 2.048 2.044	1.9920 1.9956 2.0020 2.0109 2.0215 2.0327 2.0426 2.0497 2.0523 2.0492 2.0398 2.0247	2.0304 2.0297 2.0284 2.0266 2.0242 2.0171 2.0172 2.0070 2.0015 1.9952 1.9886	0384 0341 0264 0157 0027 +.0117 +.0255 +.0371 +.0453 +.0477 0446 +.0361	I 1923 F M A M J A S O N D	2.018 2.029 2.056 2.073 2.096 2.088 2.074 2.046 2.018 2.007 1.984 1.974	2.0033 2.0212 2.0372 2.0508 2.0614 2.0683 2.0709 2.0686 2.0606 2.0471 2.0284 2.0057	1.8849 1.8898 1.8949 1.9001 1.9055 1.9106 1.9159 1.9212 1.9269 1.9322 1.9376 1.9429	+ .1184 + .1314 + .1423 + .1507 + .1559 + .1577 + .1550 + .1474 + .1337 + .1149 + .0908 + .0628
1919 J.F. M.A.M. J.J.A.S.O.N.D.	2.027 2.021 1.999 1.917 1.833 1.848 1.894 1.047 1.919 1.779 1.902	2.0051 1.9823 1.9587 1.9341 1.9165 1.9010 1.8907 1.8860 1.8871 1.8936 1.9054	1.9813 1.9739 1.9664 1.9590 1.9513 1.9440 1.9366 1.9291 1.9215 1.9146 1.9078	+.0238 +.0084 0077 0249 0348 0430 0451 0344 0210 0024 +.0207	1924 IF M A M J A S O N D	1.988 2.025 2.048 2.033 1.926 1.830 1.760 1.784 1.835 1.903 1.923 1.923	1.9808 1.9559 1.9333 1.9148 1.9016 1.8942 1.8924 1.8955 1.9028 1.9132 1.9258 1.9399	1.9483 1.9536 1.9587 1.9687 1.9687 1.9734 1.9779 1.9822 1.9859 1.9894 1.9915	+.0325 +.0023 0254 0487 0671 0792 0855 0867 0831 0762 0657 0554
1920 J F M A M J J A S O N D	1.988 2.012 2.037 1.961 1.984 2.006 1.995 2.007 2.018 2.026 1.990 1.941	1,9418 1,9643 1,9876 2,0092 2,0270 2,0383 2,0407 2,0324 2,0125 1,9811 1,9388 1,8877	1.8952 1.8893 1.8838 1.8787 1.8738 1.8693 1.8651 1.8611 1.8572 1.8537 1.8537 1.8544 1.8476	+.0466 +.0750 +.1038 +.1305 +.1532 +.1690 +.1756 +.1713 +.1274 +.0884 +.0401	1925 F M A M J A S O N D	2.036 2.060 2.061 2.036 1.976 1.950 1.934 1.941 1.958 1.989 2.003 2.003	1.9544 1.9683 1.9807 1.9904 1.9969 2.0000 2.0002 1.9986 1.9966 1.9959 1.9972 2.0011	1.9978 1.9997 2.0013 2.0025 2.0034 2.0039 2.0040 2.0039 2.0038 2.0034 2.0034 2.0030	0434 0314 0206 0121 0065 0037 0037 0054 0073 0079 0062 0019
I SOND	1.892 1.840 1.712 1.600 1.595 1.550 1.445 1.488 1.517 1.604 1.674	1.8308 1.7715 1.7715 1.7135 1.6608 1.51842 1.5650 1.5650 1.5684 1.5890 1.6193 1.6560	1.8451 1.8427 1.8407 1.8391 1.8378 1.8366 1.8364 1.8362 1.8369 1.8369 1.8378 1.8391	0143 0712 1272 1783 2210 2529 2716 2678 2678 2479 2185 1831	1926 J F M A M J A S O N D	2.029 2.019 2.045 2.061 2.050 2.033 2.017 2.014 2.019 2.032 2.033 1.999	2.0072 2.0145 2.0218 2.0281 2.0327 2.0353 2.0363 2.0359 2.0348 2.0333 2.0315 2.0293	2.0026 2.0024 2.0025 2.0027 2.0030 2.0038 2.0048 2.0059 2.0073 2.0091 2.0109 2.0131	+.0046 +.0123 +.0193 +.0254 +.0297 +.0315 +.0300 +.0275 +.0242 +.0206 +.0162

¹ Except charcoal pig iron.

TABLE 31—Concluded

Pig Iron Production¹ in the United States

Date	1	2	3	4	Date	1	2	3	4
1927 J F M A M J J A S O N D	2.001 2.021 2.021 2.051 2.057 2.039 2.013 1.979 1.978 1.966 1.953 1.946 1.939	2.0364 2.0226 2.0177 2.0119 2.0054 1.9986 1.9920 1.9859 1.9808 1.9770 1.9748	2.0155 2.0181 2.0207 2.0235 2.0264 2.0294 2.0323 2.0351 2.0376 2.0404 2.0428 2.0450	+.0109 +.0045 0030 0116 0210 0308 0403 0492 0568 0634 0680 0707	J F M A J J A S O N D	1.497 1.522 1.494 1.454 1.403 1.321 1.266 1.233 1.296 1.318 1.323 1.246	1.5093 1.4750 1.4407 1.4062 1.3719 1.3386 1.3081 1.2827 1.2651 1.2579 1.2624 1.2787		
1928 J M A M J J A S O N D	1.966 2.000 2.014 2.026 2.025 2.012 1.996 2.005 2.009 2.037 2.042 2.036	1.9756 1.9788 1.9836 1.9896 1.9896 2.0040 2.0118 2.0198 2.0280 2.0364 2.0449 2.0532	2.0470 2.0487 2.0502 2.0513 2.0522 2.0520 2.0513 2.0520 2.0513 2.0501 2.0484 2.0458 2.0423	0714 0699 0666 0617 0557 0483 0402 0315 0221 0120 0009 +.0109	1933 F M A M J A S O N D	1.264 1.297 1.243 1.318 1.457 1.625 1.762 1.772 1.705 1.641 1.558 1.581	1,3057 1,3411 1,3823 1,4271 1,4734 1,5200 1,5655 1,6086 1,6470 1,6785 1,7006 1,7119		
JF MAM LASOND	2.045 2.059 2.079 2.087 2.100 2.093 2.087 2.083 2.067 2.064 2.026 1.961	2.0609 2.0676 2.0726 2.07755 2.0762 2.0748 2.0717 2.0616 2.0540 2.0474 2.0474 2.0380	2.0380 2.0326 2.0268 2.0205 2.0138	+.0229 +.0350 +.0458 +.0550 +.0624	J F M A M J J A S O N D	1.593 1.654 1.718 1.761 1.819 1.808 1.597 1.532 1.476 1.487 1.504	1.7118 1.7021 1.6854 1.6650		
1930 J F M A M J J A S O N D	1.960 2.006 2.020 2.026 2.018 1.990 1.930 1.911 1.880 1.844 1.794	2.0266 2.0129 1.9970 1.9792 1.9602 1.9407 1.9211 1.9019 1.8829 1.8638 1.8444 1.8246			1935 F M A M J A S O N D	1.678 1.759 1.757 1.744 1.746 1.714 1.691 1.754 1.772 1.805 1.838 1.832			
1931 J F M A M J J A S O N D	1.743 1.785 1.817 1.828 1.808 1.737 1.674 1.616 1.591 1.578 1.566 1.500	1.8046 1.7846 1.7649 1.7459 1.7270 1.7077 1.6869 1.636 1.6374 1.6081 1.5765			1936 J	1.815			

¹ Except charcoal pig iron,

TABLE 32

United States Bureau of Labor Statistics Index Number of Wholesale Prices of Commodities, Monthly, January 1890-January 1936

Col. 1. Logarithms of Index.

Col. 2. Cyclical Curve (logarithms).

For details of the nature of the graduation given in Column 2 of this table, see Appendix D. $\,$

TABLE 32

	1	2		1	2		1	2		1	2
1890 J F M A M J A S O N D	1.7380 1.7388 1.7404 1.7412 1.7451 1.7435 1.7619 1.7664 1.7664 1.7566 1.7528	1.7396 1.7406 1.7420 1.7438 1.7460 1.7483 1.7507 1.7531 1.7552 1.7571 1.7585 1.7595	1895 J F M A M J A S O N D	1.6739 1.6712 1.6739 1.6955 1.6998 1.7024 1.6990 1.6946 1.6902 1.6902 1.6902	1.6832 1.6857 1.6882 1.6904 1.6922 1.6936 1.6943 1.6942 1.6932 1.6911 1.6880 1.6842	1900 J F M A M J J A S O ND	1.7559 1.7582 1.7582 1.7574 1.7490 1.7443 1.7466 1.7459 1.7427 1.7427 1.7435 1.7412	1.7524 1.7543 1.7553 1.7553 1.7545 1.7545 1.7529 1.7509 1.7483 1.7456 1.7431 1.7408 1.7390	1905 J F M A M J J A S O N D	1.7825 1.7853 1.7803 1.7810 1.7731 1.7731 1.7738 1.7753 1.7774 1.77789 1.7753	1.7792 1.7793 1.7793 1.7792 1.7790 1.7780 1.7785 1.7784 1.7784 1.7785 1.7788
1891 FMAM LASOND	1.7490 1.7528 1.7619 1.7649 1.7597 1.7466 1.7443 1.7435 1.7388 1.7372 1.7348 1.7308	1.7598 1.7594 1.7585 1.7569 1.7547 1.7519 1.7445 1.7399 1.7349 1.7296 1.7244	1896 JF MAN JASOND	1.6812 1.6767 1.6712 1.6693 1.6628 1.6542 1.6542 1.6542 1.6661 1.6684 1.6822 1.6776	1.6800 1.6757 1.6718 1.6685 1.6661 1.6644 1.6634 1.6629 1.6628 1.6629 1.6631	1901 F M A M J A S O N D	1.7419 1.7380 1.7364 1.7356 1.7332 1.7332 1.7364 1.7435 1.7490 1.7528 1.7612	1.7377 1.7369 1.7368 1.7371 1.7379 1.7391 1.7406 1.7423 1.7441 1.7462 1.7442 1.7462	1906 J F M A M J A S O N D	1.7860 1.7839 1.7825 1.7860 1.7875 1.7875 1.7760 1.7868 1.7903 1.7980 1.8035 1.8082	1.7804 1.7815 1.7826 1.7839 1.7853 1.7869 1.7896 1.7907 1.7931 1.7930 1.7993
1892 J F M A M J A S O N D	1.7218 1.7193 1.7127 1.7033 1.7059 1.7050 1.7152 1.7193 1.7202 1.7243 1.7324 1.7404	1.7196 1.7155 1.7126 1.7111 1.7112 1.7128 1.7158 1.7198 1.7244 1.7292 1.7337 1.7376	1897 F M A M J J ASOND	1.6693 1.6656 1.6656 1.6609 1.6580 1.6532 1.6561 1.6730 1.6857 1.6822 1.6803 1.6822	1.6638 1.6642 1.6647 1.6653 1.6662 1.6673 1.6689 1.6711 1.6737 1.6767 1.6769 1.6829	1902 F M A M J A S O N D	1.7544 1.7536 1.7521 1.7589 1.7657 1.7694 1.7716 1.7634 1.7686 1.8007 1.7832 1.7889	1.7533 1.7561 1.7562 1.7624 1.7659 1.7695 1.7731 1.7765 1.7795 1.7820 1.7837 1.7846	1907 JF M AA J J ASOND	1.8062 1.8122 1.8082 1.8096 1.8169 1.8202 1.8202 1.8202 1.8228 1.8254 1.8102 1.8007	1.8069 1.8106 1.8140 1.8166 1.8183 1.8184 1.8184 1.8169 1.8146 1.8117 1.8085
1893 FMAM JASOND	1.7528 1.7574 1.7497 1.7451 1.7404 1.7259 1.7152 1.7016 1.7160 1.7235 1.7093 1.7024	1.7406 1.7423 1.7427 1.7415 1.7387 1.7384 1.7289 1.7225 1.7156 1.7088 1.7024 1.6967	1898 JF M AM J J ASOND	1.6812 1.6866 1.6884 1.6893 1.7143 1.6840 1.6812 1.6794 1.6795 1.6812 1.6812	1.6855 1.6874 1.6885 1.6888 1.6883 1.6861 1.6849 1.6839 1.6838 1.6838	1903 JF M A M J J A S O N D	1.7966 1.7924 1.7803 1.7782 1.7709 1.7709 1.7679 1.7694 1.7745 1.7686 1.7657 1.7649	1.7846 1.7839 1.7824 1.7806 1.7762 1.7762 1.7742 1.7710 1.7700 1.7695 1.7694	1908 J F M A M J J A S O N D	1.7945 1.7882 1.7910 1.7938 1.7938 1.7966 1.8000 1.7993 1.8014 1.8028 1.8069 1.8116	1.8021 1.7993 1.7969 1.7953 1.7944 1.7953 1.7969 1.7992 1.8019 1.8049
1894 J F M A M J A S O N D	1.6955 1.6866 1.6767 1.6749 1.6721 1.6739 1.6767 1.6840 1.6955 1.6831 1.6803	1.6919 1.6879 1.6846 1.6819 1.6797 1.6780 1.6767 1.6762 1.6763 1.6772 1.6787 1.6808	1899 JF M A M J J A S O N D	1.6893 1.6964 1.6972 1.7042 1.7050 1.7101 1.7152 1.7243 1.7372 1.7435 1.7466 1.7536	1.6872 1.6906 1.6952 1.7008 1.7072 1.7142 1.7214 1.7283 1.7348 1.7406 1.7455 1.7494	1904 J F M A M J J A S O N D	1.7760 1.7832 1.7818 1.7731 1.7672 1.7664 1.7672 1.7767 1.7774 1.7832 1.7860	1.7697 1.7703 1.7711 1.7721 1.7732 1.7744 1.7754 1.7764 1.7764 1.7772 1.7780 1.7785 1.7789	1909 J F M A M J A S O N D	1.8102 1.8122 1.8143 1.8209 1.8280 1.8312 1.8319 1.8338 1.8382 1.8463 1.8507 1.8549	1.8112 1.8144 1.8177 1.8212 1.8249 1.8288 1.8330 1.8374 1.8418 1.8461 1.8501 1.8535

TABLE 32-Continued

	1	2		1	2		1	2		1	2
1910 J F M A M J A S O N D	1.8537 1.8531 1.8627 1.8645 1.8573 1.8513 1.8513 1.8500 1.8445 1.8319 1.8222 1.8235	1.8563 1.8582 1.8590 1.8587 1.8572 1.8544 1.8505 1.8455 1.8399 1.8339 1.82278	1915 J F M A M J J A S O N D	1.8332 1.8363 1.8370 1.8389 1.8344 1.8463 1.8344 1.8463 1.8344 1.8463 1.8555 1.8592	1.8331 1.8326 1.8323 1.8324 1.8332 1.8351 1.8381 1.8422 1.8474 1.8535 1.8603 1.8676	1920 J F M A M J J A S O N D	2.1978 2.1962 2.2003 2.2188 2.2232 2.2214 2.2196 2.2079 2.1909 2.1590 2.1552 2.0817	2.1965 2.2066 2.2141 2.2183 2.2182 2.2134 2.2036 2.1890 2.1700 2.1476 2.1226 2.0964	1925 J F M A M J A S O N D	2.0124 2.0170 2.0179 2.0082 2.0069 2.0128 2.0166 2.0145 2.0154 2.0154 2.0191 2.0145	2.0043 2.0078 2.0110 2.0137 2.0158 2.0170 2.0175 2.0175 2.0172 2.0164 2.0153 2.0139 2.0124
1911 LEMAM JJASOND	1.8202 1.8089 1.8109 1.8014 1.7993 1.7993 1.8055 1.8162 1.8202 1.8209 1.8149	1.8168 1.8124 1.8090 1.8067 1.8055 1.8053 1.8062 1.8081 1.8107 1.8139 1.8175 1.8213	1916 F M A M J A S O N D	1.8865 1.8949 1.9053 1.9122 1.9165 1.9186 1.9212 1.9299 1.9390 1.9595 1.9886 1.9965	1.8754 1.8835 1.8919 1.9006 1.9098 1.9196 1.9300 1.9413 1.9535 1.9667 1.9809 1.9958	1921 F M A M J J A S O N D	2.0569 2.0208 2.0103 1.9952 1.9832 1.9704 1.9708 1.9708 1.9736 1.9741 1.9680	2.0703 2.0453 2.0226 2.0031 1.9871 1.9751 1.9668 1.9619 1.9598 1.9600 1.9616 1.9642	1926 F M A M J A S O N D	2.0137 2.0086 2.0026 2.0013 2.0022 2.0017 1.9978 1.9961 1.9987 1.9974 1.9930 1.9908	2.0109 2.0094 2.0078 2.0061 2.0042 2.0021 1.9978 1.9972 1.9945 1.9918 1.9891
1912 JFMAM JASOND	1.8195 1.8241 1.8293 1.8432 1.8451 1.8389 1.8382 1.8432 1.8482 1.8500 1.8463 1.8463	1.8252 1.8290 1.8325 1.8357 1.8386 1.8410 1.8429 1.8453 1.8453 1.8450 1.8460	1917 F M A M J A S O N D	2.0090 2.0191 2.0322 2.0573 2.0817 2.0864 2.0899 2.0962 2.0917 2.0871 2.0892 2.0892	2.0111 2.0263 2.0407 2.0539 2.0654 2.0749 2.0822 2.0876 2.0913 2.0938 2.0957 2.0973	J F M A M J A S O N D	1.9610 1.9680 1.9676 1.9674 1.9827 1.9836 1.9974 1.9939 1.9970 1.9983 2.0022 2.0030	1.9673 1.9705 1.9739 1.9775 1.9812 1.9853 1.9895 1.9939 1.9981 2.0019 2.0051 2.0074	1927 F M A M J J A SO N D	1.9845 1.9814 1.9764 1.9736 1.9736 1.9745 1.9786 1.9836 1.9836 1.9836 1.9836	1.9842 1.9822 1.9804 1.9790 1.9773 1.9773 1.9776 1.9783 1.9785 1.9809
1913 JFMAM JJASOND	1,8470 1,8439 1,8445 1,8432 1,8382 1,8420 1,8432 1,8488 1,8476 1,8457 1,8395	1.8458 1.8455 1.8455 1.8452 1.8445 1.8445 1.8445 1.8435 1.8427 1.8419 1.8410 1.8389	1918 F M A M J J A S O N D	2.0969 2.0888 2.1018 2.1082 2.1076 2.1106 2.1206 2.1281 2.1383 2.1345 2.1345 2.1345	2.0992 2.1015 2.1044 2.1078 2.1114 2.1152 2.1182 2.1220 2.1246 2.1265 2.1276 2.1281	1923 J F M A M J J A S O N D	2.0086 2.0141 2.0191 2.0166 2.0082 2.0013 1.9930 1.9987 1.9974 1.9930 1.9917	2.0088 2.0094 2.0092 2.0083 2.0071 2.0055 2.0036 2.0015 1.9992 1.9967 1.9942 1.9918	I 1928 F M A M I J A SON D	1.9841 1.9814 1.9800 1.9850 1.9850 1.9854 1.9886 1.9895 1.9939 1.9854 1.9814	1.9839 1.9852 1.9862 1.9868 1.9871 1.9870 1.9867 1.9865 1.9843 1.9843
1914 F M A M J A S O N D	1.8363 1.8344 1.8325 1.8300 1.8287 1.8287 1.8280 1.8426 1.8463 1.8325 1.8293 1.8280	1.8378 1.8368 1.8357 1.8347 1.8340 1.8334 1.8331 1.8332 1.8333 1.8336 1.8337 1.8335	1919 J F M A M J A S O N D	2.1284 2.1133 2.1183 2.1239 2.1313 2.1323 2.1495 2.1593 2.1495 2.1511 2.1599 2.1775	2.1281 2.1280 2.1279 2.1284 2.1298 2.1326 2.1371 2.1435 2.1518 2.1619 2.1733 2.1851	1924 J F M A M J J A S O N D	1.9983 1.9987 1.9934 1.9881 1.9818 1.9773 1.9805 1.9868 1.9872 1.9921 1.9961 2.0065	1.9896 1.9878 1.9866 1.9859 1.9859 1.9865 1.9877 1.9894 1.9916 1.9943 1.9974 2.0008	1929 F M A M J A S O N D	1.9818 1.9796 1.9827 1.9800 1.9764 1.9786 1.9845 1.9836 1.9827 1.9782 1.9782 1.9708	1.9833 1.9828 1.9824 1.9826 1.9816 1.9811 1.9806 1.9795 1.9761 1.9736 1.9736

TABLE 32—Concluded

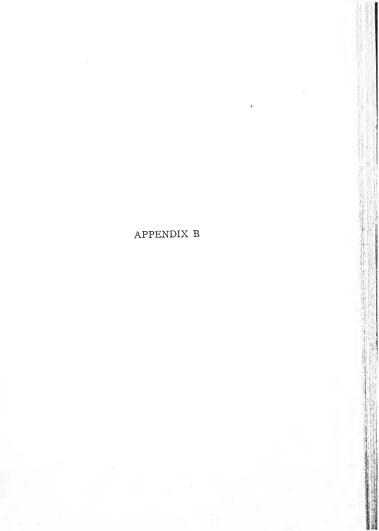
	1	2		1	2		1	2		1	2
1930 J F M A M J A S O N D	1,9661 1,9610 1,9552 1,9542 1,9484 1,9385 1,9263 1,9263 1,9263 1,9101 1,9101 1,9009	1.9666 1.9622 1.9574 1.9521 1.9464 1.9340 1.9275 1.9207 1.9139 1.9070 1.9003	1932 F M A M J A S O N D	1.8280 1.8215 1.8195 1.8162 1.8089 1.8055 1.8096 1.8143 1.8149 1.8089 1.8055 1.7966	1.8310 1.8275 1.8241 1.8206 1.8168 1.8168 1.8127 1.8084 1.8040 1.7999 1.7965 1.7939 1.7926	1934 J F M A M J A S O N D	1.8585 1.8669 1.8675 1.8651 1.8675 1.8727 1.8739 1.8831 1.8899 1.8837 1.8837 1.8837	1.8620 1.8658 1.8685 1.8707	1936 J	1.9063	
1931 F M A M J A S O N D	1.8932 1.8854 1.8584 1.8739 1.8645 1.8579 1.8573 1.8573 1.8573 1.8525 1.8470 1.8463 1.8363	1.8937 1.8873 1.8812 1.8754 1.8697 1.8641 1.8586 1.8532 1.8480 1.8432 1.8387 1.8346	1933 F M A M J A S O N D	1.7853 1.7767 1.7796 1.7810 1.7973 1.8129 1.8382 1.8420 1.8525 1.8519 1.8500	1.7925 1.7939 1.7967 1.8064 1.8130 1.8204 1.8283 1.8364 1.8441 1.8512 1.8572	I935 F M A M J A S O N D	1.8965 1.9004 1.8998 1.9036 1.9042 1.9020 1.8998 1.9058 1.9058 1.9063 1.9063				

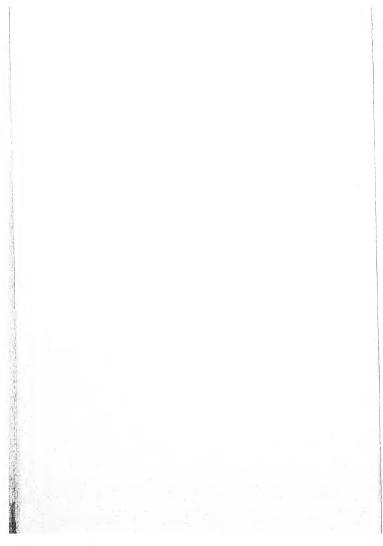
TABLE 33

Dr. Wesley C. Mitchell's Dates of High and Low Points in General Business in the United States

(See Recent Economic Changes, Vol. II, p. 892, National Bureau of Economic Research Inc., 1929.)

High		Low	
June	1857	December	1858
October	1860	June	1861
April	1865	December	1867
June	1869	December	1870
October	1873	March	1879
March	1882	May	1885
March	1887	April	1888
July	1890	May	1891
January	1893	June	1894
December	1895	June	1897
June	1899	December	1900
September	1902	August	1904
May	1907	June	1908
January	1910	January	1912
January	1913	December	1914
August	1918	April	1919
January	1920	September	1921
May	1923	July	1924
October	1926	December	1927
June	1929	March	1933





APPENDIX B

PROFESSOR IRVING FISHER'S STATISTICAL MEASURES OF 'PRICE CHANGE'

In discussing the relations between commodity prices and interest rates, Professor Irving Fisher designates level of commodity prices by the letter P, and $\mathit{changes}$ in that level by P'. He uses a third symbol $\overline{P'}$ to represent various moving averages of P'. In the course of merely verbal discussion, as distinct from mathematical or statistical presentation, P is usually referred to as 'commodity price level', and P' as 'change in commodity price level'. The third symbol $\overline{P'}$ is usually defined in a semi-mathematical fashion either as 'the distributed lag of P'' or as 'the weighted average of sundry successive P''s'.'

The symbol P, or the *level* of commodity prices, is defined mathematically as the successive values of an 'index number' of commodity prices. It may represent almost any index number that is readily available and that seems adequate for the particular purpose at hand. When discussing interest rates and commodity prices in the United States, Professor Fisher lets P represent one of the index numbers of American wholesale prices constructed by the United States Bureau of Labor Statistics.

The second symbol, P', is repeatedly referred to merely as 'price change'. But that expression seems always to be used as a contraction or abbreviation of the longer expression 'rate of price change'. Even when Professor Fisher seems to have deliberately defined P' as 'price change' rather than 'rate of price change', the context will usually show that the latter is really meant. The emphasized characteristics of P' are always those of a ratio or a function of a ratio,

¹ Cf. Irving Fisher, The Theory of Interest, p. 419.

^{2&#}x27; . . . i stands for interest rate and P' for price change . . . ' The Theory of Interest, p. 412.

^{&#}x27;In Chart 44, price change (P') is represented . . . ' Ibid., p. 414.

³ For example, '... the price change (P') is assumed to be at the rate of 5 per cent per annum' (*The Theory of Interest*, p. 413). If the author had intended P' to mean 'rate of

rather than those of an arithmetic 'difference'. The various mathematical definitions are all such that the value of P' would be unaffected by multiplying by a constant the successive terms of the price index number from which it is calculated. But its value would be definitely changed by adding a constant to, or subtracting a constant from, those terms.

The third symbol, $\overline{P'}$, is mathematically always just what it is stated to be, 'a weighted average of sundry successive P''s'. But this is essentially an operative rather than an explanatory definition. It describes one way in which $\overline{P'}$ may be calculated; but, in the absence of analysis, throws little light on what $\overline{P'}$ means.

Professor Fisher verbally defines P' as the change in prices from

one month (or year) to the next. He has proposed two arithmetic methods of measuring this 'change'. These arithmetic statements are, of course, the real definitions. The first of these arithmetic definitions appeared in an article published in 1923.4 It was given as a measure of the rise or fall of prices 'for each month'. It was calculated for any particular month by dividing the price index for the succeeding month by the price index for the preceding month and subtracting unity. In other words, if the index numbers for three consecutive months be designated a, b, c, the value of P' for the month whose price index was b would be $\frac{c}{a}-1$. This is one one-hundredth or one per cent of the percentage change in the price level from the first month to the third month. For example, if a=100 and c=125, P' would equal $\frac{25}{100}$.

It is not worth while to examine critically this 1923 definition of P'. Professor Fisher himself discarded it within eighteen months. Indeed, it is strange that, in December 1923, a year after the publication (December 1922) of his book *The Making of Index Numbers* with its detailed and exhaustive analysis of the problem of 'bias', he could

price change', we would expect him to have written ' . . . the rate of price change (P') is assumed to be 5 per cent per annum'. However, on the chart (43) to which the discussion refers, we find such notations as P'=5%, P'=10%, etc.

^{4&}quot;The Business Cycle largely a 'Dance of the Dollar'," Journal of the American Statistical Association, December 1923, pp. 1024-28.

have proposed defining P' as $\frac{c}{a} - 1$. For the function $\frac{c}{a} - 1$ has a pronounced upward 'bias'.5

The second arithmetic definition of P' appeared in an article published in 1925.6 In that article Professor Fisher proposed that the value of P' for the month whose price index is b be defined (if a, b, cbe, as before, the index numbers for three consecutive months) as $\frac{c-a}{2h}$, or, 'on an annual basis', as $\frac{6(c-a)^{\text{note}7}}{h}$. The value of $\frac{c-a}{2h}$ $\left(\text{or } \frac{6(c-a)}{b}\right)$ is, of course, the same when a, b, c, are 0, 100, 10 as when they are 95, 100, 105 or 99, 10, 100.

If the time scales and the price scales were assumed to be so related that the price figures were expressed in the time scale (the time interval from the abscissa of a to the abscissa of c being taken as unity), and if the points whose ordinates were a and c were joined by a straight line, the slope of that line (throughout its length) would be c - a.

Of course, if a new curve were now constructed each of whose infinite number of ordinates was the natural logarithm (to the base e) of an ordinate of the original straight line having the same abscissa, $\frac{c}{a} - 1$, which equals $\frac{c - a}{a}$, would be the 'slope' of the tangent to this new curve at the point whose ordinate was log a. But, as this new curve is not a straight line, only at this one point would $\frac{c}{a} - 1$ be its 'slope'.

6 "Our Unstable Dollar and the so-called Business Cycle", Journal of the American Statistical Association, Vol. XX, New Series No. 150, June 1925, pp. 179-202 incl.

" . . . a derivative of P, namely, the curve P' . . . such that the height of P' is expressed by the same figure as the slope of P" (1925 article, p. 182). At the bottom of the page there is a note on the word slope which Professor Fisher had italicized. The note reads: "The slope for any given month is measured by subtracting the index for the preceding month from that for the succeeding month and reducing the result to a percentage of the given or intervening month. This percentage, being for two months, is multiplied by six to give a per annum rate."

⁵ Professor Fisher speaks of P', both when defined as $\frac{c}{a}-1$ and when defined (in his later work) as $\frac{c-a}{2h}$, as the 'slope' of P and as the 'derivative' of P. But the reader must be warned that, for purposes of analogical comparison, he uses these strictly mathematical terms in a loose and colloquial manner.

Strictly speaking, only if a 'slope' is constant over a period can it be termed the 'slope' of a curve during the period. And, of course, only if there be a 'curve' in the strict mathematical sense of that term can there be a 'slope'. The 'slope' of a curve at a specified point on the curve is the trigonometric 'tangent' of the straight line (geometrically) tangent to the curve at the point. Only if the curve itself be a straight line can its 'slope' be constant.

The function $\frac{c-a}{2h}$ contains a totally irrelevant variable. The value of b has no more logical place in a measure of price change from the level a to the level c than has the altitude of a balloon an hour ago to its change in altitude during the past two hours. The change in altitude of the balloon may be calculated from the change in altitude during the first hour and the change during the second hour; but the altitude at the end of the first hour will not affect the change in altitude during the two hours.8

It may, of course, be argued that $\frac{c-a}{2h}$ is not intended to measure price change from the middle of the first month to the middle of the third month but from the beginning to the end of the second month; that we are not measuring the change in the altitude of the balloon during the past two hours but during the single hour that ended half an hour ago; that, for the determination (by interpolation) of the probable price level at the beginning of the second month, b is as important as a; and, similarly, as important as c for the determination of the price level at the end of the second month.

appear in full force as soon as any attempt is made to develop a rational and systematic scheme of interpolation that will yield $\frac{c-a}{2k}$ as a not-absurd function of the interpolated values, without introducing b otherwise than as it occurs in those interpolated values. For

But, after the acceptance of this condition, the difficulties re-

example, if the level of prices at the beginning of the second month be taken as the arithmetic average of a and b and the level at the end of the month as the arithmetic average of b and c, we are faced with the difficulty that a knowledge of the values of only these averages is insufficient to determine $\frac{c-a}{2b}$. The necessity of introducing b

remains.9

⁸ Of course, b is only technically irrelevant if it is introduced in such a manner that it eventually cancels out. For example, $(\log c - \log b) + (\log b - \log a) = \log c - \log a$; and $\frac{c}{b} \times \frac{b}{a} = \frac{c}{a}$.

⁹ If, through the three points $(-\frac{1}{2}, \frac{a+b}{2})$, (0, b), $(+\frac{1}{2}, \frac{b+c}{2})$, a second degree parabola $(y = A + Bx + Cx^2)$ be drawn, and another curve be constructed such that each of its ordinates is the natural logarithm of an ordinate of this parabola, $\frac{c-a}{2h}$ will be the slope of this new curve at the point (O, log b). But, not merely has b been directly introduced, but the slope is at a point only.

By itself, P' or $\frac{c-a}{2b}$ is a highly erratic function. But Professor

Fisher makes much more use of $\overline{P'}$ than of P', and $\overline{P'}$ is definitely less erratic than P'. The cumulation of P' tends to iron out some of its irregularities. We discuss the reasons for this fact later in this appendix.

Professor Fisher describes $\overline{P'}$ as 'the distributed lag of P'' or as 'the weighted average of sundry successive P''s'. It was in articles dealing with the relation of changes in commodity price levels to interest rates, bond yields and the activity of business in general that he approached the problem of deciding what particular weights should be assigned to the 'sundry successive P''s'. He presented the hypothesis that any appreciable change in the general level of commodity prices influenced the level of interest rates, etc., for long periods, though the strength of such influence declined with the passage of time. Conversely, that though a present level of interest rates, for example, had been most powerfully affected by recent changes in commodity prices, it had also been influenced, though to a less degree, by changes that had occurred in the distant past.

One of Professor Fisher's early efforts to decide upon what relative weights should be assigned to the influences of recent and remote price changes led him to base those weights on the ordinates of a skew probability curve which had its maximum ordinate in the very near past. The present writer cannot say that he grieves over the fact that this hypothesis was soon thrown overboard. The combination of the $\frac{c-a}{2b}$ method of measuring P' and the skew-probability weights for $\overline{P'}$ would have left that latter function in a position to

 $^{^{10}}$ Though the erratic nature of P' may be very clearly illustrated by means of cumulations and averages. The function $\frac{c-a}{2b}$ has no systematic upward or downward 'bias', but its cumulation can yield strange results. Consider, for example, a hypothetical monthly series running 1, 4, 16, 2, 8, 32, 4, 16, 64 . . . These figures show a pronounced upward trend; each is double that for the third month back. However, a moving three months' simple arithmetic average of the $\frac{c-a}{2b}$ functions is constant and negative.

Its value is always $-\frac{1}{16}$. If the series were presented in reverse order, it would of course show a pronounced downward trend. But the three months' moving average of the $\frac{c-a}{2b}$ functions would be constant and positive.

defy successfully any attempt at a simple presentation of its meaning. A right-angled triangle with the right angle on the x-axis and the maximum ordinate at the most recent month was substituted for the skew probability curve. Moreover, the renunciation was complete. It was no mere sop to the exigencies of computation. Professor Fisher announced that the results obtained with the right-angled triangle were distinctly more acceptable to him than were those that had been obtained through the use of the skew probability curve. With the 'triangular' weighting, the function $\overline{P'}$ is defined as a weighted average of n successive P''s in which the earliest P' has a weight of 1, the next in time a weight of 2, the third a weight of 3, and the nth (or most recent) P' a weight of n. The function $\overline{P'}$ therefore equals

$$\frac{P'_1+2P'_2+3P'_3+\ldots+nP'_n}{\Sigma n}.$$

Up to this point we have designated data by the letters a, b, and c because single letters are so easy to remember without confusion. But, as the discussion from now on is in terms of hyperbolic functions, a different nomenclature is desirable. For a, b, and c let us substitute the symbols e^{y_1} , e^{y_2} , e^{y_3} , where e stands for the base of the natural system of logarithms. 12 and y_1 , y_2 , y_3 are $\log a$, $\log b$, and $\log c$. Also, let $z_1 = y_2 - y_1$ and, in general, $z_n = y_{n+1} - y_n$; or in terms of the earlier notation, $z_1 = \log b - \log a$ and $z_2 = \log c - \log b$. In this new notation,

$$P'_{n} = \frac{e^{y_{n+2}} - e^{y_{n}}}{2 e^{y_{n+1}}} = \frac{1}{2} (e^{z_{n+1}} - e^{-z_{n}})$$

$$= \frac{1}{2} \left(\sinh z_{n+1} + \sinh z_{n} + 2 \sinh^{2} \frac{z_{n+1}}{2} - 2 \sinh^{2} \frac{z_{n}}{2} \right). \text{ note 13}$$

¹³ As
$$\sinh z$$
, or the 'hyberbolic sine of z ' equals $\frac{e^z-e^{-z}}{2}$, $2\sinh^2\frac{z}{2}+1=\frac{e^z+e^{-z}}{2}$.

Hence,
$$e^{z_{n+1}} = \sinh z_n + 1 + 2 \sinh^2 \frac{z_{n+1}}{2} + 1$$
 and $e^{-z_n} = \sinh z_n - 2 \sinh^2 \frac{z_n}{2} - 1$.

¹¹ Compare The Theory of Interest, p. 421.

 $^{^{12}}$ Unless otherwise stated, the logarithms referred to in this appendix are 'natural' logarithms (to the base e) and not 'common' logarithms (to the base 10).

Now, it is apparent that, if e^{y_n+1} be the geometric mean of e^{y_n} and e^{y_n+2} , z_n will equal z_{n+1} and hence the $\sinh^2\frac{z}{2}$ terms in the expression for P' will cancel out and disappear. And, even with data that do not constitute a geometric progression, it is apparent that, if a total (or a simple unweighted arithmetic average) of n successive P''s be taken, all but the first and last of the $\sinh^2\frac{z}{2}$ terms will cancel out and disappear. The unweighted arithmetic average of n successive P''s from P'_1 to P'_n equals

$$\frac{1}{2n} \left\{ (\sinh z_1 + 2 \sinh z_2 + 2 \sinh z_3 + \ldots + 2 \sinh z_n + \sinh z_{n+1}) + 2 \left(\sinh^2 \frac{z_{n+1}}{2} - \sinh^2 \frac{z_1}{2} \right) \right\}.$$

Furthermore, the relative influence on the average exerted by the two \sinh^2 terms that remain will tend to decrease as the value of n is increased. There will always be $\frac{n}{2}$ times as many $\sinh z$ terms as there are $\sinh^2\frac{z}{2}$ terms. If we assume (with Professor Fisher) that it is legitimate and proper to average arithmetically 'sundry successive P''s', we must conclude that the $\sinh z$ terms in the expression for P' are, at least for the purpose of analyzing the essential characteristics of such an average of P''s, fundamental and the $\sinh^2\frac{z}{2}$ terms essentially extraneous and irrelevant.

And this conclusion (derived from the fact that the influence of the $\sinh^2\frac{z}{2}$ terms tends to decrease $pari\ passu$ with increases in the number of P''s in the average) is reinforced by considering some of the essential characteristics of these terms and of the complete functions of z_1 , and z_{n+1} . In the first place, though the function $\sinh^2\frac{z}{2}$ may be thought of as a measure of absolute fluctuation, it cannot properly be thought of as a measure of advance or decline. Its value is not affected by the inherent algebraic sign of z. A decline of the data from 100 to 95 yields the same value for $\sinh^2\frac{z}{2}$ as an advance from 95 to 100. And similarly with the expression

 $\sinh^2\frac{z_{n+1}}{2} = \sinh^2\frac{z_1}{2}$. Whether this expression is, as a whole, positive or negative depends in no way on the inherent algebraic signs of z_{n+1} and z_1 . It depends only on the *absolute* values of z_{n+1} and z_1 and the external algebraic signs that precede $\sinh^2\frac{z_{n+1}}{2}$ and $\sinh^2\frac{z_1}{2}$. And the sign of the expression, even as thus derived, is, as may be seen from an examination of the complete function of z_{n+1} , note 15 and the complete function of z_1 , note 16 essentially arbitrary and accidental.

If we remember that a z is not a raw datum (e.g., a price) but a function (the logarithm) of the ratio of a datum to the preceding datum, it would seem reasonable to assume that the time order of the z's should not affect an arithmetic average of a function such as P' that is intended to measure data changes. In fact, the unweighted arithmetic average of successive P''s is unaffected by the time order of any of the z's except the earliest z and the latest z. But, unless z_{z+1} equals plus or minus z_1 , the average is affected by the time order of those two z's. If the earliest z be substituted for the latest z and vice versa, the value of the average is altered. Though the $\sinh z$ terms in the average remain unchanged, the sign of the $\sinh z$ terms in the average remain unchanged, the sign of the sinh z terms in the average remain elements the sinh z terms in the average would seem complete.

The function $\overline{P'}$ is a weighted and not a simple arithmetic average of 'sundry successive P''s'. But the conclusions we have arrived at concerning the essential irrelevancy of the \sinh^2 elements hold with respect to the weighted average as definitely as they hold with respect to the unweighted average. After the collection and cancellation of terms, $\overline{P'}$ note 17 appears as

¹⁴ The expression will vanish if $z_n + 1$ equals plus or minus z_1 .

¹⁶ Sinh $z_n + 1 + 2 \sinh^2 \frac{z_n + 1}{2}$.

¹⁶ Sinh $z_1 - 2 \sinh^2 \frac{z_1}{2}$.

 $[\]overline{P'} = \frac{P'_1 + 2P'_2 + 3P'_3 + \ldots + nP'_n}{\sum n}$

If the data constitute a geometrical progression, 18 the $\sinh^2 \frac{z}{2}$ terms cancel out and disappear as they do in the unweighted average. It is true that, when the data are not so related to one another, no such wholesale cancellation of $\sinh^2 \frac{z}{2}$ terms occurs as occurs in the case of the unweighted average. Indeed, each z is, in the weighted average, represented by a $\sinh^2 \frac{z}{2}$ item. But the absence of any relation of the sign of these terms to advance or decline of the data is as complete as it was with the unweighted average. The $\sinh^2 \frac{z}{2}$ terms are indices of mere absolute fluctuation. Their algebraic sum equals the deviation of the most recent $\sinh^2 \frac{z}{2}$ (i.e., $\sinh^2 \frac{z_{n+1}}{2}$) from the arithmetic average of the *n* preceding $\sinh^2 \frac{z}{2}$'s, divided by $\frac{n+1}{2}$. note 19 It is no more than a comparison of how the size of a particular function of the extent of the most recent fluctuation (up or down) compares with the average size of the function in the past n periods. As such, it is for our purposes, an erratic and meaningless expression.

¹⁸ Or, more generally, if the ratio of the larger of each pair of adjacent data points to the smaller be constant, as would be the case, for example, if the data ran 2, 4, 8, 4, 8, 16, 8, 4.

 $[\]frac{19}{2n} = \frac{n+1}{2}$

But, if n be made large enough, this $\sinh^2\frac{z}{2}$ expression virtually vanishes from the picture. For example, if n=120 (as it does in one of Professor Fisher's quarterly commodity price illustrations), the deviation of $\sinh^2\frac{z_{121}}{2}$ from the average of the 120 preceding $\sinh^2\frac{z}{2}$'s is divided by $\frac{121}{2}$. With data that fluctuate no more violently than do quarterly commodity price index numbers, the largeness of this divisor reduces the \sinh^2 elements in the formula to complete negligibility.

If we remove these erratic (and commonly negligible) \sinh^2 terms from the expression for $\overline{P'}$, we have

$$\frac{1}{P'} = \frac{\sinh z_1 + 3 \sinh z_2 + 5 \sinh z_3 + \dots + (2n-1) \sinh z_n + n \sinh z_{n+1}}{2 \sum n}.$$

But, as
$$\sinh z = z + \frac{z^3}{3!} + \frac{z^5}{5!} + \dots$$
, z^0 this expression equals
$$+ z_1 + \frac{z^3}{3!} + \frac{z^5}{5!} + \dots$$
$$+ 3z_2 + \frac{3z^3}{3!} + \frac{3z^5}{5!} + \dots$$
$$+ 5z_3 + \frac{5z^3}{3!} + \frac{5z^3}{5!} + \dots$$
$$+ (2n - 1) z_n + \frac{(2n - 1) z^3_n}{3!} + \frac{(2n - 1) \sum z^5_n}{5!} + \dots$$
$$+ nz_{n+1} + \frac{nz^3_{n+1}}{3!} + \frac{nz^5_{n+1}}{5!} + \dots$$

all divided by $2 \Sigma n$.

If the values assumed by z be small ('absolutely' and not algebraically), this function will approximate

$$\frac{z_1 + 3z_2 + 5z_3 + \ldots + (2n-1) z_n + nz_{n+1}}{2 \sum n}.$$

This is the value obtained by neglecting all powers of z greater than unity. Such a treatment of the function, in which cubes are the next

$$z^{20} e^z = 1 + z + \frac{z^2}{2!} + \frac{z^3}{3!} + \dots$$

and $\sinh z = \frac{e^z - e^{-z}}{2!}$

A321

higher power after unity, is, for the purposes of our present analysis, quite warranted.21

But, as $z_n = y_{n+1} - y_n$, this expression equals $(y_2 - y_1) +$ $(3y_3-3y_2)+(5y_4-5y_3)+\ldots+\left\{(2n-3)y_n-(2n-3)y_{n-1}\right\}$ $+\left\{(2n-1)y_{n+1}-(2n-1)y_n\right\}+(ny_{n+2}-ny_{n+1}),$ divided by $2 \sum n$; which equals $-y_1 - 2y_2 - 2y_3 - \ldots - 2y_n - y_{n+1} +$ $n (y_{n+1} + y_{n+2})$, divided by $2 \sum n$. If $Y_n = \frac{y_n + y_{n+1}}{2}$, this expression becomes

$$- Y_{1}, - Y_{2}, -Y_{3} - \ldots - Y_{n} + nY_{n+1}, \text{ divided by } \Sigma n, \text{ or } \frac{2}{n+1} (Y_{n+1} - \frac{Y_{1} + Y_{2} + \ldots + Y_{n}}{n}).$$

In other words, the value to which $\overline{P'}$ approximates (if the month to month-or year to year-fluctuations of the data are not too violent—and they are not with commodity price index numbers) may be described as follows. Take a two-months' moving average of the logarithms of the data (or take the logarithms of the geometric means of adjacent values). With this average as new data, $\overline{P'}$ will approximate $\frac{2}{4}$ times the deviation of a datum value from the arithmetic average of the n preceding data values.²² It is the deviation of the logarithm of present price from an average of the logarithms of past prices.

The function $\frac{2}{n+1}$ $(Y_{n+1} - \frac{Y_1 + \ldots + Y_n}{n})$ is the slope of the straight line joining Y_{n+1} to the mid point of the moving average $Y_1 + \dots + Y_n$. It is therefore *technically* correct to describe it as a measure of rate of price change. For example, if the Y's all fell on the straight line Y = A + Bx (as would be the case if the original

²¹ If z be 'absolutely' small, sinh z does not differ greatly from z. For example, if prices one month are even as much as 125 per cent of what they were in the preceding month, the difference will be extremely small. If $e^z = 1.25$ then z = .2231 . . . and $\sinh z = .2250$, . .

²² If common, and not natural, logarithms are used, the result will, of course, be 0.434 ... times \overline{P}' instead of \overline{P}' .

data fell on a compound interest curve), the function would always equal B. No matter what the value of n the arithmetic average of the Y's would advance $pari\ passu$ with the value of the most recent Y from which the average was to be subtracted.

But no such condition would exist if the Y's fell on a periodic curve such as a sine curve (plus a constant). If n equalled the number²⁸ of data points in one period or 'cycle', the function points would lie on another sine curve of smaller amplitude or 'swing' than the data curve, but with maxima and minima on the same dates. With an adjusted scale, it would be an exact reproduction of the data curve, though it would be technically correct to describe it as a measure of rate of change of that curve. But it might easily be more misleading than enlightening to do so.

A sine curve has no long-term trend. In general, if the data show no definite long-term trend, the average of the Y's will, if n be taken sufficiently large, tend to be virtually constant. And $\overline{P'}$ will therefore tend to reproduce the data—minus a constant.

There are innumerable examples of such trendless curves. Some of the most perfect are series that, from their mathematical nature, move within definite limits. The digits of the decimal development of an incommensurable number, such as the 707 calculated digits of π . The number of spots in each successive throw of a pair of dice. Percentages that cannot exceed one hundred, such as the percentage of blast furnaces in blast, etc.

Less perfect examples come from the field of percentages that never approach one hundred; the percentage of the population in receipt of poor relief, the percentage of banks in the hands of receivers, the ratio of bank reserves to bank deposits, etc.

But, even with series that possess unmistakable trends, $\overline{P'}$ may closely approximate P. If the fluctuations of the data (from which the average is to be subtracted) happen to be extremely large as compared with the movements of the average, $\overline{P'}$ will, over short periods, often virtually reproduce P. $^{\text{note 24}}$

²³ Or a multiple of that number.

²⁴ Compare *The Theory of Interest*, Chart 49 (opp. p. 426). In this chart are presented quarterly figures for \overline{P}' and i (short term interest rates in the United States) for the period 1915–1927. In this period occurred the violent war and post-war movements

It is of course true, as Professor Fisher says, that "It certainly stands to reason that in the long run a high level of prices due to previous monetary and credit inflation ought not to be associated with any higher rate of interest than the low level before the inflation took place. It is inconceivable that, for instance, the rate of interest in France and Italy should tend to be permanently higher because of the depreciation of the franc and the lira, or that a billion-fold inflation as in Germany or Russia would, after stabilization, permanently elevate interest accordingly." ²⁵

The function $\overline{P'}$ compares prices with a moving-average base instead of with zero, and therefore cannot remain high indefinitely. But the statistical evidence that the particular base introduced by $\overline{P'}$ is, even empirically, a good base is not strong. Correlations between P and i usually run higher than those between $\overline{P'}$ and i.

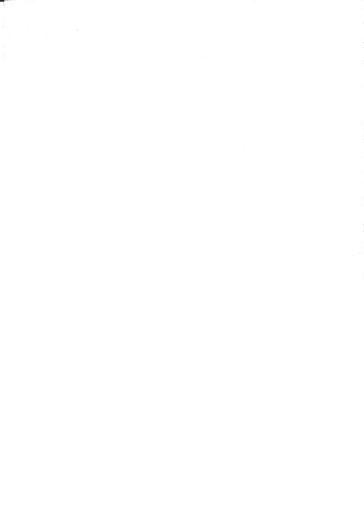
And again, if the substitution of $\overline{P'}$ for P, instead of lowering, raised the coefficients of correlation noticeably, it is questionable whether we would be warranted in assuming that it was because $\overline{P'}$ was a 'weighted average of sundry successive P''s' rather than because it was a deviation of P from a moving base. Professor Fisher writes, ''It seems fantastic, at first glance, to ascribe to events which occurred last century any influence affecting the rate of interest today''. ²⁶ If for the word 'events' we substitute the words 'commodity price changes' (which are the 'events' Professor Fisher is discussing) and for the words 'any influence' the particular measure of that influence Professor Fisher proposes, we might be tempted to counter with, 'Why only at first glance?' He immediately continues with, ''And yet that is what the correlations with distributed effects of P' show.'' But is it?

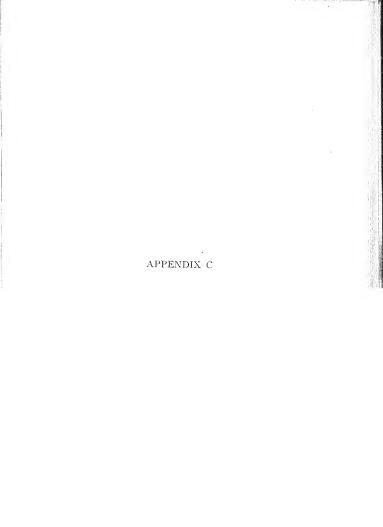
of prices and interest rates. The value of n is huge, 120. The similarity between \overline{P}' and P, both of which are given in the chart, is striking.

Professor Fisher found that the maximum correlation (+0.738) between \overline{P}' and i was obtained when n was made 120. But the correlation between P (the raw data) and i gave +0.709 without lagging and, if i was lagged two quarters (half a year), +0.891, (The Theory of Interest, pp. 427 and 431.)

²⁵ The Theory of Interest, p. 440. The italics are Professor Fisher's.

²⁸ The Theory of Interest, p. 428.







THE MEANING OF GOLD YIELDS OF BONDS PAYABLE PRINCIPAL AND INTEREST IN CURRENCY (See Table 19 and Charts 25, 26 and 28)

 The meaning of bond yields in a year such as 1925 in the United States when there was no problem of currency depreciation in terms of gold.

If a 5 per cent \$1000 face value bond, with interest payable semi-annually, four years to run, sells for \$1036.63, it is said to yield 4 per

cent per annum to the purchaser.1

Or, if the present value of each interest payment and of the principal payment be obtained by discounting at 2 per cent per half-year true discount each future payment, the sum of these present values will be \$1036.63. For example, there are eight interest payments of \$25, the first payable six months hence, the second one year hence, etc. There is also the principal payment of \$1000 payable four years hence. Now the present value of the first interest payment of \$25 is \$25 + 1.02 or \$24.51; the present value of the second interest payment of \$25 is \$25 ÷ (1.02)^2 or \$24.03; etc. The use of 1.02 as a divisor instead of $\sqrt{1.04}$ is, as mentioned in note 1, a convention of the bond tables. Now, the present values of the eight interest payments of \$25 each and the principal payment of \$1000 are: \$24.51; \$24.03; \$23.56; \$23.10; \$22.64; \$22.20; \$21.76; \$21.34, and \$853.49. The total of these present values is \$1036.63, the price paid for the bond.

2. The meaning of a gold yield of a bond in a period of depreciated currency, when the interest and principal of the bond are both payable

in currency.

Bond No. 5 in Appendix A, Table 3 is a New York and Harlem Railroad 7 per cent bond which matured May 1, 1873. The interest

was payable May 1 and November 1.

The average greenback price of this bond in January 1865 was \$1038.75. The average gold price of greenbacks in January 1865 was \$46.3 in gold for \$100 in greenbacks. Multiplying \$1038.75 by .463, we obtain \$480.94 as the gold price of this Harlem bond in January 1865. The gold yield to maturity of this bond at this gold price was calculated and found to be 16.43 per cent per annum.

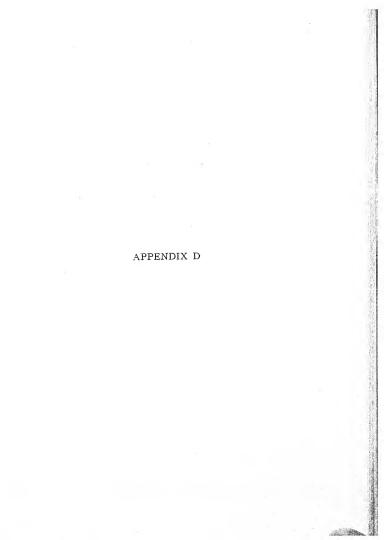
The meaning of this yield may be illustrated as follows: The gold

 $^{^4\}mathrm{Really}~2$ per cent semi-annually under the convention on which the ordinary bond tables are constructed.

values of the seventeen future interest payments of \$35 each and the principal payment of \$1000 were, on the day on which each payment was made, \$24.32; \$23.99; \$27.77; \$23.81; \$25.83; \$24.86; \$25.11; \$26.26; \$25.96; \$27.30; \$30.39; \$31.44; \$31.44; \$31.20; \$31.15; \$31.18; \$29.90; \$854.25. Dividing the first interest payment by 1.04713 (note2) the second interest payment by (1.04713) (1.08215); the third interest payment by (1.04713) (1.08215); the third interest payment by (1.04713) (1.08215); etc., we obtain a set of present values in gold of the future gold values of the future currency interest payments of \$35 each and the currency principal payment of \$1000. These present values (in gold) were \$23.23; \$21.21; \$22.68; \$17.97; \$18.02; \$16.02; \$14.96; \$14.45; \$13.20; \$12.83; \$13.20; \$12.83; \$13.20; \$12.62; \$11.66; \$10.69; \$9.87; \$9.13; \$8.09; \$231.06. The total of these present values (in gold) is \$480.89—five cents less than the gold price of the bond in January 1865. The gold yield of the bond was therefore a trifle less than 16.43 per cent per annum.

The yield (4 per cent) referred to in the first section of this Appendix is a 'pronised' yield. If all payments are made on time, it will also be a 'realized' yield. The yield (16.43 per cent) referred to in the second section is a 'realized' yield—if the payments are made on time. It, of course, cannot be a 'promised' yield as the future cannot be known.

 $^{^{2}1.04713 = (1.08215)^{\}frac{12}{15}}$. Assuming the purchase as on the 15th of the month, there are only three and one-half months from date of purchase (January 15, 1865) to the first interest payment (May 1, 1865).





METHODS FOR COMPUTING CYCLICAL AND TREND GRADUATIONS AND MOVING SEASONALS

CYCLICAL GRADUATION

 $y = A + Bx + Cx^2 + Dx^3 + Ex^4 + Fx^6$ as closely as is possible with such simple multiples as 7 and 10. Its other mathematical characteristics, including its ability to describe cyclical material such as could be represented by a superposition of sine curves of various periods, are discussed in full in *The Smoothing of Time Series*, by Frederick R. Macaulay (National Bureau of Economic Research, 1931), pp. 73–5, etc.

TREND GRADUATION

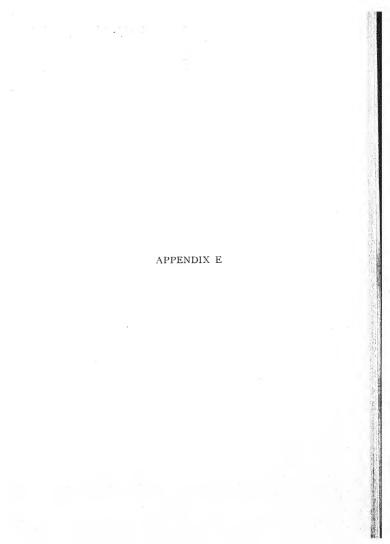
This is a 'third degree parabolic graduation'. It will fit almost exactly any curve representable by an equation of the form $y = A + Bx + Cx^2 + Dx^3$.

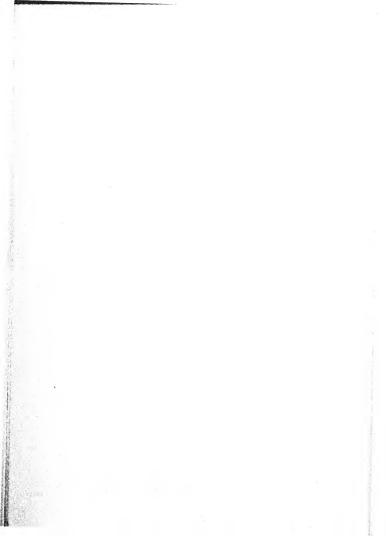
For a description of its mathematical characteristics see *The Smoothing of Time Series*, pp. 59-60, etc. To fit it to monthly data, take a 4-month moving total of an 8-month moving total of the data. Subtract a 17-month moving total of the data. Take a 2-month moving total of a 12-month moving total of the results. Divide by 360. This graduation was applied to the 43-term cyclical graduation described in the preceding section by taking as the 'months' to which this graduation was to be applied the Januaries, Mays, and Septembers of the 43-term graduation. Intermediate values were read off a large scale chart on which a smooth curve had been drawn through the calculated values with French curves.

MOVING SEASONALS

The moving seasonals of Chart 20 were constructed by taking a 7-month moving average of a 9-month moving average of the deviations of the data

for successive Januaries, Februaries, etc., from the 43-term graduation of the series as a whole. These twelve moving averages, one for each nominal month, were then smoothed with French curves. This preliminary moving seasonal was then corrected for irregularities in the algebraic sum of successive twelve-month periods by taking a 2-month moving average of a 12-month moving average of the preliminary moving seasonal and calling the deviations of the preliminary seasonal from this graduation the final moving seasonal.





SHORT TERM INTEREST RATES

THE MORE important of the short term interest rates presented in this study are those for call money, time money and commercial paper. The call money rates (Appendix A, Table 10, column 1 and Table 21) and the commercial paper rates (Appendix A, Table 10, column 3, and Table 23) are given monthly from January 1857; the time money rates (Appendix A, Table 10, column 2, and Table 22) from January 1890.¹ All three rates are from New York City markets. It was almost inevitable that these particular series should be chosen. No other short term interest series fulfilled so many of our requirements.²

First, the loans on which the rates are quoted are standardized. Though some call or time loans might carry higher or lower rates than those quoted, there was, at least hypothetically, a standard type of loan whose rate was quoted, and with which the non-standard loan could be compared. Commercial paper rates might fluctuate but the loans on which the quotations were made were standardized. It is true that the standardization of all three types of loan was much less exact in the earlier than in the later period. Moreover, the standard loan itself seems to have changed somewhat with the passage of years. 'Commercial paper' in the 'sixties or even 'seventies was a more speculative investment than in the 'nineties.

¹ For the reasons why the time money rates are carried back only to January 1890 see the section on time money.

² Two other series of short term interest rates are presented in this book: commercial paper rates in Boston monthly, January 1831 to December 1860, and rates for bankers' acceptances in New York, January 1918 to January 1936. The Boston commercial paper rates will be found in Appendix A, Tables 24 and 25 and the New York bankers' acceptance rates in Appendix A, Tables 26. The Boston rates are given for their general interest and because New York rates for this early period before 1857 are not obtainable in any such carefully collected manner. The New York bankers' acceptance rates are presented for their own sake and because they are often useful in checking the significance of an apparent change in direction of movement.

of movement.

3 The standard call or time loan in the earlier period was based on "mixed" collateral, worth in the market about 130 per cent of the amount of the loan. In the later period, 'all industrial' collateral began to be considered more and more acceptable. Non-standard loans were made at lower or higher rates. Collateral consisting entirely of government bonds usually called for a lower rate; collateral of a less marketable or more fluctuating type than the standard called for a higher rate. At present, curb market securities call for a higher rate than New York Stock Exchange securities.

Second, the published rates are in general accurate. Collection and publication seem to have been done usually with great regularity and care—though here again the rates of the earlier period are distinctly less reliable than those of the later period. However, even the early rates are seldom obscured by such hidden or difficult-to-measure considerations as the 'commissions' that occur in real estate mortgage transactions or the 'balances' required by banks of their customers.

Third, all three rates are indices of money market conditions in New York City and hence have very direct relations to the New York stock and bond markets. Though money market conditions in other centers may often have an appreciable effect on the New York security markets, it is much less direct and immediate. While changes in the rediscount rate of even the Bank of England have sometimes had a marked influence on American money rates and on the movement of the prices of American stocks and bonds, it has always been indirect, and in the earlier period covered by this study it was almost always quite negligible.

Fourth, they are relatively adequate indices. In this respect they are unlike the rates charged by ordinary banks or the rates at which money is borrowed on real estate. Tightness in the call money market manifests itself primarily in high rates, and not, as in the real estate mortgage market, by difficulty of obtaining loans.

Fifth, the rates have almost always applied to large volumes of loans.

Sixth, they are rates that can be carried far back in time. Short

⁶ It is true that time loan rates have been, in some disturbed periods, quoted with 'commissions'. However, something can always be learned about the amount of such 'commissions' from the financial newspapers and magazines of the period. Moreover, there is an impersonality in the time loan market that is lacking in the case of loans of a bank to its regular customers, whose individual credit determines, to a considerable extent, the treatment they receive.

The fact that only a small proportion of the total borrowing of the country is done through call money, time money, or commercial paper (in the strict sense), but that most is done directly from the banks by their own commercial customers is not important for our purposes. These loans have no such homogeneity as the loans giving rise to the three rate series with which we are comparing them. Moreover, while they would be important in a discussion of the effect of interest charges on the cost of doing business, they do not have the direct relation to the security markets that is found in call rates, time rates or even commercial paper rates. Since the Federal Reserve system, with its rediscounting privileges, was established, the relation of commercial paper rates to time money rates is not so close as formerly.

economic series are often interesting and important but the dangers of generalizing from them are great. The newspapers and magazines are cluttered up with charts showing apparently interesting relationships between series extending over half a dozen years or so. All too often, when such series are extended over a longer period, it is found that the interesting relationships appear only in the half dozen years. The short term interest rate series presented in this study show interesting relationships over long periods.⁶

While the general nature of the loans giving rise to the three rates—on call money, time money, and commercial paper—is doubtless well known to the reader, a somewhat detailed description would seem appropriate at this point. Both call and time loans are made to stock or bond brokers, or to investment bankers, who place in the hands of the lenders stocks or bonds, or both, as collateral. The proceeds of these loans are used for the most part to finance speculative operations in the financial markets or the distribution of new issues of securities. Commercial paper is a generic term applied to promissory notes on which merchants and manufacturers borrow money for use in the ordinary course of their business. No stock or bond collateral is deposited to secure the loan. The note may or may not bear an endorsement, and thus become 'two name' paper. Ordinarily the note

⁶ No series used for purposes of comparison in this book is carried further back than January 1857. The only series that could be carried further back, easily and with no decrease in accuracy, was that for clearings in New York City, which can be carried back to October 1853. Some deadline seemed highly desirable as comparisons between the series was the primary object. No better deadline presented itself than January 1857. For further discussion of this date, see Ch. III.

TCall loans are sometimes made on the security of bankers' acceptances deposited with the lender. They usually bear a lower rate of interest than those having stocks or bonds as collateral, because the acceptance collateral enjoys an extremely dependable and steady market. The proceeds of this type of call loan are ordinarily used for a purpose different from that to which other call loans are put, and the volume of such call funds outstanding has never been of important proportions. The rates dealt with in this book apply only to call loans secured with stocks or bonds as collateral.

8 Of course, ordinary bank loans are often secured by the deposit of stocks or bonds as collateral, but they are not time loans. What are technically known as time loans are made to stock and bond brokers and investment bankers on securities as collateral, and, as already stated, the proceeds are almost invariably used for speculative and investment distribution purposes. It is in this technical sense that we use the term 'time loan'.

is accompanied by a financial statement of the borrower for the information of the purchaser of the paper. Generally, only those borrowers whose credit is well established and well known can make effective use of commercial paper as a means of procuring short term loans.

Neither call nor time loans are eligible for rediscount at the Federal Reserve banks. Commercial paper, when it meets the requirements laid down in the Federal Reserve Act, is eligible for rediscount. Call loans are made for an indefinite period but subject to call on twenty-four hours' notice, the rate of interest being adjustable from day to day. Time loans usually run from two to six months, though they are made for as short a period as one month or as long as six or seven months. Commercial paper now usually runs from four to six months. The amount of sixty to ninety day paper is at present quite negligible. Earlier, say before 1900, the proportion of such shorter term paper was much greater.

Call money rates are made in the New York Stock Exchange. The Money Committee of the New York Stock Exchange Clearing Corporation, after having studied the offerings from brokers and bankers whether made at fixed rates or at the market, and having examined the statements of brokers concerning what they wish to borrow and at what rates, fixes and posts at twenty minutes before eleven each morning a 'Renewal Rate'. This rate is set at the point that seems likely to result in placing a maximum amount of funds. This determination does not of itself, of course, obligate either borrower or lender to observe the rate. As a matter of fact, 'outside' rates, that is rates on transactions made elsewhere than at the money desk, often vary from the so-called 'official rate'—occasionally by

⁹ The term 'commercial paper' is given a special and rather precise definition in the Federal Reserve Act for the purposes of administering the system set up under that law. The words are employed in a somewhat more inclusive sense here.

¹⁰ Recent practice has developed what are sometimes called 'call loans specials'. These take the form of the ordinary call loan, but borrower and lender enter into a gentleman's agreement that renewals will be allowed from day to day at a fixed rate of interest for a specified term. Call loans made for sums over five thousand dollars are exempt from the New York State Usury Law. It is questionable whether time loans are exempt. It may also be noted that, generally speaking, call loans are now called as a matter of course in a somewhat more impersonal manner to suit the convenience of the lender than was formerly the case.

substantial margins. Nevertheless, in ordinary times some 95 per cent or more of the call loans, new and renewed, carry the renewal rate. There is no 'official' rate on new loans. The call money, rate employed throughout this book is the renewal rate, or in periods when exact information has been lacking, estimates of it. Methods employed in these estimates are explained fully later in this appendix.

The years covered by this book fall into three periods with respect to the manner in which call rates on the New York Stock Exchange were actually made. In the first period, before September 1917, the rates were made at the 'Money Post' in almost exactly the same manner as the prices of stocks were made. The renewal rate was largely a matter of chance. After between \$2,000,000 and \$3,000,000 of new loans had been made, approximately the average of the rates of interest to be paid upon these loans was taken as the rate at which old loans should be renewed for that day. During the second period, September 1917-January 1919, the money market was under the supervision and control of the Money Committee. Since January 1919 the money desk on the floor of the Exchange has taken the place of the old 'money post'. 12

11 Formerly, the rates have sometimes varied very considerably according to the type of collateral, though variations due to this cause became less and less with the passage of time. The quotations used in constructing our index numbers were, in earlier times, those from 'mixed collateral'—i.e., rails and industrials listed on the New York Stock Exchange. At present, the distinction between rail and industrial collateral, for the purpose of determining rates, is not made.

12 See Bartow Griffiss, The New York Call Money Market.

When a call loan is made, there are, of course, a lender and a borrower of money. Now, because the security behind the call loan is Stock Exchange collateral, there are a borrower and a lender of Stock Exchange collateral. The lender of money may be thought of as a borrower of collateral, and the borrower of money may be thought of as a lender of collateral. In general, they are not so thought of, because the essential element is that one individual wishes to borrow money and the other wishes to lend, while the passing of the collateral is thought of as a mere adjunct to the transaction. However, sometimes the demand is for collateral, not for money. When a broker has sold a stock short, he wishes to borrow that stock. He offers to lend money. However, when he wishes to borrow money, he must give a greater value of stock collateral than the amount of money that he wishes to borrow. When he wishes to borrow a stock, however, he must give a larger amount of money than the value of the stock. On this money that he lends the broker who lends him the stock he receives interest, though at a lower rate than the ruling rate for call loans. Sometimes this rate is so low as to be a zero, or even a minus rate. The stock is then said to be lending 'flat' or 'at a premium'. The rate of interest paid on this money is termed the 'lending rate on stocks' and is really a

Time loans are almost all placed by brokers acting as intermediaries between borrowers, usually stock brokers or investment bankers, and lenders, usually banks. There is no agency here performing functions similar or corresponding to the money desk of the New York Stock Exchange in the case of call loans.

The commercial paper market is an 'open market' in the sense that transactions are of a sort that do not bring the borrower and the lender into direct contact as is the case when a customer procures a loan from his bank. The borrower on commercial paper simply makes a promissory note, has it endorsed or not, according to circumstances (now ordinarily not), and offers it for sale to a broker, who buys it and holds it or, as is usually the case, sells it to a bank or other investor who wishes to place funds temporarily in such paper. The note may be bought and sold in this way several times before maturity. The holder at maturity, either directly or through a broker, presents it to the maker for payment. The rates on such loans naturally vary with maturity and also with the goodness of the name or names they bear. Such loans may be eligible for rediscount at the Reserve banks and their rates thus be more directly affected by the prevailing rediscount rate than are the rates of time loans, which are not eligible for rediscount. Member banks now as a matter of practice obtain needed funds from the Reserve system largely on their own notes with government bonds as collateral or upon customers' eligible paper without collateral.

The decrease during the last few years in the amount of commercial paper outstanding is due primarily to the elimination of the commercial paper 'broker'. Large corporations have established direct relations with entire chains of banks, and when they wish money they get it directly. Even smaller borrowers have recently tended more and more to deal directly with the banks. Bankers' acceptances have probably not taken up much of the commercial paper business. The overlap is small. For example, a large amount of commercial paper originates in the textile houses and these do not enter the acceptance (Footnote 12 concluded)

peculiar type of call money. In the early days, when there was often a demand for government bonds, the rate of interest paid on loans that were secured by them was often much lower than the rate on loans secured by other collateral, no matter how good the collateral might be. This low rate of interest on loans secured by government bonds was really a type of call loan, in its nature between the lending

rate on stocks and ordinary call money.

market. Cotton financing is the biggest item in the acceptance market. It is extremely difficult to collect any very reliable and continuous series of quotations for short term interest rates in New York City before 1866.¹³ The *Commercial and Financial Chronicle* was first pub-

¹³ There is one source for early commercial paper rates (almost certainly Boston rates) giving practically continuous and apparently uniform quotations monthly as far back as January 1831: Bigelow and Martin. The Bigelow series runs from January 1831 into the 'nineties. For the period 1831–60 Martin seems to have copied, or at least used, Bigelow's table. Bigelow's table of Boston (?) rates is reproduced in Appendix A, Table 25. Martin's table (for the period 1831–1860) is reproduced in Appendix A, Table 24.

Erastus B. Bigelow, inventor of the power loom, a New England mill owner, published in 1862, at Boston, a large quarto entitled The Tariff Question ... with statistical and comparative tables. Appendix 112 (pp. 204, 205) contains a table entitled Statement of the Comparative Rates of Interest in England, France and the United States each month in each year, from 1831 to 1860. Compiled from authentic sources. The American rates are described as "Street Rates on First Class Paper in Boston and New York, at the beginning, middle and end of the month". Where this table contains two quotations for a month, interpretation is sometimes difficult. In his discussion of these rates (pp. 66-69) Bigelow makes no statement concerning the "authentic sources" from which his table was compiled. The book was noticed and the interest table copied in the London Economist of December 27, 1862, pp. 1434, 1435. Again no discussion of sources. The book was reviewed by Leslie Stephen in Machillan's Magazine, Vol. 7, p. 126. No references were made there to the interest tables.

Joseph G. Martin, a Boston stock broker, published from 1856 to 1897 a series of books on the History of the Boston Stock Market. The first, Twenty-one Years in the Boston Stock Market, (Boston, 1856), contained no American interest rates. The second, Seventy-three Years History of the Boston Stock Market (Boston, 1871), contained a table (pp. 37-40) entitled Interest Rates for Money, 1831-1871. No statement is made in this table or elsewhere in the book whether these are New York or Boston rates. The only comment is: "The following rates are for first-class, three to six months, bankable paper." However, when Martin reprints the same series of interest rates in his later book, One Hundred Years' History of the Boston Stock Market (1798-1898), he calls the series The Course of the Boston Money Market.

Now, in view of the facts that Martin's first book (1856) contained no American interest rates, that Bigelow's book appeared in 1862 and that the table in Martin's second book (1871) (as far as can be gathered from the form in which Martin presents his material) is almost identical with Bigelow's table for the years 1831 to 1860, it seems fair to assume that Martin's early figures were taken from Bigelow's book. However, in spite of the dates of publication, it is possible that Bigelow obtained his interest rates from unpublished material collected by Martin. Martin was intensely interested in all that related to the statistical history of the Boston stock and money markets and was continually collecting quotations of all kinds. A large amount of his unpublished manuscript material is now in the Widener Library, Harvard University.

lished July 1, 1865, but only gradually began its careful collection of short term interest rate material. Though the amount of data in existence for the period before 1866 is quite large, it is extremely irregular with respect to both quality and periods for which there are quotations. Moreover, upon close examination, the material that does exist is found to be extremely heterogeneous; variations in quoted rates for the same date are sometimes traceable to the fact that the quotations are for different types of loan and sometimes seem the result merely of obtaining information from different primary sources, such as different brokers.

At present, the chief primary sources for interest rates in New York City in the period before the publication of the Commercial and Financial Chronicle are the daily newspapers, Hunt's Merchants' Magasine, and the Bankers' Magazine. Of these sources, the newspapers, as a group, are much the most regular in their quotations. Nevertheless, it is impossible to work continuously with one paper. Any one paper either stops quoting or its quotations become unmistakably very inaccurate. One of the signs of such inaccuracy is the quoting of an unchanging rate day after day for long periods, the context showing that proper attention is not being given to the subject. It might be thought that if we always had at least one newspaper giving quotations our problem could be easily solved. However, the newspapers do not always agree. When quoting commercial paper they are not always quoting the same grade. This is especially important to watch in this early period. The rate of discount on commercial paper 'not well known' was often two or three times as great as on 'first class acceptances'. The newspapers rather commonly quote 'commercial paper' without any specifications as to grade. Moreover, there is unmistakable evidence that this did not always mean the highest grade.

Hunt's Merchants' Magazine and the Bankers' Magazine are even more irregular in their quotations than the newspapers. For example, neither quotes interest rates of any kind during the important year 1857. Moreover, the dangers involved in shifting back and forth from one to the other are just as real as in the case of the newspapers. (Footnote 3ª concluded)

Martin calls the rates Boston rates, and Bigelow calls them Boston and New York rates. Now Boston and New York rates were not identical, and an examination of the newspapers and periodicals has convinced me that the Bigelow-Martin rates are Boston and not New York rates.

Quotations for what is termed the same type of loan continually vary. Neither Hunt's Merchants' Magazine nor the Bankers' Magazine is always a primary source. For example, when Hunt's Merchants' Magazine in January 1859 (Vol. 40, p. 76) begins to quote interest rates again (having lapsed for some years) and we find back rates for October 25, November 24, December 6 and December 14, 1858, we must not assume that all these figures are primary sources. The October and November figures are almost certainly taken from the Bankers' Magazine of December 1858 (p. 510). In the same way Hunt's Merchants' Magazine figures from May 1861 to October 1861 are from the Bankers' Magazine. Crude mistakes that are obviously due to errors in copying often appear. Numerous mistakes are apparent even when Hunt's Merchants' Magazine is copying from its own files.¹⁴

Aside from the general heterogeneity of the data, another source of embarrassment in the early period is the difficulty of obtaining quotations when the prevailing rates are high. There are two reasons for this difficulty. First, in times of financial panic all newspaper quotations tended to cease. Not only was there an apparent prejudice against publication but also it was often extremely difficult to discover what the rates really were. 'High and irregular' runs the legend. Second, because of the usury laws, high rates were disguised by means of 'commissions'. 15

Secondary sources for interest rates in the period before 1866 are magazine and newspaper articles, and brokers' annual reviews. So few of these articles and reviews are still in existence that they are of little value except as partial checks on the accuracy of complete tables such as Bigelow's or those we have constructed for this volume. For the period January 1862 to December 1865 we have used Wesley

¹⁴ For example, comparison of dates in the table of rates in Vol. 42, p. 196 with the tables in Vol. 41, pp. 716, 580 and 452 is quite startling.

The Commercial and Financial Chronicle was the first journal to make any attempt at regularly quoting these commissions. The earlier publications seldom even mentioned commissions, let alone quoting them. As an example of the results of this practice, the reader may examine the table of interest rates for 1868-70 drawn up by the then Manager of the New York Clearing House (Commercial and Financial Chronicle, February 4, 1871, p. 138). The rate for each week in 1869 is given as 7 per cent. During 1869 call loan rates, as averaged from quotations in the Commercial and Financial Chronicle, exceeded 7 per cent nineteen weeks out of the fifty-two, while corresponding average weekly rates on commercial paper exceeded 7 per cent every week in the year.

C. Mitchell's table of monthly call loan rates given in his History of the Greenbacks, p. 367. We checked with original sources and decided that Dr. Mitchell's figures were probably as good as could be constructed for this very difficult period. Dr. Mitchell makes some comments on the inadequacy of the sources for this war period 1862-65.

"To my knowledge there are no systematic records of rates of interest on long-time business loans, and the data for short-time loans are unusually meagre and doubtful. In 1860, Hunt's Merchant's Magazine and the Bankers' Magazine-the most prominent business periodicals of the daywere publishing each month tables showing the rates of interest paid in New York for loans of several different kinds. But during the War, they ceased these systematic reports and one can glean from them but occasional scattering statements" (p. 365).

"Under these circumstances, it seems justifiable to attempt constructing a new table from the reports of the daily newspapers. On examination, however, one finds that this course also is open to objection. In the first place, regular statements can be found only for one kind of transaction -loans on call. In the second place, whenever the rates for call loans rise above 7 per cent the reporter is apt to say merely that the ruling rate is 'the legal maximum plus a small commission'. In the third place, one is justified in feeling some suspicions of the accuracy of newspaper reports. However, I have compiled a table from the financial columns of the newspapers of the rate for call loans every Saturday from 1862 to 1865. In doing so, I have been compelled to supplement one paper by another, for no one gives the reports with perfect regularity for the whole period" (pp. 366-7).

In the period January 1866 to January 1923 we have relied almost entirely on the Commercial and Financial Chronicle and its Financial Review. These two sources are practically identical. Where they differ we have in the earlier period given a little more consideration to the Chronicle, in the later period to the Financial Review. There is some evidence, both internal and external, that in the later period the figures in the Chronicle were reconsidered and checked before being incorporated in the Review. In periods of violent fluctuation, when highs and lows gave little evidence concerning averages, we have examined newspapers and magazines other than the Chronicle. However, we have kept as close to the Chronicle as we could, being convinced that it was the best source and also that it was extremely undesirable to move from source to source if we wished to have a homogeneous series of quotations.

In the period January 1923 to January 1936 we have kept to the *Chronicle* for time money rates and commercial paper rates, but have used the *Federal Reserve Bulletin* figures for call money rates. These figures are monthly averages of the daily renewal rates given by the *Chronicle*.

The sources most used in obtaining the original data, from which the monthly averages were constructed, were:

I For Call Money Rates

Jan. 1857-Dec. 1859 Journal of Commerce

Jan. 1860-Dec. 1861 Hunt's Merchants' Magazine

Jan. 1862-Dec. 1865 Wesley C. Mitchell's History of the Greenbacks

Jan. 1866-Dec. 1889 Commercial and Financial Chronicle

Jan. 1890—Dec. 1919 Financial Review (published by the Commercial and Financial Chronicle) and Commercial and Financial Chronicle

Jan. 1920-Dec. 1922 Financial Review

Jan. 1923-Jan. 1936 Federal Reserve Bulletins

II For 90-Day Time Money Rates

Jan. 1890 16-Dec. 1923 Financial Review

Jan. 1924 - Jan. 1936 Commercial and Financial Chronicle

III For 60 to 90 Day Commercial Paper Rates 17

Jan. 1857-Dec. 1859 Journal of Commerce

Jan. 1860—Dec. 1861 Hunt's Merchants' Magazine and Bankers' Magazine

¹⁶ No monthly index of time money rates was constructed further back than January 1890. Before the Federal Reserve system came into being, the movements of time money and of commercial paper rates were so similar that it is worth collecting figures for both rates only when the accuracy of the original data is sufficiently great to make the differences between the two rates significant. An examination of the sources for commercial paper rates and time money rates in the period before January 1890 suggests that significant differences between the two series would not be obtainable for very many years previous to 1890. In the earliest period it is practically impossible to get any continuous quotations for time money. However, beginning with January 1890, the Commercial and Financial Chronicle published in their Financial Review, each year, a very complete table of time money rates weekly for various maturities from thirty days to six months.

17 The rates for January 1857 to December 1865 are attempts to estimate what the rates were for 60-90 day prime double name paper. In this early period it is often

Jan. 1862-June 1862 Hunt's Merchants' Magazine, Bankers' Magazine and New York newspapers

July 1862-Dec. 1865 New York newspapers

Financial Review and Commercial and Financial Jan. 1866-Jan. 1936 Chronicle

The above sets of sources are the ones most used in each period. All possible sources were used in the earliest period. No single source stood out in the way that the Commercial and Financial Chronicle does after 1867. For example, though the New York Journal of Commerce call money rates were weighted more heavily from January 1857 to December 1859 than the rates obtained from any other single source, quotations for odd months in 1858 and the entire year 1859 were obtained from Hunt's Merchants' Magazine and the Bankers' Magazine. Quotations for 1859 were also obtained from the New York Herald. An attempt was made to weigh and consider these various quotations and to determine to what extent they should influence us, if at all, in accepting the figures of the Journal of Commerce.

For commercial paper rates during the same period, January 1857 to December 1859, we weighted most heavily the same source as was most heavily weighted for call money rates, namely the Journal of Commerce, However, the Bankers' Magazine was quoting throughout 1857, irregularly in 1858, and throughout 1859, Hunt's Merchants' Magazine was quoting rates twice a month in the later part of 1858 and throughout 1859. The New York Chamber of Commerce published a compilation of monthly rates for the year 1858. To go into details as to where each item was found would be wearisome and futile. It may be mentioned, however, that for the early period the following newspapers were carefully examined:

New York Herald

New York Evening Post (daily and semi-weekly)

New York Commercial Advertiser

New York Tribune (daily and semi-weekly)

New York Weekly Herald

(Footnote 17 concluded)

not clear what grade of paper is being quoted. The rates for January 1866 to December 1923 are for 60-90 day prime double name paper. The rates for January 1924 to January 1936 are for 4-6 month prime double (or single) name paper. In this period 60-90 day paper was quoted nominally at the same rate as 4-6 month paper. The amount of the shorter maturity paper was becoming negligible.

Journal of Commerce New York Sun New York Times

Shipping and Commercial List and New York Price Current

In some cases, a few hours were sufficient to convince one that nothing helpful in the way of either figures or text was to be found. In other cases, useful information was found here and there.

No intricate mathematical method of averaging was used in getting monthly figures from the daily newspaper quotations. All quotations, and remarks on rates, obtainable from the various papers for a particular month were tabulated and an estimated average made from careful inspection. There were, of course, many gaps in the daily quotations. Many simple little devices were used in connection with the various sources.

In the period January 1860 to December 1861, where the most used sources given in the table above are *Hunt's Merchants' Magazine* and the *Bankers' Magazine*, the rates used are almost exact arithmetic averages of the rates obtained from these two sources. Newspaper quotations were scanty but seemed to corroborate the magazine rates. In 1866 and 1867 we did not accept the rates from the *Chronicle* without question as we did in the later period. The quotations were carefully checked with other sources and final estimates made. 18

²⁸ We did not change Dr. Mitchell's figures for call money rates in the last six months of 1865 though compilations from the *Chronicle* gave appreciably different results, for we did not feel sufficient confidence in the accuracy of these earliest *Chronicle* figures. The rates we derived from the *Chronicle* compare as follows with Mitchell's rates derived from newspapers.

	1865	
	Chronicle	Mitchell
July	5.38	5,5
August	6.10	5,9
September	5.00	6.0
October	8.44	7.0
November	6.84	6.8
December	6.88	6.8

Before any conclusions are drawn from the table, attention should be called to the rather complicated manner in which the Chronicle was quoting all its rates at this time. Even the quotations for call money rates do not impress the reader with their adequacy and the commercial paper rates are almost unusable because they vary with the type of loan. Note the following quotations from the Chronicle:

The type of collateral influenced call money rates markedly for a considerable period during the regime of the national banking system. As an extreme example, attention may be drawn to the fact that loans on government bonds in the early days were somewhat analogous to loans based on short sales at present. In both cases, the real borrower—the party for whom the borrowing was most important—was the borrower of the security. Call loans with United States government bonds as collateral were made by banks to obtain bonds to deposit with the United States Treasury, in order that the bank might issue currency. They were primarily loans of government bonds, not loans of money.¹⁹

In the earlier period the call loan market was not developed to anything like its present degree. The call loan was not so strictly 'call' (Footnote 1s concluded)

July 8, 1865, p. 42

".... Dry goods bills are current at 6½ to 7½ per cent; grocers 6½ to 7½; produce commission 7½ to 9 per cent."

July 15, 1865

"Discounts are dull. There is a larger supply of bills, especially of grocers, but the demand is quiet, the rates ranging from 6 to 10 per cent. We quote the best grades of the several classes of paper as follows:—

Dry Goods	6½ to 7	Bankers	6 to	7
Grocers	6½ to 7	Produce Commission	9 to 1	10"

November 11, 1865

March 31, 1866, p. 394

"The following are the rates for the various classes of loans:

	per cent
Call loans	5 to
Loans on bonds and mortgage	6 to 7
Prime endorsed bills 2 months	6½ to 7½
Good endorsed bills 3 and 4 months	7 to 8
" -single names	9 to 10
Lower grades	10 to 15"

These last quotations are in a form distinctly easier to handle than the form in which the preceding quotations appeared. By 1868 the Chronicle quotations are all relatively easy to use.

[&]quot;Prime bills pass at 7 to 9 per cent, and second class names at 10 to 15 per cent. Bankers bills are current at 7 to 8 per cent, dry goods commission at 8 to 10, produce commission at 9 to 12 per cent."

¹⁰ Compare . . . "the demand for Government Bonds was so large to put in the Treasury as collateral that the rates to Government Bond dealers fell off 3 per cent, although this transaction is rather a loan of Government Bonds than a loan of money" (Commercial and Financial Chronicle, March 29, 1879), p. 317.

as at present, and the market was not so impersonal as it has become. In the period January 1890 to December 1923 almost complete reliance was placed on the time money figures contained in the Financial Review though for numerous dates these were checked and compared with the Chronicle's figures and text. This was especially true in periods when 'commissions' were being paid. The Chronicle's text was then used to help us to measure their effect on the rate actually paid. Throughout the period January 1890 to date the time loan rates are for loans with 'mixed collateral'

In the period from 1857 to about 1910 our 'commercial paper' may be thought of as rather strictly rates for 60-90 day paper. After this period this short maturity paper becomes more and more rare, and the rates are, more and more, rates for 3 to 4 month paper. However, in this later period, what 60-90 day paper was made commonly went at the 3-4 month rate. After 1890, and until the very recent period. the quotations used were usually entitled 'double name choice 60-90 day paper'. In the early days where there were quotations for prime endorsed bills 2 month, and good endorsed bills 3 and 4 month, the method by which 'double name choice 60-90 day paper' was estimated was to use the quotation for 'prime endorsed bills 2 month' as the more important single piece of evidence, but sometimes to adjust the figures in the light of changes in the quotations for 'good endorsed bills 3 and 4 month", and sometimes in the light of the text. 'Prime paper' seemed usually to mean A No. 1 short time (2 month) endorsed notes.

Nearly all commercial paper is at present single name. In the earlier period there was a certain amount of extra fine two name paper. Present day newspaper and magazine quotations for 'double name choice 60–90 day paper' are really quotations for commercial paper that is neither 60–90 day nor two name. They are really quotations for 4 to 6 month high grade single name paper.

Commercial paper is made by the larger department and men's furnishing stores, jobbers of dry goods, hardware, shoes, groceries,

²⁰ Compare... "The precautionary feeling among lenders is naturally on the increase as the Fall months draw nearer, and its working is fairly illustrated in a circumstance we recently heard of a bank's calling in a loan from one party and lending to another at a much lower rate, simply because the latter was a better borrower and would pay up on call, without asking any extension" (Ibid., August 16, 1873), p. 213.

floor coverings, etc., the manufacturers of cotton, silk and woolen goods, clothing, etc.

In constructing monthly average rates from weekly averages for call money, time money or commercial paper, if the week-end (Saturday) occurred on the 1st or 2d of the month, it was considered as a week entirely in the preceding month. If the week-end occurred on the 4th, 5th or 6th of the month, the week was considered as entirely in the later month. If it occurred on the 3d of the month, the weeks average was considered a quotation for half a week in the earlier month and half a week in the later month.

Most of the monthly rates were constructed from weekly figures, except when conditions were so disturbed as to make it necessary to examine daily rates. In such disturbed times the *Chronicle* generally quoted daily rates or at least discussed them. When the *Chronicle* quoted them, no other source was commonly referred to.

In constructing monthly call rate averages from weekly rates, the first operation (with the data before 1890) was to obtain a set of weekly average rates. The Chronicle commonly quoted a high rate and a low rate for the week. If, for any particular week, the range between these rates was quite small, their arithmetic average was considered to be the weekly average rate.

But the actual 'high' and 'low' and estimated 'ruling' weekly rates given by the Financial Reviews back to the beginning of 1890 show in figures a condition that the Chronicle in the earlier years had so often verbally described. Almost invariably, when the difference between the 'high' rate and the 'low' rate is at all large, the 'ruling' rate is much closer to the 'low' than the 'high' rate. As we were unable to invent an 'average' (beyond the harmonic, for example) that gave a good description of the relation, we constructed a nomograph (designed to fit the Financial Review figures as closely as possible) from which, given a 'high' and a 'low' rate, it was possible to read a 'ruling' rate. When, in the period before 1890, the weekly range was large and reliable daily rates were not obtainable, we used this nomograph (in conjunction with any verbal comment) to calculate a weekly average or 'ruling' rate. If reliable daily rates were obtainable we used them to construct the weekly average, having first used the nomograph (and verbal comment) to obtain a daily average for any day in which the range was abnormally large.

We believe this procedure gives a much better approximation to a weighted average of the rates of all the loans of the week than can be obtained by a blind use of arithmetic averages of high and low rates. But it naturally results in a series with no such stupendous peaks as series based on arithmetic averaging.





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